# MEASUREMENT OF THE FORM FACTORS IN THE DECAY $K_{I}^{O} \rightarrow \pi \mu \nu^{*}$

G. Donaldson, D. Fryberger, D. Hitlin, J. Liu, B. Meyer<sup>\*\*</sup>, R. Piccioni<sup>\*\*\*</sup>, A. Rothenberg<sup>†</sup>, D. Uggla, and S. Wojcicki<sup>††</sup>

> Physics Department and Stanford Linear Accelerator Center Stanford University, Stanford, California 94305

> > D. Dorfan ††

Physics Department University of California Santa Cruz, California 95060

### ABSTRACT

A Dalitz plot of  $1.6 \times 10^6 \text{ K}_{\text{L}}^0 \rightarrow \pi \mu \nu$  decays has been studied to measure the t dependence of the vector and scalar form factors. The observed slopes,  $\lambda_+ = 0.030 \pm 0.003 \text{ and } \lambda_0 = 0.020 \pm 0.003$ , are compatible with current algebra and soft pion predictions,  $\mu$  - e universality, and K\* (890) dominance of the vector form factor.

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\*\* Present Address: Weizmann Institute of Science, Rehovoth, Israel

\*\*\* Present Address: Harvard University, Cambridge, Mass. 02138

† Present Address: Rockefeller University, New York, N.Y. 10021

†† Alfred P. Sloan Foundation Fellow

We present herewith the analysis of an experiment performed at the Stanford Linear Accelerator Center, in which the Dalitz plot of  $1.6 \times 10^6 K_{\mu 3}^0$  decays was studied to extract the strong interaction form factors of the decay.

With the assumption of V-A Cabibbo theory and time-reversal invariance, the matrix element for  $K_{L}^{0} \rightarrow \pi \mu \nu$  decay may be written in terms of two real form factors  $f_{+}$  and  $f_{-}$ , which depend only on t, the square of the four-momentum transfer to the lepton pair:

$$M \propto \left[ \bar{u}_{\ell} \gamma_{\mu} (1 + \gamma_{5}) u_{\nu} \right] \left[ f_{+}(t) (p_{K} + p_{\pi}) + f_{-}(t) (p_{K} - p_{\pi}) \right] ,$$

where  $t = (p_K - p_{\pi})^2$ . The Dalitz plot distribution is usually written in terms of  $f_+(t)$  and  $\xi(t) = f_-(t)/f_-(t)$ . We have chosen, however, to analyze the Dalitz plot distribution using the form factors  $f_+(t)$  and  $f_0(t) = f_+(t) + \left[t/(m_K^2 - m_{\pi}^2)\right]f_-(t)$ , which represent the vector and scalar exchange amplitudes respectively. These form factors are more directly related to theoretical predictions, and are less strongly correlated. The Dalitz plot distribution is then given by

$$\frac{d^{2}N(E_{\pi}, E_{\mu})}{dE_{\pi}dE_{\mu}} = \alpha f_{+}(t)^{2} + \beta f_{+}(t) f_{0}(t) + \gamma f_{0}(t)^{2},$$

where  $\alpha$ ,  $\beta$  and  $\gamma$  are kinematic factors. Note that since the form factors are functions only of t, their t dependence may be extracted without prior parametrization by analyzing the Dalitz plot in bands of constant  $E_{\pi}$ .

The t dependence of  $f_+$  and  $f_0$  is expected to be understood in terms of poles of definite mass which saturate the dispersion relations for these form factors. Further, with the assumption that the eight vector and axial-vector currents of the weak interactions form a chiral SU(3)  $\otimes$  SU(3) algebra, and using the PCAC hypothesis, the value <u>and</u> slope of  $f_0$  at unphysical points are predicted to be<sup>1,2</sup>

$$f_0(m_K^2) = f_K / f_{\pi} = (1.27 \pm 0.03) f_+(0),$$

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and

$$m_{\pi}^{2} \frac{df_{0}}{dt} \Big|_{t = m_{K}^{2} + m_{\pi}^{2}} = \frac{m_{\pi}^{2}}{2(m_{K}^{2} - m_{\pi}^{2})} \left(\frac{f_{K}}{f_{\pi}} - \frac{f_{\pi}}{f_{K}}\right) = 0.021 \pm 0.003$$

respectively, in the limit of vanishing pion mass. These results are expected to be valid to 10% for the physical pion. The history of the experimental determination of these form factors has been confusing: the recent review of Chounet, Gaillard and Gaillard<sup>3</sup> attempted to bring some order to the situation, concluding that the current algebra and PCAC ideas, which have been successful in other areas, were not in agreement with  $K_{\mu3}$  data.

This experiment was performed at the SLAC K<sup>o</sup> spectrometer facility<sup>4</sup>, concurrent with the measurement of the charge asymmetry in  $K_{L}^{o} \rightarrow \pi^{\mp} \mu^{\pm} \nu$ decay<sup>5</sup>. Briefly, some features of the experiment are: 1) A high energy  $K_{L}^{o}$ beam with low neutron contamination, 2) Determination of the  $K_{L}^{o}$  momentum by time-of-flight measurement, 3) Momentum analysis of charged decay products with a 12.6 kG-m magnet, 4) A muon filter consisting of 7.7 interaction lengths of lead, and 5) A resolution on the Dalitz plot compatible with 5 × 5 MeV binning.

A sample of  $0.8 \times 10^6$  accepted Monte Carlo events was used to determine the detection efficiency as a function of position on the Dalitz plot, and to search for biases in the data. The Monte Carlo program generated tapes in the same format as raw data tapes; these were then processed through the same analysis programs as the data. Although the results are insensitive to the form factors used in the Monte Carlo, the latter were chosen to correspond to the experimentally observed values. The momentum spectrum of the  $K^{0}_{L}$  beam was initially derived from a sample of  $K^{0}_{L} \rightarrow \pi^{+}\pi^{-}\pi^{0}$  decays obtained with a looser trigger, and later refined by comparison with the actual  $K^{0}_{L} \rightarrow \pi \mu \nu$  decays.

Several sources of contamination were investigated. The  $\pi \rightarrow \mu \nu$  decays

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following  $K_{\pi3}^{o}$ ,  $K_{e3}^{o}$ ,  $K_{\mu3}^{o}$  and  $K_{\pi2}^{o}$  decays were studied by Monte Carlo. The subtraction of such events amounted to about 5% of the data remaining after the  $P_{0}^{\prime 2}$  cut, which was used to reject a majority of the  $K_{\pi3}^{o}$  decays. Pion penetration was less than 0.1%, as demonstrated by the excellent agreement between the number of  $2\mu$  events (mostly  $K_{\mu3}^{o}$  followed by  $\pi$  decay) in the data and Monte Carlo. Decays of  $K_{L}^{o}$ 's which had diffractively scattered before the decay volume were also subtracted. This 1% correction had no noticeable effect on the results, but did significantly improve the agreement of some of the experimental distributions with the Monte Carlo.  $K_{L}^{o}$  interactions in helium were investigated by taking separate data with a 1" thick carbon slab at several positions within the decay volume. Less than 0.1% of the accepted data were due to interactions and such events were evenly distributed over the Dalitz plot.

A detailed study was made to look for systematic differences between the data and the Monte Carlo, particularly with respect to geometrical biases in the wire chambers which could directly affect the Dalitz plot. No such discrepancies were found. A comparison of several experimental and Monte Carlo distributions is shown in Fig. 1.

The Dalitz plot analysis is complicated by a quadratic ambiguity associated with the transformation of the charged decay products to the  $K_L^o$  rest frame. In principle, the  $K_L^o$  time-of-flight measurement can resolve this ambiguity, but because of the high momentum of our beam, this information alone was insufficient for part of the data. Hence the beam momentum spectrum information was also used. Monte Carlo studies indicated that this procedure chose the correct solution for 80% of the data. The same procedure has been applied to the Monte Carlo events, and a detailed study indicates that no bias is introduced.

Radiative corrections which take into account the resolution and efficiency

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of the apparatus were applied to the data. We used the virtual corrections of Ginsberg<sup>6</sup>, but calculated the inner bremsstrahlung contribution by generating a large sample of Monte Carlo  $K_{L}^{0} \rightarrow \pi\mu\nu\gamma$  events according to the matrix element of Fearing, Fischbach and Smith<sup>7</sup>, and subsequently analyzing them as  $K_{\mu3}^{0}$  decays. This treatment of radiative corrections significantly reduced the anomalous behavior of  $f_{0}$  at low t as presented in a preliminary report of these data.<sup>8</sup>

We have made unparametrized fits to the data, as well as a 2-parameter fit assuming linear t dependence of  $f_+$  and  $f_0$  with  $f_0(0) \equiv f_+(0)$ . Excellent fits to the data have been obtained by both methods. The results are shown in Table 1 and Fig. 2. The errors quoted in  $\lambda_+$  and  $\lambda_0$  derived from the 2-parameter fit are twice the statistical error, to allow for possible systematic effects.

#### TABLE I

Fit	x <sup>2</sup>	Deg. of Freedom	$\lambda_{+}$	λ <sub>0</sub>
Unparametrized	332	352	$0.032 \pm 0.004$	$0.017 \pm 0.005$
2-parameter fit	396	398	$0.030 \pm 0.003$	$0.020 \pm 0.003$

We have investigated the variation of  $\lambda_{+}$  and  $\lambda_{0}$  among many subsets of the data, such as low, medium and high  $K_{L}^{0}$  momenta, pion charge, inbending and outbending topology, and low, medium and high muon center-of-mass energy. In addition, two subsets involving the quadratic ambiguity were also examined, containing either events in which one solution was at least twenty times more probable than the other, or events in which both solutions fell in the same  $5 \times 5$  MeV bin on the Dalitz plot. None of these subsets yielded results which differed significantly from those obtained with the entire sample.

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In conclusion, we find that both the vector and scalar form factors in  $K_{\mu3}^{0}$  decay exhibit a linear t dependence in the physical region, with slopes  $\lambda_{+} = 0.030 \pm 0.003$  and  $\lambda_{0} = 0.020 \pm 0.003$  respectively. This value of  $\lambda_{+}$  is consistent with K\*(890) dominance of the vector form factor, <sup>9</sup> and with the current world averages for  $\lambda_{+}$  as determined in studies of  $K_{e3}$  decay, in accord with  $\mu$ -e universality<sup>10</sup>. An extrapolation of  $f_{0}$  using  $\lambda_{0} = 0.020$  yields a value of  $(1.25 \pm 0.04) f_{+}(0)$  at  $t = m_{K}^{2}$ , in excellent agreement with the Callan-Treiman-Mathur-Okubo-Pandit current algebra prediction. Further, the extrapolated slope of  $f_{0}$  confirms the prediction of Dashen and Weinstein. The traditional parameter  $\xi$  is found by a separate unparametrized fit to be  $0.01 \pm 0.04$ , and to be independent of t. Our experimental results thus support the hypotheses that chiral SU(3)  $\otimes$  SU(3) and SU(2)  $\otimes$  SU(2) are good symmetries of the strong interactions, and that symmetry breaking terms are small.

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9.	If the vector form factor is given by K* dominance, $f_{+} = m_{K*}^2 / (m_{K*}^2 - t)$ ,
	then our data should yield $\lambda_{+} = 0.029$ if the linear parametrization is
	used. We are grateful to Prof. J. J. Sakurai for a stimulating comment
	on this point.
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	Energy Physics, Chicago, 1972.

#### Figure Captions

- 1. Comparison of several experimental (solid lines) and Monte Carlo distributions (dots). (a) Laboratory muon momentum. (b) Difference between the transverse momentum of the neutrino and the total momentum of the neutrino in the  $K_L^0$  rest frame; the accepted data were required to lie to the left of the dotted lines. (c) Absolute value of the direction cosine of the the pion in the horizontal plane in the rear chambers. (d) Missing mass squared. (e)  $\pi$ - $\mu$  opening angle in the laboratory system. (f) Decay vertex distribution along the beam direction.
- 2. The values of (a) vector form factor normalized to unity at t=0, (b) scalar form factor, and (c)  $\xi$  parameter as obtained from the unparametrized fits. The Callan-Treiman point was not used in the fit. The solid line indicates the best linear fit in (a) and (b), and the best fit to a constant in (c). The unparametrized fit yields  $f_0(0)/f_+(0) = 1.06 \pm 0.03$ . We do not take this difference from unity to be significant, in view of the quality of the 2-parameter fit with the constraint  $f_0(0)/f_+(0) = 1$ .



Fig. 1



Fig. 2

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