# Beam-beam simulations <br> with crossing anlge + crab-waist 

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## BB simulations

- New "crossing angle + crab waist" idea has solved disruption problems related to collisions with high current, small sizes beams $\rightarrow$ back to two "conventional" rings
- With very small emittances and relatively low currents (comparable to present $B$-Factories values) a Luminosity of $10^{36} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$ is reachable without large emittance blow-up


Crabbed waist removes bb betratron coupling introduced by the crossing angle
Vertical waist has to be a function of $x$ :
$\mathrm{Z}=0$ for particles at $-\sigma_{\mathrm{x}}\left(-\sigma_{\mathrm{x}} / 2 \theta\right.$ at low current $)$
$Z=\sigma_{x} / \theta$ for particles at $+\sigma_{x}\left(\sigma_{x} / 2 \theta\right.$ at low current $)$
Crabbed waist realized with a sextupole in phase with the IP in $X$ and at $\pi / 2$ in $Y$

## Luminosity considerations

Ineffectiveness of collisions with large crossing angle is illusive!!! Loss due to short collision zone (say $l=\sigma_{z} / 40$ ) is fully compensated by denser target beam (due to much smaller vertical beam size!)

Number of particles in collision zone: $\delta \mathrm{N}_{2}=\mathrm{N}_{2} \frac{l_{\text {cross }}}{\sigma_{z}} \quad l_{\text {cross }}=2 \sigma_{\mathrm{x}} / \theta$

$$
\begin{aligned}
& \mathrm{L}=\frac{\mathrm{N}_{1} \cdot \delta \mathrm{~N}_{2} \cdot \mathrm{f}_{0}}{4 \pi \sigma_{x} \sigma_{y}} \quad \xi_{1 y}=\frac{\mathrm{r}_{\mathrm{e}} \cdot \delta \mathrm{~N}_{2} \cdot \beta_{\mathrm{y}}}{2 \pi \gamma \sigma_{\mathrm{y}}\left(\sigma_{\mathrm{x}}+\sigma_{\mathrm{y}}\right)} \\
& \mathrm{L}=\frac{\gamma \xi_{1 \mathrm{y}} \mathrm{~N}_{1} \mathrm{f}_{0}}{2 \mathrm{r}_{\mathrm{e}} \beta_{\mathrm{y}}}\left(1+\frac{\sigma_{\mathrm{y}}}{\sigma_{\mathrm{x}}}\right) \simeq 2.167 \cdot 10^{34} \frac{\mathrm{E}(\mathrm{GeV}) \cdot \mathrm{I}(\mathrm{~A}) \cdot \xi_{1 \mathrm{y}}}{\beta_{\mathrm{y}}(\mathrm{~cm})} \simeq 1.2 \cdot 10^{36} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}
\end{aligned}
$$

No dependence on crossing angle! Universal expression: valid for both, head-on and crossing angle collisions!

## Tune shifts

## Raimondi, Shatilov, Zobov:

(Beam Dynamics Newsletter, 37, August 2005)

$$
\sigma_{x} \rightarrow \sqrt{\sigma_{z}^{2} \tan ^{2}(\theta / 2)+\sigma_{x}^{2}}
$$

$$
\begin{aligned}
& \xi_{x}=\frac{r_{e} \mathrm{~N}}{2 \pi \gamma} \frac{\beta_{x}}{\sqrt{\sigma_{z}^{2} \tan ^{2}(\theta / 2)+\sigma_{x}^{2}}\left(\sqrt{\sigma_{z}^{2} \tan ^{2}(\theta / 2)+\sigma_{x}^{2}}+\sigma_{y}\right)} \\
& \xi_{y}=\frac{\mathrm{r}_{\mathrm{e}} \mathrm{~N}}{2 \pi \gamma} \frac{\beta_{\mathrm{y}}}{\sigma_{\mathrm{y}}\left(\sqrt{\sigma_{z}{ }^{2} \tan ^{2}(\theta / 2)+\sigma_{x}^{2}}+\sigma_{y}\right)}
\end{aligned}
$$

SuperB:

$$
\sqrt{\sigma_{\mathrm{z}}^{2} \tan ^{2}(\theta / 2)+\sigma_{\mathrm{x}}^{2}}=100 \mu \mathrm{~m} \gg \sigma_{\mathrm{x}}=2.67 \mu \mathrm{~m}
$$

$$
\underline{\sqrt{\sigma_{z}^{2} \tan ^{2}(\theta / 2)+\sigma_{x}^{2}}} \simeq 8000!!!
$$

$$
\xi_{\mathrm{x}}=\frac{2 \mathrm{r}_{\mathrm{e}} \mathrm{~N}}{\pi \gamma} \frac{\beta_{x}}{\sigma_{z}^{2} \theta^{2}}=0.002
$$

One dimensional case for $\beta_{y} \gg \sigma_{x} / \theta$

$$
\xi_{y}=\frac{r_{e} N}{\pi \gamma} \frac{\beta_{y}}{\sigma_{y} \sigma_{z} \theta}=0.072
$$ but with crabbed waist for $\beta_{y}<\sigma_{x} / \theta$ also!

## "Crabbed" waist optics

Sextupole lens


Anti-sextupole Iens


Appropriate transformations from first sextupole to IP and from IP to anti-sextupole:

$$
\begin{aligned}
& \mathrm{T}_{\mathrm{x}}=\left(\begin{array}{cc}
\mathrm{u}_{\mathrm{x}} & 0 \\
-\mathrm{F}_{\mathrm{x}}^{-1} & \mathrm{u}_{\mathrm{x}}{ }^{-1}
\end{array}\right) \quad \tilde{\mathrm{T}}_{\mathrm{x}}=\left(\begin{array}{cc}
\mathrm{u}_{\mathrm{x}}^{-1} & 0 \\
-\mathrm{F}_{\mathrm{x}}^{-1} & \mathrm{u}_{\mathrm{x}}
\end{array}\right) \quad \tilde{\mathrm{T}}_{\mathrm{x}} \mathrm{~T}_{\mathrm{x}}=\left(\begin{array}{cc}
1 & 0 \\
-2 \mathrm{u}_{\mathrm{x}} \mathrm{~F}_{\mathrm{x}} & 1
\end{array}\right) \\
& \mathrm{T}_{\mathrm{y}}=\left(\begin{array}{cc}
\mathrm{u}_{\mathrm{y}} & \mathrm{~F}_{\mathrm{y}} \\
-\mathrm{F}_{\mathrm{y}}{ }^{-1} & 0
\end{array}\right) \quad \tilde{\mathrm{T}}_{\mathrm{y}}=\left(\begin{array}{cc}
0 & \mathrm{~F}_{\mathrm{y}} \\
-\mathrm{F}_{\mathrm{y}}{ }^{-1} & \mathrm{u}_{\mathrm{y}}
\end{array}\right) \quad \tilde{\mathrm{T}}_{\mathrm{y}} \mathrm{~T}_{\mathrm{y}}=\left(\begin{array}{cc}
-1 & 0 \\
-2 \mathrm{u}_{\mathrm{y}} \mathrm{~F}_{\mathrm{y}}^{-1} & -1
\end{array}\right)
\end{aligned}
$$

# Synchrotron modulation of $\xi_{y}$ 

 (Qualitative picture) Head-on collision.

Relative displacement from a bunch center

Conclusion: one can expect improvements of lifetime of halo-particles!
$\xi_{y}$ increase caused by hourglass

## effect I. Koop et al, BINP

Dependence of $\xi_{y}$ on $\beta_{y}$ for constant beam sizes at IP


## SuperB parameters



Horizontal Plane


Vertical Plane

Collisions with uncompressed beams
Crossing angle $=2 * 25 \mathrm{mrad}$
Relative Emittance growth per collision about $1.5^{*} 10^{-3}$ $\varepsilon_{y}{ }^{\text {out }} / \varepsilon_{y}{ }^{\text {in }}=1.0015$

## GuineaPig modifications

- With the large crossing angle scheme and long bunches the actual collision region is very short
- The code solves Poisson equation for all the volume occupied by the particles $\rightarrow$ very long computing time, not needed!
- Modification of the code to perform fields calculation in the collision region only
- Computing time was reduced by a factor 10 !!


## E. Paoloni, Pisa GuineaPig modified



## Luminosity vs Number of particles /bunch

## Crab-waist simulations

- The new idea is being checked by several beam-beam codes:
- Guinea-Pig: strong-strong , ILC centered
- BBC (Hirata): weak-strong
- Lifetrack (Shatilov): weak-strong with tails growths calculation
- Ohmi: weak-strong (strong-strong to be modified for long bunches and large angles)


## Ohmi's weak-strong code



Luminosity


## Vertical blow-up

K2 is the strength of the sextupolar nonlinearity introduced to have crab waist

## DAФNE (M.Zobov, LNF)

- Hirata's BBC code simulation (weak-strong, strong beam stays gaussian, weak beam has double crossing angle)
- $N_{p}=2.65 \times 10^{10}, 110$ bunches
- $I_{b}=13 \mathrm{~mA}$ (present working current)
- $\sigma_{x}=300 \mu \mathrm{~m}, \sigma_{y}=3 \mu \mathrm{~m}$
- $\beta_{x}=0.3 \mathrm{~m}, b_{y}=6.5 \mathrm{~mm}$
- $\sigma_{z}=25 \mathrm{~mm}$ (present electron bunch length)
- $\theta=2 \times 25 \mathrm{mrad}$
- $Y_{\text {IP }}=y+0.4 /\left(\theta^{*} x^{*} y^{\prime}\right)$ crabbed waist shif $\dagger$
- $L_{0}=2.33 \times 10^{24}$ (geometrical)
- $L(110$ bunches, 1.43 A$)=7.7 \times 10^{32}$
- $L_{\text {equil }}=6 \times 10^{32}$


## (Geometric) Luminosity



Takes into account both bb interactions and geometric factor due to crab waist

## Vertical Tails

## (max amplitude

 after 10 damping times)

M.Zobov, LNF

## Luminosity vs bunch current for 2 different working points



# Present WP: <br> $v_{\mathrm{x}}=0.11$ <br> $v_{y}=0.19$ 

## Possible WP: <br> $v_{\mathrm{x}}=0.057 v_{\mathrm{y}}=$ 0.097

M.Zobov, LNF

## Luminosity with shorter bunch, smaller $\sigma_{x}$

## 110 bunches


M.Zobov, LNF

With the present achieved beam parameters (currents, emittances, bunchlenghts etc) a luminosity in excess of $10^{33}$ is predicted.
With $2 A+2 A L>2^{*} 10^{33}$ is possible
Beam-Beam limit is way above the reachable currents

Luminosity scan


M. Zobov

## D.Shatilov, BINP

## Beam-Beam Tails

Without Crab Waist


With Crab Waist
dafne2_3_wsx25
 Greatly reduced
( $A$ is the amplitude in number of beamsize $\sigma$ )

$$
A_{y}=45
$$

Bunch core blowup also reduced

## Beam size and tails vs Crab-waist

Simulations with beam-beam code LIFETRAC
Beam parameters for DAФNE2
An effective "crabbed" waist map at IP:

$$
\begin{aligned}
& y=y_{0}+\frac{V}{\theta} x y_{0}^{\prime} \\
& y^{\prime}=y_{0}^{\prime}
\end{aligned}
$$



Optimum is shifted from the "theoretical" value $\mathrm{V}=1$ to $\mathrm{V}=0.8$, since it scales like $\sigma_{z} \theta / \operatorname{sqrt}\left(\left(\sigma_{z} \theta\right)^{2}+\sigma_{x}{ }^{2}\right)$
D.N. Shatilov, BINP

## Some resonances



(present with crossing angle only)


SC Wigglers

Wigglers off


DAФNE Wigglers
DAФNE Wigglers
Very weak luminosity dependence from damping time given the very small beam-beam blow-up

Preliminary results on Super PEPII M. Zobov, D. Shatilov

First approach with new parameters, weak-strong code

$$
=1.65 \times 10^{35} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}
$$

$$
\begin{aligned}
& \varepsilon_{x}=20 \mathrm{~nm} \\
& \varepsilon_{y}=0.2 \mathrm{~nm} \\
& \sigma_{x}=14.4 \mu \mathrm{~m} \\
& \sigma_{y}=0.4 \mu \mathrm{~m} \\
& \sigma_{z}=10 \mathrm{~mm} \\
& \sigma_{E}=7 \times 10^{-4} \\
& \beta_{x}=10 \mathrm{~mm} \\
& \beta_{y}=0.8 \mathrm{~mm} \\
& v_{s}=0.03 \\
& c_{s}=2.2 \mathrm{~km} \\
& f_{c o l}=238 \mathrm{MHz} \\
& \theta=2 \times 14 \mathrm{mrad} \\
& \tau_{x}=35 \mathrm{~ms} \\
& \mathrm{~N}_{1}=1.3 \times 1{ }^{2} 11 \\
& \mathrm{~N}_{2}=4.4 \times 10^{10} \\
& I_{1}=5 \mathrm{~A} \\
& \mathrm{I}_{2}=1.7 \mathrm{~A}
\end{aligned}
$$

## Tune scan for Super-PEPII



No dependence on tunes


Synchrobetatron resonances


## Conclusions

- The "crossing angle with crab waist" scheme has shown big potentiality and exciting results $\rightarrow$ LNF, Pisa, BINP and KEKB physicists are working on the bb simulation with different codes to explore its properties and find the best set of parameters
- This scheme is promising also for increasing luminosity at existing factories, as DAФNE, KEKB and possibly PEPII

