# Measurement of Time-Dependent $C P$-Violating Asymmetries in $B^{0}$ Meson Decays to $\eta^{\prime} K_{L}^{0}$ 

The BABAR Collaboration

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#### Abstract

We present a preliminary measurement of $C P$-violating parameters $S$ and $C$ from fits of the time-dependence of $B^{0}$ meson decays to $\eta^{\prime} K_{L}^{0}$. The data were recorded with the BABAR detector at PEP-II and correspond to $232 \times 10^{6} B \bar{B}$ pairs produced in $e^{+} e^{-}$annihilation through the $\Upsilon(4 S)$ resonance. By fitting the time-dependent $C P$ asymmetry of the reconstructed $B^{0} \rightarrow \eta^{\prime} K_{L}^{0}$ events, we find $S=0.60 \pm 0.31 \pm 0.04$ and $C=0.10 \pm 0.21 \pm 0.03$, where the first error quoted is statistical and the second is systematic. We also perform a combined fit using both $\eta^{\prime} K_{S}^{0}$ and $\eta^{\prime} K_{L}^{0}$ data, and find $S=0.36 \pm 0.13 \pm 0.03$ and $C=-0.16 \pm 0.09 \pm 0.02$.


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## 1 Introduction

Decays of $B^{0}$ mesons to charmless hadronic final states such as $\phi K^{0}, K^{+} K^{-} K^{0}, \eta^{\prime} K^{0}, \pi^{0} K^{0}$ and $f_{0}(980) K^{0}$ proceed mostly via a single penguin (loop) amplitude with the same weak phase as in $B$ decays to a charmonium state plus a $K^{0}$ meson [1, 2]. However Cabibbo-Kobayashi-Maskawa (CKM)-suppressed amplitudes and new particles in the loop can introduce other weak phases whose contribution is not negligible [1, 3].

Fig. 1(a) shows the diagram describing the $B-\bar{B}$ mixing. The amplitudes shown in Fig. 1(b)(d) are relevant for the decay $B^{0} \rightarrow \eta^{\prime} K^{0}$. All of the amplitudes are suppressed by small CKM matrix elements, but the tree diagram for $B^{0}$ shown in Fig. 1(d) is expected to be smaller [2, 4] since there is additional CKM suppression and color suppression.


Figure 1: Feynman diagrams describing (a) $B-\bar{B}$ mixing, the decay $B^{0} \rightarrow \eta^{\prime} K^{0}$ via (b, c) internal gluonic penguin and (d) color-suppressed tree.

For the decay $B^{0} \rightarrow \eta^{\prime} K^{0}$, the additional contributions of other weak phases from CKMsuppressed amplitudes are expected to be small, so the time-dependent $C P$ asymmetry measurement provides an approximate measurement of $\sin 2 \beta$. We define $S$ and $C$ as the coefficients of sine and cosine oscillation terms, respectively, in the $B \bar{B}$ decay rate distributions (see Eqn. (1) below). $\Delta S$ is the deviation between $S$ in the decay $B^{0} \rightarrow \eta^{\prime} K^{0}$ and $S$, equal to $\sin 2 \beta$, in the charmonium $K^{0}$ decays. Theoretical bounds for this deviation have been calculated with an $\mathrm{SU}(3)$ analysis $[5,6]$. Such bounds have been improved [7] by the measurements of $B^{0}$ decays to a pair of neutral charmless light pseudoscalar mesons $[8,9]$, with the conclusion that $\Delta S$ is expected to be less than 0.10 (with a theoretical uncertainty less than $\sim 0.03$ due to the assumptions in the calculation). QCD factorization calculations conclude that $\Delta S$ is even smaller [10]. A significantly larger value of $\Delta S$ could arise from non-Standard-Model amplitudes [3].

The $C P$-violating asymmetry in the decay $B^{0} \rightarrow \eta^{\prime} K^{0}$ has been measured previously by the $B A B A R$ [11] and Belle [12] experiments using the final state $\eta^{\prime} K_{S}^{0}$. In the measurement presented in this paper we use events reconstructed in the $\eta^{\prime} K_{L}^{0}$ final state. We present also the measurement
of $C P$-violating asymmetry combining present $\eta^{\prime} K_{L}^{0}$ data with the $\eta^{\prime} K_{S}^{0}$ data used in the previous BABAR measurement [11].

## 2 The BABAR Detector and Dataset

The results presented in this paper are based on data collected in 1999-2004 with the BABAR detector [13] at the PEP-II asymmetric $e^{+} e^{-}$collider [14] located at the Stanford Linear Accelerator Center. An integrated luminosity of $211 \mathrm{fb}^{-1}$, corresponding to about 232 million $B \bar{B}$ pairs, was recorded at the $\Upsilon(4 S)$ resonance ("on-resonance", center-of-mass energy $\sqrt{s}=10.58 \mathrm{GeV}$ ).

The asymmetric beam configuration in the laboratory frame provides a boost of $\beta \gamma=0.56$ to the $\Upsilon(4 S)$. Charged particles are detected and their momenta measured by the combination of a silicon vertex tracker (SVT), consisting of five layers of double-sided detectors, and a 40-layer central drift chamber, both operating in the 1.5 T magnetic field of a solenoid. The tracking system covers $92 \%$ of the solid angle in the center-of-mass (CM) frame.

Charged-particle identification (PID) is provided by the average energy loss $(\mathrm{d} E / \mathrm{d} x)$ in the tracking devices and by an internally reflecting ring-imaging Cherenkov detector (DIRC) covering the central region. A $K / \pi$ separation of better than four standard deviations $(\sigma)$ is achieved for momenta below $3 \mathrm{GeV} / c$, decreasing to $2.5 \sigma$ at the highest momenta in the $B$ decay final states. Photons and electrons are detected by a $\mathrm{CsI}(\mathrm{Tl})$ electromagnetic calorimeter (EMC). The EMC provides good energy and angular resolutions for detection of photons in the range from 30 MeV to 4 GeV . The energy and angular resolutions are $3 \%$ and 4 mrad , respectively, for a 1 GeV photon.

The flux return (IFR) for the solenoid is composed of multiple layers of iron and resistive plate chambers for the identification of muons and long-lived neutral hadrons.

## 3 Event Selection and Analysis Method

Monte Carlo (MC) simulations of the signal decay modes, $B \bar{B}$ backgrounds, and detector response are used to establish the event selection criteria. We reconstruct $\eta^{\prime}$ mesons through the decays $\eta^{\prime} \rightarrow \rho^{0} \gamma\left(\eta_{\rho \gamma}^{\prime}\right)$ and $\eta^{\prime} \rightarrow \eta \pi^{+} \pi^{-}\left(\eta_{\eta \pi \pi}^{\prime}\right)$ with $\eta \rightarrow \gamma \gamma$. The photon energy $E_{\gamma}$ in laboratory system must be greater than 50 MeV for $\eta$ candidates, and greater than 200 MeV in $\eta_{\rho \gamma}^{\prime}$. We make the following requirements on the invariant masses (in $\mathrm{MeV} / c^{2}$ ): $490<m_{\gamma \gamma}<600$ for $\eta, 510<m_{\pi \pi}<$ 1000 for $\rho^{0}, 945<m_{\eta \pi \pi}<970$ for $\eta_{\eta \pi \pi}^{\prime}$, and $930<m_{\rho \gamma}<980$ for $\eta_{\rho \gamma}^{\prime}$. We require the PID information of the signal pions to be consistent with the pion hypothesis.

Signal $K_{L}^{0}$ candidates are reconstructed from clusters of energy deposited in the EMC or from hits in the IFR not associated to any charged track in the event. Because the energy of the $K_{L}^{0}$ is not measured, we determine the $K_{L}^{0}$ candidate laboratory momentum from its flight direction determined from the $\eta^{\prime}$ vertex and the centroid of the EMC (or IFR) candidate and the constraints of $K_{L}^{0}$ and $B^{0}$ masses to their nominal values [15].

A $B$ meson candidate is characterized kinematically by the energy difference $\Delta E \equiv E_{B}^{*}-\frac{1}{2} \sqrt{s}$, where $E_{B}^{*}$ is the CM energy of the $B$ meson. Signal events are peaked within $\pm 10 \mathrm{MeV}$ of $\Delta E=0$ while background events extend towards positive values of $\Delta E$ (this is a consequence of the mass constraint used to determine the $K_{L}^{0}$ momentum). We require $-0.01<\Delta E<0.08 \mathrm{GeV}$. This choice is dictated by the need of preserving a region with enough background for a fit to that component.

To reject background due to continuum $e^{+} e^{-} \rightarrow q \bar{q}$ events ( $q=u, d, s, c$ ), we make use of the angle $\theta_{T}$ between the thrust axis of the $B$ candidate and that of the rest of the tracks and neutral
clusters in the event, calculated in the center-of-mass frame. The distribution of $\cos \theta_{T}$ is sharply peaked near $\pm 1$ for combinations drawn from jet-like $q \bar{q}$ pairs and is nearly uniform for the isotropic $B$ meson decays; we require $\left|\cos \theta_{T}\right|<0.8$ in the $\eta^{\prime} \rightarrow \eta \pi^{+} \pi^{-}$subdecay mode and $\left|\cos \theta_{T}\right|<0.75$ in the $\eta^{\prime} \rightarrow \rho^{0} \gamma$ subdecay.

For further suppression of continuum background we require that the total missing transverse momentum projected along the $K_{L}^{0}$ direction, where the total momentum is calculated with all charged tracks and neutral clusters (without the $K_{L}^{0}$ ), is no more than $0.45 \mathrm{GeV} / c$ lower than the calculated transverse momentum of the $K_{L}^{0}$ candidate. We also require that the cosine of the polar angle $\theta$ of the total missing momentum in laboratory system to be less than 0.95 .

The purity of the $K_{L}^{0}$ candidates reconstructed in the EMC is further improved by a cut on the output of a neural network (NN) that takes cluster-shape variables as its inputs. The NN was trained using MC signal events and data events in the side band distribution (defined as $0.04<\Delta E<0.08 \mathrm{GeV})$. We validated the performance of the NN using $K_{L}^{0}$ candidates in the reconstructed $B^{0} \rightarrow J / \psi K_{L}^{0}$ events.

All selection criteria have been chosen using MC signal and background events to maximize the expected statistical significance of signal yield in the data.

The $B \bar{B}$ backgrounds were estimated using Monte Carlo simulations of $B^{0} \bar{B}^{0}$ and $B^{+} B^{-}$. We found a small evidence of $B \bar{B}$ background from $b \rightarrow c$ decays in the sub-decay mode $\eta^{\prime} \rightarrow \rho^{0} \gamma$, so we added this component to the fit.

For each $B^{0} \rightarrow \eta^{\prime} K_{L}^{0}$ candidate ( $B_{C P}$ ), we reconstruct the decay vertex of the other $B$ meson $\left(B_{\mathrm{tag}}\right)$ from the remaining charged tracks in the event and identify its flavor. The time difference $\Delta t \equiv t_{C P}-t_{\mathrm{tag}}$, where $t_{C P}$ and $t_{\mathrm{tag}}$ are the proper decay times of the $B_{C P}$ and $B_{\mathrm{tag}}$, respectively, is obtained from the measured distance between the $B_{C P}$ and $B_{\text {tag }}$ decay vertices and from the boost ( $\beta \gamma=0.56$ ) of the $e^{+} e^{-}$beam system. The distribution of $\Delta t$ is:

$$
\begin{equation*}
F(\Delta t)=\frac{e^{-|\Delta t| / \tau}}{4 \tau}\left\{1 \mp \Delta \omega \pm(1-2 \omega)\left[-\eta S \sin \left(\Delta m_{d} \Delta t\right)-C \cos \left(\Delta m_{d} \Delta t\right)\right]\right\} \tag{1}
\end{equation*}
$$

where the upper (lower) sign denotes a decay accompanied by a $B^{0}\left(\bar{B}^{0}\right)$ tag, $\tau$ is the mean $B^{0}$ lifetime, $\Delta m_{d}$ is the mixing frequency, $\eta$ is the $C P$ eigenvalue of the final state $(\eta=+1$ for $\eta^{\prime} K_{L}^{0}, \eta=-1$ for $\eta^{\prime} K_{S}^{0}$ ) and the mistag parameters $\omega$ and $\Delta \omega$ are the average and difference, respectively, of the probabilities that a true $B^{0}\left(\bar{B}^{0}\right)$ meson is tagged as $\bar{B}^{0}\left(B^{0}\right)$. The tagging algorithm, based on six tagging categories, is an improved version of what was used in the previous $B A B A R$ publication [11]. Separate neural networks are trained to identify primary leptons, kaons, soft pions from $D^{*}$ decays, and high-momentum charged particles from $B$ decays. Each event is assigned to one of the tagging categories based on the source of tagging information and on the estimated mistag probability. The distribution $F(\Delta t)$ is convolved with a resolution function to account for the finite vertex resolution of the detector.

## 4 Maximum Likelihood Fit

We use an unbinned, multivariate maximum-likelihood fit to extract signal yields and $C P$ violating parameters. We use the following discriminating variables: $\Delta E$, a Fisher discriminant $\mathcal{F}, \Delta t$. In the decay mode $\eta^{\prime} \rightarrow \rho^{0} \gamma$ we add the $\eta^{\prime}$ mass and the variable $\mathcal{H}$, defined as the cosine of the $\rho$ meson's rest frame decay angle of a pion with respect to the $\eta^{\prime}$ flight direction. The Fisher discriminant combines four variables: the angles with respect to the beam axis of the $B$ momentum and $B$ thrust
axis in the $\Upsilon(4 S)$ frame, and the zeroth and second angular moments of the energy flow excluding the $B$ candidate around the $B$ thrust axis.

We indicate with $j$ the event species: signal, continuum background, or $B \bar{B}$ background. For each species $j$ and each flavor-tagging category $c$, we define a total probability density function (PDF) for an events $i$ as:

$$
\begin{equation*}
\mathcal{P}_{j, c}^{i}=\mathcal{P}_{j}\left(\Delta E^{i}\right) \mathcal{P}_{j}\left(\mathcal{F}^{i}\right) \mathcal{P}_{j}\left(M_{\eta^{\prime}}^{i}\right) \mathcal{P}_{j}\left(\mathcal{H}^{i}\right) \mathcal{P}_{j}\left(\Delta t^{i}, \sigma_{\Delta t}^{i}, c\right) \tag{2}
\end{equation*}
$$

where $\sigma_{\Delta t}^{i}$ is the error on $\Delta t$ for an event $i$. We define the extended likelihood function for the $N_{c}$ input events in category $c$ as

$$
\begin{equation*}
\mathcal{L}_{c}=\exp \left(-\sum_{j} n_{j} f_{j, c}\right) \prod_{i}^{N_{c}}\left(n_{\mathrm{sig}} f_{\operatorname{sig}, c} \mathcal{P}_{\mathrm{sig}, c}^{i}+n_{q \bar{q}} f_{q \bar{q}, c} \mathcal{P}_{q \bar{q}}^{i}+n_{B \bar{B}} f_{B \bar{B}, c} \mathcal{P}_{B \bar{B}}^{i}\right) \tag{3}
\end{equation*}
$$

where $n_{j}$ is the number of events with species $j$, and $f_{j, c}$ is the fraction of category- $c$ events with species $j$. We fix $f_{\text {sig,c }}$ and $f_{B \bar{B}, c}$ to $f_{B_{f l a v}, c}$, the values measured with a sample of neutral $B$ decays to flavor eigenstates, $B_{\text {flav }}$.

The total likelihood function for all categories is given as the product of the likelihoods over the seven tagging categories (including a category for untagged events for yield determination).

## 5 Results

The reconstruction efficiency is $10.3 \%$ and $11.6 \%$ for $\eta_{\rho \gamma}^{\prime} K_{L}^{0}$ and $\eta_{\eta \pi \pi}^{\prime} K_{L}^{0}$ respectively. In Table 1 we give the number of the signal yield and the parameters $S$ and $C$. Note that the sign of the $C P$ eigenvalue of the final state is out of the definition of $S$ parameter (see Eqn. (1)), so $S$ parameter has the same sign in $\eta^{\prime} K_{S}^{0}$ and $\eta^{\prime} K_{L}^{0}$ events. The $\eta^{\prime} K_{S}^{0}$ data are those used in $B A B A R$ previous measurement [11]. Combining $\eta_{\eta \pi \pi}^{\prime} K_{L}^{0}$ events and $\eta_{\rho \gamma}^{\prime} K_{L}^{0}$ events, we measure $S=0.60 \pm 0.31$ and $C=0.10 \pm 0.21$. In this fit we have 42 free parameters: $S, C$, signal yields (2), $B \bar{B}$ background yield (1), continuum background yields (2) and fractions (12), background $\Delta t, \Delta E, \mathcal{F}, \eta^{\prime}$ mass and $\mathcal{H}$ PDF parameters (23). In the final fit, combining $\eta^{\prime} K_{S}^{0}$ and $\eta^{\prime} K_{L}^{0}$, we have 138 free parameters: $S, C$, signal yields (7), $B \bar{B}$ background yield (3), continuum background yields (7) and fractions (42), background $\Delta t, \Delta E, \mathcal{F}, \eta^{\prime}$ mass and $\mathcal{H}$ PDF parameters (77).

Table 1: Results with statistical errors for the $B^{0} \rightarrow \eta^{\prime} K^{0}$ time-dependent fits (decays with $K_{L}^{0}$ in upper part on the table and decays with $K_{S}^{0}$ in lower part of the table).

| Mode | Signal yield | $S$ | $C$ |
| :--- | :---: | ---: | ---: |
| $\eta_{\eta \pi \pi}^{\prime} K_{L}^{0}$ | $137 \pm 22$ | $0.38 \pm 0.44$ | $0.34 \pm 0.29$ |
| $\eta_{\rho \gamma}^{\prime} K_{L}^{0}$ | $303 \pm 49$ | $0.88 \pm 0.43$ | $-0.15 \pm 0.29$ |
| $\eta_{\eta}^{\prime}(\gamma \gamma) \pi \pi$ |  |  |  |
| $\eta_{\rho \gamma}^{\prime} K_{\pi^{+} \pi^{-}}^{0}$ | $188 \pm 15$ | $0.01 \pm 0.28$ | $-0.18 \pm 0.18$ |
| $\eta_{\eta(3 \pi) \pi \pi}^{\prime} K_{\pi^{+} \pi^{-}}^{0}$ | $430 \pm 26$ | $0.44 \pm 0.19$ | $-0.30 \pm 0.13$ |
| $\eta_{\eta(\gamma \gamma) \pi \pi}^{\prime} K_{\pi^{0} \pi^{0}}^{0}$ | $44 \pm 9$ | $0.79 \pm 0.47$ | $0.11 \pm 0.35$ |
| $\eta_{\rho \gamma}^{\prime} K_{\pi^{0} \pi^{0}}^{0}$ | $89 \pm 23$ | $-0.04 \pm 0.57$ | $-0.65 \pm 0.42$ |
| Combined fit | $1245 \pm 67$ | $0.36 \pm 0.68$ | $0.41 \pm 0.40$ |



Figure 2: The likelihood ratio $\mathcal{L}(S g) /[\mathcal{L}(S g)+\mathcal{L}(B g)]$ for $\eta_{\eta \pi \pi}^{\prime} K_{L}^{0}$ (left) and $\eta_{\rho \gamma}^{\prime} K_{L}^{0}$ (right). The points represent the on-resonance data, the histograms are from PDF generated events of background (blue area) and background plus signal (shaded red area).

The agreement between PDF simulated events and data is investigated using likelihood ratios. We generate signal and background Monte Carlo samples from the PDFs and, using the fitted parameter values from nominal fit, we calculate the likelihoods for both samples. In Fig. 2 we show the likelihood ratio $\mathcal{L}(S g) /[\mathcal{L}(S g)+\mathcal{L}(B g)]$ for the two sub-decays $\eta_{\rho \gamma}^{\prime} K_{L}^{0}$ and $\eta_{\eta \pi \pi}^{\prime} K_{L}^{0}$ for data and for the PDF generated events. In Fig. 3 we show the projection onto $\Delta E$ of a subset of the data for which the signal likelihood (computed without the plotted variable) exceeds a mode-dependent threshold that optimizes the sensitivity. We show in Fig. 4 the $\Delta t$ projection and asymmetry for $B^{0} \rightarrow \eta^{\prime} K_{L}^{0}$.

## 6 Systematic Uncertainties and Cross-checks

The contributions to the systematic uncertainties in $S$ and $C$ for $\eta^{\prime} K_{L}^{0}$ are summarized in Table 2.
We evaluate the uncertainties associated with the PDF shapes by variation of the parameters describing each discriminating variable. Systematic errors associated with signal parameters ( $\Delta t$ resolution function, tagging fractions, and dilutions) are determined by varying their values within their errors. Uncertainties due to $\Delta m_{d}$ and $\tau_{B}$ are obtained by varying these parameters by the uncertainty in their world average values [15]. All changes are combined in quadrature obtaining an error of 0.02 for $S$ and 0.01 for $C$.

We vary the SVT alignment parameters in the signal Monte Carlo events by the size of misalignments found in the real data, and assign the resulting shift in the fit results as the systematic error of 0.01 for both $S$ and $C$.

The systematic errors due to interference between the CKM-suppressed $\bar{b} \rightarrow \bar{u} c \bar{d}$ amplitude and the favored $b \rightarrow c \bar{u} d$ for some tag-side $B$ decays are found to be negligible for $S$ and gives a contribution to the $C$ uncertainty of about 0.01 .

The systematic error due to $B \bar{B}$ background is estimated to be 0.03 in $S$ and 0.01 in $C$


Figure 3: Projection onto $\Delta E$ for $B^{0} \rightarrow \eta^{\prime} K_{L}^{0}$ (sum of the sub-decay modes $\eta_{\rho \gamma}^{\prime} K_{L}^{0}$ and $\eta_{\eta \pi \pi}^{\prime} K_{L}^{0}$ ) of a subset of the data for which the signal likelihood (computed without the plotted variable) exceeds a mode-dependent threshold that optimizes the sensitivity. Points with errors represent the data, solid curve the full fit functions and dashed blue curve the total background functions.


Figure 4: Projections onto $\Delta t$ for $\eta^{\prime} K_{L}^{0}$ (sum of the sub-decay modes $\eta_{\rho \gamma}^{\prime} K_{L}^{0}$ and $\eta_{\eta \pi \pi}^{\prime} K_{L}^{0}$ ) of a subset of the data for which the signal likelihood exceeds a mode-dependent threshold that optimizes the sensitivity. Points with errors represent the data, solide curve the full fit functions, and dashed blue curve the total background functions, for (a) $B^{0}$ and (b) $\bar{B}^{0}$ tagged events. The asymmetry between $B^{0}$ and $\bar{B}^{0}$ tags is shown in (c).
parameter. An uncertainty of 0.01 is assigned to account for limitations of Monte Carlo statistics and modeling of the signal. We assign an uncertainty of 0.01 to account for the uncertainty in the position and size of the beam spot, determined from variation of these quantities in signal MC. The total systematic error is obtained by summing individual errors in quadrature.

Table 2: Estimates of systematic errors for $\eta^{\prime} K_{L}^{0}$.

| Source of error | $\sigma(S)$ | $\sigma(C)$ |
| :--- | :---: | :---: |
| PDF Shapes | 0.02 | 0.01 |
| SVT alignment | 0.01 | 0.01 |
| Tag-side interference | 0.00 | 0.01 |
| $B \bar{B}$ Background | 0.03 | 0.01 |
| MC statistics/modeling | 0.01 | 0.01 |
| Beam spot | 0.01 | 0.01 |
| Total | 0.04 | 0.03 |

We have also performed a number of checks of our results. When we fit the combined sample $\eta^{\prime} K_{S}^{0}$ and $\eta^{\prime} K_{L}^{0}$ with the value for $C$ fixed to zero, we find $S=0.37 \pm 0.13$. We produce samples of pseudo-experiments generated with events produced to match the PDF distributions. From these samples, we verify that the fit bias on $S$ and $C$ is negligible and that there is a good agreement between expected and observed errors. The fit was also verified with our $B^{0} \rightarrow J / \psi K_{L}^{0}$ data sample.

## 7 Conclusion

In a sample of 232 million $B \bar{B}$ pairs we have reconstructed $137 \pm 22 \eta_{\eta \pi \pi}^{\prime} K_{L}^{0}$ events and $303 \pm 49$ $\eta_{\rho \gamma}^{\prime} K_{L}^{0}$ events. We use these events to measure the time-dependent asymmetry parameters $S$ and $C$ :

$$
\begin{aligned}
& S=0.60 \pm 0.31 \text { (stat) } \pm 0.04 \text { (syst) } \\
& C=0.10 \pm 0.21 \text { (stat) } \pm 0.03 \text { (syst) }
\end{aligned}
$$

Using this sample and the $\eta^{\prime} K_{S}^{0}$ sample found in Ref. [11], we obtain a total of $1245 \pm 67 \eta^{\prime} K^{0}$ events and with a combined fit of all data we measure:

$$
\begin{aligned}
& S=0.36 \pm 0.13 \text { (stat) } \pm 0.03 \text { (syst) } \\
& C=-0.16 \pm 0.09 \text { (stat) } \pm 0.02 \text { (syst) }
\end{aligned}
$$

All these results are preliminary. Our result for $S$ differs from the $B A B A R$ value of $\sin 2 \beta=$ $0.722 \pm 0.040 \pm 0.023$ in charmonium decays [16] by 2.8 standard deviation.

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