

## Charmless 2- and 3-body B decays and the angle $\alpha(\phi_2)$

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### Abstract

We present preliminary measurements of branching fractions and  $CP$ -asymmetry parameters in two- and three-body charmless hadronic  $B$  decays. The available data sample consists of 227 million  $\mathcal{T}(4S) \rightarrow B\bar{B}$  decays collected with the *BABAR* detector at the PEP-II asymmetric-energy  $e^+e^-$  collider at SLAC. We establish the observation of the decays  $B^0 \rightarrow \pi^0\pi^0$  and  $B^0 \rightarrow K^0\bar{K}^0$  and constrain the CKM angle  $\alpha$  with a full SU(2) isospin analysis in the  $B \rightarrow \pi\pi$  system and with a  $B^0 \rightarrow \pi^+\pi^-\pi^0$  time-dependent Dalitz plot analysis.

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# 1 Introduction

According to the Standard Model  $CP$  violation is attributed to the presence of one complex phase in the CKM quark-mixing matrix. The relations between the matrix elements  $V_{ij}$  are usually represented as a triangle in the complex plane, the Unitarity Triangle. The program of the  $B$  factories aims at overconstraining its sides and angles. Most measurements of branching fractions and  $CP$  parameters presented in this talk can be used to extract information about the angle  $\alpha = \arg[-V_{td}V_{tb}^*/V_{ud}V_{ub}^*]$ .

More detail about the analyses presented here can be found in the conference contributions[1].

## 2 Hadronic Charmless $B$ Decays

These results are based on the analysis of 227 million  $B\bar{B}$  decays recorded by the *BABAR* detector at the PEP-II asymmetric-energy  $e^+e^-$  collider at SLAC. The *BABAR* detector is described in detail elsewhere[2].

Decays of a  $B$  meson into final states with two or three charmless particles are rare, with branching fractions typically of  $\mathcal{O}(10^{-5})$ . Signal decays are identified using two kinematic variables: (1) the difference  $\Delta E$  between the energy of the  $B$  candidate in the  $e^+e^-$  center-of-mass (CM) frame and  $\sqrt{s}/2$  and (2) the beam-energy substituted mass  $m_{ES} = \sqrt{(s/2 + \mathbf{p}_i \cdot \mathbf{p}_B)^2/E_i^2 - \mathbf{p}_B^2}$ , where  $\sqrt{s}$  is the total CM energy, and the  $B$  momentum  $\mathbf{p}_B$  and the four-momentum of the initial state  $(E_i, \mathbf{p}_i)$  are defined in the laboratory frame.

The main common background consists of continuum ( $e^+e^- \rightarrow q\bar{q}$ ) events where two or three mesons combine kinematically to mimic a  $B$  decay. To suppress this jet-like background, a cut on the sphericity of the event is applied. Additionally, a Fisher discriminant  $\mathcal{F}$  is defined as an optimized linear combination of  $\sum_i p_i$  and  $\sum_i p_i \cos^2 \theta_i$ , where  $p_i$  is the momentum and  $\theta_i$  is the angle with respect to the thrust axis of the  $B$  candidate, both in the CM frame, for all tracks and neutral clusters not used to reconstruct the  $B$  meson. Alternatively a neural network is trained on those two variables and the angles with respect to the beam axis of the  $B$  momentum and  $B$  thrust axis in the  $\Upsilon(4S)$  frame. Background sources from  $B$  decays are vector-pseudoscalar decays, where one of the decay products remains undetected, and cross-feed among the charmless modes.

The determination of  $CP$  parameters relies on the tagging technique and a precise measurement of the flight time. Those particles in the event that are not used to reconstruct the decay mode under study provide information about whether the other  $B$  meson decayed as a  $B^0$  or  $\bar{B}^0$ . The  $CP$  asymmetry parameters in  $B^0 \rightarrow \pi^+\pi^-$  decays are determined with a maximum likelihood fit including information about the  $B$  flavor and the difference  $\Delta t$  between the decay times. The decay rate distribution  $f_+$  ( $f_-$ ) for the tagged  $B = B^0$  ( $\bar{B}^0$ ) is given by

$$f_{\pm}(\Delta t) = \frac{e^{-|\Delta t|/\tau}}{4\tau} [1 \pm S_{\pi\pi} \sin(\Delta m_d \Delta t) \mp C_{\pi\pi} \cos(\Delta m_d \Delta t)],$$

where  $\tau$  is the mean  $B^0$  lifetime and  $\Delta m_d$  is the mixing frequency due to the neutral- $B$ -meson eigenstate mass difference.

All new results described here are summarized in the two tables showing branching fractions and  $CP$  parameters.

## 2.1 $B \rightarrow \pi\pi$ modes

We updated the time-dependent  $CP$  asymmetry measurement in the decay  $B^0 \rightarrow \pi^+\pi^-$ . After selection of events with two charged tracks, a maximum-likelihood fit is performed using  $m_{ES}$ ,  $\Delta E$ ,  $\mathcal{F}$  and  $\theta_C$ , the Čerenkov angle measured by the detector of internally reflected Čerenkov light which provides good  $K - \pi$  separation in the relevant momentum region. Signal and background yields of the four related  $h^+h^-$  modes ( $h \equiv \pi, K$ ) are determined in a first fit and fixed in the final fit where information about  $B$ -flavor and decay-time is added. We measure the  $CP$  parameters in the decay  $B^0 \rightarrow \pi^+\pi^-$  to be  $C_{\pi\pi} = -0.09 \pm 0.15 \pm 0.04$  and  $S_{\pi\pi} = -0.30 \pm 0.17 \pm 0.03$  which does not indicate presence of significant  $CP$  violation. As shown in Fig. 1 this result is not compatible with Belle's measurement with 152 million  $B^0$ 's[3].

For the analysis of the modes  $B^+ \rightarrow \pi^+\pi^0$  and  $B^0 \rightarrow \pi^0\pi^0$  candidate  $\pi^0$  mesons are reconstructed as pair of photons in the electromagnetic calorimeter with requirements on minimum energy and lateral shower shape. For high momentum  $\pi^0$ 's the two-photon mass resolution is approximately 8 MeV/ $c^2$ . For both the  $B^0 \rightarrow \pi^0\pi^0$  signal and the  $B^\pm \rightarrow \rho^\pm\pi^0$  background the  $m_{ES}$  and  $\Delta E$  variables are correlated and therefore a two-dimensional PDF from a smoothed, simulated distribution is used. To eliminate systematic uncertainties associated with the choice of fit function of the  $\mathcal{F}$  distribution, a parametric step function is used[4]. The result of the maximum likelihood fit for  $B^0 \rightarrow \pi^0\pi^0$  is  $n(B^0 \rightarrow \pi^0\pi^0) = 61 \pm 17$ . The significance of the event yield is found to exceed  $5.0\sigma$  including systematic effects. The event yield is transformed into a measurement of the branching fraction  $\mathcal{B}(B^0 \rightarrow \pi^0\pi^0) = (1.17 \pm 0.32 \pm 0.10) \times 10^{-6}$ . Considering the improved understanding of the  $\pi^0$  detection efficiency and the additional data this result is consistent with our previous measurement[4]. In the same fit the time-integrated  $CP$  asymmetry, defined as  $C_{\pi^0\pi^0} = (|A_{00}|^2 - |\overline{A}_{00}|^2) / (|A_{00}|^2 + |\overline{A}_{00}|^2)$ , where  $A_{00}$  ( $\overline{A}_{00}$ ) is the  $B^0$  ( $\overline{B}^0$ )  $\rightarrow \pi^0\pi^0$  decay amplitude is measured. We find  $C_{\pi^0\pi^0} = -0.12 \pm 0.56 \pm 0.06$ . Finally the charge asymmetry and branching fraction for the decay  $B^+ \rightarrow \pi^+\pi^0$  are measured and shown in the tables.

## 2.2 Twobody charmless decays with kaons

$B \rightarrow K\pi$  decays are dominated by  $b \rightarrow s$  penguin transitions and are interesting modes to look for possible new physics or constrain the CKM angle  $\gamma$ [5]. New results presented here are included in the tables. We note that the charge asymmetry  $\mathcal{A}_{K^+\pi^0} = (6 \pm 6 \pm 1)\%$  is consistent with zero, while the measured direct asymmetry  $\mathcal{A}_{K^+\pi^-} = (-13.3 \pm 3.0 \pm 0.9)\%$  is not[6]. The time-dependent  $CP$  parameters of  $B \rightarrow K_s^0\pi^0$  are related to the angle  $\beta$  and discussed in[7].

The branching fraction and asymmetry of the previously unobserved decay  $B^0 \rightarrow K^0\overline{K}^0$  is measured with a significance of  $4.5\sigma$  including systematic uncertainties. Figure 2 shows the background-subtracted  $\Delta E$  distributions. The background subtraction is performed by weighting events using the *sPlot* technique[8].

## 2.3 $B^0 \rightarrow \rho^\pm\pi^\mp$

The final state of the decay  $B^0 \rightarrow \rho^\pm\pi^\mp$  is not a  $CP$  eigenstate and the decay  $B^0 \rightarrow \rho^0\pi^0$  has not yet been observed. A direct extraction of  $\alpha$  using simple isospin relations like in the  $B \rightarrow \pi\pi$  system does not appear promising. Instead, we performed a full time-dependent Dalitz analysis of the charmless three-body system  $B^0 \rightarrow \pi^+\pi^-\pi^0$  with 213 million  $B\overline{B}$  pairs, which allows a theoretically cleaner extraction of the angle  $\alpha$ [9] compared to the previously adopted quasi-twobody approach.

The 16 coefficients of the bilinear form factor terms occurring in the time-dependent decay rate of the  $B^0$  meson are determined in a maximum-likelihood fit with an event yield of  $n(B^0 \rightarrow \pi^+\pi^-\pi^0) = 1184 \pm 58$ . The physically relevant quantities are derived from these coefficients, resulting in the measurement of the direct  $CP$ -violation  $\mathcal{A}_{\rho\pi} = -0.088 \pm 0.049 \pm 0.013$  and  $C = 0.34 \pm 0.11 \pm 0.05$  and the mixing-induced  $CP$ -violation parameter  $S = -0.10 \pm 0.14 \pm 0.04$ . For the dilution and strong phase shift we obtain  $\Delta C = 0.15 \pm 0.11 \pm 0.03$  and  $\Delta S = 0.22 \pm 0.15 \pm 0.03$ , respectively. These results can be expressed in terms of the asymmetries  $\mathcal{A}_{\rho\pi}^{+-}$  ( $\mathcal{A}_{\rho\pi}^{-+}$ ), which involve only diagrams where the  $\rho(\pi)$  meson is emitted by the W boson, and are shown in Tab. 2. For the relative strong phase  $\delta_{+-}$  between the  $B^0 \rightarrow \rho^-\pi^+$  and  $B^0 \rightarrow \rho^+\pi^-$  transitions we find  $(-67_{-31}^{+28} \pm 7)^\circ$ .

### 3 Extraction of $\alpha$

We use the isospin relations of reference[10] to extract information on the angle difference  $\delta = \alpha - \alpha_{\text{eff}}$ , based on the measurement of the branching fraction[11]  $\mathcal{B}(B^0 \rightarrow \pi^+\pi^-) = (4.7 \pm 0.6 \pm 0.2) \times 10^{-6}$  in conjunction with the asymmetries  $C_{\pi^+\pi^-}$  and  $C_{\pi^0\pi^0}$  and the  $B^0 \rightarrow \pi^0\pi^0$  and  $B^\pm \rightarrow \pi^\pm\pi^0$  decay rates described here. We scan over all values of  $|\delta|$  and calculate a  $\chi^2$  for the decay amplitudes, given these five measurements and the two isospin constraints for each value of  $|\delta|$ . The  $\chi^2$  is converted into a confidence level, as shown in Fig. 3, from which we derive an upper bound on  $|\delta|$  of  $35^\circ$  at the 90% C.L.

From the measured coefficients of the amplitude relations in the Dalitz analysis we can extract an independent bound on  $\alpha$ , with little theoretical assumptions. We find  $\alpha = (113_{-17}^{+27} \pm 6)^\circ$ , while only a weak constraint is achieved at the significance level of more than two standard deviations.

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### References

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Decay	$\mathcal{B} \times 10^{-6}$	$N\sigma$
$B^+ \rightarrow \pi^+\pi^0$	$5.8 \pm 0.6 \pm 0.4$	5.0
$B^0 \rightarrow \pi^0\pi^0$	$1.17 \pm 0.32 \pm 0.10$	
$B^+ \rightarrow K^+\pi^0$	$12.0 \pm 0.7 \pm 0.6$	
$B^0 \rightarrow K^0\pi^0$	$11.4 \pm 0.9 \pm 0.6$	
$B^+ \rightarrow K^0\pi^+$	$26.0 \pm 1.3 \pm 1.0$	
$B^0 \rightarrow \bar{K}^0\bar{K}^0$	$1.19 \pm 0.38 \pm 0.13$	4.5
$B^+ \rightarrow K^+\bar{K}^0$	$< 2.35$ 90% C.L.	

Table 1: Summary of branching fractions measured with 227 million  $B\bar{B}$  pairs. The last column ( $N\sigma$ ) shows the significance including systematic effects.

Parameter	Value
$S_{\pi\pi}$	$-0.30 \pm 0.17 \pm 0.03$
$C_{\pi\pi}$	$-0.09 \pm 0.15 \pm 0.04$
$\mathcal{A}_{\pi^+\pi^0}$	$-0.01 \pm 0.10 \pm 0.02$
$C_{\pi^0\pi^0}$	$-0.12 \pm 0.56 \pm 0.06$
$\mathcal{A}_{K^+\pi^0}$	$0.06 \pm 0.06 \pm 0.01$
$\mathcal{A}_{K^0\pi^+}$	$-0.087 \pm 0.046 \pm 0.010$
$\mathcal{A}_{\rho\pi}^{+-}$	$-0.21 \pm 0.11 \pm 0.04$
$\mathcal{A}_{\rho\pi}^{-+}$	$-0.47 \pm 0.15 \pm 0.06$

Table 2: Summary of updated  $CP$  parameters.

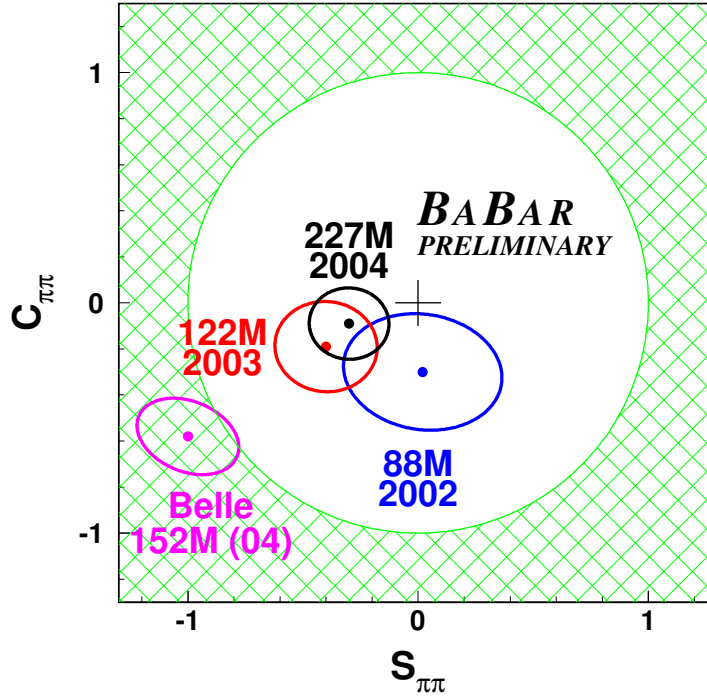


Figure 1: Central values and  $1\sigma$  contours of the time-dependent  $CP$  parameters  $C_{\pi\pi}$  and  $S_{\pi\pi}$  in the decay  $B^0 \rightarrow \pi^+\pi^-$  on different *BABAR* datasets in contrast to the measurement from Belle.

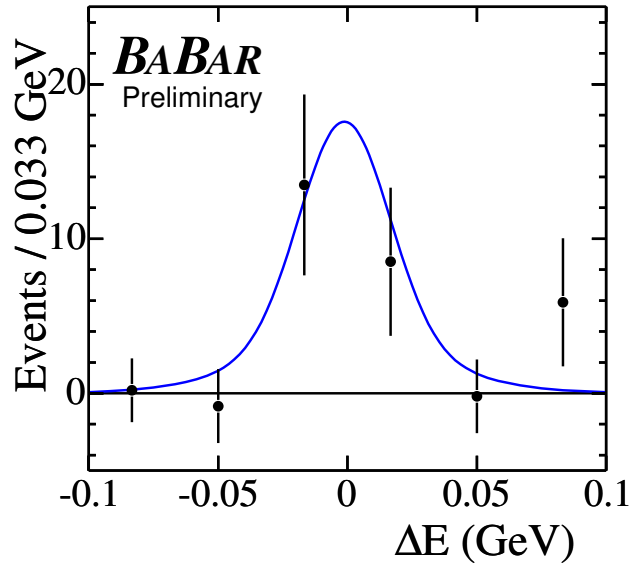


Figure 2:  $\Delta E$  distribution for background subtracted  $B^0 \rightarrow K^0 \bar{K}^0$  events (see text).

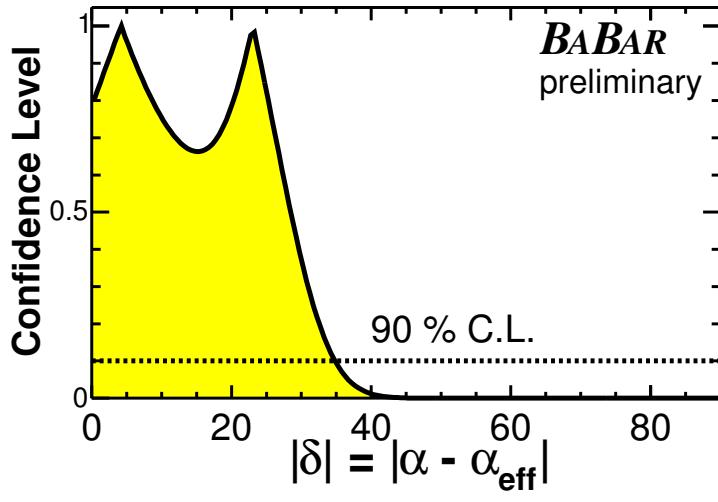


Figure 3: Confidence level for the parameter  $\delta$  from the full  $B \rightarrow \pi\pi$  isospin analysis.

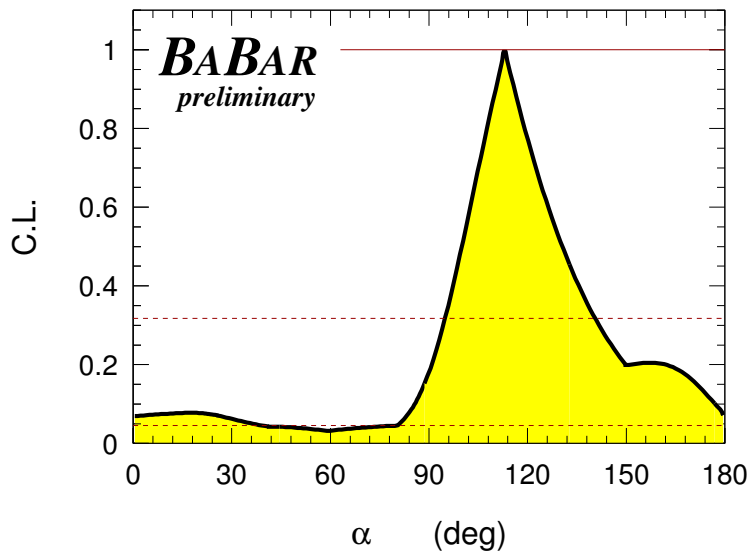


Figure 4: Confidence level for the CKM angle  $\alpha$  from the  $B^0 \rightarrow \pi^+\pi^-\pi^0$  Dalitz analysis.