

Unique Graviton Exchange Signatures

at LC's



Many new physics scenarios lead to contact-int.-like deviations in e^+e^- processes....

- Z' , $\tilde{\nu}$, LQ, DL, extra dim's, string excitations, ...
- If deviations ARE seen, how do we know which [if any of the above] it is?
- Try fits to various hypotheses ... OR
- Look for something unique for graviton exchange ..., at a single \sqrt{s} [~~dim-6~~ or dim 8]

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Unique Graviton Exchange Signatures :

Consider $e^+e^- \rightarrow f\bar{f}$ ($m_f = 0$)

$$\frac{1}{\sigma} \frac{d\sigma}{d\cos\theta} = \frac{3}{8} \left[1 + \cos^2\theta + \frac{8}{3} A_{FB} \cos\theta \right]$$

In the SM, Z' or ^{any} contact int cases

$$= a_0 P_0 + a_2 P_2 + a_1 P_1$$

$P_n \equiv P_n(\cos\theta)$
Legendre Poly's

$$\left| \int_{-1}^1 dz P_n P_m = \frac{2}{n+1} \delta_{nm} \right|$$

$$\langle P_n \rangle \equiv \int_{-1}^1 \frac{1}{\sigma} \frac{d\sigma}{dz} P_n(z) dz \quad [z \equiv \cos\theta]$$

$$\rightarrow \begin{cases} \langle P_0 \rangle \equiv 1 & \langle P_1 \rangle = \frac{2}{3} A_{FB} & \langle P_2 \rangle = \frac{1}{10} \\ \rightarrow & & \\ \rightarrow & \langle P_{n>2} \rangle = 0 \end{cases}$$

• Z' / contact int $\langle P_1 \rangle \neq \langle P_1 \rangle_{SM}$

• $\tilde{\nu} / X$ $\langle P_1 \rangle, \langle P_2 \rangle \neq SM \text{ values}$

But $\langle P_{n>2} \rangle$ still = 0 !

$$\frac{dG}{dz} = N_c \frac{\pi a^2}{s} \left\{ \tilde{P}_{ij} [A_{ij}^e A_{ij}^f (2P_0 + P_2)/3 + B_{ij}^e B_{ij}^f \cdot P_1] \right.$$

$$\left. - \frac{\lambda s}{2\pi \alpha \Lambda_H^4} \tilde{P}_i \left[\frac{(2P_3 + 3P_1)}{5} v_i^e v_i^f + a_i^e a_i^f P_2 \right] \right.$$

$$\left. + \frac{s^4}{16\pi^2 \alpha^2 \Lambda_H^8} [16P_4 + 5P_2 + 14P_0] / 35 \right\}$$

• $\langle P_3 \rangle$ at order $s/\pi \alpha \Lambda_H^4$

• $\langle P_4 \rangle$ at order $(\quad)^2$

→ $\langle P_3 \rangle \neq 0$ will be dominant

$$A_{LR}(z) \equiv \tilde{P}_{ij} [B_{ij}^e A_{ij}^f (P_2 + 2P_0)/3 + A_{ij}^e B_{ij}^f \cdot P_1]$$

$$- \frac{\lambda s}{2\pi \alpha \Lambda_H^4} \tilde{P}_i \left[\frac{(2P_3 + 3P_1)}{5} a_i^e v_i^f + P_2 v_i^e a_i^f \right]$$

{ above }

For the Normalized Distribution $0.375(1+z^{**2})$, what are the Legendre Poly Moments as we increase nbins??

NBINS	P_2 MOMENT	P_4 MOMENT
0.1000000000D+02	0.9004000000D-01	-0.2675850000D-01
0.2000000000D+02	0.9750250000D-01	-0.6828453125D-02
0.5000000000D+02	0.9960006400D-01	-0.1098806944D-02
0.2000000000D+03	0.9997500025D-01	-0.6874533861D-04
0.1000000000D+04	0.9999900000D-01	-0.2749992541D-05

this is 0.1
in the cont. lim.

this is 0 in
the cont. limit

NOW WE KEEP NBINS=20 & CHANGE THE ANGLE CUT

CUT(MR)	COS(CUT)	P_2	P_4
0.0	0.1000000000D+01	0.9750250000D-01	-0.6828453125D-02
.01	0.9999500004D+01	0.9742830551D-01	-0.6898110097D-02
.05	0.9987502604D+00	0.9565225028D-01	-0.8559000078D-02
0.1	0.9950041653D+00	0.9015889880D-01	-0.1361589379D-01
0.2	0.9800665778D+00	0.6903092903D-01	-0.3189468450D-01

OR IN MORE DETAIL FOR a $0.375(1+z^{**2})+z$ distribution which gives $P_1=2/3$ and $P_3=0$ in the cont limit..still for 20 bins & angle cuts as above

P_2	P_4	P_1	P_3
0.9750250000D-01	-0.6828453125D-02	0.6650000000D+00	-0.5818750000D-02
0.9742830551D-01	-0.6898110097D-02	0.6649002557D+00	-0.5915603692D-02
0.9565225028D-01	-0.8559000078D-02	0.6625098141D+00	-0.8230135856D-02
0.9015889880D-01	-0.1361589379D-01	0.6550819162D+00	-0.1534061274D-01
0.6903092903D-01	-0.3189468450D-01	0.6260036782D+00	-0.4197362741D-01

"real" LC $\sqrt{s} = 500 \text{ GeV}$

$\theta \geq 50 \text{ mrad}$

SM

	$\langle P_2 \rangle$	$\langle P_4 \rangle$	$\langle P_1 \rangle$	$\langle P_3 \rangle$	
μ, τ	0.9583178524D-01	-0.8575064935D-02	0.3193237706D+00	-0.3966851446D-02	} Unpol. Cross- Section
b	0.9583178524D-01	-0.8575064935D-02	0.4194039034D+00	-0.52101133163D-02	
c	0.9583178524D-01	-0.8575064935D-02	0.4073311326D+00	-0.5060137206D-02	
t	0.4408526168D-01	-0.6871751178D-02	0.2691767856D+00	-0.3343892374D-02	
μ, τ	0.9583178524D-01	-0.8575064935D-02	0.4978149864D+00	-0.6184187587D-02	} $\frac{d\sigma^+ - d\sigma^-}{d\Omega}$
b	0.9583178524D-01	-0.8575064935D-02	0.4194039034D+00	-0.52101133163D-02	
c	0.9583178524D-01	-0.8575064935D-02	0.4073311326D+00	-0.5060137206D-02	
t	0.4408526168D-01	-0.6871751178D-02	0.2691767856D+00	-0.3343892374D-02	

Note $\langle P_2 \rangle_{t\bar{t}} \ll 0.1$ due to finite m_t^2/s terms

$\langle P_2 \rangle \approx 0.1$ + $\langle P_{3,4} \rangle$ small for massless guys
as before

$\langle P_3 \rangle$ appears flavor dependent... leaks in from $\langle P_1 \rangle$

since AFB is sensitive to final f couplings

Now what if we bring Λ_H from ∞ (SM) to
2 TeV?

$$\sqrt{s} = 500 \text{ GeV}$$

$$\Lambda_H = 2 \text{ TeV}$$

	$\langle P_2 \rangle$	$\langle P_4 \rangle$	$\langle P_1 \rangle$	$\langle P_3 \rangle$ ✓	
μ, τ	0.8404986807D-01	-0.8032733352D-02	0.2858088512D+00	-0.1268972869D-01	} $\frac{d\sigma^+ + d\sigma^-}{dz}$
b	0.5409391190D-01	-0.6653835427D-02	0.3761896817D+00	-0.1604285987D-01	
c	0.1176024162D+00	-0.9004093559D-02	0.4479671249D+00	0.5926959655D-02	
t	0.5450228551D-01	-0.7144569407D-02	0.2829118150D+00	0.3915261996D-03	
μ, τ	0.8235699163D-01	-0.8131522069D-02	0.4841933136D+00	-0.9767800563D-02	} $\frac{d\sigma^+ - d\sigma^-}{dz}$
b	0.5409391190D-01	-0.6653835427D-02	0.3761896817D+00	-0.1604285987D-01	
c	0.1176024162D+00	-0.9004093559D-02	0.4479671249D+00	0.5926959655D-02	
t	0.5450228551D-01	-0.7144569407D-02	0.2829118150D+00	0.3915261996D-03	

$\langle P_3 \rangle$ shifted substantially from SM case

perform fit to $\langle P_{3,4} \rangle$ deviations ...

$$\frac{1}{\sigma} \frac{d\sigma}{dz} \Big|_{SM+grav} = \sum_{n=0}^{\infty} a_n P_n \quad !!$$

$\therefore \langle P_{3,4} \rangle \neq 0 \Rightarrow$ graviton exchange!

Not so simple in Real World ...

(i) finite bin width + N_{bins}

(ii) cuts near beam pipe remove full $\cos\theta$ range [orthogonality]

⋮

e.g. SM $N_{bin} = 20$ $\theta^{cut} = 50 \text{ mrad}$

$$\langle P_2 \rangle = 0.0957 \quad \langle P_4 \rangle = -8.56 \cdot 10^{-3}$$

(0.1) (0)

$$\langle P_3 \rangle = -8.23 \cdot 10^{-3}$$

(0)

$$\langle P_n \rangle = \int_{-1}^1 \frac{1}{\sigma} \frac{d\sigma}{dz} P_n(z) dz \Rightarrow \sum_n \left[\int_{bin} \frac{1}{\sigma} \frac{d\sigma}{dz} dz \right] P_n(z_{bin})$$

Real World Effects induce spurious contributions to moments which need to be "background subtracted"

Look at $\frac{1}{\sigma} \frac{d\sigma}{dz} \sim \frac{d\sigma^+ + d\sigma^-}{dz}$

and

$$\sim P \frac{d\sigma^+ - d\sigma^-}{dz}$$

stat, lumi
pol, ...

$$\chi^2 = \sum_{\text{dir}} \sum_{\mathcal{S}} \sum_{n=3,4} (\langle P_n \rangle - \langle P_n \rangle_{\text{SM}})^2 / \text{err}_{n\mathcal{S}}^2$$

$$\geq 2.5$$

($\chi_{\text{SM}}^2 = 0$ by definition)

$$SL/L = 0.25\% \quad , \quad \delta^p/p = 0.3\% \quad \text{etc}$$

→ $e^+e^- \rightarrow f\bar{f}$ ID reach for gravity [Plot]
→

- This method will work for processes w/o u- or t-channel poles ...

(→ they contain all P_n , e.g.,)

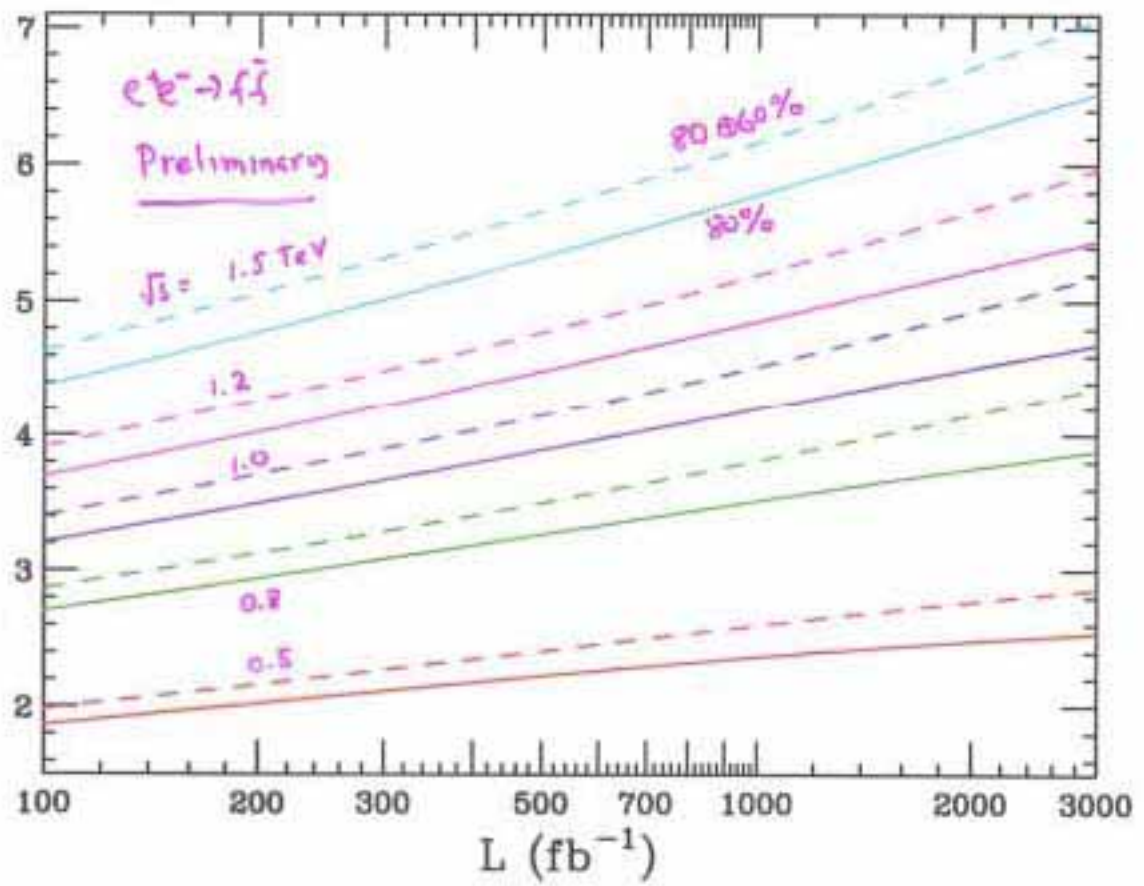
X $e^+e^- \rightarrow e^+e^-$, $\gamma\gamma$, ZZ $e_L^- e_R^+ \rightarrow W^+ W^-$ X

However

$e_R^- e_L^+ \rightarrow W^+ W^-$ is pure s-channel:

$$+ \frac{1}{\sigma} \frac{d\sigma}{dz} = a_0 P_0 + a_2 P_2 \quad \text{in SM \{or Z'...\}}$$

Δ_H (TeV)



again, Gravity induces $\left\{ \begin{array}{l} \langle P_1 \rangle \\ \langle P_3 \rangle, \langle P_4 \rangle \neq 0 \end{array} \right.$ ← note

For ALL final state W^+W^- polarizations

→ not Z' or contact int $[\sim \bar{e}e W_{\mu\nu} W^{\mu\nu}]$
 ($\langle P_2 \rangle$ deviation only)

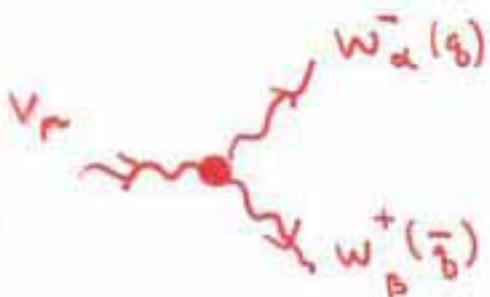
But anomalous couplings do induce $\left\{ \begin{array}{l} \langle P_1 \rangle \\ \langle P_{3,4} \rangle \neq 0 \dots \end{array} \right.$

$$\frac{d\sigma}{d\Omega} = \frac{\pi \alpha^2}{2s} \beta \left(\Sigma_{TT} + \Sigma_{TL+LT} + \Sigma_{LL} \right) \quad (e^- e^+)$$

$$\Sigma_{TT} = 2\beta^2 F_1^2 (1-\gamma^2)$$

$$\Sigma_{LL} = (1-\gamma^2) \frac{\beta^2 s^2}{4M_W^4} \left\{ F_3 - (1-2\mu_W^2/s) F_1 + \frac{\beta^2 s^2}{2M_W^2} F_2 \right\}^2$$

$$\Sigma_{LT+TL} = \frac{5\beta^2}{2M_W^2} \left\{ (F_3 + \beta \gamma F_5)^2 (1+\gamma^2) + F_5^2 (1-\gamma^2)^2 + 2(F_3 + \beta \gamma F_5) \gamma (1-\gamma^2) F_5 \right\}$$



$$F_5 \sim g_s^V \epsilon^{\mu\nu\rho\sigma} (q-\bar{q})_\rho \quad (\not{q}, \not{\bar{q}})$$

(appears at 1-loop in SM) $_{\nu\nu\gamma}$

BUT $\langle P_1 \rangle, \langle P_{3,4} \rangle \neq 0$ only for TL+LT final state

$\Rightarrow \langle P_{1,3,4} \rangle \neq 0$ in $e^-_R e^+ \rightarrow W^+ W^-$

Excludes Z' + contact int's AND

$\langle P_{1,3,4} \rangle \neq 0$ in TT/LL modes

Excludes g_5^V -type couplings as source!

IF a pure RH e^- beam were available ...

χ^2 w/ $\langle P_{1,3} \rangle \neq$ only \rightarrow [Fig]

However .. we don't have 100% RH e^-

Best case w/ $P_{e^+} = 60\%$ is to combine $d\sigma$'s

w/ different P_{e^-,e^+} signs to extract $d\sigma_{e^-_R}$

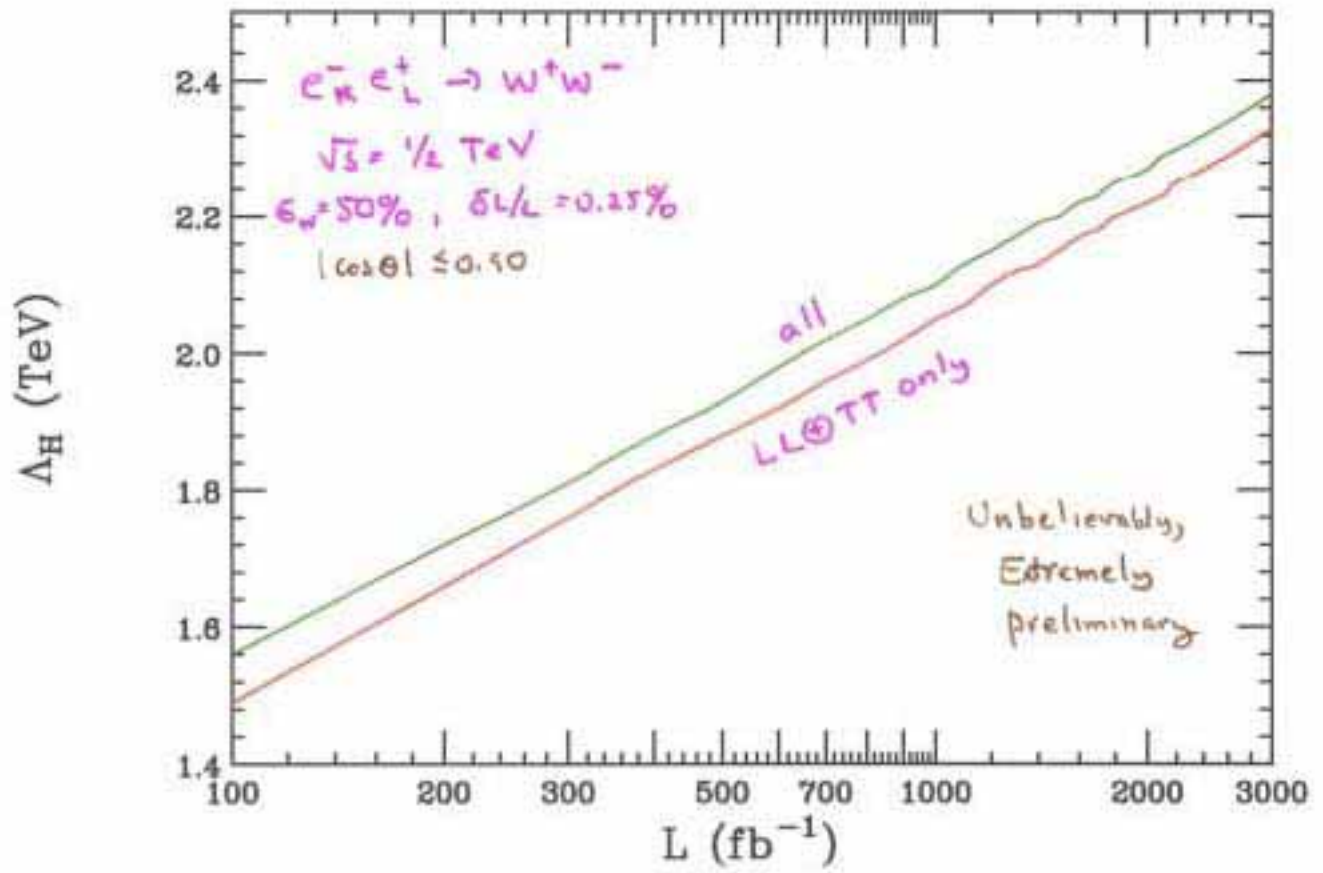
• recall $d\sigma_{e^-_R} \ll d\sigma_{e^-_L}$ - lots of systematics

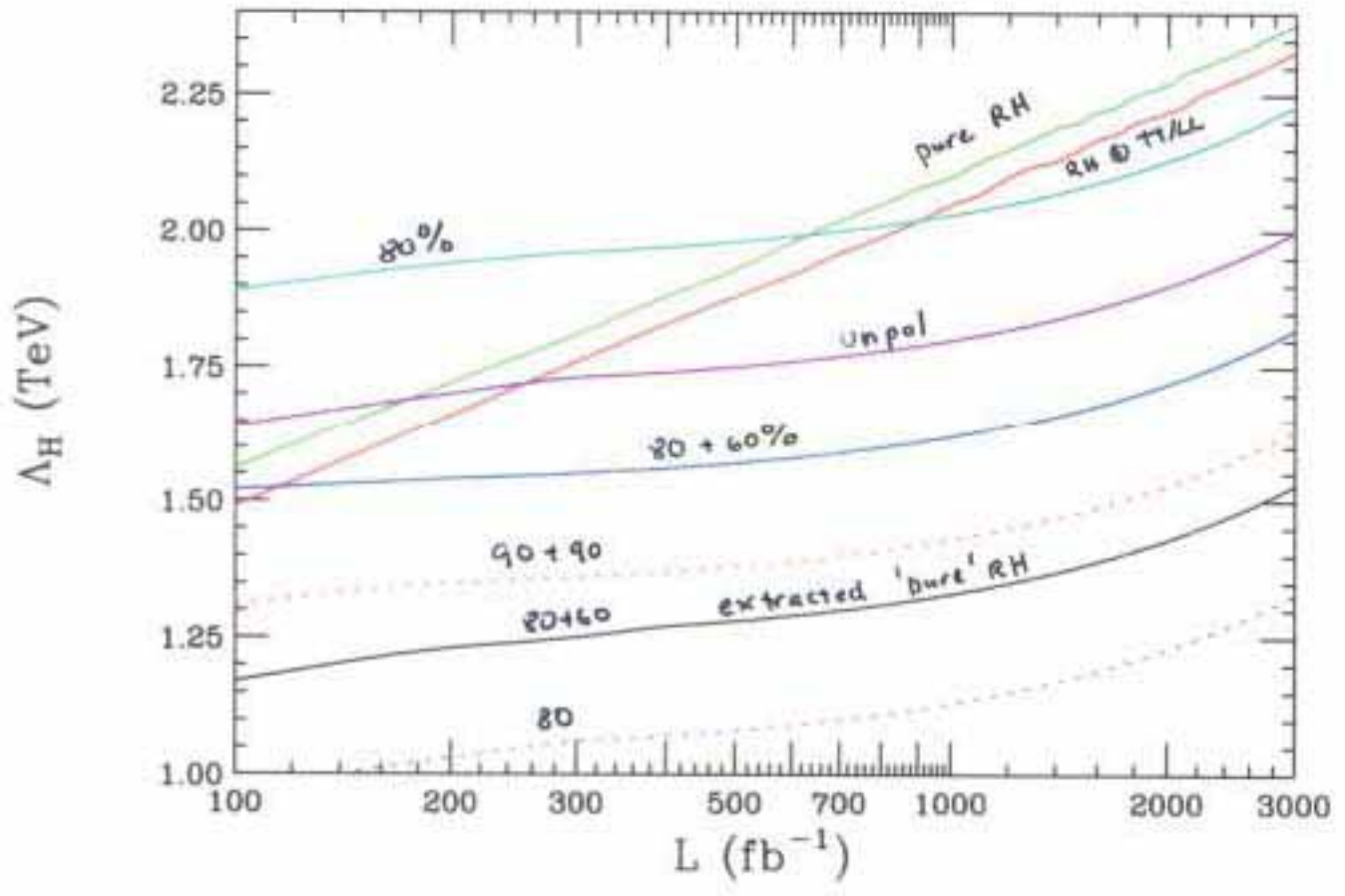
... First pass analysis .. [Fig]

\rightarrow Seems like poor reach in comparison to

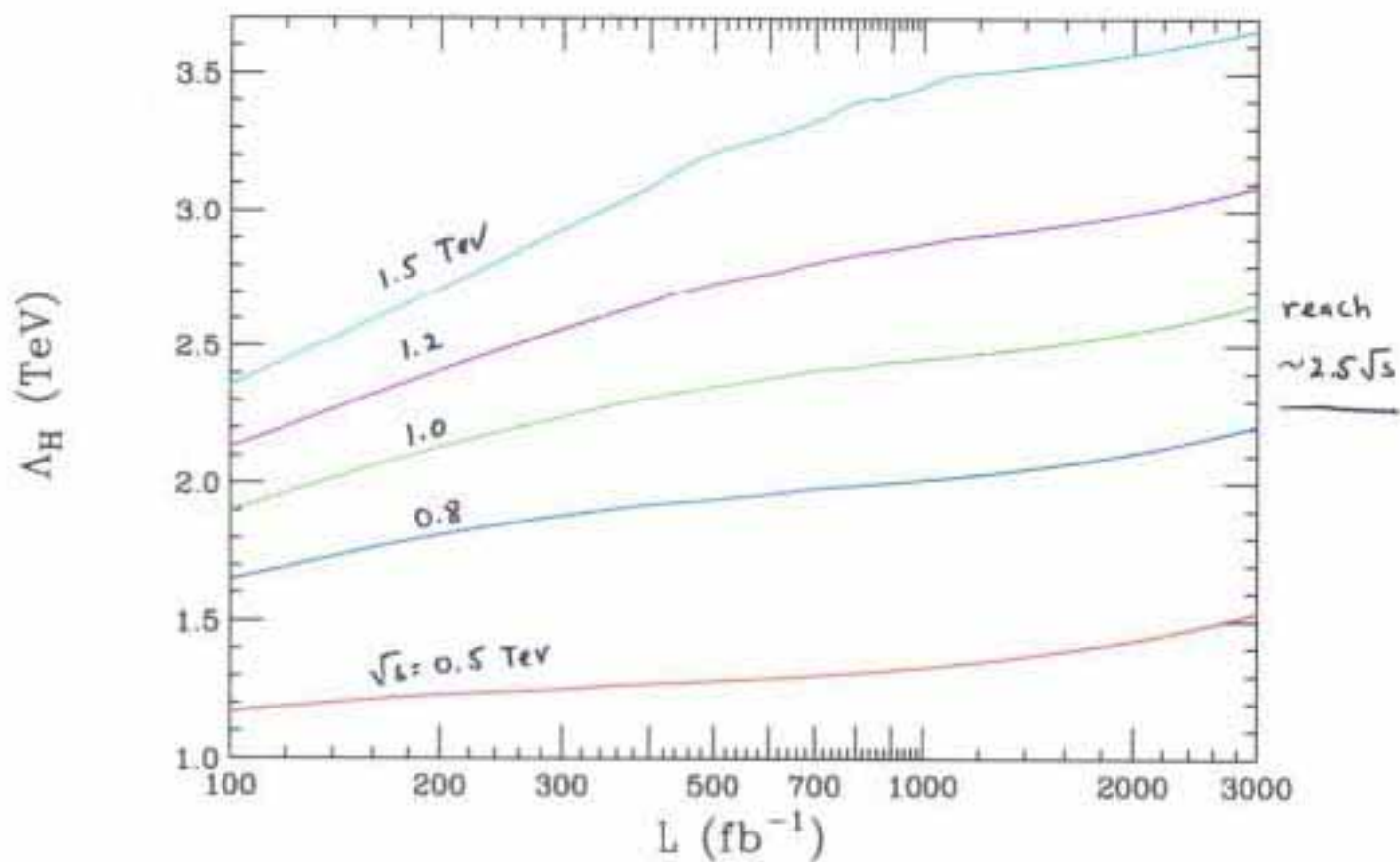
$\rightarrow e^+ e^- \rightarrow f \bar{f}$

5 σ ID reach





Fit to $e^-e^+ \rightarrow W^+W^-$; extracted



Conclusions

- Graviton exchange signatures can be **uniquely** ID'd in $e^+e^- \rightarrow f\bar{f}$ and, possibly, $e^+e^- \rightarrow W^+W^-$
- More work needs to be done to really understand how well this can be done