## Observation of $B^{+} \rightarrow \eta \rho^{+}$and search for $B^{0}$ Decays to $\eta^{\prime} \eta, \eta \pi^{0}, \eta^{\prime} \pi^{0}$, and $\omega \pi^{0}$

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We present measurements of branching fractions for five $B$-meson decays to two-body charmless final states. The data, collected with the BABAR detector at the Stanford Linear Accelerator Center, represent 459 million $B \bar{B}$ pairs. The results for branching fractions are, in units of $10^{-6}$ (upper limits at $90 \%$ C.L. $): \mathcal{B}\left(B^{+} \rightarrow \eta \rho^{+}\right)=9.9 \pm 1.2 \pm 0.8, \mathcal{B}\left(B^{0} \rightarrow \eta^{\prime} \eta\right)=0.5 \pm 0.4 \pm 0.1(<1.2)$, $\mathcal{B}\left(B^{0} \rightarrow \eta \pi^{0}\right)=0.9 \pm 0.4 \pm 0.1(<1.5), \mathcal{B}\left(B^{0} \rightarrow \eta^{\prime} \pi^{0}\right)=0.9 \pm 0.4 \pm 0.1(<1.5)$, and $\mathcal{B}\left(B^{0} \rightarrow \omega \pi^{0}\right)=$ $0.07 \pm 0.26 \pm 0.02(<0.5)$. The first error quoted is statistical and the second systematic. For the $\eta \rho^{+}$mode, we measure the charge asymmetry $\mathcal{A}_{c h}\left(B^{+} \rightarrow \eta \rho^{+}\right)=0.13 \pm 0.11 \pm 0.02$.

Measurements of charmless $B$ decays are now routinely used to test the accuracy of theoretical predictions based on, for example, QCD factorization [1, 2], flavor $\operatorname{SU}(3)$ symmetry [3-5], perturbative QCD [6], or soft collinear effective theory [7]. We present measurements of the branching fraction and charge asymmetry for the decay $B^{+} \rightarrow \eta \rho^{+}$(charge conjugate reactions are implied throughout this paper), superseding our previous result that found a $4.7 \sigma$ signal for this decay [8] with a luminosity of about one-half that used in this paper. In addition we search for the decays $B^{0} \rightarrow \eta^{\prime} \eta$, $B^{0} \rightarrow \eta \pi^{0}, B^{0} \rightarrow \eta^{\prime} \pi^{0}$, and $B^{0} \rightarrow \omega \pi^{0}$. None of these decays have been observed previously though limits have been reported by BABAR [9], Belle [10], and CLEO [11].

In the Standard Model (SM) the dominant processes that contribute to these decays are described by tree amplitudes and to a lesser extent penguin (loop) amplitudes. For $B^{0} \rightarrow \eta^{\prime} \pi^{0}$ and $B^{0} \rightarrow \eta \pi^{0}$ the colorsuppressed tree diagram is suppressed by approximate cancellation between the amplitudes for the $\pi^{0}$ and for the isoscalar meson that contains the spectator quark. The approximate ranges of expectations $[1-7]$ for the branching fraction are $\sim 10 \times 10^{-6}$ for $B^{+} \rightarrow \eta \rho^{+}, 0.3-$ $2 \times 10^{-6}$ for $B^{0} \rightarrow \eta^{\prime} \eta, 0.2-1.0 \times 10^{-6}$ for $B^{0} \rightarrow \eta^{(\prime)} \pi^{0}$, and $\sim 0.1 \times 10^{-6}$ for $B^{0} \rightarrow \omega \pi^{0}$. Direct $C P$ violation could be detected as a charge asymmetry, defined as $\mathcal{A}_{c h} \equiv\left(\Gamma^{-}-\Gamma^{+}\right) /\left(\Gamma^{-}+\Gamma^{+}\right)$, where the superscript on the width $\Gamma$ corresponds to the sign of the $B^{ \pm}$meson; $\mathcal{A}_{c h}$ for $B^{+} \rightarrow \eta \rho^{+}$is expected to be small since the decay is dominated by a single amplitude.

These $B^{0}$ decays are also of interest in constraining the expected value of the time-dependent $C P$-violation asymmetry parameter $S_{f}$ in the $B$ decay with final state $f=\eta^{\prime} K_{S}^{0}[5,12,13]$. The leading-order SM calculation gives the equality $S_{\eta^{\prime} K_{S}^{0}}=S_{J / \psi K_{S}^{0}}$, where the latter has been precisely measured [14], and equals $\sin 2 \beta$ in the SM. The $C P$ asymmetries in the charmless $B$ decays are not only sensitive to contributions from new physics, but also to contamination from sub-leading SM amplitudes. Recent theoretical calculations of the size of the change in $S_{\eta^{\prime} K_{S}^{0}}$ from these sub-leading amplitudes finds no more than 0.03 [7, 15]. The most stringent constraint from data on such contamination uses $\mathrm{SU}(3)$ and the measured branching fractions of the decays $B^{0} \rightarrow \eta^{\prime} \eta, B^{0} \rightarrow \eta \pi^{0}$, $B^{0} \rightarrow \eta^{\prime} \pi^{0} \quad[5,12,13]$. Recently it has also been suggested [16, 17] that $B^{0} \rightarrow \eta^{\prime} \pi^{0}$ and $B^{0} \rightarrow \eta \pi^{0}$ can be used to constrain the contribution from isospin-breaking effects on the value of $\sin 2 \alpha$ in $B \rightarrow \pi^{+} \pi^{-}$decays.

The results presented here are based on data collected with the BABAR detector [18] at the PEP-II asymmetric $e^{+} e^{-}$collider located at the Stanford Linear Accelerator Center. We recorded a data sample at the $\Upsilon(4 S)$ resonance (center-of-mass energy $\sqrt{s}=10.58 \mathrm{GeV}$ ) with
an integrated luminosity of $418 \mathrm{fb}^{-1}$, corresponding to $(459 \pm 5) \times 10^{6} B \bar{B}$ pairs.

Charged particles from the $e^{+} e^{-}$interactions are detected and their momenta measured by a combination of five layers of double-sided silicon microstrip detectors and a 40-layer drift chamber, both operating in the 1.5 T magnetic field of a superconducting solenoid. Photons and electrons are identified with a $\mathrm{CsI}(\mathrm{Tl})$ electromagnetic calorimeter (EMC). Further charged particle identification (PID) is provided by the average energy loss $(d E / d x)$ in the tracking devices and by an internally reflecting ring imaging Cherenkov detector (DIRC) covering the central region.

We establish the event selection criteria with the aid of a detailed Monte Carlo (MC) simulation of the $B$ production and decay sequences, and of the detector response [19]. These criteria are designed to retain signal events with high efficiency. Applied to the data, they result in a sample much larger than the expected signal, but with well characterized backgrounds. We extract the signal yields from this sample with a maximum likelihood (ML) fit.

The $B$-daughter candidates are reconstructed through their decays $\pi^{0} \rightarrow \gamma \gamma, \eta \rightarrow \gamma \gamma\left(\eta_{\gamma \gamma}\right), \eta \rightarrow \pi^{+} \pi^{-} \pi^{0}\left(\eta_{3 \pi}\right)$, $\eta^{\prime} \rightarrow \eta_{\gamma \gamma} \pi^{+} \pi^{-}\left(\eta_{\eta \pi \pi}^{\prime}\right), \eta^{\prime} \rightarrow \rho^{0} \gamma\left(\eta_{\rho \gamma}^{\prime}\right), \omega \rightarrow \pi^{+} \pi^{-} \pi^{0}$, $\rho^{0} \rightarrow \pi^{+} \pi^{-}$and $\rho^{+} \rightarrow \pi^{+} \pi^{0}$. Table I lists the requirements on the invariant masses of these particles' final states. All requirements are kept loose $(>3 \sigma)$ for later fitting except for the $\pi^{0}$ invariant mass which is not included in the fits. Secondary charged pions in $\eta, \eta^{\prime}$, and $\omega$ candidates are rejected if classified as protons, kaons, or electrons by a combination of their DIRC, $d E / d x$, and EMC PID signatures.

TABLE I: Selection requirements on the invariant masses of resonances and the laboratory energies of photons from their decay.

| State | Invariant mass $(\mathrm{MeV})$ | $E(\gamma)(\mathrm{MeV})$ |
| :--- | :---: | :---: |
| Prompt $\pi^{0}$ | $120<m(\gamma \gamma)<150$ | $>50$ |
| $\eta_{\gamma \gamma}$ | $490<m(\gamma \gamma)<600$ | $>100$ |
| $\eta_{3 \pi}$ | $520<m\left(\pi^{+} \pi^{-} \pi^{0}\right)<570$ | $>30$ |
| $\eta_{\eta \pi \pi}^{\prime}$ | $910<m\left(\pi^{+} \pi^{-} \eta\right)<1000$ | $>100$ |
| $\eta_{\rho \gamma}^{\prime}$ | $910<m\left(\pi^{+} \pi^{-} \gamma\right)<1000$ | $>200$ |
| $\omega$ | $735<m\left(\pi^{+} \pi^{-} \pi^{0}\right)<825$ | $>30$ |
| $\rho^{0}$ | $510<m\left(\pi^{+} \pi^{-}\right)<1000$ | - |
| $\rho^{+}$ | $470<m\left(\pi^{+} \pi^{0}\right)<1070$ | $>30$ |

We reconstruct the $B$-meson candidate by combining the four-momenta of a pair of daughter mesons, with a vertex constraint if the ultimate final state includes at least two charged particles. Since the natural widths of the $\eta, \eta^{\prime}$, and $\pi^{0}$ mesons are much smaller than the resolution, we also constrain their masses to nominal val-
ues [20] in the fit of the $B$ candidate. From the kinematics of the $\Upsilon(4 S)$ decay we determine the energysubstituted mass $m_{\mathrm{ES}}=\sqrt{\frac{1}{4} s-\mathbf{p}_{B}^{2}}$ and the energy difference $\Delta E=E_{B}-\frac{1}{2} \sqrt{s}$, where $\left(E_{B}, \mathbf{p}_{B}\right)$ is the $B$-meson 4 -momentum vector, and all values are expressed in the $\Upsilon(4 S)$ rest frame. The resolution in $m_{\mathrm{ES}}$ is 3.0 MeV and in $\Delta E$ is $24-50 \mathrm{MeV}$, depending on the decay mode. We require $5.25 \mathrm{GeV}<m_{\mathrm{ES}}<5.29 \mathrm{GeV}$ and $|\Delta E|<0.25$ $\mathrm{GeV}\left(<0.2 \mathrm{GeV}\right.$ for $B^{0} \rightarrow \eta^{\prime} \eta$ and $\left.B^{+} \rightarrow \eta \rho^{+}\right)$.

Backgrounds arise primarily from random combinations of particles in continuum $e^{+} e^{-} \rightarrow q \bar{q}$ events $(q=$ $u, d, s, c)$. We reduce these with requirements on the angle $\theta_{\mathrm{T}}$ between the thrust axis of the $B$ candidate's decay products in the $\Upsilon(4 S)$ rest frame and the thrust axis of the rest of the charged tracks and neutral calorimeter clusters in the event. The distribution is sharply peaked near $\left|\cos \theta_{\mathrm{T}}\right|=1$ for $q \bar{q}$ jet pairs and nearly uniform for $B$-meson decays. We require $\left|\cos \theta_{\mathrm{T}}\right|<0.7-0.9$ depending on the decay mode.

In the ML fit we discriminate against $q \bar{q}$ background with a Fisher discriminant $\mathcal{F}$ that combines five variables [21]: the polar angles, with respect to the beam axis in the $\Upsilon(4 S)$ rest frame, of the $B$ candidate momentum and of the $B$ thrust axis; the flavor tagging category [22]; and the zeroth and second angular moments of the energy flow, excluding the $B$ candidate, about the $B$ thrust axis. It provides about one standard deviation of separation between $B$ decay events and combinatorial background.

We also impose restrictions on decay angles to exclude the most asymmetric decays where soft-particle backgrounds concentrate and the acceptance changes rapidly. We define the decay angle $\theta_{\text {dec }}^{k}$ and its cosine $\mathcal{H}_{k}$ for a meson $k$ as the angle between the momenta of a daughter particle and the meson's parent, measured in the meson's rest frame. We require for the $\eta_{\rho \gamma}^{\prime}$ decays $\left|\mathcal{H}_{\rho^{0}}\right|<0.9$ and for $\eta^{(\prime)} \pi^{0}\left|\mathcal{H}_{\pi^{0}}\right|<0.95$. For $B^{0} \rightarrow \eta_{\rho \gamma}^{\prime} \eta_{\gamma \gamma}$ we suppress the background $B \rightarrow K^{*} \gamma$ by requiring $\left|\mathcal{H}_{\eta}\right|<0.86$. These distributions are uniform for signal except for $\mathcal{H}_{\rho^{0}}$ which has a $1-\mathcal{H}_{\rho}^{2}$ distribution.

For the $B^{+} \rightarrow \eta \rho^{+}$decay, we define $\theta_{\text {dec }}^{k}$ as the angle between the $\pi^{0}$ and the negative of the $B$ momentum in the $\rho$ rest frame. We require $-0.75<\mathcal{H}_{\rho^{+}}<0.95$. For the $B^{0} \rightarrow \omega \pi^{0}$ decay, $\left|\mathcal{H}_{\omega}\right|$ is defined as the cosine of the angle between the normal to the $\omega$ decay plane (the plane of the three pions in the $\omega$ rest frame) and the flight direction of the $B$, measured in the $\omega$ rest frame. Both of these quantities have a $\mathcal{H}^{2}$ distribution for signal.

The average number of candidates found per selected event is in the range 1.06 to 1.47 , depending on the final state. We choose the candidate with the largest probability for the fit to the $B$ decay tree.

We obtain yields for each channel from a ML fit with the input observables $\Delta E, m_{\mathrm{ES}}, \mathcal{F}, m_{k}, k=1,2$ (the daughter invariant mass spectrum of the $\eta, \eta^{\prime}, \omega$, or $\rho^{+}$ candidate), and $\mathcal{H}_{k}$ the helicity of the $\omega$ or $\rho^{+}$candidate.

The selected sample sizes are given in the second column of Table II. Besides any signal events, the samples contain combinatorial background from $q \bar{q}$ (dominant) and $B \bar{B}$ with $b \rightarrow c$, and a component from other charmless $B \bar{B}$ modes that we estimate from the simulation to be no more than two percent of the sample. The latter events have ultimate final states different from the signal, but with similar kinematics so that broad peaks near those of the signal appear in some observables, requiring a separate component in the probability density function (PDF).

The likelihood function is

$$
\begin{align*}
& \mathcal{L}=\exp \left(-\sum_{j} Y_{j}\right) \prod_{i}^{N} \sum_{j} Y_{j} \times  \tag{1}\\
& \mathcal{P}_{j}\left(m_{\mathrm{ES}}{ }^{i}\right) \mathcal{P}_{j}\left(\Delta E^{i}\right) \mathcal{P}_{j}\left(\mathcal{F}^{i}\right) \mathcal{P}_{j}\left(m_{1}^{i}\right)\left[\mathcal{P}_{j}\left(m_{2}^{i}\right), \mathcal{P}_{j}\left(\mathcal{H}_{\omega, \rho^{+}}^{i}\right)\right]
\end{align*}
$$

where $N$ is the number of events in the sample, and, for each of the three components $j, Y_{j}$ is the yield of events and $\mathcal{P}_{j}\left(x^{i}\right)$ the PDF for observable $x$ in event $i$. For the mode $B^{0} \rightarrow \eta_{\eta \pi \pi}^{\prime} \eta_{3 \pi}$ we found no need for the charmless $B \bar{B}$ background component. For the $B^{+} \rightarrow \eta_{\gamma \gamma} \rho^{+}$ and $B^{0} \rightarrow \omega \pi^{0}$ decays we split the charmless $B \bar{B}$ PDF into components made from backgrounds with and without a $\rho^{+}$. The factored form of the PDF indicated in Eq. 1 is appropriate since correlations among observables measured in the data are small. Distortions of the signal yields caused by this approximation are measured in simulation and included in the bias corrections and systematic errors discussed below.

We determine the PDFs for the signal and charmless $B \bar{B}$ background components from fits to MC simulated events. Large control samples of $B$ decays to charmed final states of similar topology $\left[B^{+} \rightarrow \bar{D}^{0}\left(K^{+} \pi^{-} \pi^{0}\right) \pi^{+}\right.$ and $B^{+} \rightarrow \bar{D}^{0}\left(K^{+} \pi^{-} \pi^{0}\right) \rho^{+}$] are used to verify the simulated resolutions in $\Delta E$ and $m_{\mathrm{ES}}$. Where the control data samples reveal small differences from MC, we shift or scale the resolution used in the ML fits. We develop PDFs for the combinatorial background with fits to the data from which the signal region $\left(5.27 \mathrm{GeV}<m_{\mathrm{ES}}<\right.$ 5.29 GeV and $|\Delta E|<0.1 \mathrm{GeV}$ ) has been excluded.

We use the following functional forms for the PDFs: sum of two Gaussians for $\mathcal{P}_{\text {sig }}\left(m_{\mathrm{ES}}\right), \mathcal{P}_{\text {sig }, B \bar{B}}(\Delta E)$, and the sharper structures in $\mathcal{P}_{B \bar{B}}\left(m_{\mathrm{ES}}\right)$ and $\mathcal{P}_{j}\left(m_{k}\right)$; linear or quadratic dependences for combinatorial components of $\mathcal{P}_{B \bar{B}, q \bar{q}}\left(m_{k}\right)$ and for $\mathcal{P}_{q \bar{q}}(\Delta E)$; quadratic functions for $\mathcal{P}_{j}\left(\left|\mathcal{H}_{\omega}\right|\right)$ and $\mathcal{P}_{j}\left(\mathcal{H}_{\rho^{+}}\right)$; and a Gaussian of different widths below and above the peak, plus a broad Gaussian, for $\mathcal{P}_{j}(\mathcal{F})$. The $q \bar{q}$ background in $m_{\mathrm{ES}}$ is described by the function $x \sqrt{1-x^{2}} \exp \left[-\xi\left(1-x^{2}\right)\right]$, with $x \equiv 2 m_{\mathrm{ES}} / \sqrt{s}$ and parameter $\xi$. These are discussed in more detail in Ref. [23] and can be seen in Fig. 1 for the $B^{+} \rightarrow \eta \rho^{+}$decay.

We allow the parameters most important for the determination of the combinatorial background PDFs to

TABLE II: Number of events $N$ in the sample, fitted signal yield $Y_{S}$ in events (ev.) with statistical error, measured bias, detection efficiency $\epsilon$, daughter branching fraction product ( $\prod_{\mathcal{B}}^{i}$ ), and measured branching fraction $\mathcal{B}$ with statistical error for each decay chain, and the measured charge asymmetry $\mathcal{A}_{c h}$ for the decay $B^{+} \rightarrow \eta \rho^{+}$. For the combined measurements the significance $\mathcal{S}$ (with systematic uncertainties included), branching fraction with statistical and systematic error, and in parentheses the $90 \%$ C.L. upper limits.

| Mode | $N$ (ev.) | $Y_{S}(\mathrm{ev}$. | Bias (ev.) | $\epsilon(\%)$ | П $\mathcal{B}_{i}(\%)$ | $\mathcal{S}(\sigma)$ | $\mathcal{B}\left(10^{-6}\right)$ |  | $\mathcal{A}_{\text {ch }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\overline{\eta \rho^{+}}$ |  |  |  |  |  | 9.0 | $9.9 \pm 1.2 \pm 0.8$ |  | $\mathbf{0 . 1 3} \pm 0.11 \pm 0.02$ |
| $\eta_{\gamma \gamma} \rho^{+}$ | 104609 | $326_{-42}^{+44}$ | $17 \pm 9$ | 16.7 | 39.4 |  | $10.2 \pm 1.4$ |  | $0.07 \pm 0.12$ |
| $\eta_{3 \pi} \rho^{+}$ | 47918 | $123_{-26}^{+27}$ | $13 \pm 7$ | 11.7 | 22.6 |  | $9.1 \pm 2.2$ |  | $0.28 \pm 0.21$ |
| $\eta^{\prime} \eta$ |  |  |  |  |  | 1.4 | $\mathbf{0 . 5} \pm \mathbf{0 . 4} \pm \mathbf{0 . 1}$ | (<1.2) |  |
| $\eta_{\eta \pi \pi}^{\prime} \eta_{\gamma \gamma}$ | 2191 | $8.8{ }_{-5.1}^{+6.4}$ | $0.9 \pm 0.5$ | 25.6 | 6.9 |  | $1.0{ }_{-0.6}^{+0.8}$ |  |  |
| $\eta_{\eta \pi \pi}^{\prime} \eta_{3 \pi}$ | 896 | $3.22_{-4.1}^{+5.1}$ | $0.2 \pm 0.2$ | 16.7 | 4.0 |  | $1.0{ }_{-1.4}^{+1.7}$ |  |  |
| $\eta_{\rho,}^{\prime} \eta_{\gamma \gamma}$ | 39723 | $0.7_{-8.6}^{+12.2}$ | $0.0 \pm 0.5$ | 25.6 | 11.6 |  | $0.1_{-0.6}^{+0.7}$ |  |  |
| $\eta_{j} \eta_{\rho \gamma}^{\prime} \eta_{3 \pi}$ | 20672 | $0.7_{-6.8}^{+9.4}$ | $2.0 \pm 1.0$ | 18.2 | 6.7 |  | $0.9-0.2_{-1.2}^{+1.7}$ |  |  |
| $\eta \pi^{0}$ |  |  |  |  |  | 2.2 | $0.9 \pm 0.4 \pm 0.1$ | ( $<1.5$ ) |  |
| $\eta_{\gamma \gamma} \pi^{0}$ | 9085 | $18.6{ }_{-21.7}^{+23.9}$ | $4.4 \pm 2.2$ | 20.5 | 39.4 |  | $0.4 \pm 0.6$ |  |  |
| $\eta_{3 \pi} \pi^{0}$ | 4030 | $23.3_{-11.1}^{+12.5}$ | $1.7 \pm 0.9$ | 17.3 | 22.6 |  | $1.33_{-0.6}^{+0.7}$ |  |  |
| $\eta^{\prime} \pi^{0}$ |  |  |  |  |  | 3.1 | $\mathbf{0 . 9} \pm \mathbf{0 . 4} \pm \mathbf{0 . 1}$ | (<1.5) |  |
| $\eta_{\eta \pi \pi}^{\prime} \pi^{0}$ | 3784 | $20.6{ }_{-8.0}^{+9.4}$ | $1.8 \pm 0.9$ | 22.5 | 17.5 |  | $1.1 .{ }_{-0.4}^{+0.5}$ |  |  |
| $\eta_{\rho \gamma}^{\prime} \pi^{0}$ | 19789 | $12.22_{-16.3}^{+18.4}$ | $2.7 \pm 1.4$ | 18.9 | 29.5 |  | $0.4_{-0.6}^{+0.7}$ |  |  |
| $\omega \pi^{0}$ | 39822 | $2.4{ }_{-16.8}^{+19.9}$ | $0.5 \pm 0.5$ | 18.4 | 89.1 | 0.3 | $0.07 \pm 0.26 \pm 0.02$ | ( $<0.5$ ) |  |

vary in the fit, along with the yields for all components. Specifically, the free background parameters are most or all of the following, depending on the decay mode: $\xi$ for $m_{\mathrm{ES}}$, linear and quadratic coefficients for $\Delta E$, area and slope of the combinatorial component for $m_{k}$, and the mean, width, and width difference parameters for $\mathcal{F}$. Results for the signal yields are presented in the third column of Table II for each sample.

We test and calibrate the fitting procedure by applying it to ensembles of simulated experiments composed of $q \bar{q}$ events drawn from the PDF, into which we have embedded the expected number of signal and charmless $B \bar{B}$ background events randomly extracted from the fully simulated MC samples. We find biases of $0-17$ events, somewhat dependent on the signal yield. The bias values obtained for simulations that reproduce the yields found in the data are given in the fourth column of Table II. Figure 1 shows PDFs and projections of subsamples of the data, enriched with a threshold requirement on the signal likelihood (computed without the variable plotted) for the $B^{+} \rightarrow \eta \rho^{+}$decay. Figure 2 shows projections for the other four modes.

We determine the reconstruction efficiencies, given in Table II, as the ratio of reconstructed and accepted events in simulation to the number generated. We compute the branching fraction for each channel by subtracting the fit bias from the measured yield, and dividing the result by the efficiency and the number of produced $B \bar{B}$ pairs [23]. We assume that the branching fractions of the $\Upsilon(4 S)$ to $B^{+} B^{-}$and $B^{0} \bar{B}^{0}$ are each equal to $50 \%$. Table II gives the numbers pertinent to these computations.

We combine results where we have multiple de-
cay channels by adding for each channel the function $-2 \ln \left\{\left[\mathcal{L}(\mathcal{B}) / \mathcal{L}\left(\mathcal{B}_{0}\right)\right] \otimes G\left(\mathcal{B} ; 0, \sigma^{\prime}\right)\right\}$, where $\mathcal{B}_{0}$ is the central value from the fit, $\sigma^{\prime}$ is the part of the systematic uncertainty uncorrelated with other channels, and $\otimes G$ denotes convolution with a Gaussian function; the part of the systematic uncertainty common to all channels is then added in quadrature. We give the resulting final branching fractions for each mode in Table II with the significance, taken as the square root of the difference between the value of $-2 \ln \mathcal{L}(\mathcal{B})$ (with only additive systematic uncertainties included) for zero signal and the value at its minimum. The $90 \%$ confidence level (C.L.) upper limits are taken to be the branching fraction below which lies $90 \%$ of the total of the likelihood integral in the positive branching fraction region.

The systematic uncertainties on the branching fractions arising from lack of knowledge of the PDFs have been included in part in the statistical error since most background parameters are free in the fit. For the signal, the uncertainties in PDF parameters are estimated from the consistency of fits to MC and data in control modes. Varying the signal-PDF parameters within these errors, we estimate yield uncertainties of 0.3-7 events, depending on the decay mode. The uncertainty from fit bias (Table II) includes the statistical uncertainty from the simulated experiments added in quadrature with one-half of the fit-bias correction. We estimate the uncertainty from modeling the charmless $B \bar{B}$ backgrounds by accounting for the uncertainties in the knowledge of their branching fractions. These additive errors are the largest systematic errors for the modes with small signal yield (but not $\left.B^{+} \rightarrow \eta \rho^{+}\right)$.


FIG. 1: Signal-enhanced projections for $\eta_{\gamma \gamma} \rho^{+}$(left) and $\eta_{3 \pi} \rho^{+}$(right) for (a,g) $m_{\mathrm{ES}},(\mathrm{b}, \mathrm{h}) \Delta E,(\mathrm{c}, \mathrm{i}) \mathcal{F},(\mathrm{d}, \mathrm{j}) m_{\eta},(\mathrm{e}, \mathrm{k}) m_{\rho}$, (f,l) $\mathcal{H}_{\rho}$. The total ( $q \bar{q}$ plus $B \bar{B}$ ) background fit function is shown as blue dot-dashed, signal as magenta dashed, and the total as a solid blue line. These plots are made with a minimum requirement on the likelihood that has an efficiency for signal of $15-35 \%$ while reducing the background by between two and three orders of magnitude.

Uncertainties in our knowledge of the efficiency, found from auxiliary studies, include $0.4 \% \times N_{t}$ and $1.5 \% \times N_{\gamma}$, where $N_{t}$ and $N_{\gamma}$ are the number of tracks and photons, respectively, in the $B$ candidate. The uncertainty in the total number of $B \bar{B}$ pairs in the data sample is $1.1 \%$. Published data [20] provide the uncertainties in the $B$ daughter product branching fractions ( $0.7-3.9 \%$ ). The uncertainties in the efficiency from the event selection are about $0.5 \%$.

We observe the decay $B^{+} \rightarrow \eta \rho^{+}$with a significance of 9 standard deviations. The branching fraction ( $9.9 \pm$ $1.2 \pm 0.8) \times 10^{-6}$ and charge asymmetry $0.13 \pm 0.11 \pm 0.02$ are in good agreement with the theoretical expectations. We do not find evidence for the other four decays though the sensitivity of these measurements is now comparable to the range of the theoretical estimates.

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FIG. 2: Signal-enhanced projections of the $B^{0}$-candidate $m_{\text {ES }}$ and $\Delta E$ mass for (a, b) $B^{0} \rightarrow \eta^{\prime} \eta$, (c, d) $B^{0} \rightarrow \eta \pi^{0}$, (e, f) $B^{0} \rightarrow \eta^{\prime} \pi^{0}$, and $(\mathrm{g}, \mathrm{h}) B^{0} \rightarrow \omega \pi^{0}$. Points with errors represent data, solid curves the full fit functions (both signal modes combined), dot-dashed curves the background functions (the peaking $B \bar{B}$ background component is small), and dashed curve the fit signal function. These plots are made with a minimum requirement on the likelihood that has an efficiency for signal of 45-75\%.
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