

Unexpected Effects of

Final-State Interactions in QCD

Stan Brodsky

SLAC + JLab

Mini-Workshop on Single Spin Asymmetries

Urbana Nov 27-28, 2003

* Diffraction in DIS

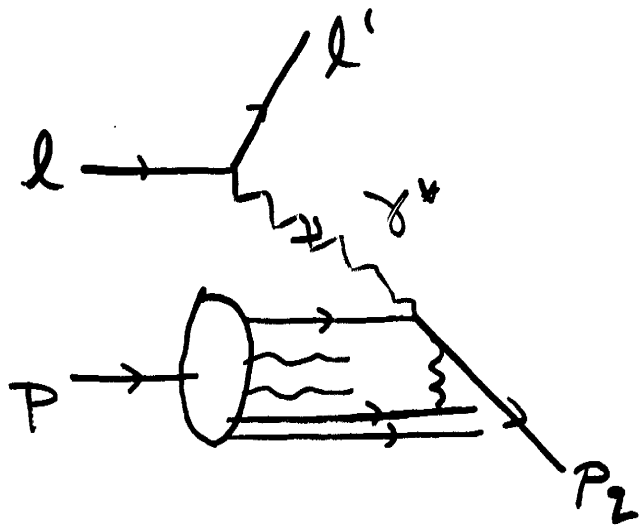
* Nuclear Shadowing

* Single-Spin Asymmetries - Sivers Effect

⇒ Structure Functions are not

Parton Densities

Unexpected Role of Final State Interactions in Deep Inelastic Scattering



gluon exchange
after photon cuts
not in LFWF

* Single-spin asymmetry

$$\vec{S}_p \cdot \vec{q} \times \vec{P}_2$$

Bjorken-scaling

* Diffraction at Leading Twist

* Nuclear Shadowing (interference of diff channels)

* Energy Loss, P_T Broadening

Diffraction, Nuclear Shadowing, Pomeron
not in nuclear wavefunction!

Unexpected Effects of
Final-State Interactions
in QCD

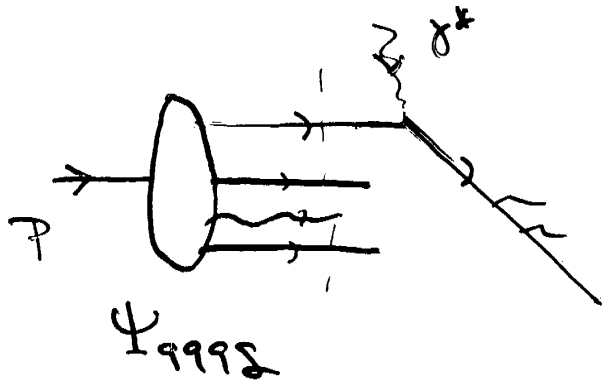
Collaborations with

- Doe Sung Hwang and Egon Schn. It
- Paul Hoyer, Nils Marchal, Stéphane Peise, F. Sannino

Density matrix formulation with

- Carl Carlson, Doe Sung Hwang

Parton model interpretation of DIS



$$F_2(x, Q^2) = \sum_{2FP} e_q^2 x q(x, Q^2)$$

$$q(x, Q^2) = \sum_{n \geq 3} \int_0^{k_{\perp} < Q} d^2 k_{\perp} dx |\Psi_n(x, k_{\perp})|^2 \delta(x - x_n)$$

$$H_{LF} |\Phi\rangle = k_{\perp}^2 |\Phi\rangle$$

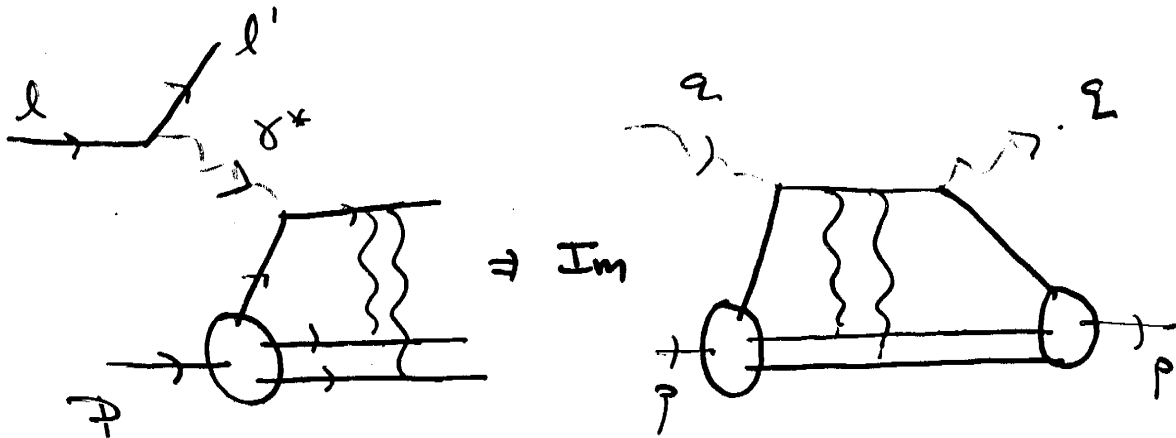
$$\langle n | \Phi \rangle = \Psi_n(x, k_{\perp})$$

$q(x, Q^2)$, Ψ_n determined by target LF WF alone

All final-state interactions inconsequential
- power-law, phase

Oh = Yukawa theory

New perspectives on Final-State Interactions



$$F_{q/N}(x_B, Q^2) = \frac{1}{8\pi} \int dy^- e^{-ix_B P^+ y^-}$$

$$\langle N(p) | \bar{q}(y^-) \delta^+ \mathbb{P} e^{i g \int_0^{y^-} d\omega^- A^+(\omega^-)} q(0) | N(p) \rangle$$

Usual argument $A^+ = 0$ gauge

no effect from FSI!

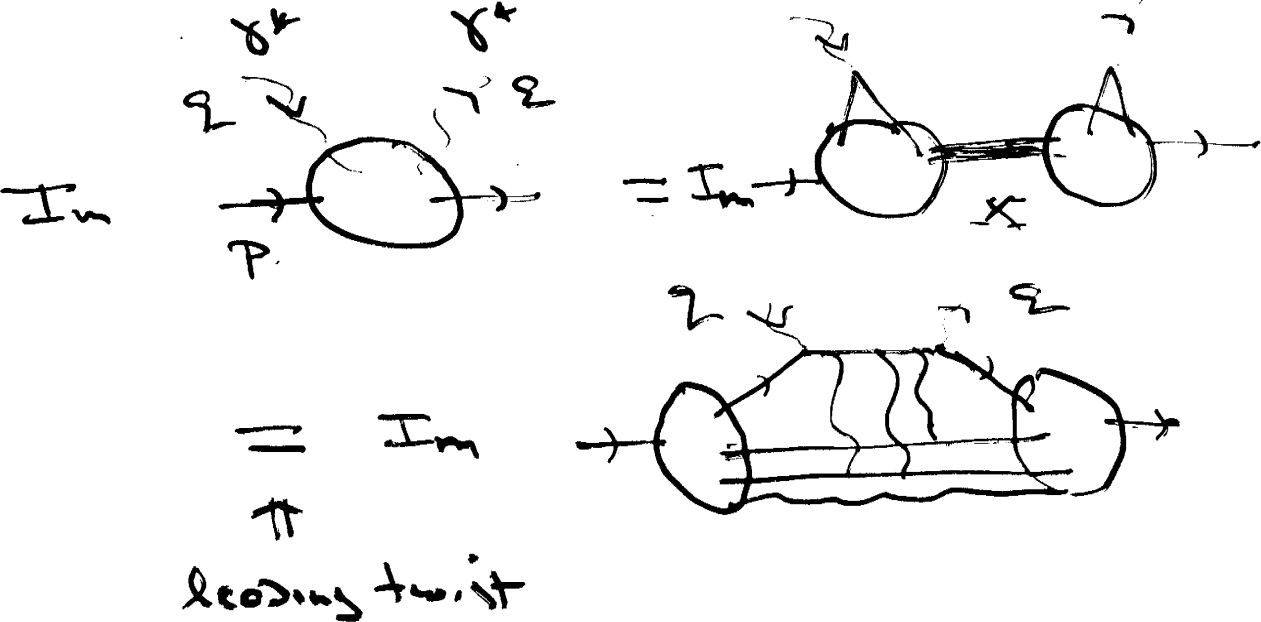
phase irrelevant

∞ Identify $F_{q/N}$ with LC Prob. Dist

$$F_{q/N}(x_B, Q^2) = \sum_i \int_{k_{i,1}^+ < Q^2} [\prod dx d^2k_\perp] |\Psi_i(x, \vec{k}_\perp)|^2 \sum_j \delta(x_B - x_j)$$

Usual proof:

QCD Factorization For virtual Compton amplitude:

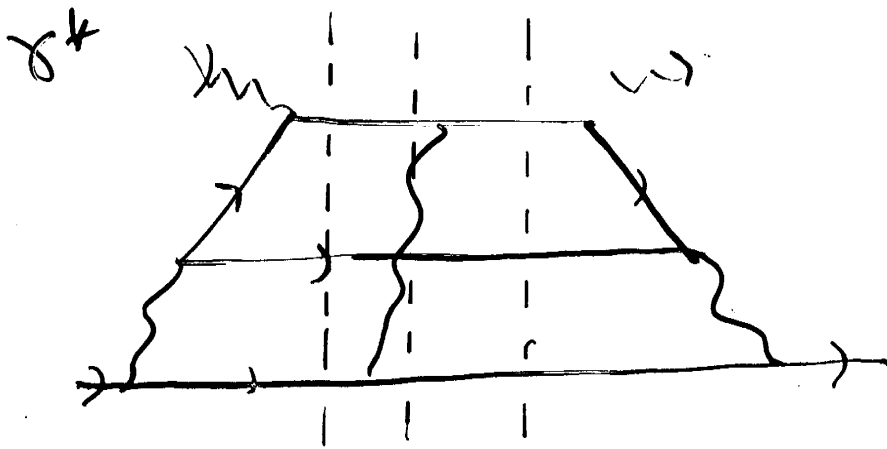


$$P_{q/N}(x_B, Q^2) = \frac{1}{8\pi} \int dy^- e^{-ix_B P^+ y^-}$$

$$\langle N(p) | \bar{q}(y^-) \gamma^+ P e^{ig \int_0^{y^-} d\omega^- A^+(\omega)} q(0) | N \rangle$$

Choose light-cone gauge : $A^+ = 0$,
 Path-ordered exponential = 1





Usual argument: no time for f.s.i.

- three denominators of order v
- numerator coupling finite in l.c.g.

∞ f.s.i. suppressed by power of $\frac{1}{v}$

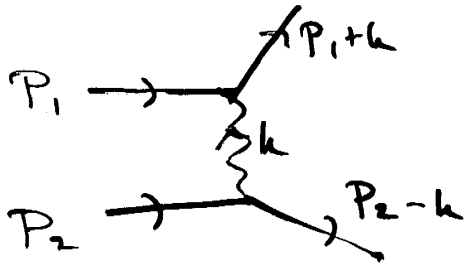
Equivalent to setting P.O.E. = 1.

$$\int_0^{\delta^-} d\omega^- A^+(\omega^-) = 0.$$

in $A^+ = 0$ gauge.

But argument is wrong!

Consider elastic scattering in QED at 5777



$$M = g^2 (2P_1 + k)^\mu d_{\mu\nu} (2P_2 - k)^\nu$$

$$d^{\mu\nu} = \frac{1}{k^2} \left[-g^{\mu\nu} + \frac{n^\mu k^\nu + k^\mu n^\nu}{n \cdot k} \right]$$

$$\stackrel{\circ}{\circ} M = -g^2 \frac{(2P_1 + k) \cdot (2P_2 - k)}{k^2} \approx -2g^2 \frac{s}{t}$$

gauge indep (from $g^{\mu\nu}$)

However, if we assume leading term comes from

$$S = 2P_1 \cdot P_2 = P_1^- P_2^+$$

Take: $M \approx g^2 (2P_1^-) d_{\mu\nu} (2P_2^+)$

correct in Feynman gauge, not in l.c.g.!

In l.c.g. dominant term is from d^{++} \neq

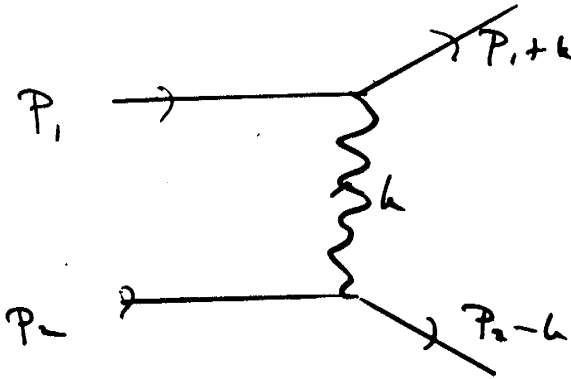
$$M_{lc} = \frac{S^2}{k^2} = \frac{-k_-^2 2P_2^+}{k^+} = -2g^2 \frac{s}{t}$$

where $k^+ = \frac{-k_-^2}{P_1^-} \rightarrow 0$ largest term from A_{++} in l.c.g.

Light-cone gauge evaluation

$$n^\mu = (0, 2, 0, 0)$$

$$n^2 = 0$$



$$2p_1 \cdot k + k^2 = 0$$

$$M = e^2 (2p_1 + k)_\mu \left[\frac{-g^{\mu\nu} + \frac{n^\mu k^\nu + k^\mu n^\nu}{n \cdot k}}{k^2 + i\epsilon} \right] (2p_2 - k)_\nu$$

where: $n \cdot k = k^+ = \frac{-k_\perp^2}{p_1^-} \rightarrow 0$ for $s \gg -t$

Dominant term in l.c.g. from non-relativistic current

$$M = e^2 \frac{-k_\perp^2 \frac{2p_2^+}{k^+}}{k^2 + i\epsilon} \Rightarrow -2e^2 \frac{s}{t}$$

\vec{A}_\perp plays crucial role in l.c.g.: $k^+ = 0(\frac{1}{p_1^-})$

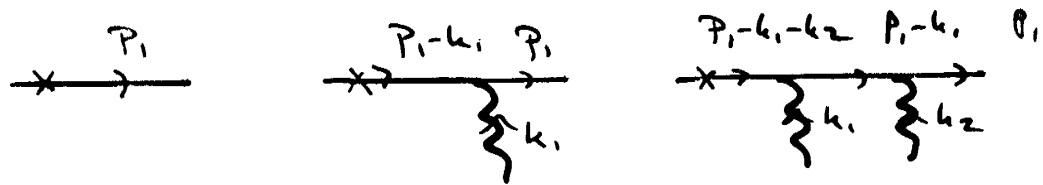
Similarly: $\int d\omega^\mu A_\mu \neq \int d\omega^- A^+$ in l.c.g.

Interpretation of $\mathcal{P} \exp \left[i g \int_0^\infty dy^- A^+(y^-) \right]$

$$1 + i g \int_0^\infty dy_1^- A^+(y_1^-) \left[1 + i g \int_{y_1^-}^\infty dy_2^- A^+(y_2^-) + \dots \right]$$

$$= 1 + g \int_{-\infty}^\infty \frac{dk_1^+}{2\pi} \frac{\tilde{A}^+(k_1^+)}{k_1^+ - i\epsilon} + g^2 \int_{-\infty}^\infty \frac{dk_1^+}{2\pi} \frac{dk_2^+}{2\pi} \frac{\tilde{A}^+(k_1^+) \tilde{A}^+(k_2^+)}{(k_1^+ + k_2^+ + i\epsilon)(k_2^+ - i\epsilon)}$$

where $A^+(y^-) = \int_{-\infty}^\infty \frac{dk^+}{2\pi} \tilde{A}^+(k^+) e^{-ik^+ y^-}$



$$\frac{g^2 \mathcal{P}_1^- \tilde{A}^+(k_1) \mathcal{P}_1^- \tilde{A}^+(k_2)}{[-\mathcal{P}_1^- (k_1^+ + k_2^+) + i\epsilon] [-\mathcal{P}_1^- k_2^+ + i\epsilon]}$$

• POE equiv. to eikonal amplitude

→ Correct in Feynman gauge

* Incorrect in l.c.g. where $\tilde{A}^+(k) = 0$.

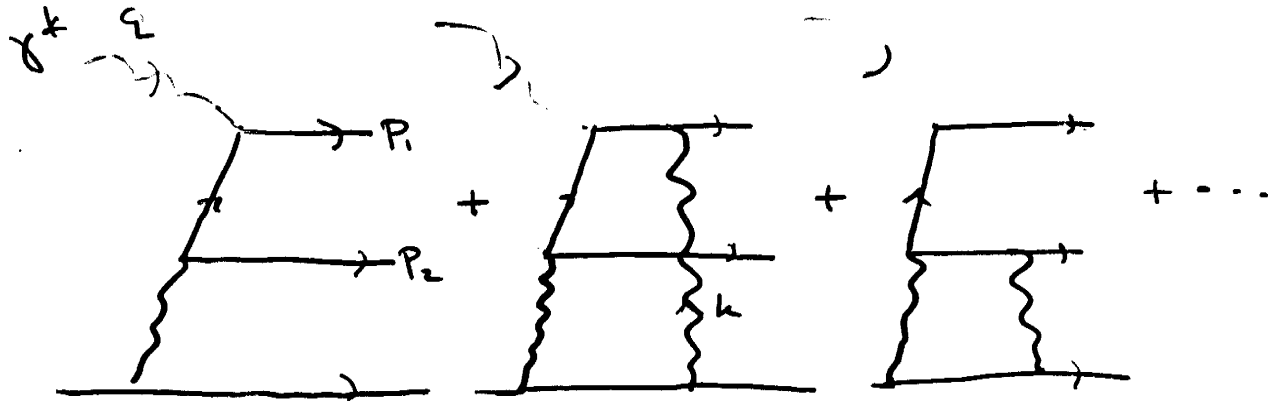
⇒ Need to keep $\int dy_m A^m$ in l.c.g.

Since $(2\vec{P}_1 - \vec{k}_2) \cdot \vec{A}_2$ contributes at l.o.

Explicit calculation of FSI

BHAPS

$q^+ \leq 0$
frame



LFTOPT : gluon exchanged after photon sets

Find non-zero leading-twist FSI effect

Leading twist diffraction, Eikonal form

Shadowing correction, not Coulomb phase

Gauge-independent:

Checked: Feynman, LCG [$A^+ = 0$] $\left\{ \begin{matrix} ML \\ PV \\ k \end{matrix} \right.$ prescription

Lesson for LCG:

$$g^{\mu\nu} = \frac{n^\mu k^\nu + k^\mu n^\nu}{n \cdot k}$$

At pole: $n \cdot k = k^+ = O(\frac{1}{v})$.

$$n^\mu = (0, 2, \vec{0}_L)$$

$$n \cdot n = 0$$

Light-Cone Gauge Prescriptions

$$d_{LC}^{\mu\nu}(k) = \frac{i}{k^2 + i\epsilon} \left[-g^{\mu\nu} + \frac{n^\mu k^\nu + k^\mu n^\nu}{n \cdot k} \right]$$

The pole at $n \cdot k = k^+ = 0$ requires an analytic presc:

$$\frac{1}{k^+} = \begin{cases} \frac{k^+}{(k^+ - i\epsilon)(k^+ + i\epsilon)} & \text{Principal value} \\ \frac{1}{k^+ - i\epsilon} & \text{Korchegov} \\ \frac{1}{k^+ - i\epsilon \epsilon(k^-)} & \text{Mandelstam-Liebbrandt} \end{cases}$$

$$\epsilon(x) = \theta(x) - \theta(-x)$$

$$M-L: \frac{k^-}{k^+ k^- - i\epsilon} = \frac{k^-}{k^2 - k_\perp^2 - i\epsilon} \quad \text{causal similar to Feynman-prop.}$$

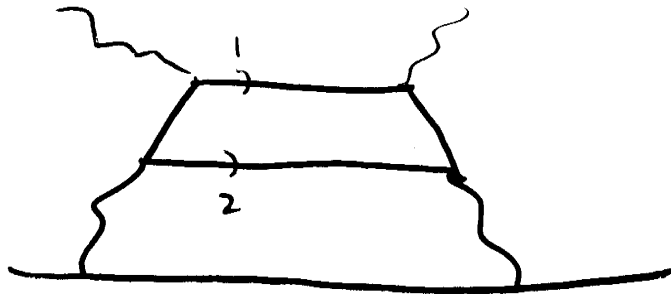
Korchegov: non-causal!

* Find FSI of current jet vanishes in LC pres!

* But corresponds to solving LC w.f. in external field!

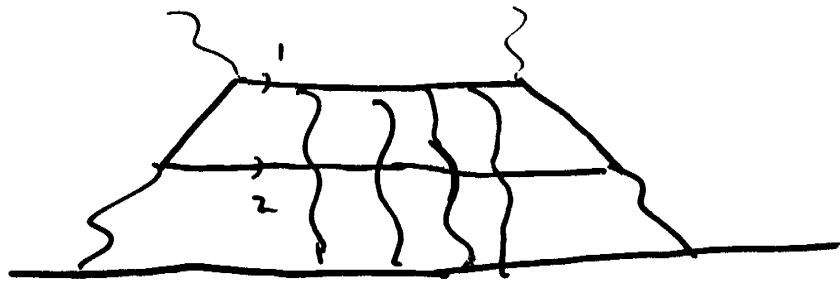
McClerran et al

Consider



$$g^+ \leq 0$$

In Feynman gauge, must keep

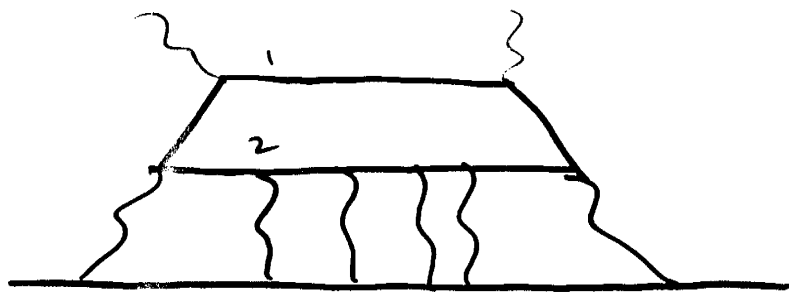


Shadowing
effect from
on-shell
states

$$|m|^2 \Rightarrow \left| \frac{\sin [g^2 W(r_\perp, R_\perp) / 2]}{g^2 W(r_\perp, R_\perp) / 2} m_0 \right|^2$$

$$\begin{aligned} W(r_\perp, R_\perp) &= \int d^2 k_\perp \frac{1 - e^{i r_\perp \cdot \vec{k}_\perp}}{k_\perp^2} e^{i R_\perp \cdot \vec{k}_\perp} \\ &= \frac{1}{2\pi} \log \left(\frac{|R_\perp + r_\perp|}{|R_\perp|} \right) \end{aligned}$$

In Light-Cone gauge (Korchemsky prescription)
 must keep



Final state
 rescattering
 of P_2 line

These graphs are suppressed in Feynman gauge
 but in l.c.g

$$d_{lc}^{\mu\nu} = \frac{i}{k^2 + i\epsilon} \left[-g^{\mu\nu} + \frac{n^\mu k^\nu + n^\nu k^\mu}{n \cdot k} \right]$$

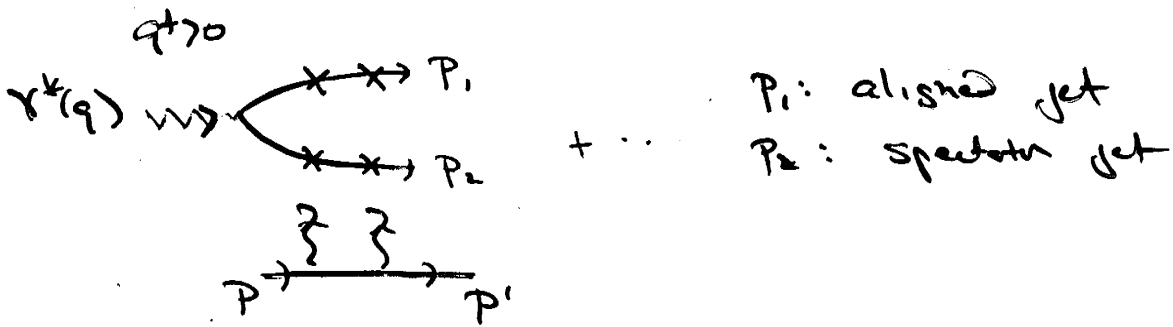
and $n \cdot k = k^+ = O(\frac{1}{v})$ for on-shell states!

* Result: identical answer as Feynman gauge

* Not included in l.c.g wavefunctions!

M-L, PV prescriptions differ by res. 3. trans.

Effect of Rescattering on the DIS Cross Section

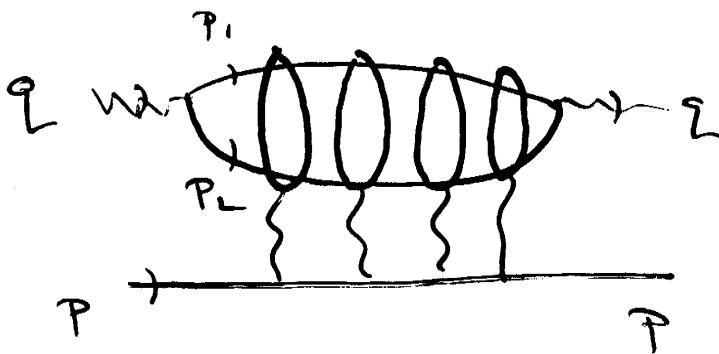


$$Q^4 \frac{d\sigma}{dQ^2 dx_B} = \frac{\alpha}{16\pi^2} \frac{1-y}{y^2} \frac{1}{2Mv} \int \frac{dP_{\perp}^-}{P_{\perp}^-} d^2r_{\perp} d^2R_{\perp} |M|^2$$

$$|M| = \left| \frac{\sin [g^2 W(\vec{r}_{\perp}, \vec{R}_{\perp})/2]}{g^2 W(\vec{r}_{\perp}, \vec{R}_{\perp})/2} M_{\text{Born}}(P_{\perp}^-, \vec{r}_{\perp}, \vec{R}_{\perp}) \right|$$

< 1 for all $\vec{r}_{\perp}, \vec{R}_{\perp}$

Equiv. to sum of cuts of forward virt. const. angl.



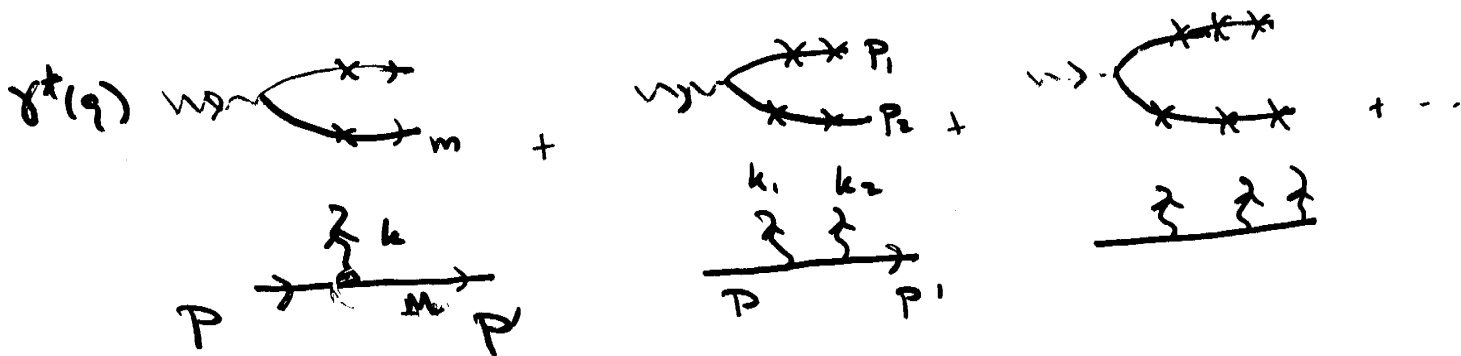
Find shadowing only arises from diagrams involving attachments to P_1 in F.G.

Cuts give Glauber-Gribov shadowing

Same result as Feynman, l.c.g. (ML)

↑ from $\frac{2P_{\perp}^-}{kt^+}$ term

Model calculation



Scalar quarks, crossed + uncrossed graphs, large + seagulls

Eikonal factorization in $\vec{r}_\perp, \vec{R}_\perp$
 Verified to 3-loops in Feynman, l.e.g.

$$* \quad \mathcal{M} = \mathcal{M}_{\text{Born}} [1 - e^{-ig^2 W}]$$

$$\mathcal{M}_{\text{Born}} = -2ieM Q P_2^- V(m, r_\perp)$$

$$V(m, r_\perp) = \int \frac{d^2 P_\perp}{(2\pi)^2} \frac{e^{i\vec{r}_\perp \cdot \vec{P}_\perp}}{P_\perp^2 + m^2} = \frac{1}{2\pi} k_0(m, r_\perp)$$

$$m^2 = P_2^- M X_B + m^2$$

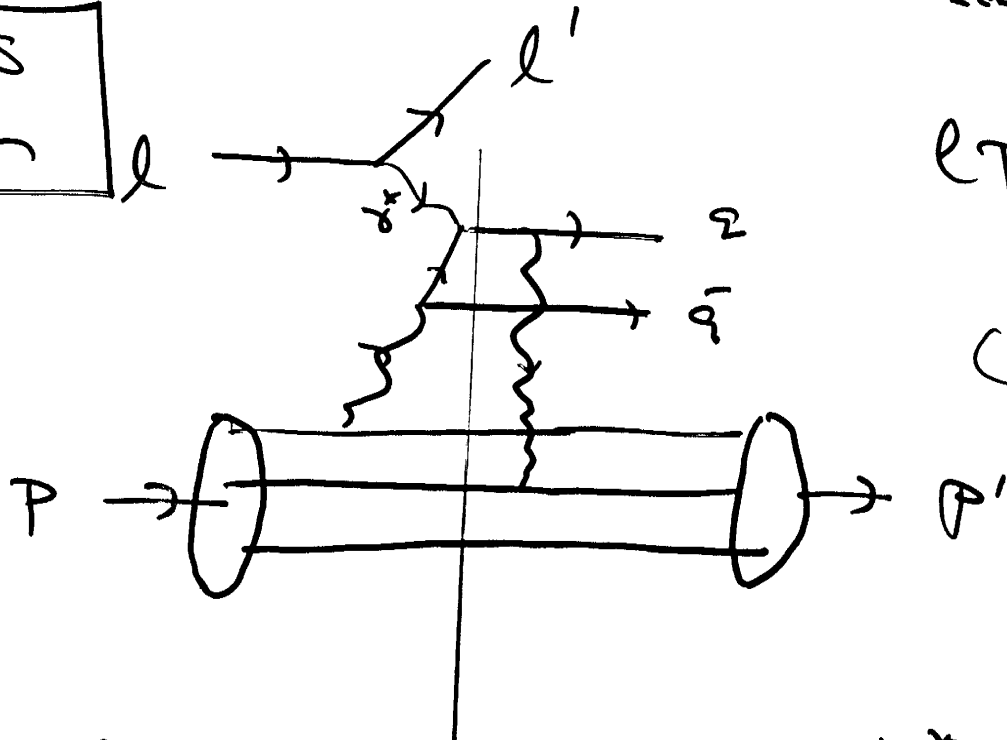
$$W(\vec{r}_\perp, \vec{R}_\perp) = \int \frac{d^2 k_\perp}{(2\pi)^2} \frac{1 - e^{i\vec{r}_\perp \cdot \vec{k}_\perp}}{k_\perp^2} e^{i\vec{R}_\perp \cdot \vec{k}_\perp} = \frac{1}{2\pi} \ln \frac{R_\perp}{r_\perp}$$

$$Q^4 \frac{d\sigma}{dQ^2 dk_B} = \frac{\alpha}{16\pi^2} \frac{1-y}{y^2} \frac{1}{2Mv} \int \frac{dP_2^-}{P_2^-} d^2 r_\perp d^2 R_\perp |M|^2$$

Non-universal Pomeron Coupling

Hoyer, Peigné, Muraud
Semin, VSB

DIS
Diffraction



$l \rightarrow l' p' X$
($190 \text{ } g^2$)

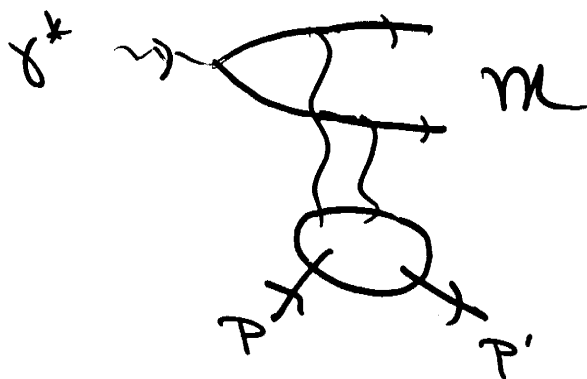
- 2nd gluon occurs after γ^* interaction exchange
- Cut gives imaginary phase!
- Coupling depends on color dipole moment \uparrow Q^2
Hebecker, Quack, SJD
- oo Pomeron not part of proton wf.
- Not universal!

$P_{\gamma/P}(x), P_{g/P}(x), P_{\bar{g}/P}(x), P_{P/P}(x)$

No!

Diffractive Dissociation (large rapidity gaps)

is leading twist in QCD



$$\frac{d\sigma}{dM^2}(\gamma^* P \rightarrow M P')$$

Review by Hebecker
Kopelke, Nicksow

$$\frac{d\sigma_T}{dM^2} \sim \left(\frac{1}{m^2 + Q^2} \right)^2,$$

$$\sigma_T \sim \frac{1}{Q^2}$$

aligned jet regime

$B_j + \log \sigma_T$

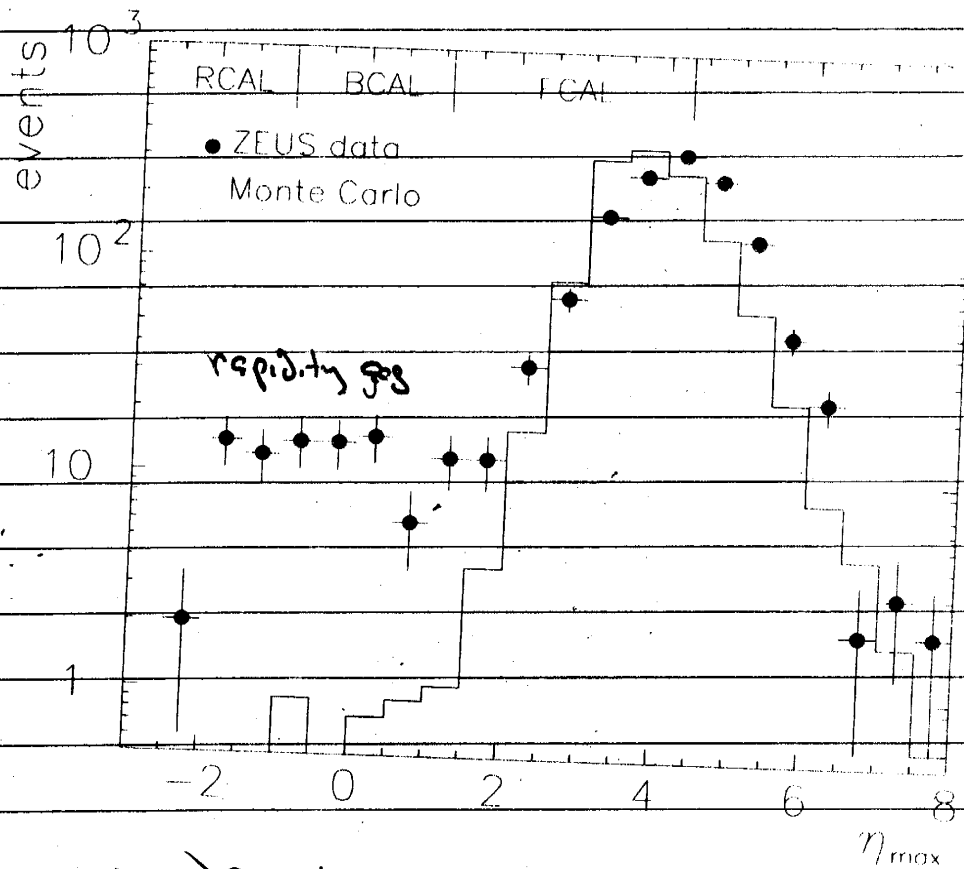
large color dipole

Hoyer, Magner, SJB

- Coherence for $L_{\perp \text{max}} = \frac{2\sqrt{2}}{Q^2} > R_N$

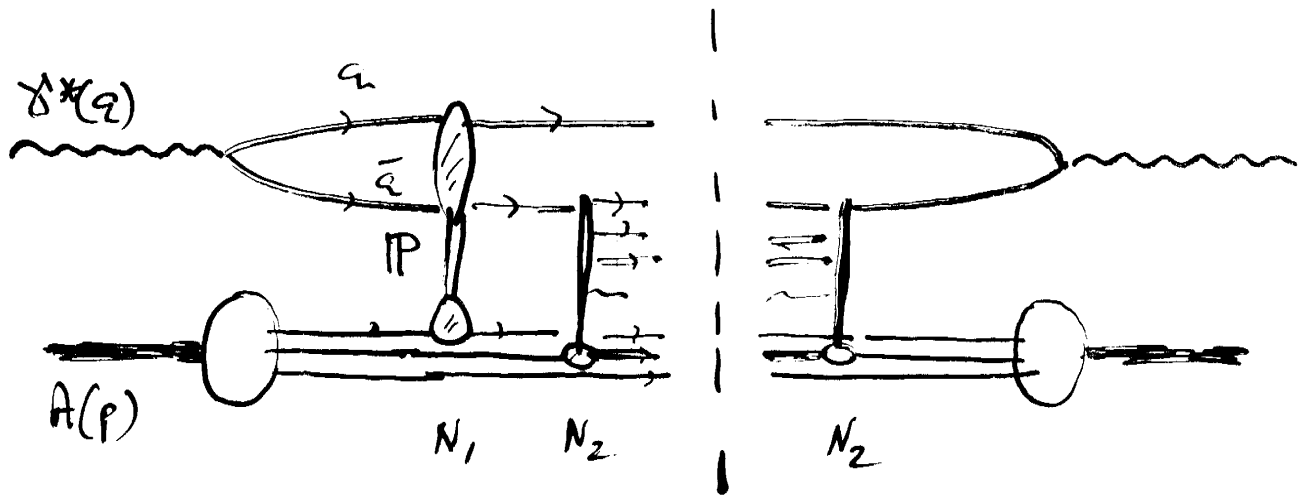
- Shadowing in nuclei for

$$L_{\perp \text{max}} = \frac{2\sqrt{2}}{Q^2} > R_A$$



minimal excitation
 of proton

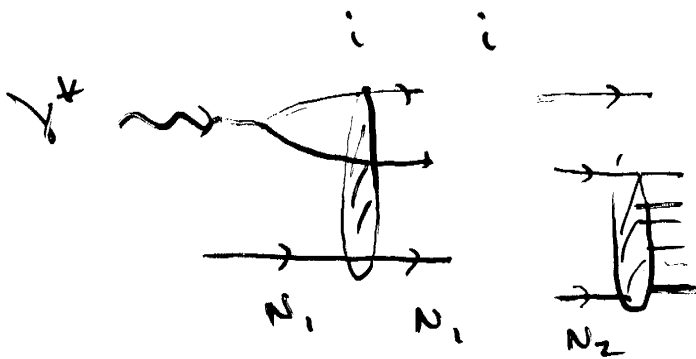
Ref: Hebecker
 hep-ph/9909504



- Nuclear shadowing due to destructive interference
of diffracted amplitude (2-steps + 1-step)

Glauber, Gribov

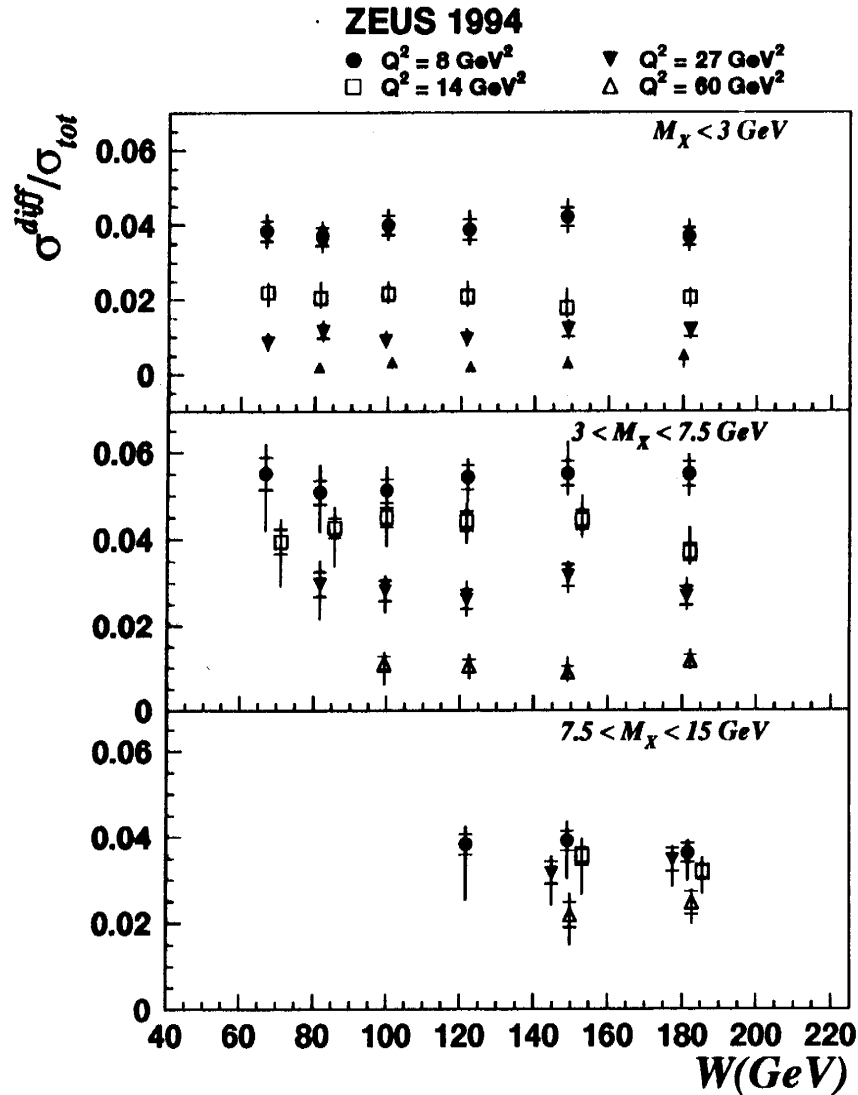
→ Phase structure critical



→ Diffraction $\gamma^* N_1 \rightarrow \bar{q} q N_1$ } leading twist
} finite fraction
of JPS

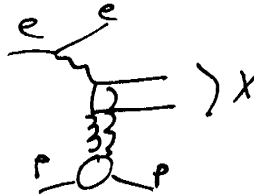
* None of this in l.c. wfs!
- $\Psi(x, k_T)$ real! FST!

Comparison of diffractive and DIS cross sections



Diffractive cross section has same energy dependence as inclusive cross section !

p QCD



$$\frac{\sigma^{\text{diff}}}{\sigma^{\text{tot}}} \sim \frac{(xg)^2}{(xg)} \sim (W^2)^{\text{eff}}$$

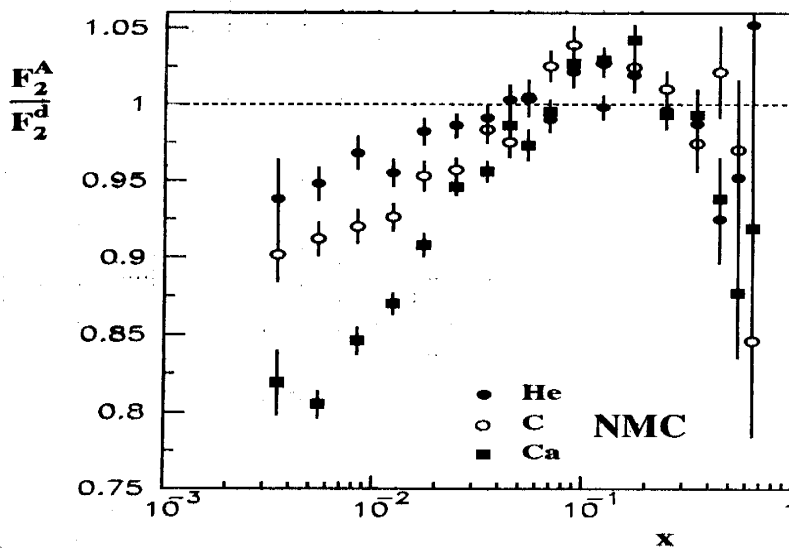
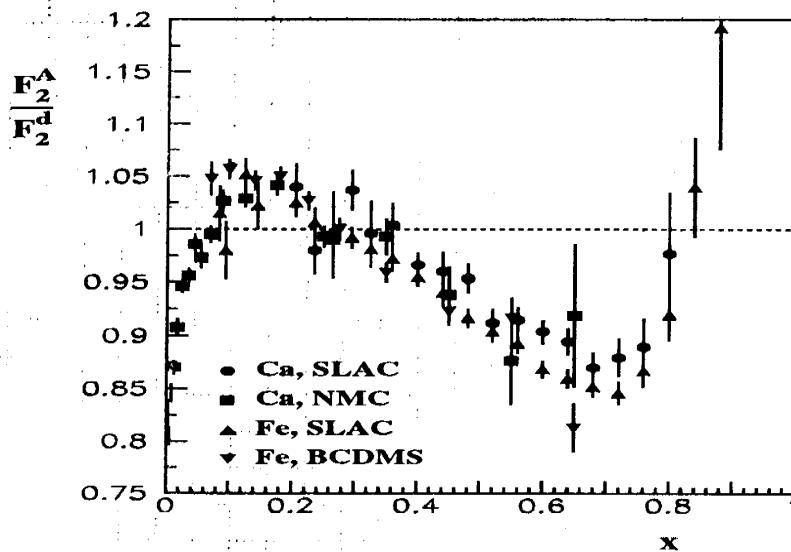
optical theorem

$$\frac{d\sigma^{\text{diff}}}{dt} \Big|_{t=0} \sim \sigma^{\text{diff}} \sim (\sigma^{\text{tot}})^2 \sim (W^2)^{\text{eff}}$$

Regge

$$\sigma^{\text{diff}} \sim (W^2)^{0.03}$$

Nuclear structure functions



coherence length of hadronic configurations

$$\lambda \simeq \frac{1}{Mx} > 2 \text{ fm} \leftrightarrow x < 0.1$$

* Nuclear shadowing due to
destructive interference of
 diffractive channels.

Pomeron exchange $\Rightarrow i$ $(-e^{i\pi\alpha_P(0)})$
 Cut contribution $\Rightarrow i$

* But $\Psi_{n/N}(x_i, \vec{k}_{zi}, d_i)$
 $\Psi_{n/A}(x_i, \vec{k}_{zi}, d_i)$

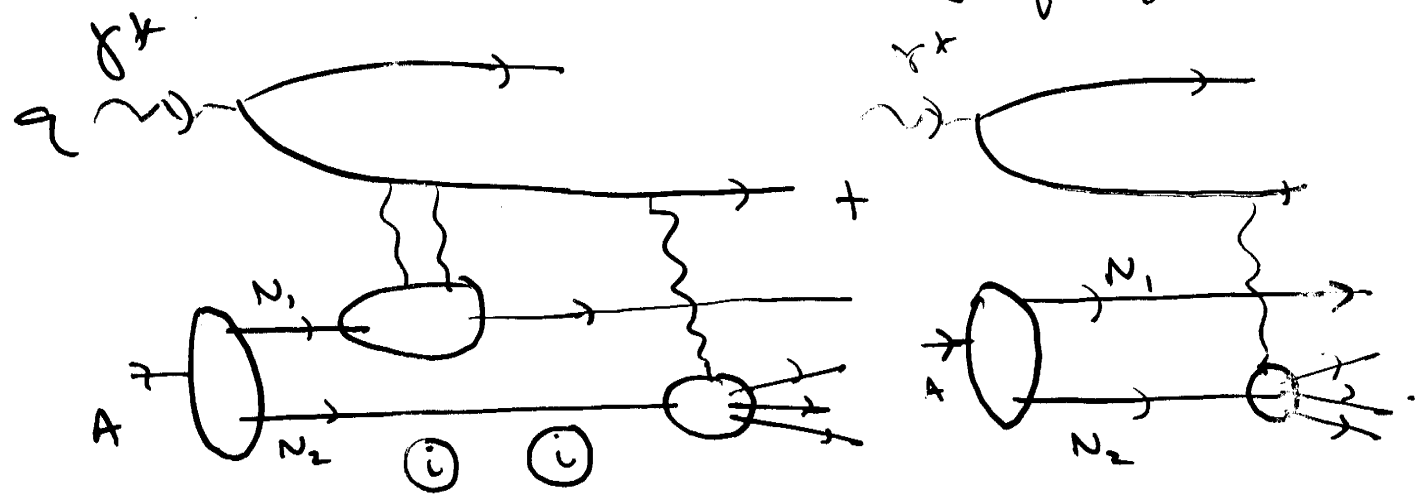
are real! No phase info from
 intermediate or shell states
 for stable targets.

— Anti-shadowing from non-singular
 Reggeon exchange.

H.J. Lu
 + S.J.B.

Diffraction leads to nuclear shadowing:

Gribov, Glauber
Pomplun, Gottfried & Susskind
Gottfried & Susskind



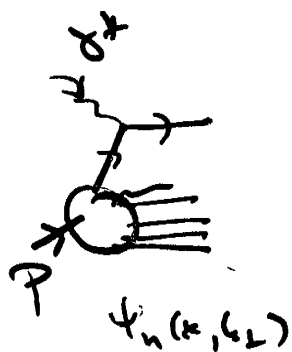
- * Destructive interference leads to shadowing at low x .
Frankfurt, St. Petersburg
- * Shadowing \rightarrow quark, gluon distributions
- * Reggeon exchange leads to antishadowing
Lu, S.B

Paradox

- * Nuclear shadowing is result of
 - destructive interference of diffractive amplitudes
- ∴ Phases are critical

- * Diffractive Dissociation of Proton
 - leaves proton intact
 - leading twist, finite fraction of DIS
- ⇒ Contradiction with usual assumption (parton model)

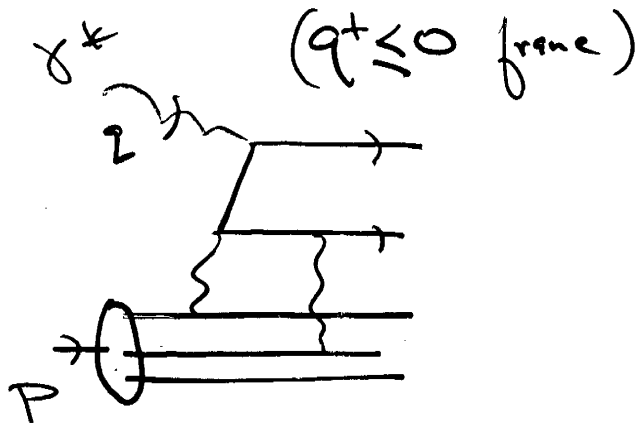
$$F_2(x, Q^2) = \sum_f e_f^2 \times q(x, Q^2)$$



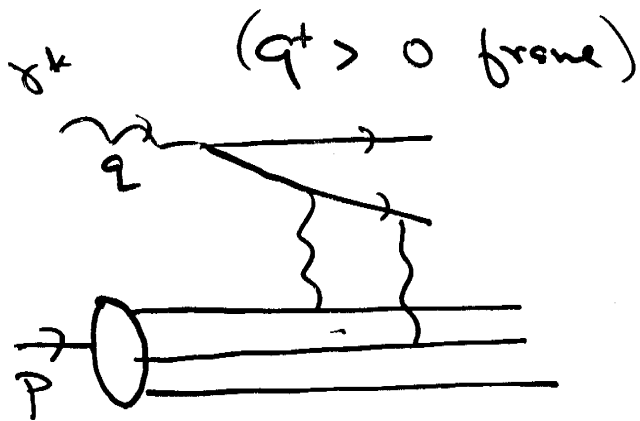
$$q(x, Q^2) = \sum_n \int [d^2k_T / dx] |\Psi_n(x, k_z)|^2$$

light-cone prob. distributions

$\Psi_n(k, k_z)$ are real!



Non-zero
 Diffractive contribution
 to DIS
 Leading Twist.

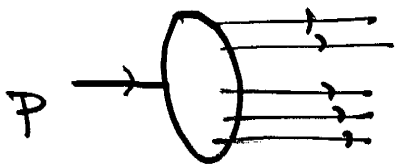


Color Dipole
 Model
 for Diffractive DIS

Not part of LC Prob. Distribution!

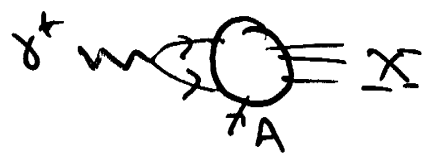
Complex Phase vs.

Real LC Wavefunction

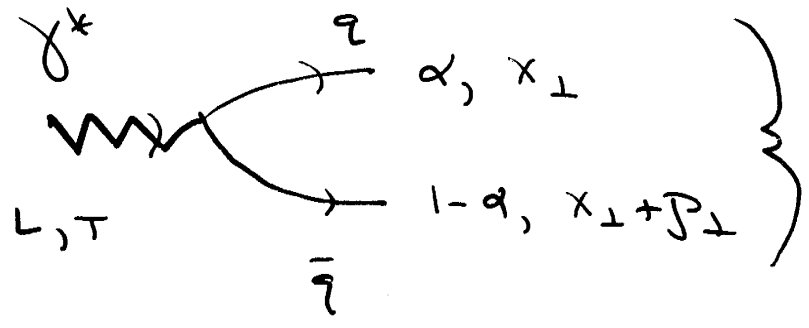


Real w.f. for stable proton

Color dipoles \Rightarrow analyzing quark interactions
in nuclei



Kopeliovich
SJB, Hebecker, Quark,
Piller et al



$$\Psi_{\gamma^*}(\alpha, p_\perp)$$

DIS:

$$\sigma_{T,L}^{\gamma^*}(v, Q^2) = \int_0^1 d\alpha \int d^2 p_\perp \sigma(p_\perp) W_{T,L}(\alpha, p_\perp)$$

$\bar{q}q$ cross section on target

$$W_T(\alpha, p_\perp) = \frac{6\alpha_{em}}{(2\pi)^2} N^2 [\alpha^2 + (1-\alpha)^2] k_\perp^2(Np)$$

$$W_L(\alpha, p_\perp) = \frac{24\alpha_{em}}{(2\pi)^2} N^2 [\alpha(1-\alpha)] k_0^2(Np)$$

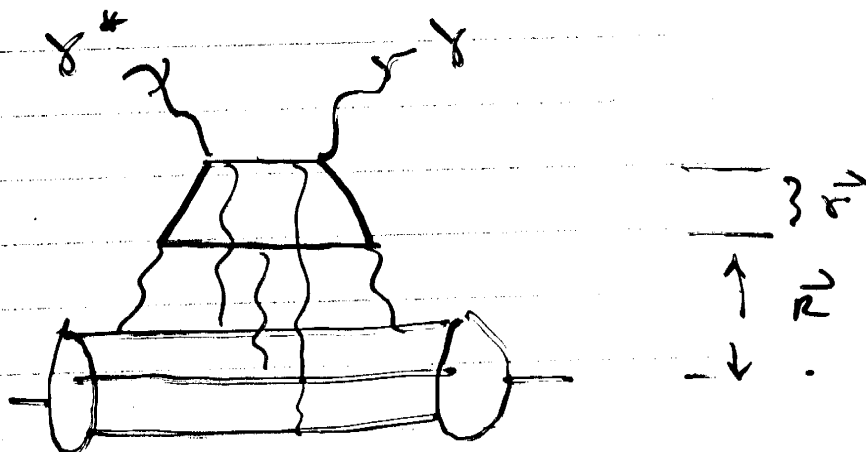
$$N^2 = \alpha(1-\alpha)Q^2$$

* W_T : large p : $A^{2/3}$

* W_L : small p : A^1 color transparency

Drell-Yan: $\sigma_T, \sigma_L, \sigma_{LT}, \sigma_{TT}$

Is the hardball approximation for DVCS accurate?



Dipole-
dipole
interactions

Khrapavich
Hebecker, Quack
SIB

I. DIS, FSI and shadowing, diffraction

$$W = \frac{1}{2\pi} \log \frac{|\vec{R} + \vec{r}|}{|\vec{R}|}$$

Correction factor

$$\frac{\sin^2 W g^{1/2}}{W^2 g^{1/2}} < 1$$

Hoyer
Peters
Mardel
Schnitz
SIB

Expect phases,
in DVCS

$$\sum_p \vec{k} \times \vec{k}'$$

SSA

Hwang
Schubert
SIB

Hwang, Verdehaegen (in progress)
SIB

Alternative:

Regge form gives phase
close, Gounis, SIB

for $\gamma^* p \rightarrow \gamma^* p$
LPS model

References

"Structure functions are not parton probabilities"

S.J.B., P. Hoyer, N. Merchal, S. Peigné
+ F. Sannino

PRD 65 114025 (2002) hep-ph/0104291

"Final-state interactions and Single-spin"

Asymmetries in Semi-inclusive Deep Inelastic Scat."

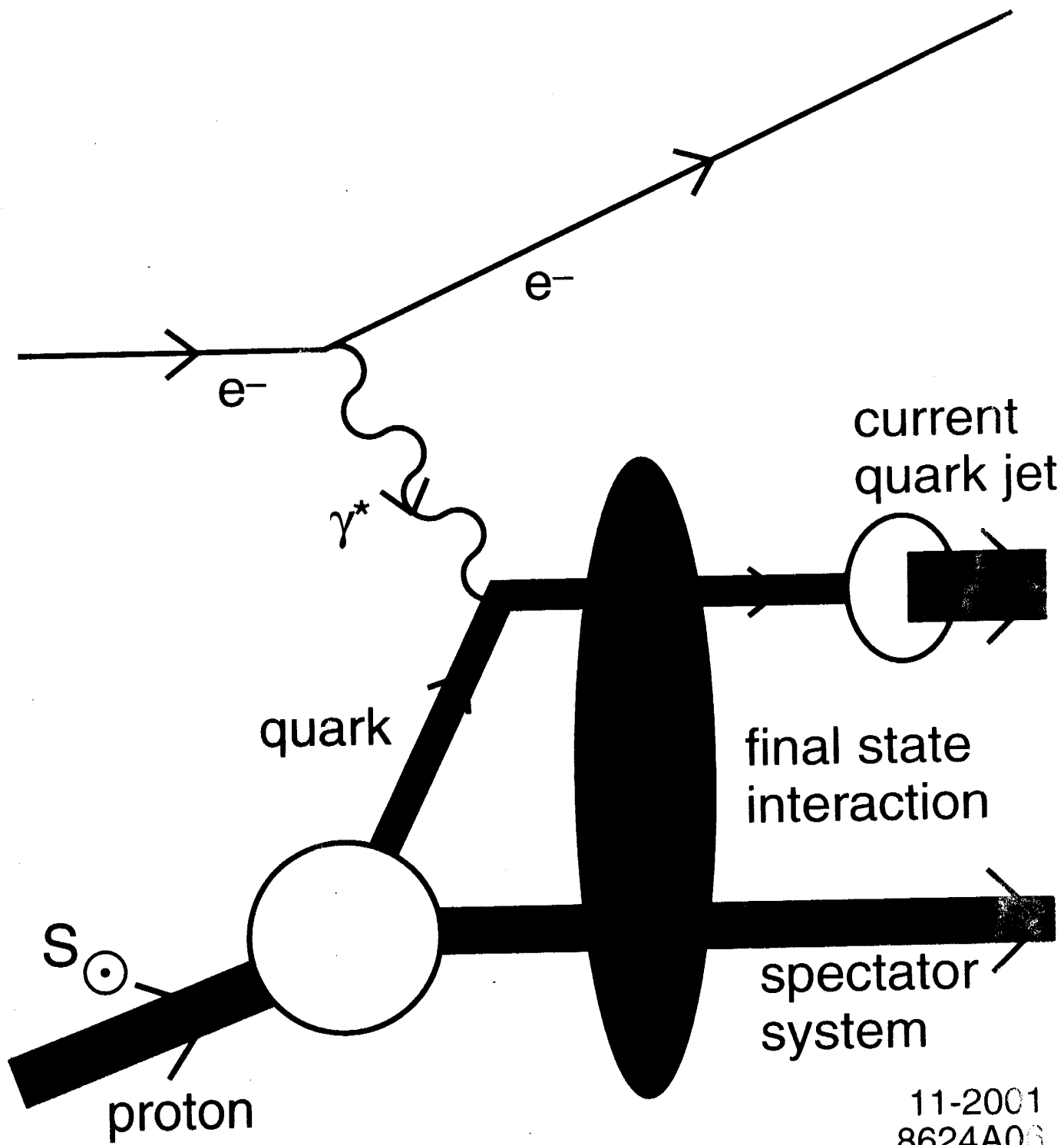
S.J.B., Dae Sung Hwang, I. Schmidt

PLB 530 99 (2002) hep-ph/0201296

* J.C. Collins hep-ph/0204004

* X. Ji + F. Yuan hep-ph/0206057

* S.J.B., A. Mebecher + E. Gorch PRD 55, 2584
(1997)



11-2001
8624A06

Hermes, SMC observe
 large proton spin asymmetry
 in $e\vec{p} \rightarrow e'\pi X$

$$A_{UN} = P_y \Rightarrow \int_P \cdot (\vec{q} \times \vec{p}_\pi) \quad \text{correlation}$$

T-odd : requires spin amplitudes
 with different phase

Conventional argument :

FSE from gluon exchange are

twist - 3 : so suppressed in Bj limit

Collins, Jaffe : opportunity to measure

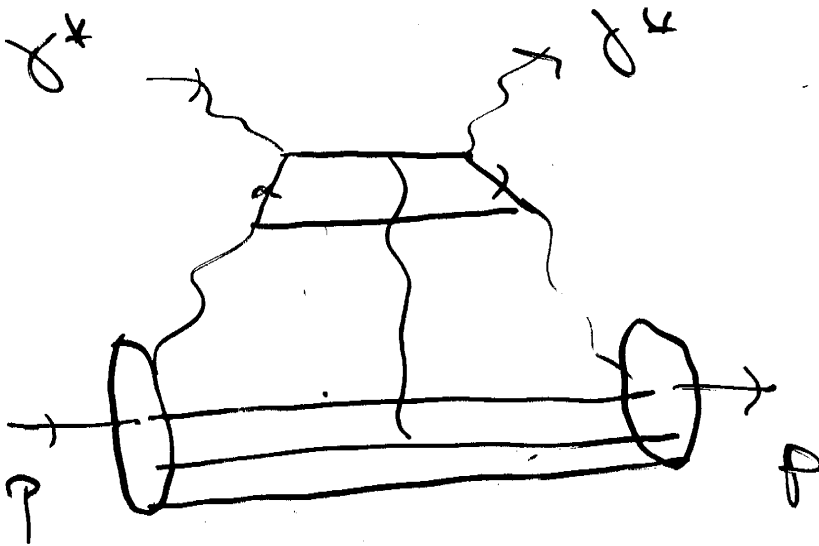
transversity : $\delta q \times H_{\perp}$

Single Spin Asymmetry $\underline{A_N} = A_{UN}$

$$i \vec{s} \cdot \vec{p} \times \vec{q}$$

Need interfering amplitudes
with non-zero phase.

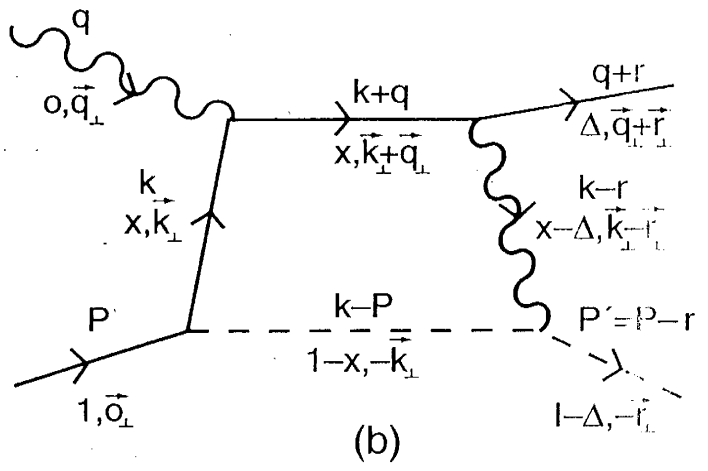
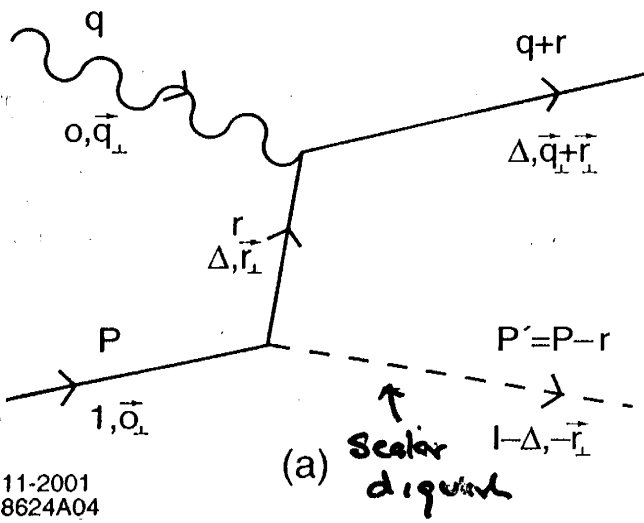
(otherwise \times)



Gauge
invariant

Rescattering \Rightarrow non-unitary phase
at leading twist!

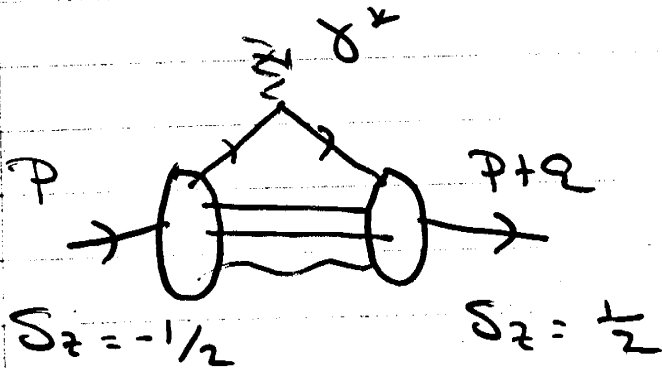
Hoyer, Mardel, Sennino, Peigne, 2023



11-2001
8624A04

Pauli Form Factor $F_2(q^2)$

$\kappa = F_2(0)$



Requires overlap of LCWFs with $\Delta L_z = 1$
Drell + Bj

e.g. (3q)
 $\psi^{1/2}$
 $-1/2 - 1/2 - 1/2$ \oplus
 $L_z = +2$

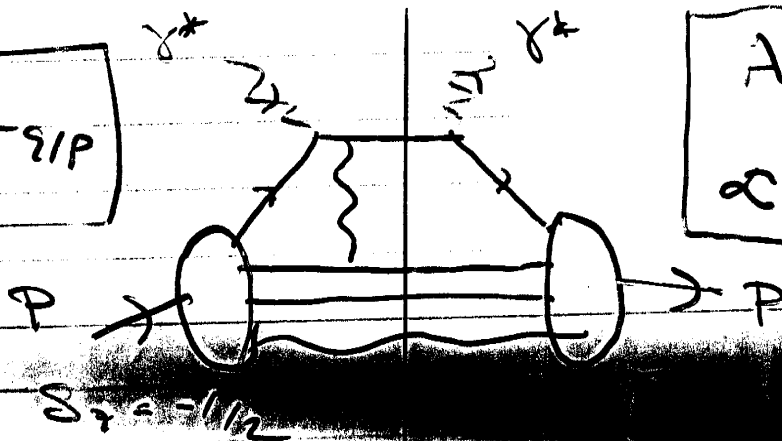
$\psi^{-1/2}$
 $-1/2 - 1/2 - 1/2$
 $L_z = +1$

$\psi^{1/2}$
 $1/2 1/2 - 1/2$ \oplus
 $L_z = 0$

$\psi^{-1/2}$
 $1/2 1/2 - 1/2$
 $L_z = -1$

Same matrix elements appear in SSA

$\kappa_P = \sum_{q \in P} e_q^2 \kappa_{q/P}$



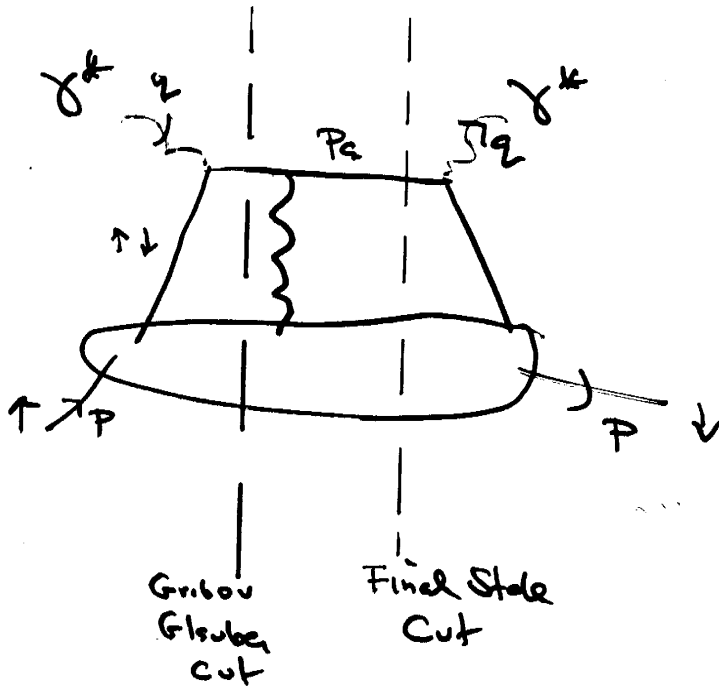
$A_{UN} = SSA$
 $\propto \sum e_q^2 \kappa_{q/P} \alpha_s$

Explicit calculation of FSI SSA I. A. Schmitz
 D.S. Hwang
 SdB

hep/ph/0201296

Collins, X. Ji

Overlap of wavefunctions with $\Delta L_z = 1$



$$[e^{i(\chi_1 - \chi_2)}]$$

$\chi_1 - \chi_2$: IR Finite

$$i \vec{S}_p \cdot \vec{q} \times \vec{P}_q = i \vec{S}_p \cdot \vec{q} \times \vec{r}$$

$$\vec{P}_q = \vec{q} + \vec{r}$$

$$P_y = A_n \approx \frac{\alpha_s(r_\perp^2) \times_{Bj} M |r_\perp^2| \ln r_\perp^2}{r_\perp^2}$$

Bjorken scaling for finite r_\perp

Some matrix elements as $a_p = F_2(0)$

$|\Psi^\uparrow(p^\uparrow, \vec{p}_\perp=0)\rangle$

$|\Psi^\uparrow(p^\uparrow, \vec{p}_\perp=0)\rangle$

$$= \int \frac{d^2 k_\perp dx}{\sqrt{x(1-x)} 16\pi^3} \left[\Psi_{+1/2}^\uparrow(x, \vec{k}_\perp) \left| \frac{1}{2}; x p^\uparrow, \vec{k}_\perp \right\rangle + \Psi_{-1/2}^\uparrow(x, \vec{k}_\perp) \left| -\frac{1}{2}; x p^\uparrow, \vec{k}_\perp \right\rangle \right]$$

$$\left[\begin{array}{l} \Psi_{+1/2}(x, \vec{k}_\perp) = \left(M + \frac{m}{x}\right) \varphi \quad L_z = 0 \\ \Psi_{-1/2}(x, \vec{k}_\perp) = -\frac{k'_\perp + i k^2}{x} \varphi \quad L_z = 1 \end{array} \right.$$

$$\varphi = \varphi(x, \vec{k}_\perp) = \frac{\frac{g}{\sqrt{1-x}}}{k^2 - \frac{k_\perp^2 + m^2}{x} - \frac{k_\perp^2 + \lambda^2}{1-x}}$$

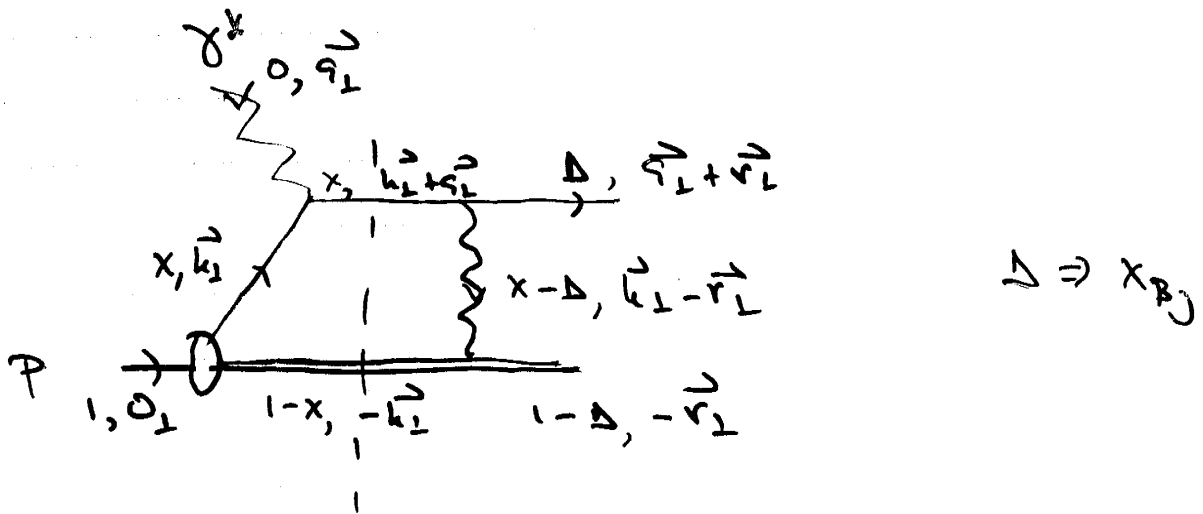
$$\left. \begin{array}{l} \rightarrow A(\uparrow \rightarrow \uparrow) = \left(M + \frac{m}{\Delta}\right) G \left(h + i \frac{e_1 e_2}{8\pi} \beta_1\right) \\ \rightarrow A(\downarrow \rightarrow \uparrow) = \left(\frac{r'_1 - i r^2}{\Delta}\right) G \left(h + i \frac{e_1 e_2}{8\pi} \beta_2\right) \end{array} \right.$$

$$G = -g e_1 p^\uparrow \sqrt{\Delta} 2\Delta(1-\Delta)$$

$$h = \frac{1}{r_\perp^2 + \Delta(1-\Delta) \left(-M^2 + \frac{m^2}{\Delta} + \frac{\lambda^2}{1-\Delta}\right)}$$

β_1, β_2 Coulomb phase
 for $L_z = 0, \pm$

Calculation of Final-State Phase



$$\text{Cut: } i\pi \delta \left(P^- + q^- - \frac{\lambda^2 + k_{\perp}^2}{(1-x)P^+} - \frac{m^2 + (k_{\perp}^2 + q_{\perp}^2)}{xP^+} \right)$$

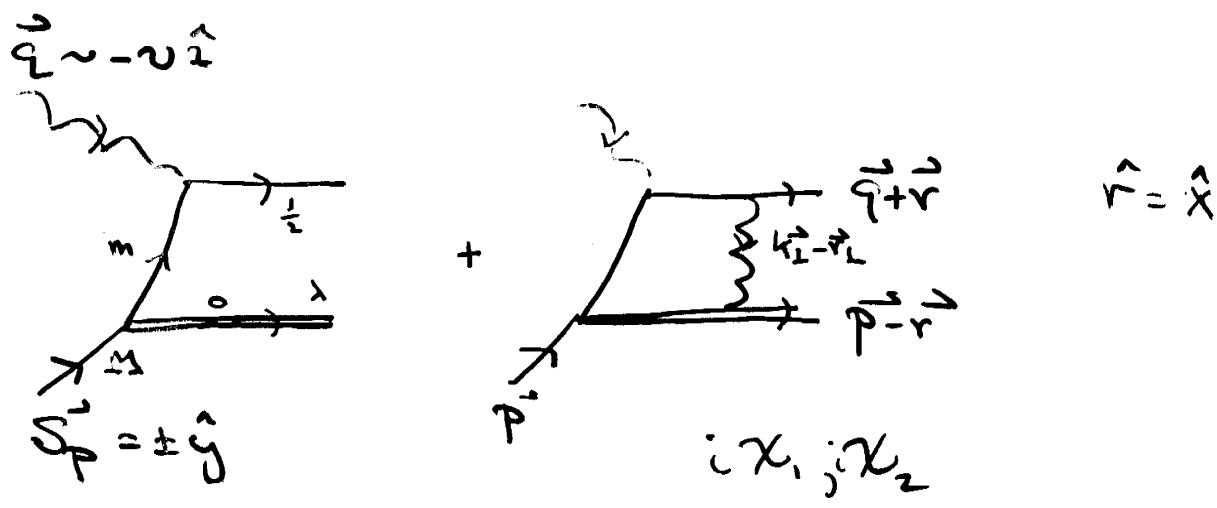
$$= \frac{i\pi}{P^+} \frac{\Delta^2}{q_{\perp}^2} \delta(x - \Delta - \delta), \quad \delta = 2\Delta \frac{q_{\perp}^2 + (k_{\perp}^2 - q_{\perp}^2)}{q_{\perp}^2}$$

$$g_1(L_2=20) = \int_0^1 dd \frac{1}{\alpha(1-\alpha)q_{\perp}^2 + \alpha\lambda^2 + (1-\alpha)\Delta(1-\Delta)(-k_{\perp}^2 + \frac{m^2}{\Delta} + \frac{\lambda^2}{1-\Delta})}$$

$$g_2(L_2=1) = \int_0^1 dd \frac{\alpha}{\dots}$$

$$* \quad g_1 - g_2 = \int_0^1 dd \frac{1-\alpha}{L} \quad \left. \vphantom{\int_0^1} \right\} \text{IR finite for } q_{\perp}^2 \neq 0$$

$$\frac{e_1 e_2}{4\pi} \Rightarrow (F d\delta(M^2 = e^{-\eta/2} (\vec{k}_{\perp} - \vec{v}_{\perp})^2)) \quad \text{in } \mathbb{R}^3.$$



$$\sigma \propto \epsilon^{abcd} P_\mu S_a Q_\nu r_c = M \vec{S} \cdot \vec{q} \times \vec{r}$$

$$A_n = P_y = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$$

$$= \frac{C_F \alpha_s (M^2) (\Delta M + m) r_x}{(\Delta M + m)^2 + r_\perp^2}$$

$$\otimes \left[r_\perp^2 + \Delta(1-\Delta) \left(-M^2 + \frac{m^2}{\Delta} + \frac{\lambda^2}{1-\Delta} \right) \right]$$

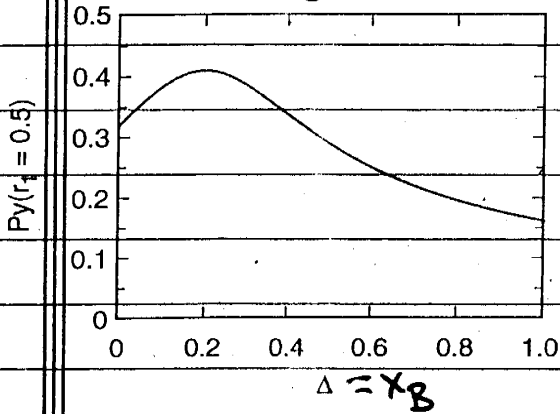
$$\otimes \left[\frac{1}{r_\perp^2} \ln \frac{r_\perp^2 + \Delta(1-\Delta) \left(-M^2 + \frac{m^2}{\Delta} + \frac{\lambda^2}{1-\Delta} \right)}{\Delta(1-\Delta) \left(-M^2 + \frac{m^2}{\Delta} + \frac{\lambda^2}{1-\Delta} \right)} \right]$$

$$\Delta = x_{Bj}$$

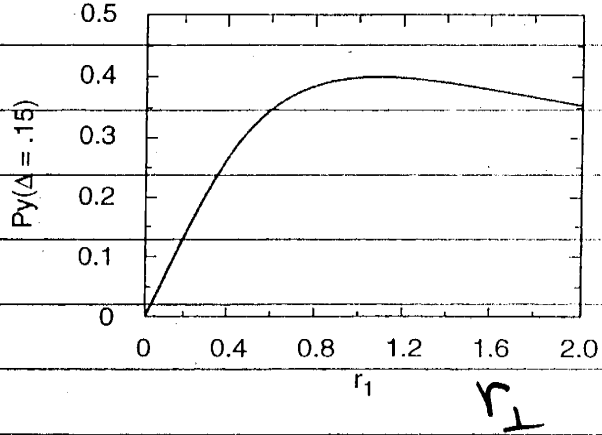
$$\mathcal{M}_{MS}^2 = \langle e^{-S/2} (k_\perp - r_\perp)^2 \rangle$$

$$P_y = A_{UT}$$

(a)

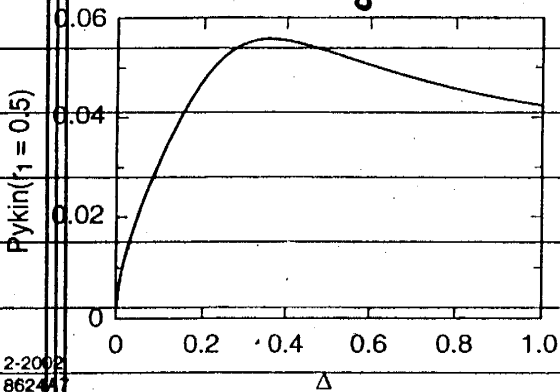


(b)

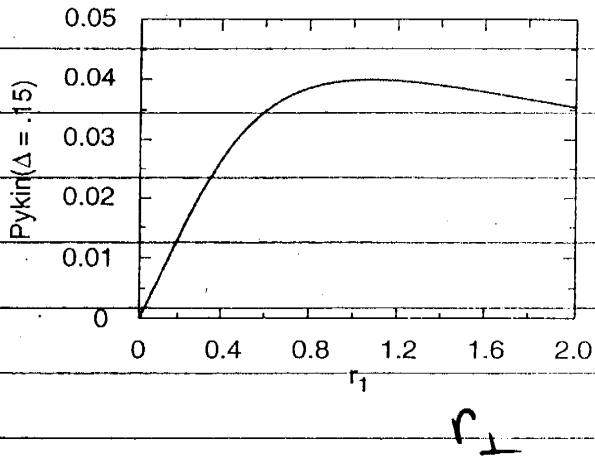


for S along Pe

(c)



(d)



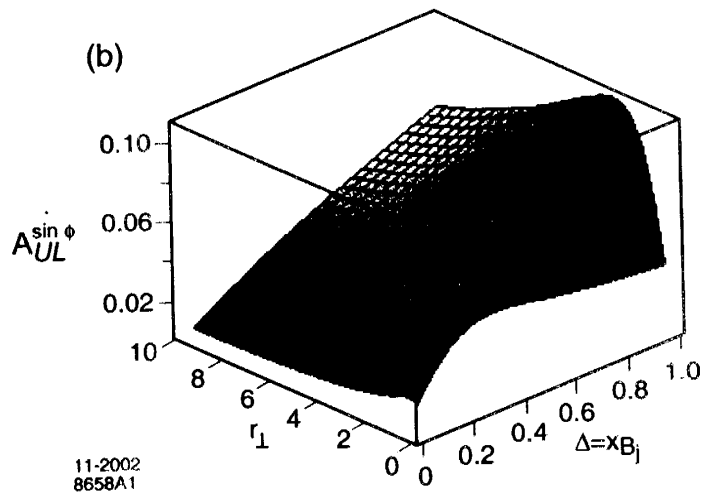
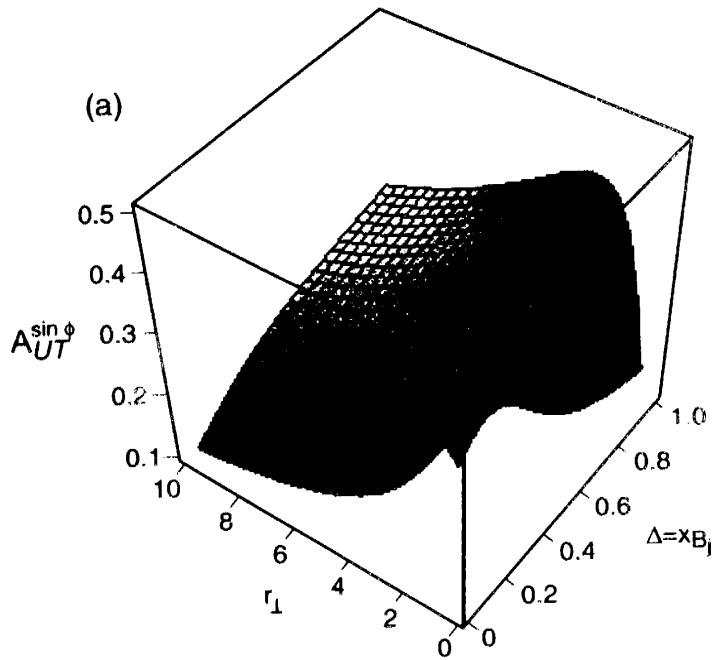
2-2002
862447

$$k = \frac{\Phi}{2} \sqrt{1-g} = \sqrt{\frac{2Mx_{23}}{E}} \sqrt{\frac{1-g}{g}}$$

$\sim 0.26 \sqrt{x_{23}}$
for Hermes

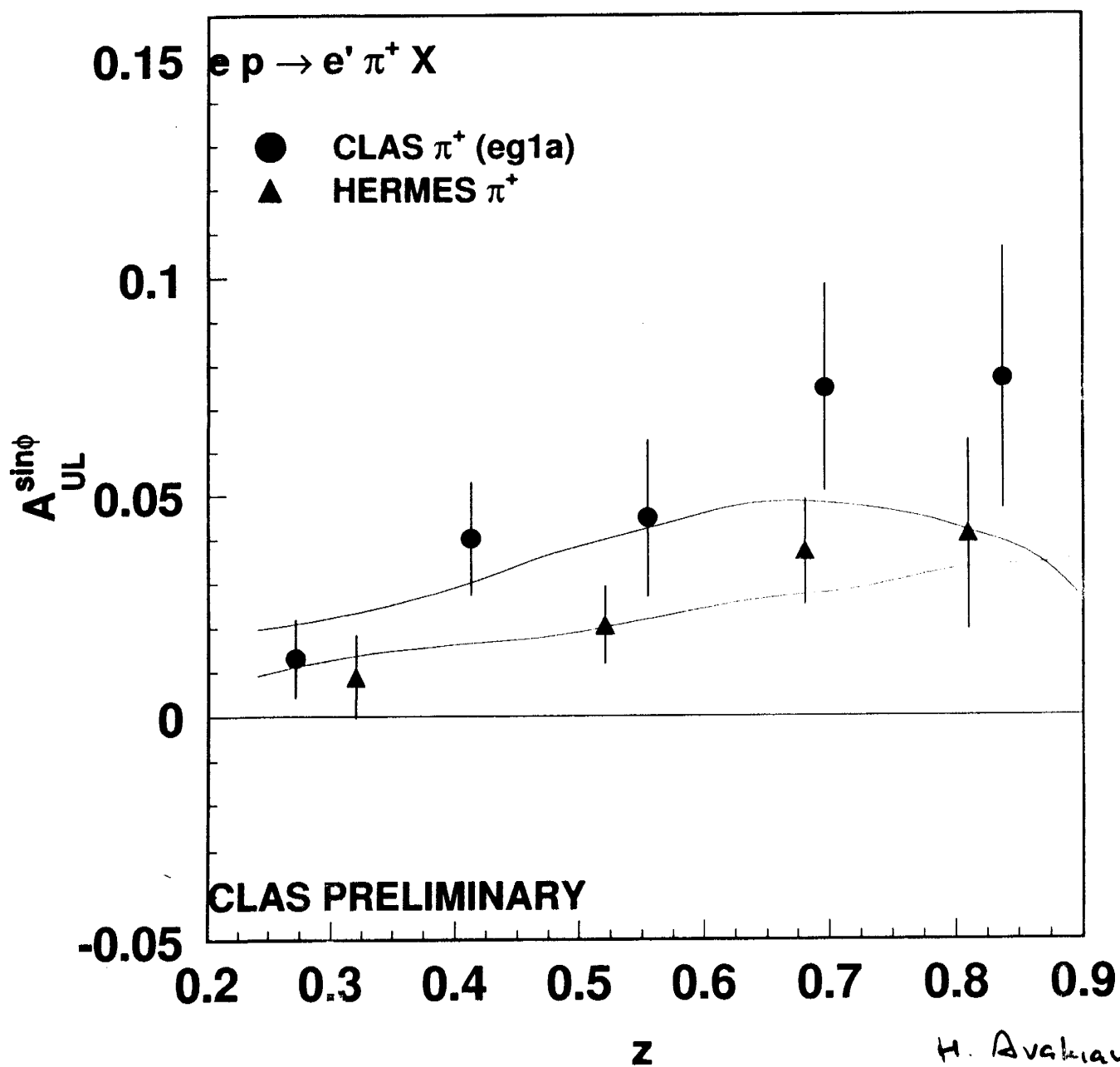
kinematic factor for $\hat{S}_p = \hat{e}$

probe polarization along incident light



11-2002
8658A1

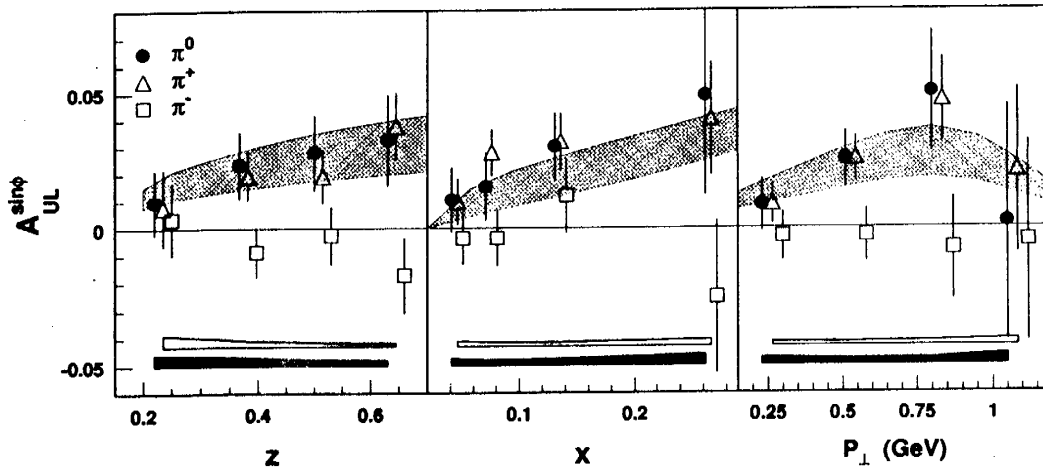
Prediction from BHS : Sivers Effect



Does Hermes see the Collins effect in A_{UL} ?

Yes ?

- Data agrees with u -quark dominance, follow predictions.
- Not much constraint on h_1 , band shows $g_1 \leq h_1 \leq (f_1 + g_1)/2$.



No ?

- Effect is suppressed with a longitudinal target.
- Compete with other higher-twist effects.
- Could be the Sivers Effect ?

Sivers Effect is T -odd, allowed in SIDIS?

S. Brodsky, D.S.Hwang and I. Schimdt, PLB 530, 99(2002).

- Quark final state interactions \Rightarrow a phase difference.
- T -odd Sivers distribution f_{1T} allowed at the leading order.

Confirmed by J. C. Collins, PLB 536, 43(2002).

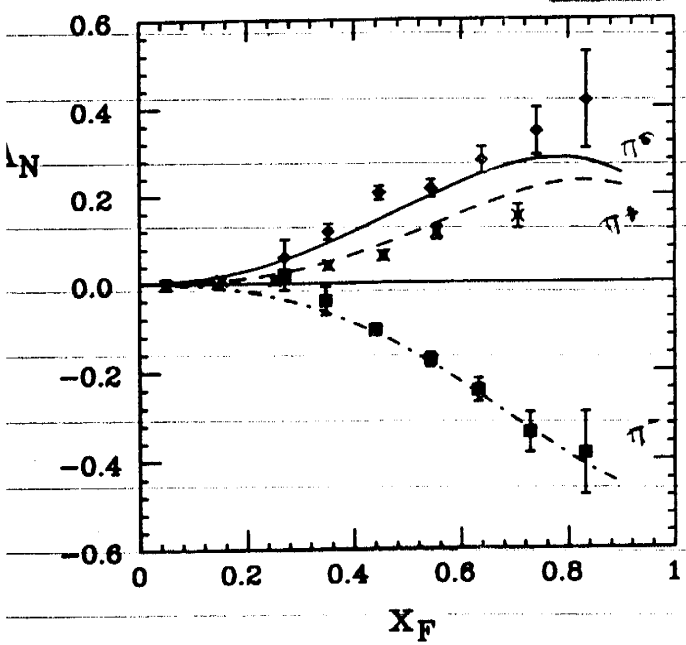
Light cone gauge approach: X. Ji and F. Yuan, PLB 543, 66(2002).

➔ SSA $A_{UT} \propto \kappa_N$ nucleon anomalous magnetic moment.
 $A_{UT}^{\pi^+}(p)$ and $A_{UT}^{\pi^-}(n)$ similar in size, opposite in sign.

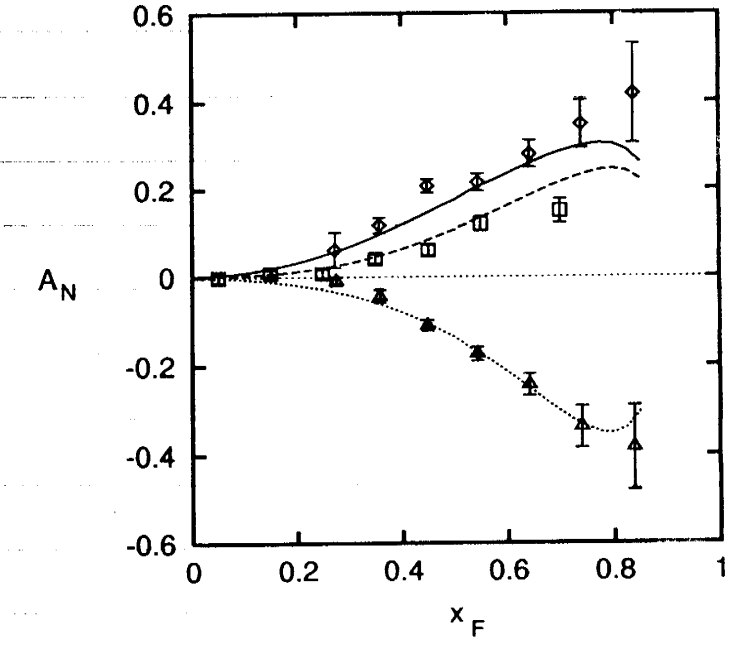
Collins Effect and Transversity

There is another possible explanation ...
 the E704 single-spin asymmetry could be due to:

Sivers Effect:
 T-odd distribution function



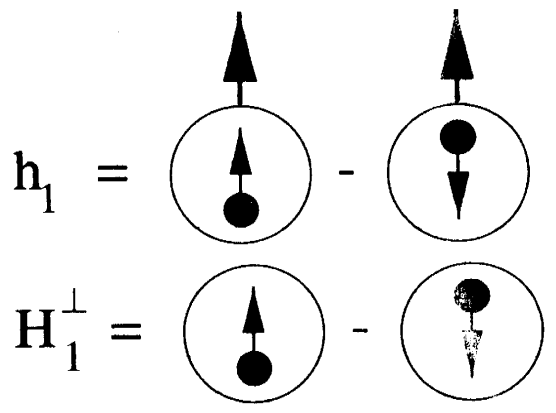
Collins Effect:
 T-odd fragmentation function H_1^\perp



Collins Effect

In this case, $A_N \sim h_1(x) H_1^\perp(z)$

\Rightarrow access to transversity!

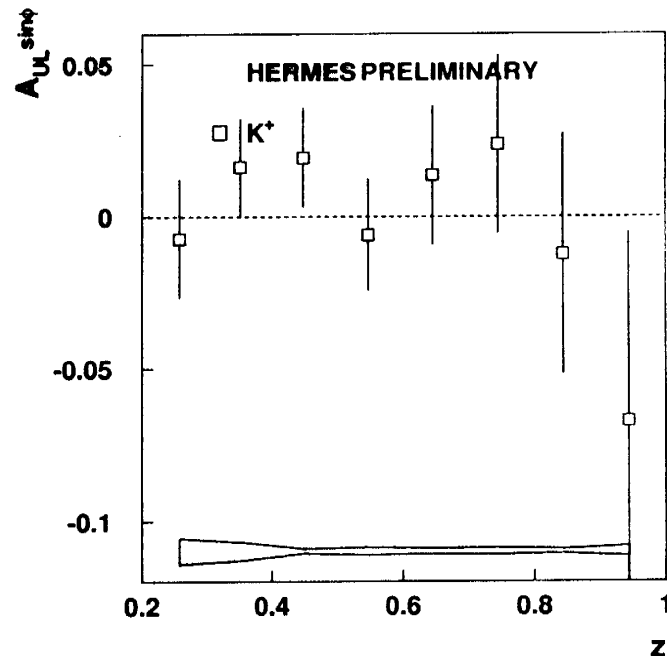
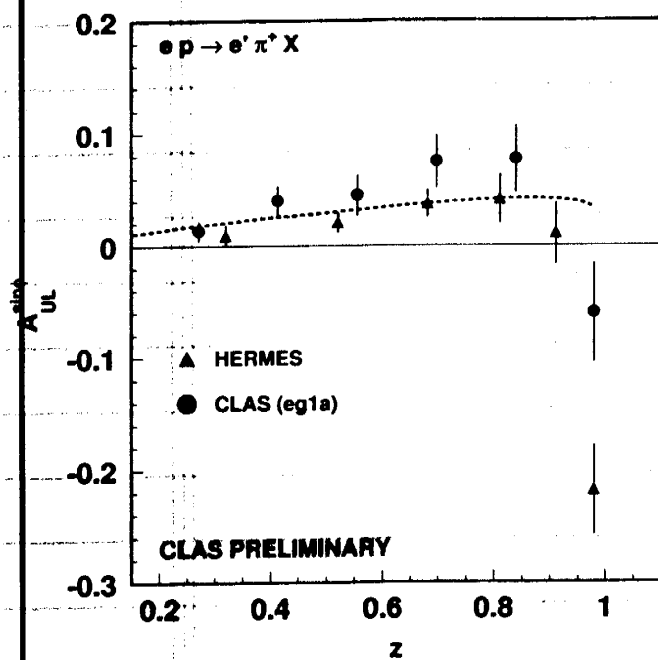


How to separate?

Single Spin Asymmetries in DIS

LPol Target SSA for π^+ and K^+

$$A_{UL} \propto D_L(y) \times \frac{h_L^u(x) H_1^u(z)}{u(x) D_1^u(z)} \quad ?$$



The z -dependence of target SSA from CLAS is consistent with HERMES measurement.

The behavior of target SSA for π^+ and K^+ is consistent in agreement with factorization and u -quark dominance.

$z \rightarrow 1$ Exclusive limit; coherence

Anomalous moment $\kappa = F_2(0)$

$$\kappa_p = \sum_q e_q \kappa_{q/p}$$

3 quark model:

$$\kappa_p = 2\left(\frac{2}{3}\right) \kappa_{u/p} + \left(-\frac{1}{3}\right) \kappa_{d/p}$$

$$\kappa_n = 2\left(-\frac{1}{3}\right) \kappa_{d/n} + \left(\frac{2}{3}\right) \kappa_{u/n}$$

Isospin: $\kappa_p + \kappa_n = \frac{2}{3} \kappa_{u/p} + \frac{1}{3} \kappa_{d/p}$

≈ 0

$$\kappa_{u/n} = \kappa_{d/p} \approx -2 \kappa_{u/p}$$

* Predict large SSA for neutron target

$$* \text{SSA}(\gamma^* n \rightarrow u X)$$

$$= -2 \text{SSA}(\gamma^* p \rightarrow u X)$$

$$* \text{SSA}(\gamma^* p \rightarrow d X) = -2 \text{SSA}(\gamma^* p \rightarrow u X)$$

Final State Interaction Produces

Single-Spin Asymmetry

with respect to the jet production plane

$$\vec{S}_p \cdot \vec{q} \times \vec{P}_{\text{jet}}$$

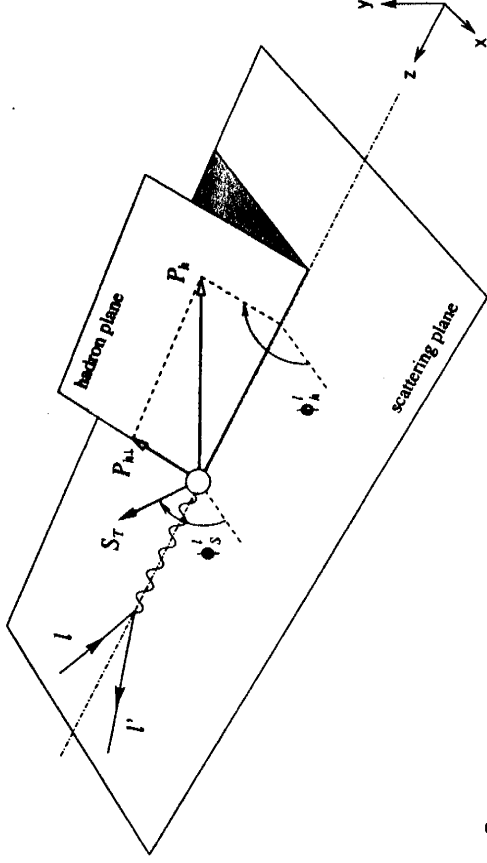
Find jet direction using thrust, etc.

Quark Fragmentation leads to

$$\vec{S}_p \cdot \vec{q} \times \vec{P}_\pi$$

- * New QCD mechanisms
- * Bjorken scaling
- * Reflects $\Lambda_{\text{QCD}} \neq 0$ Matrix elements.
- * Similar to $F_2(0)$

Collins effect vs Sivers effect



$$\begin{aligned}
 \sigma_{UT}(x, z, \mathbf{P}_{h\perp}^2) &= (\sigma_{UT})_{Collins} + (\sigma_{UT})_{Sivers} \\
 &= |S_T|(1-y) \cdot \frac{P_{h\perp}}{zM_h} \sin(\phi_h^\ell + \phi_S^\ell) \cdot \sum e_q^2 h_1^q(x) H_1^{\perp q}(z, \mathbf{P}_{h\perp}^2) \\
 &\quad + |S_T|(1-y + \frac{1}{2}y^2) \frac{P_{h\perp}}{zM_N} \sin(\phi_h^\ell - \phi_S^\ell) \cdot \sum e_q^2 f_{1T}^{\perp(1)q}(x) D_1^q(z, \mathbf{P}_{h\perp}^2)
 \end{aligned}$$

- Longitudinal target has $\phi_S^\ell = 0$. Need a transversely polarized target (Hermes run-II).
- Collins angle: $\phi_C = \phi_h^\ell + \phi_S^\ell$, \blackrightarrow target spin rotation \approx out-of-plane detection.

* Sivers effect: indep of ϕ_h^ℓ

: hadronization not necessary

Single-Spin Asymmetry in Semi-Inclusive DIS

Distinguish Sivers vs Collins Effects

- Sivers: $\vec{S}_p \cdot \vec{q} \times \vec{P}_{jet}$

* no hadronization necessary
 * observe quark direction $\vec{P}_q = \vec{P}_{jet}$

- Collins: T-odd fragmentation necessary

H, \pm : $\vec{S}_q \cdot \vec{P}_H \times \vec{P}_R$

- Sivers: $\sin(\phi_H^q - \phi_{SP}^q)$ indep. of $\phi_q^!$

- Collins: $\sin(\phi_H^q + \phi_{SP}^q)$

- Sivers: A_{UL}, A_{UT} same in charged current *
 $\nu p \rightarrow H X$

Collins: $A_{UL}, A_{UT} = 0$ *

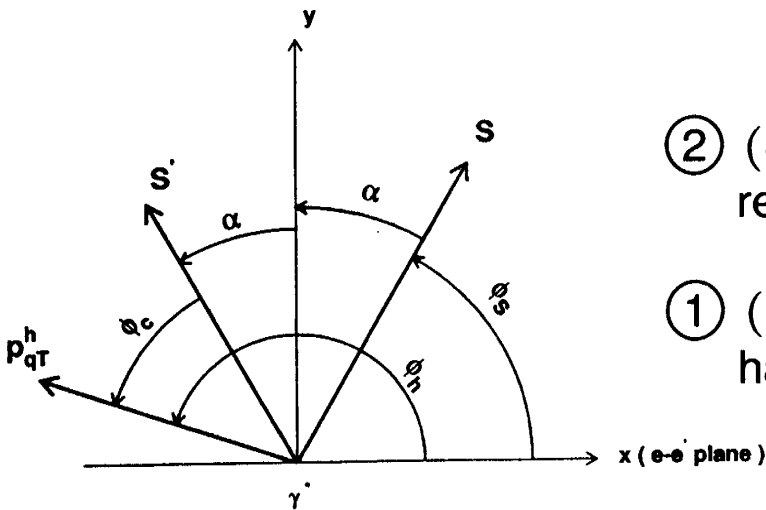
$\propto \frac{2C_L C_R}{C_L + C_R}$ $\neq 0$ neutral current

T-odd Distribution vs Fragmentation Function

There are actually two similar terms in $d\sigma_{UT}$...

$$\begin{aligned} \textcircled{1} \quad \sin(\phi_h^l + \phi_S^l) \quad \otimes \quad h_1 &= \begin{array}{c} \uparrow \\ \bullet \\ \uparrow \end{array} - \begin{array}{c} \uparrow \\ \bullet \\ \downarrow \end{array} \quad \otimes \quad H_1^\perp = \begin{array}{c} \uparrow \\ \bullet \end{array} - \begin{array}{c} \downarrow \\ \bullet \end{array} \\ \textcircled{2} \quad \sin(\phi_h^l - \phi_S^l) \quad \otimes \quad f_{1T}^\perp &= \begin{array}{c} \uparrow \\ \bullet \end{array} - \begin{array}{c} \bullet \\ \downarrow \end{array} \quad \otimes \quad D_1 = \begin{array}{c} \bullet \end{array} \end{aligned}$$

$f_{1T}^\perp = \text{T-odd distribution function}$



$\textcircled{2} \quad (\phi_h^l - \phi_S^l) = \text{angle of hadron relative to initial quark spin}$

$\textcircled{1} \quad (\phi_h^l + \phi_S^l) = \pi + (\phi_h^l - \phi_S^l) = \text{hadron relative to final quark spin}$

Cannot distinguish in:

- longitudinal-target case ...

→ transverse component has $\phi_S^l = 0$.

- inclusive π production, e.g. $p^\uparrow p \rightarrow \pi X$

→ jet axis not known

In general,

initial, final state interactions

will produce single-spin asymmetries

$$\vec{S} \cdot \vec{p}_1 \times \vec{p}_2$$

wrt virtually any production or
scattering plane!

Perturbatively calculable at large $r_{1\perp}^2, r_{2\perp}^2$

New measure of $\alpha_S(r_{1\perp}^2)$

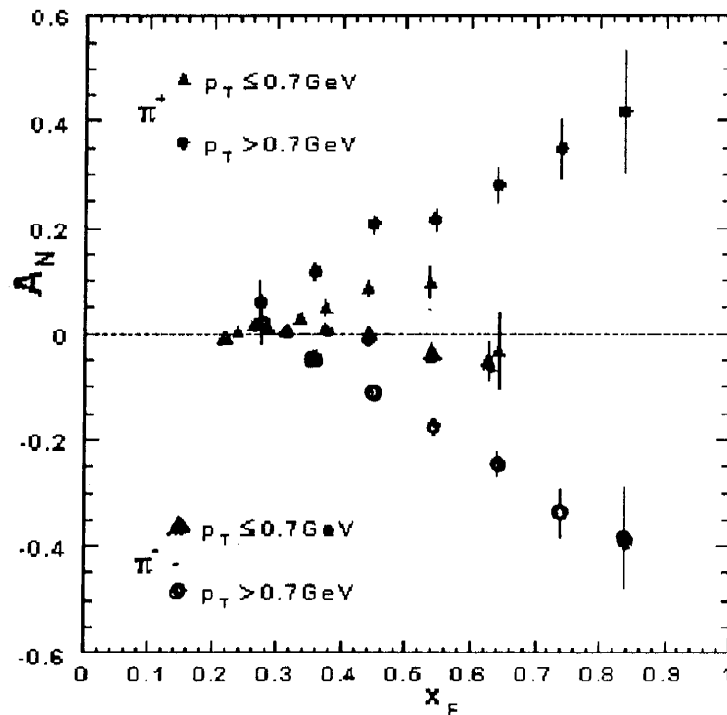
Application to Drell-Yan: $\vec{S}_p \cdot \vec{p}_\pi \times \vec{q}$
 $\pi p \rightarrow X^+ X^- X$

$e^+ e^- \rightarrow \Lambda_\tau X$: $\vec{S}_\Lambda \cdot \vec{p}_\Lambda \times \vec{q}$

AN: $p p \rightarrow \pi X$: $\vec{S}_p \cdot \vec{p}_\pi \times \vec{p}_p$

$p p \rightarrow \Lambda_\tau X$: $\vec{S}_\Lambda \cdot \vec{p}_\Lambda \times \vec{p}_p$

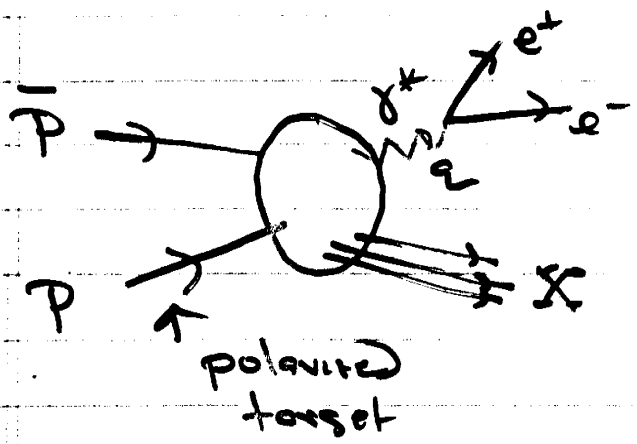
- Classic $\vec{k} \times \vec{p} \cdot \vec{s}_\perp$ asymmetry in $\vec{p}_\perp p \rightarrow \pi X$



E704 at Fermilab

- In QCD both these asymmetries are twist-three effects, expected to vanish like p_\perp / \sqrt{s}
 Nevertheless both are strikingly large. Unusual among twist three effects (for example g_2) which are usually hard to find.
- Concentrate on HERMES asymmetry here, although similar analysis applies to E704.

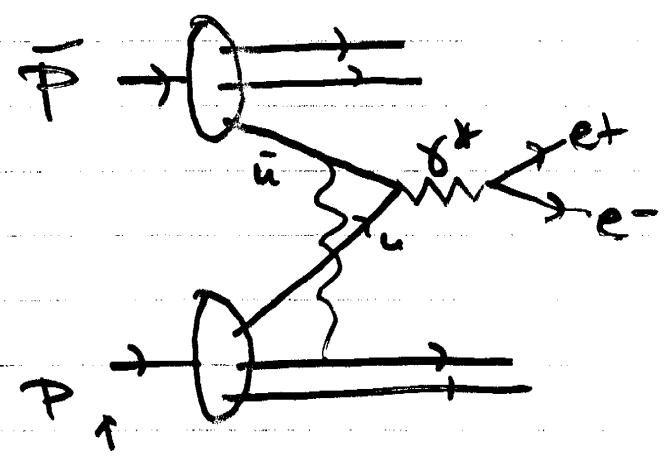
Single-Spin Asymmetries in \bar{P} collision



$$\vec{S}_P \cdot \vec{P}_{\bar{P}} \times \vec{Q}$$

"T-odd" observable

* New theory due to initial state gauge ints. for SIDIS



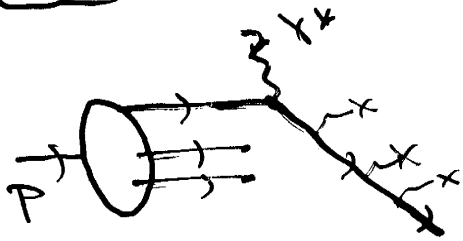
Interference of amplitudes produces phase gauge-indep

Same interference of $\Delta L_z = 1$ states prod. $M_A^{\bar{P}}$

* $A_{UN} \sim \alpha_s \frac{M r_{\perp}}{r_{\perp}^2 + M^2} M_A^e$ $\vec{Q} = \vec{P}_{\bar{P}} + \vec{r}_{\perp}$

- * Scales in Dy limit at fixed r_{\perp} !
- * opposite in sign to SIDIS SSA

Proposal by Ji and Yuan (also Collins)



$$\Psi \rightarrow \Psi L$$

complex phase

Augment LFWF (log) with phase

$$L_1 = \mathbb{P} \exp \left[i g \int_0^{\infty} d\tilde{z}_\perp \cdot \vec{A}_\perp (z^- = \infty, \vec{z}_\perp) \right]$$

where $\vec{A}_\perp = -\frac{g}{2\pi} \theta(z^-) \vec{\nabla}_\perp \ln \alpha^2 \vec{z}_\perp^2$ $\left\{ \begin{array}{l} + \\ - \end{array} \right.$

$$A^+ = A^- = 0$$

- corresponds to Coulomb field of charged particle moving at $v=c$

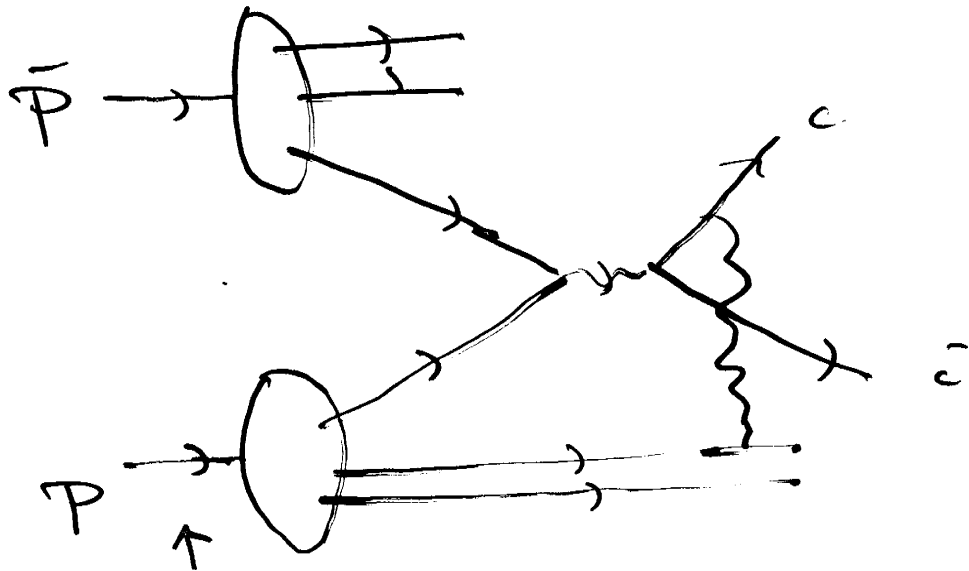
Equivalently

$$D^{\mu\nu}(q) = -\frac{i}{q^2} \left(g^{\mu\nu} - \frac{q^\mu n^\nu + q^\nu n^\mu}{q \cdot n + i\epsilon} \right)$$

* Non-causal b.c. (BHMPs)

* Process specific - not universal

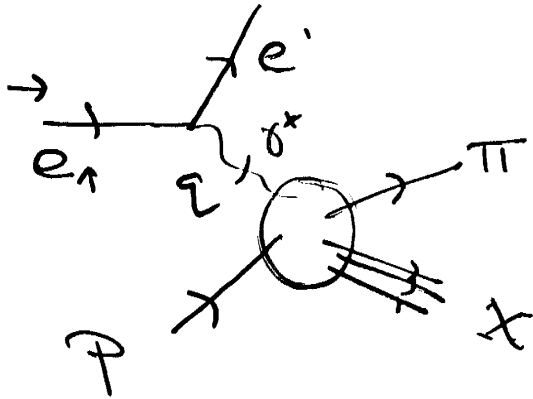
SSA in $\bar{P} P \rightarrow e X$



$$i \int \bar{P} \cdot P \times P_e$$

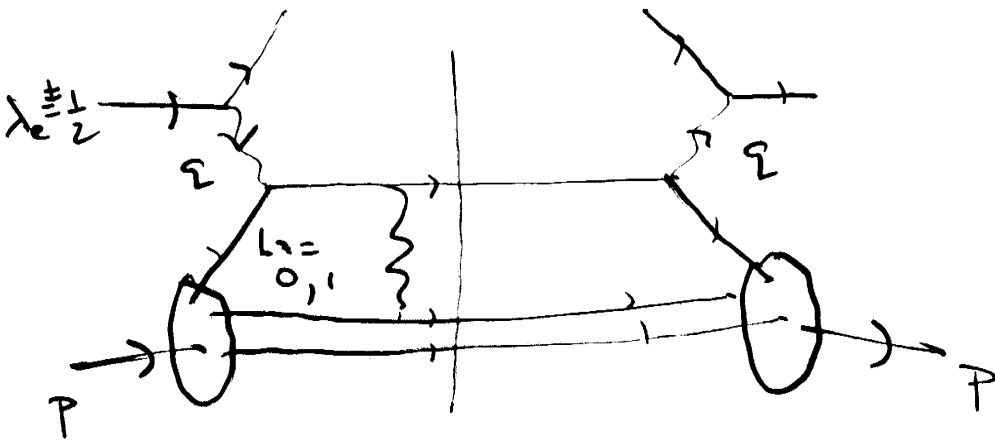
Coulomb phase accumulated along r

Not part of ψ_P^{LF}



$$\sum e \cdot \vec{q} \times \vec{P}_\pi$$

T-odd
ALU



interference
L, T
currents

Invisible
to target spin

$$ALU \sim \alpha_s \frac{Q r_\perp}{Q^2 + r_\perp^2}$$

similar
to
BRS

Afonsev
Coulson

$$\alpha_s \sim 0.3$$

same for
 π, h, P, \dots

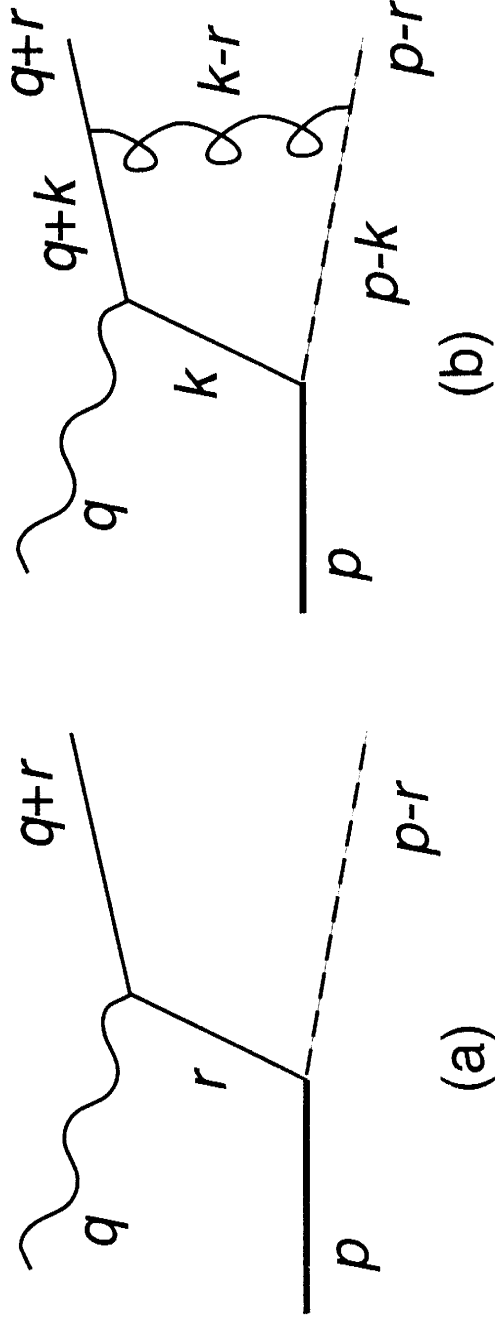
Coulson
Kewey
SJB

$$\sum \gamma \cdot \vec{q} \times \vec{P}_\pi$$

vector pol of virtual
density matrix $\sum \alpha_i \alpha_j$

AA+C. Carlson on Beam SSA

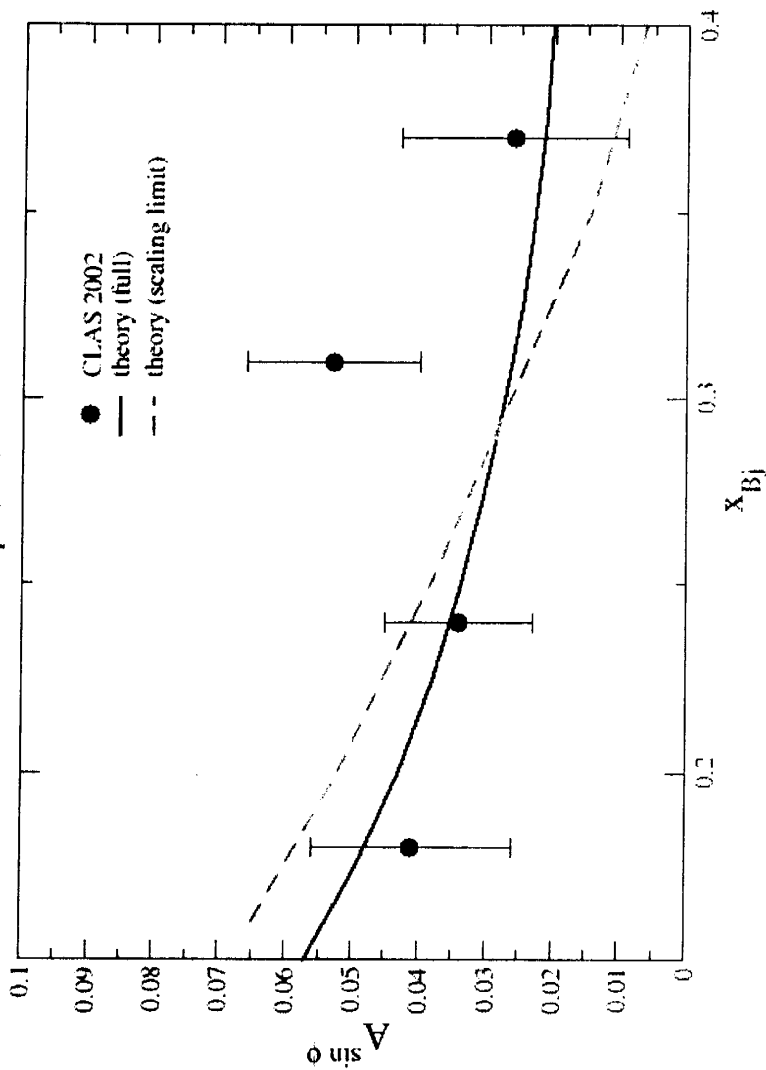
- Assume BHS mechanism for generating single-spin asymmetries, viz.
 - Gluon exchange takes place in the final state, generating both phase differences and transverse-momentum dependence
 - No assumptions are required on the details of nucleon spin structure



Jefferson Lab

Calculations vs CLAS Data (from Afanasev & Carlson)

Single-Spin Beam Asymmetry
 $p(e,e'\pi^+)X$



A_{LU}



Parity-Conserving Single-Spin

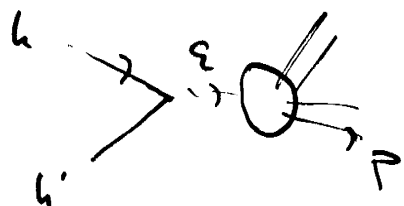
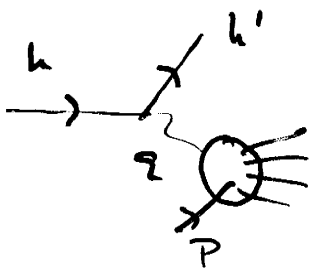
Asymmetries in Scattering Processes (*Early history*)

- George C. Stokes, *Trans. Camb. Phil. Soc.* **9**, 399 (1852), introduced parameters describing polarization states of light.
- N. F. Mott, *Proc. R. Soc. (London)*, **A124**, 425 (1929), noticed that polarization and/or asymmetry is due to spin-orbit coupling in the Coulomb scattering of electrons (Extended to high energies by AA et al., hep-ph/0208260).
- Julian Schwinger, *Phys. Rev.* **69**, 681 (1946); *ibid.*, **73**, 407 (1948), suggested a method to polarize fast neutrons via spin-orbit interaction in the scattering off nuclei
- Lincoln Wolfenstein, *Phys. Rev.* **75**, 1664 (1949); A. Simon, T.A. Welton, *Phys. Rev.* **90**, 1036 (1953), formalism of polarization effects in nuclear reactions

Jefferson Lab

Carlson
Hessing
M... (unclear)

Density Matrix of Virtual Photon



$$L^{\mu\nu} W_{\mu\nu} = n^{ac} n^{bd} [E_a^{\mu\nu} L_{\mu\nu} E_b] [E_c^{\rho\sigma} W_{\rho\sigma} E_d^{\alpha\beta}]$$

$$\equiv n^{ac} n^{bd} P_{ab}^{\lambda} P_{cd}^h$$

$$\equiv \text{Tr} [P^{\lambda} P^h]$$

$$n^{ab} = (1, -1, -1, -1)$$

$\epsilon^{\mu} \propto q^{\mu}$ gives 0

timelike: $a = 1, 2, 3$ } $SO(3)$
 spacelike: $a = 0, 1, 2$ } $SO(2,1)$

$$P = \frac{1}{3} \left[\mathbb{I}_{3 \times 3} + \frac{3}{2} \sum^i \Sigma^i + 3 T^{ij} \Sigma^{ij} \right]$$

$i, j = 1, 2, 3$

e.g.:

$$P^{\lambda} = -2 (k^i k'^j + k'^i k^j) \Sigma^{ij}$$

$$+ \frac{4}{3} (k^i k^i + q^2) \mathbb{I}$$

$$- 2(\lambda e q^0 k^i) \Sigma^i$$

tensor pol
 of virtual γ (timelike)
 vector pol

{ tensor + vector polarisation
 of virtual photon

interacts with

{ tensor + vector polarisation
 of hadronic current

$$\left[\Sigma_{\mu\nu}^i \cdot \Sigma_{had}^i \right]$$

$$\left[T_{\mu\nu}^i \quad T_{had}^i \right]$$

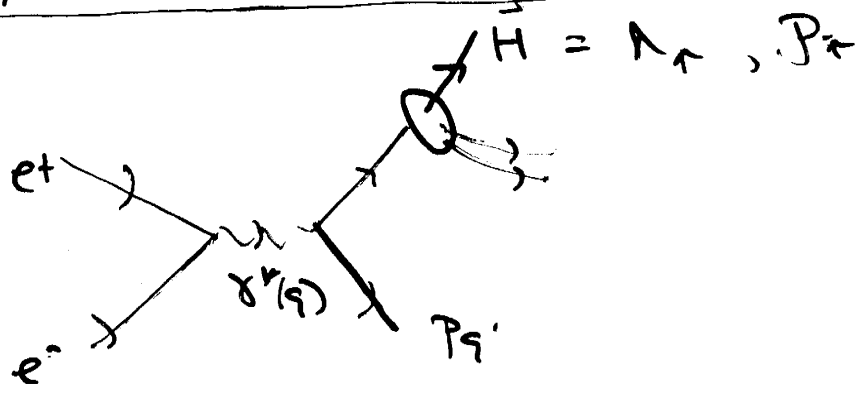
$$\begin{aligned}
 & \cdot \text{Tr} \left[\Sigma_{\mu\nu}^i \Sigma_{had}^i \right] \\
 & \frac{1}{2} \delta^{ij} \delta_{\mu\nu} + \frac{1}{2} \delta^{ij} \delta_{\mu\nu} \\
 & - \frac{1}{2} \delta^{ij} \delta_{\mu\nu}
 \end{aligned}$$

$$SO(3), \quad SO(2,1)$$

reduces $L_{\mu\nu} W_{\mu\nu}$ to

eff. degrees of freedom

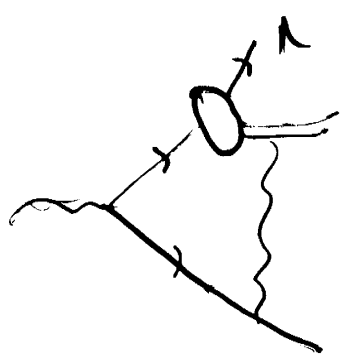
SSA in e^+e^- annihilation



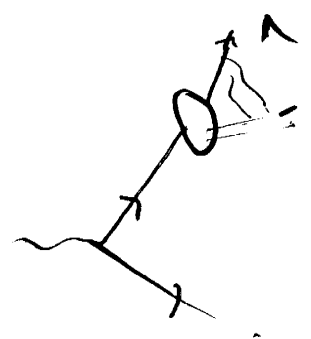
$$e^+e^- \rightarrow \Lambda_{\uparrow} p_{\downarrow} \pi, k$$

$$\sigma \propto \epsilon_{\mu\nu\rho\sigma} S_{\uparrow}^{\mu} P_{\downarrow}^{\nu} \int P_{\downarrow}^{\rho} P_{\downarrow}^{\sigma}$$

$$\Rightarrow \sqrt{s} S_{\uparrow} \cdot P_{\downarrow} \times P_{\downarrow}$$



\sim Siere's



\sim Collins

Conclusions

- * T-odd Physics
 ⇒ new insight into QCD
 role ↙ ISI, FSI

- * Sivers + Collins effects both present in QCD
 BHS, Collins
- * Mechanisms understood at perturbative level
- * α_s^2 (α_s^3) ?
- * SSA related to Diffractive DIS, shadowing
- * k_T distributions, energy loss
 from ISI, FSI
 Bodwin, Lepage, SJR ; Boer, Hwang, SJR
 Metz, Polychin et al ; Boer, Mulders
- * DIS structure functions measure BHMPS
 augmented LPDFs Ji, Yang
 ⇒ solve QCD in external field
- * Many questions of principle
 Sum rules; factorization (process indep.); DGLAP
 for nuclei

New Questions:

* How is momentum sum rule maintained
in the face of shadowing?

* What is the mechanism which produces
anti-shadowing?

→ Reggeons, $\gamma_N \rightarrow \rho_N$: constructive poles
at threshold

* How does the DHC sum rule
account for shadowing?

$$\int_{\nu_M}^{\infty} \frac{d\nu}{\nu} \left[\sigma_P^{\gamma A} - \sigma_A^{\gamma A} \right] = \frac{2\pi^2 \alpha \chi_A^2}{M_A^2}$$

Back face is shadowed at high ν !

Antishadowing from $\gamma_N \rightarrow \rho_N$ at threshold?