

# Why Super- $B$ ?

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SLAC, June 14

- Introduction
- Bounds on non-SM contributions  
Brief look at  $B_d$  and  $B_s$  mixing
- Some future clean measurements  
Few examples — fuller list in many reports
- Exciting theoretical developments  
Zero-bin factorization, annihilation
- Conclusions

[Höcker & ZL, hep-ph/0605217, to appear in ARNPS]

# We do not understand much about flavor

- SM flavor problem: hierarchy of masses and mixing angles
- NP flavor problem: TeV scale (hierarchy problem)  $\ll$  flavor & CPV scale

$$\epsilon_K: \frac{(s\bar{d})^2}{\Lambda^2} \Rightarrow \Lambda \gtrsim 10^4 \text{ TeV}, \quad B_d \text{ mixing: } \frac{(b\bar{d})^2}{\Lambda^2} \Rightarrow \Lambda \gtrsim 10^3 \text{ TeV}$$

- Almost all extensions of the SM have new sources of CPV & flavor conversion (e.g., 43 new CPV phases in SUSY)
- A major constraint for model building (flavor structure: universality, heavy squarks, squark-quark alignment, ...)
- The observed baryon asymmetry of the Universe requires CPV beyond the SM (not necessarily in flavor changing processes, nor in the quark sector)

# Spectacular track record

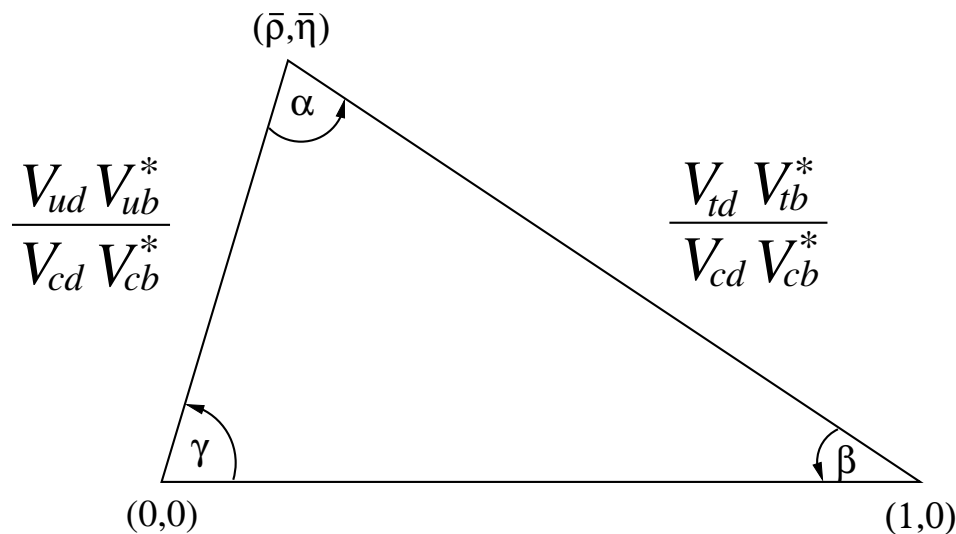
- Flavor and  $CP$  violation are excellent probes of New Physics
  - $\beta$ -decay predicted neutrino (Fermi)
  - Absence of  $K_L \rightarrow \mu\mu$  predicted charm (GIM)
  - $\epsilon_K$  predicted 3rd generation (KM)
  - $\Delta m_K$  predicted charm mass (GL)
  - $\Delta m_B$  predicted heavy top
- If there is NP at the TEV scale, it must have a very special flavor /  $CP$  structure
- Or will the LHC find just a SM-like Higgs?

# What is usually said to be done

- Exhibit hierarchical structure of CKM ( $\lambda \simeq 0.23$ )

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\bar{\rho} - i\bar{\eta}) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \bar{\rho} - i\bar{\eta}) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

- Measurements often shown in the  $(\bar{\rho}, \bar{\eta})$  plane — a “language” to compare data

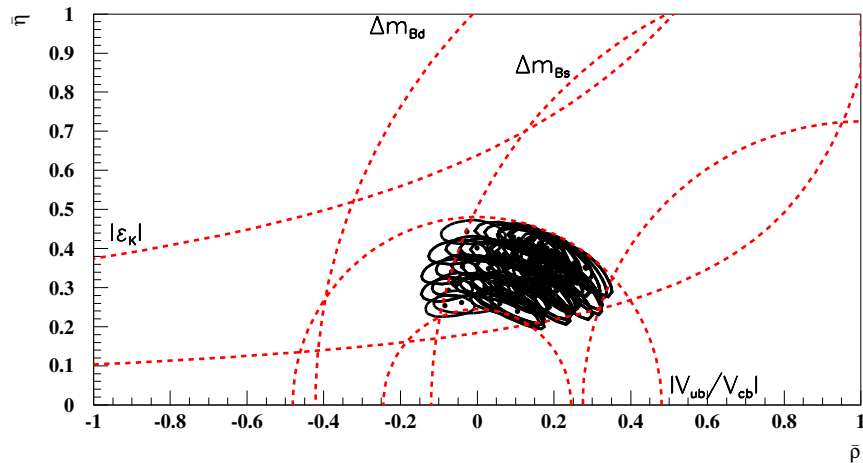


$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

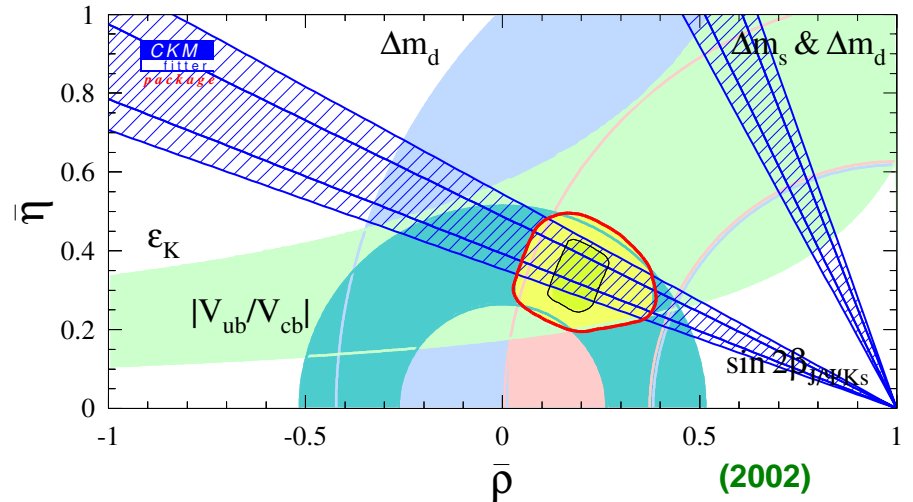
Angles and sides are directly measurable in numerous different processes

Goal: overconstraining measurements sensitive to different short dist. phys.

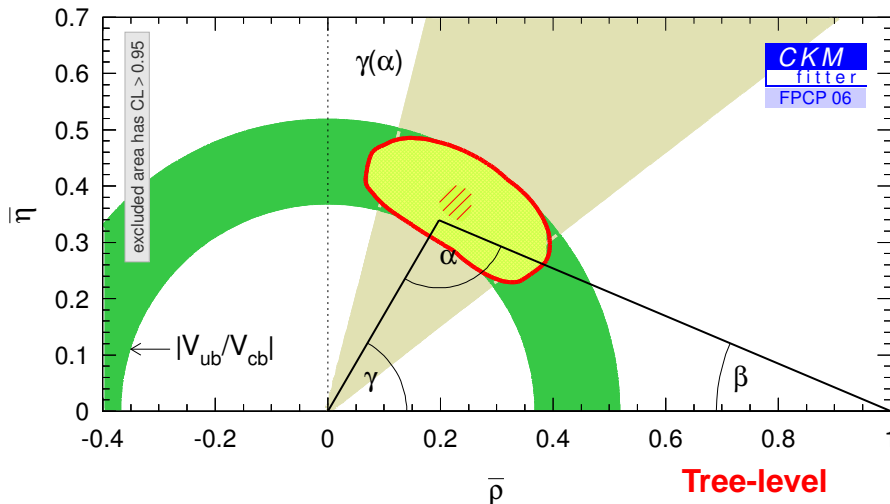
# Remarkable progress at $B$ factories



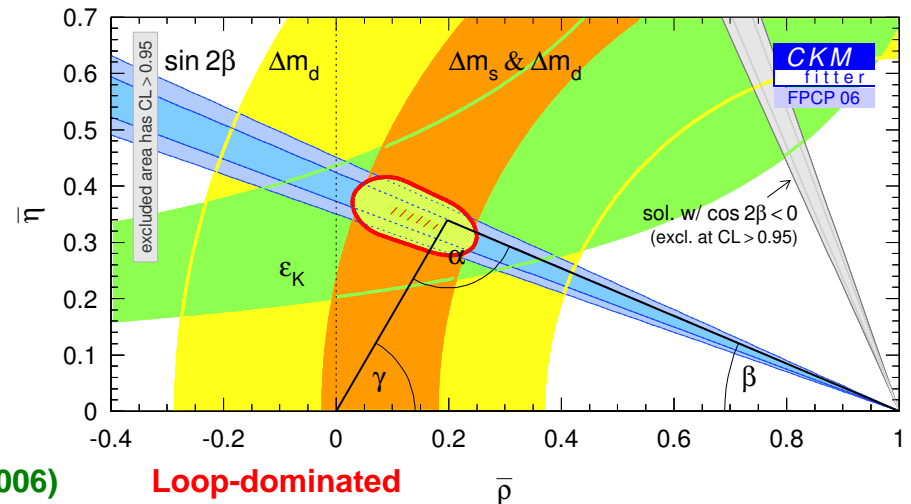
(1998)



(2002)



(2006)



- The CKM picture is verified  $\Rightarrow$  looking for corrections rather than alternatives

# Missing messages

- $\mathcal{O}(20-30\%)$  non-SM contribution to most loop-mediated transitions still allowed

Stopping at  $\mathcal{O}(1 \text{ ab}^{-1})$  datasets and giving up approaching percent level constraints would be a little bit like not having LEP after SPS, or ILC after LHC

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- We continue to fail to convey excitement of this program to non-experts:
  - The interesting messages are not simple to explain  
Not just one, single, critical measurement; theory is often quite complicated
  - The simple messages are not interesting  
Lincoln Wolfenstein does not care what  $\rho$  and  $\eta$  are, so why should you / I / ...?

# **Bounds on non-SM**



# Important features of the SM

- The SM flavor structure is very special:
  - Single source of  $CP$  violation in CC interactions
  - Suppressions due to hierarchy of mixing angles
  - Suppression of FCNC processes (loops)
  - Suppression of FCNC chirality flips by quark masses (e.g.,  $S_{K^*\gamma}$ )

Many suppressions that NP might not respect  $\Rightarrow$  sensitivity to very high scales

- It is interesting / worthwhile / possible to test all of these

# Parameterization of NP in mixing

- Assume: (i)  $3 \times 3$  CKM matrix is unitary; (ii) Tree-level decays dominated by SM

Concentrate on NP in mixing amplitude; two new param's for each neutral meson:

$$M_{12} = \underbrace{M_{12}^{\text{SM}} r_q^2 e^{2i\theta_q}}_{\text{easy to relate to data}} \equiv \underbrace{M_{12}^{\text{SM}} (1 + h_q e^{2i\sigma_q})}_{\text{easy to relate to models}}$$

- Tree-level constraints unaffected:  $|V_{ub}/V_{cb}|$  and  $\gamma$  (or  $\pi - \beta - \alpha$ )

- Observables sensitive to  $\Delta F = 2$  new physics:

$$\Delta m_{B_q} = r_q^2 \Delta m_{B_q}^{\text{SM}} = |1 + h_q e^{2i\sigma_q}| \Delta m_q^{\text{SM}}$$

$$S_{\psi K} = \sin(2\beta + 2\theta_d) = \sin[2\beta + \arg(1 + h_d e^{2i\sigma_d})] \quad S_{\rho\rho} = \sin(2\alpha - 2\theta_d)$$

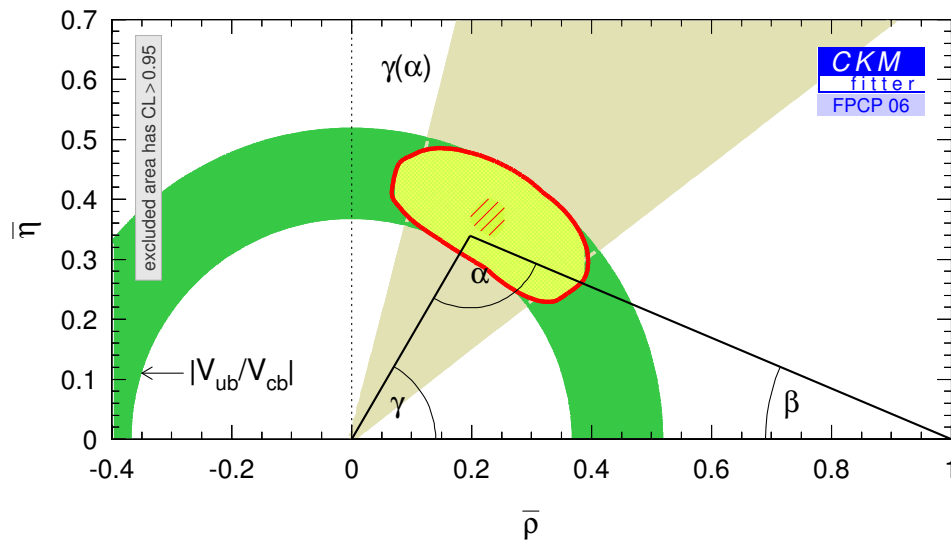
$$S_{\psi\phi} = \sin(2\beta_s - 2\theta_s) = \sin[2\beta_s - \arg(1 + h_s e^{2i\sigma_s})]$$

$$A_{\text{SL}}^q = \text{Im} \left( \frac{\Gamma_{12}^q}{M_{12}^q r_q^2 e^{2i\theta_q}} \right) = \text{Im} \left[ \frac{\Gamma_{12}^q}{M_{12}^q (1 + h_q e^{2i\sigma_q})} \right] \quad \Delta\Gamma_s = \Delta\Gamma_s^{\text{SM}} \cos^2 2\theta_s$$

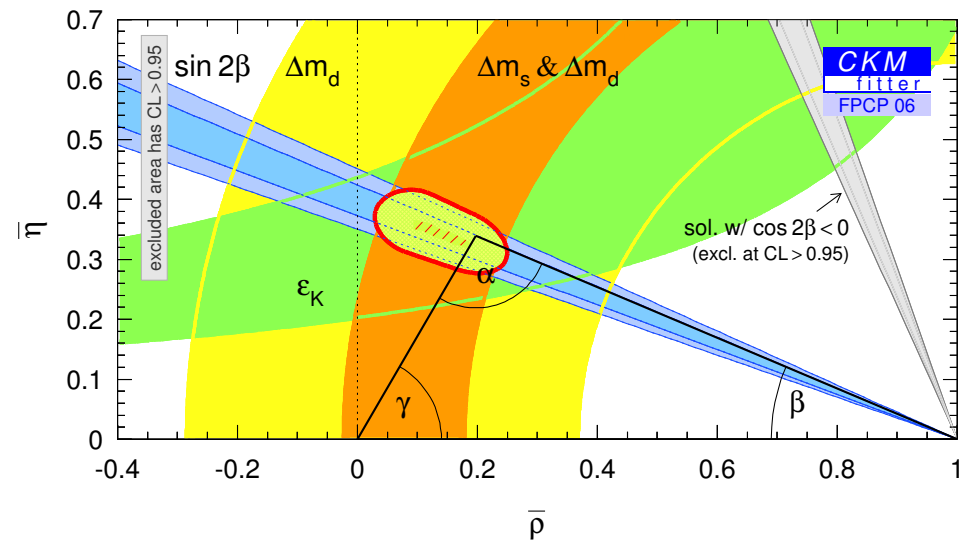
# Constraining new physics in loops

- $B$  factories:  $\bar{\rho}, \bar{\eta}$  determined from (effectively) tree-level & loop-induced processes

Tree-level

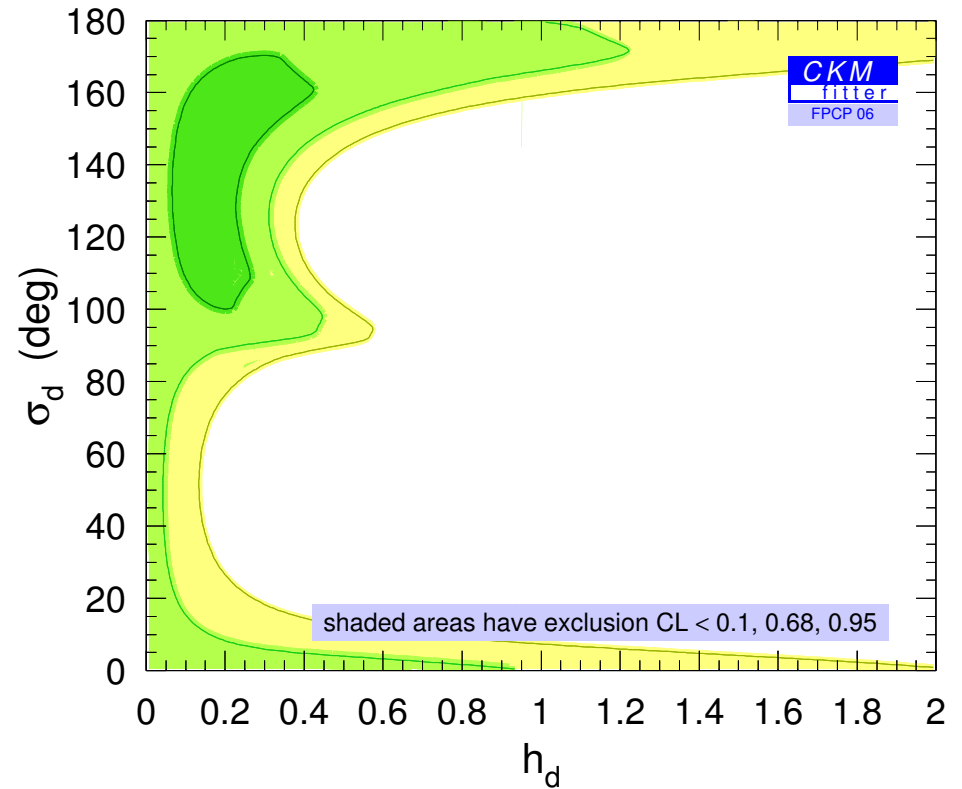
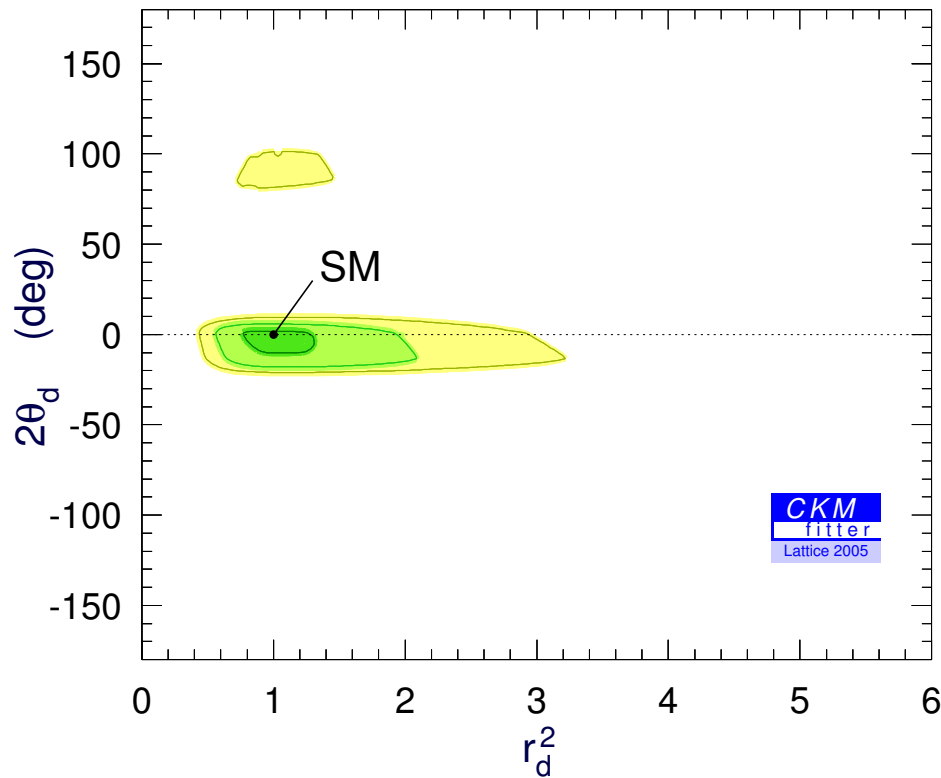


Loop-induced



- $\bar{\rho}, \bar{\eta}$  constrained to SM region even in the presence of NP in loops
- $\epsilon_K, \Delta m_d, \Delta m_s, |V_{ub}|$ , etc., can be used to overconstrain the SM and test for NP
- NP: more parameters  $\Rightarrow$  independent measurements critical

# The parameter space $r_d^2$ , $\theta_d$ and $h_d$ , $\sigma_d$



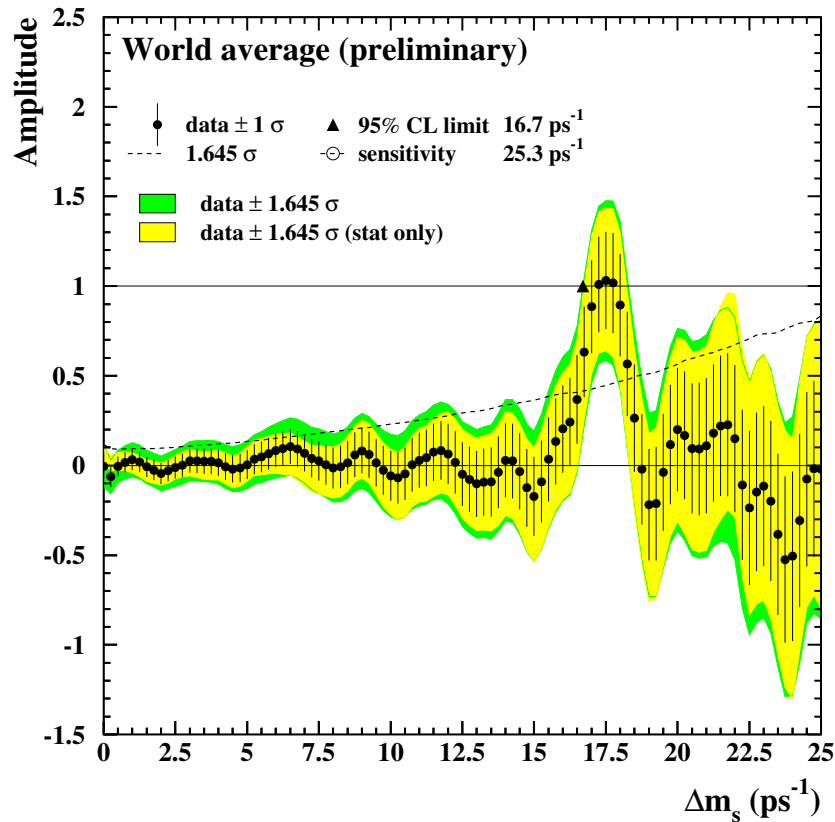
$r_d^2, \theta_d$ :  $|M_{12}/M_{12}^{\text{SM}}|$  can only differ significantly from 1 if  $\arg(M_{12}/M_{12}^{\text{SM}}) \sim 0$

$h_d, \sigma_d$ : NP may still be comparable to SM:  $h_d = 0.23^{+0.57}_{-0.23}$ , i.e.,  $h_d < 1.7$  (95% CL)

- Recent data restricts NP in mixing for the first time — still plenty of room left

# News of the year: $\Delta m_s$

- $\Delta m_s = (17.31^{+0.33}_{-0.18} \pm 0.07) \text{ ps}^{-1}$  [CDF, hep-ex/0606027] (prob. of bkgd fluctuation: 0.2%)



CDF:  $\sim 3\sigma$ ; world average:  $\sim 4\sigma$

## Weights in world average at 17.5 $\text{ps}^{-1}$

ALEPH	10.2%	LEP	14.6%
DELPHI	4.1%		
OPAL	0.4%		
SLD	8.2%	SLC	8.2%
CDF1	0.9%	Tevatron	77.2%
CDF2	67.9%		
D0	8.4%		

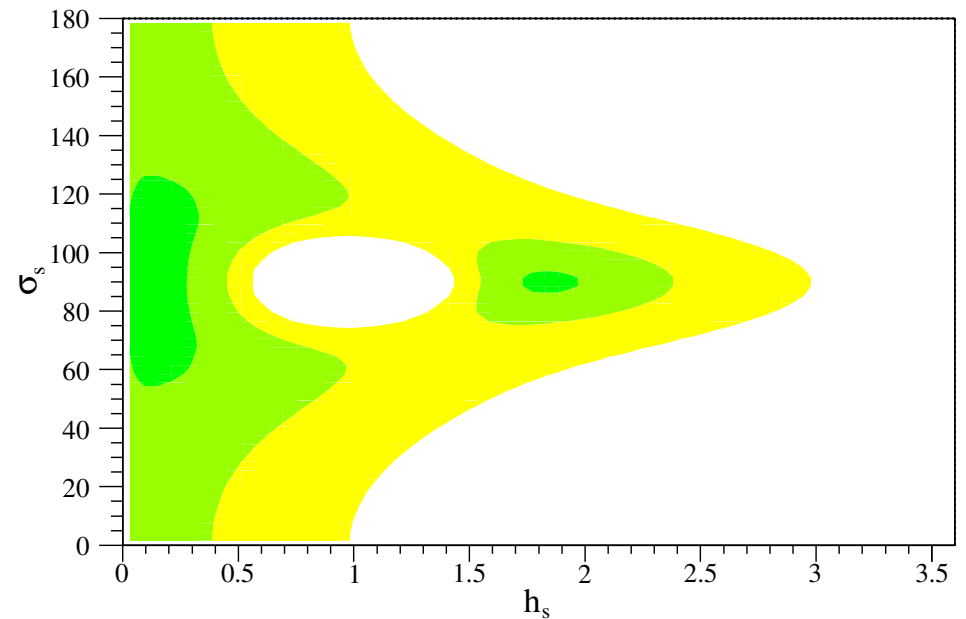
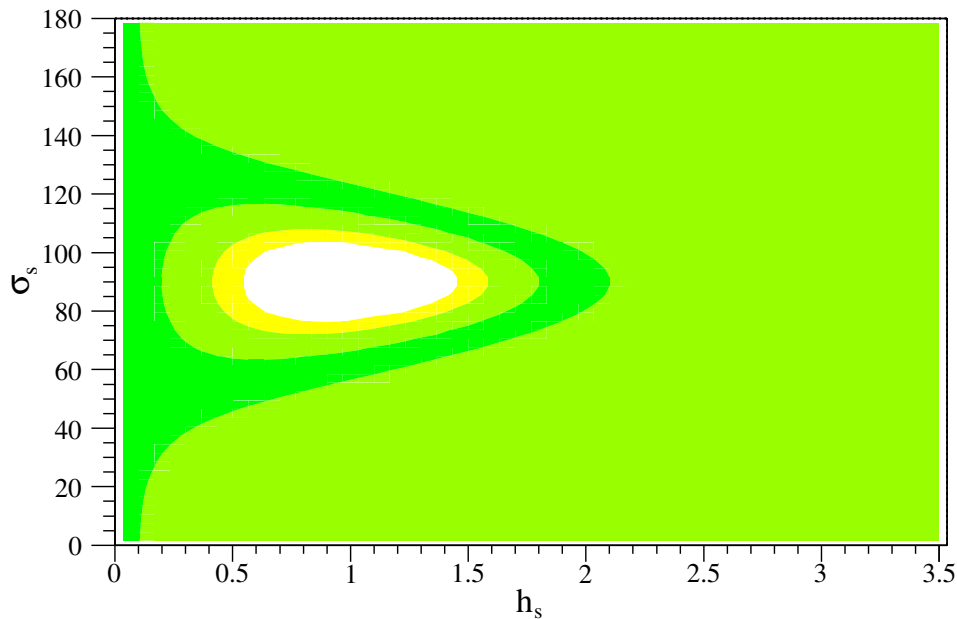
[from O. Schneider]

First time that sensitivity is significantly greater than where (hint of) signal is seen

A  $> 5\sigma$  measurement before the LHC turns on now appears certain

# New physics in $B_s^0 \bar{B}_s^0$ mixing

- Before and after the measurement of  $\Delta m_s$  (and  $\Delta \Gamma_s$ ): [ZL, Papucci, Perez, hep-ph/0604112]



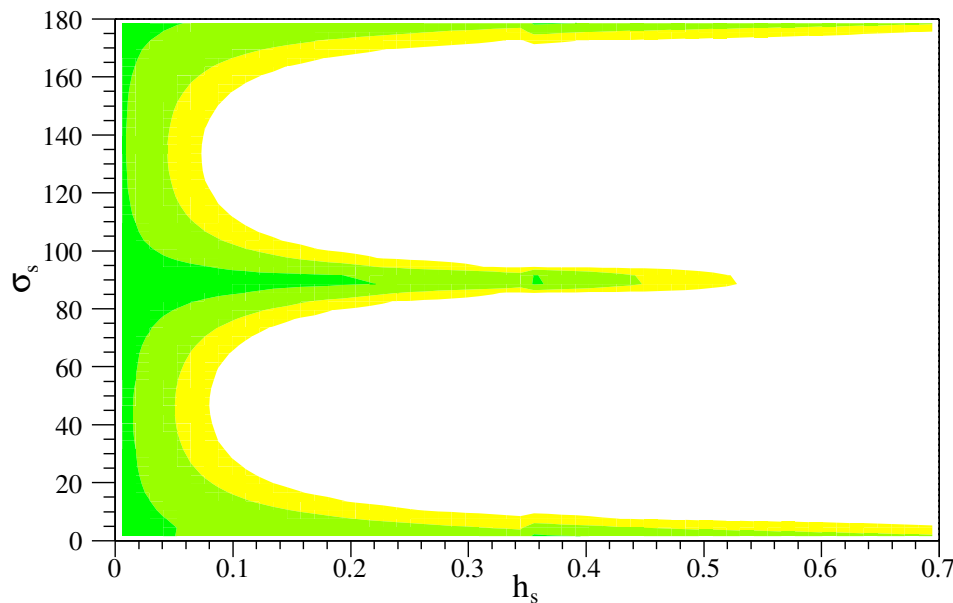
- To learn more about the  $B_s^0$  system, need  $CP$  asymmetry in  $B_s \rightarrow \psi\phi$ , etc.

# Constraints with measurement of $S_{B_s \rightarrow \psi\phi}$

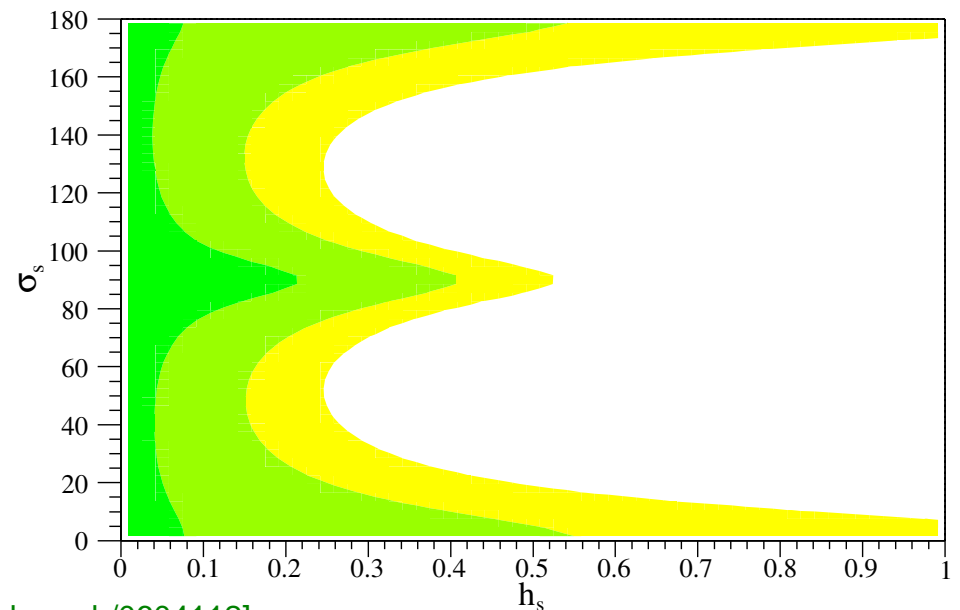
- $S_{\psi\phi}$  is analog of  $S_{\psi K}$  ( $\sin 2\beta$ ), and similarly clean

In SM:  $\beta_s = \arg(-V_{ts}V_{tb}^*/V_{cs}V_{cb}^*) = \mathcal{O}(\lambda^2)$ ; prediction:  $\sin 2\beta_s = 0.0365 \pm 0.0020$

- Assume  $S_{\psi\phi}$  measured to be SM  $\pm 0.03$  /  $\pm 0.10$  (1/0.1 yr nominal LHCb data)



[ZL, Papucci, Perez, hep-ph/0604112]



- Unless there is an easy-to-find narrow resonance at ATLAS & CMS, this could be (one of) the most interesting early measurements(s)

# **Some important processes**



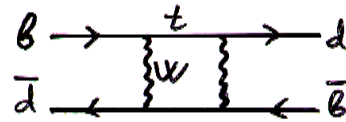
# What are we really after?

- At scale  $m_b$ , flavor changing processes are mediated by  $\mathcal{O}(100)$  higher dimension operators

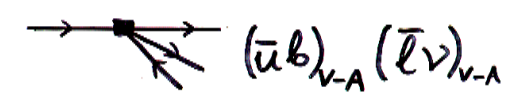
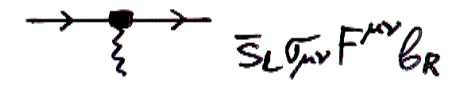
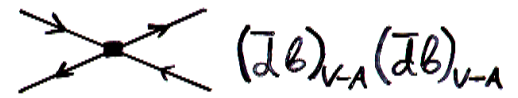
Depend only on a few parameters in SM  $\Rightarrow$  intricate correlations between  $s, c, b, t$  decays

E.g.: in SM  $\frac{\Delta m_d}{\Delta m_s}, \frac{b \rightarrow d\gamma}{b \rightarrow s\gamma}, \frac{b \rightarrow dl^+\ell^-}{b \rightarrow sl^+\ell^-} \propto \left| \frac{V_{td}}{V_{ts}} \right|$ , but test different short dist. physics

weak/NP scale



$\sim 5 \text{ GeV}$



- Question: does the SM (i.e., integrating out virtual  $W, Z$ , and quarks in tree and loop diagrams) explain all flavor changing interactions? Right coeff's? Right op's?
- New physics most likely to modify SM loops, so study: mixing & rare decays, compare tree and loop processes,  $CP$  asymmetries

# CPV in $b \rightarrow s, d$ penguins

- Measuring same angle in decays sensitive to different short distance physics may give best sensitivity to NP ( $f_s = \phi K_S, \eta' K_S$ , etc.)

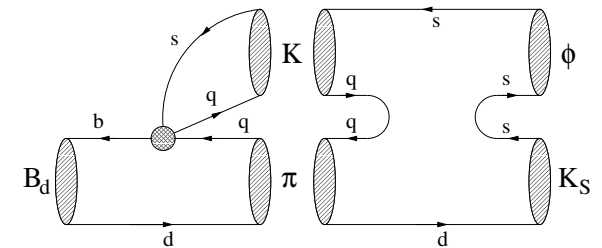
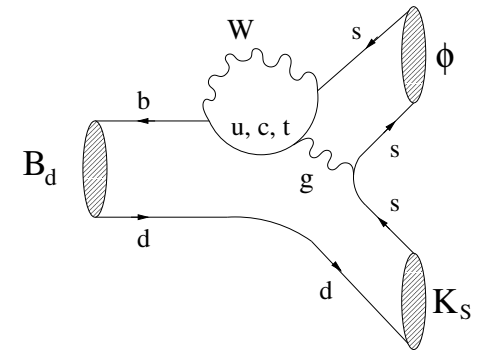
Amplitudes with one weak phase expected to dominate:

$$\bar{A} = \underbrace{V_{cb}V_{cs}^*}_{\mathcal{O}(\lambda^2)} \underbrace{\langle \text{"P"} \rangle}_1 + \underbrace{V_{ub}V_{us}^*}_{\mathcal{O}(\lambda^4)} \underbrace{\langle \text{"P + } T_u \text{"} \rangle}_{\mathcal{O}(1)}$$

SM: expect:  $S_{f_s} - S_{\psi K}$  and  $C_{f_s} \lesssim 0.05$

NP:  $S_{f_s} \neq S_{\psi K}$  possible; expect mode-dependent  $S_f$

Depend on size & phase of SM and NP amplitude



NP could enter  $S_{\psi K}$  mainly in mixing, while  $S_{f_s}$  through both mixing and decay

- Interesting to pursue independent of present results — there is room left for NP

# Is there NP in $b \rightarrow s$ transitions?

$f_{CP}$	SM predictions for $(-\eta_{f_{CP}} S_{f_{CP}} - \sin 2\beta)$ my estimates*	BHNR	Beneke	$-\eta_{f_{CP}} S_{f_{CP}}$
$\psi K$	0.01			$+0.687 \pm 0.032$
$\eta' K$	0.05	$+0.01^{+0.01}_{-0.02}$	$+0.01^{+0.01}_{-0.01}$	$+0.48 \pm 0.09$
$\phi K$	0.05	$+0.02$	$+0.02^{+0.01}_{-0.01}$	$+0.47 \pm 0.19$
$\pi^0 K_S$	0.15	$+0.06^{+0.04}_{-0.03}$	$+0.07^{+0.05}_{-0.04}$	$+0.31 \pm 0.26$
$K^+ K^- K_S$	0.15			$+0.51 \pm 0.17$
$K_S K_S K_S$	0.15			$+0.61 \pm 0.23$
$f^0 K_S$	0.25			$+0.75 \pm 0.24$
$\omega K_S$	0.25	$+0.19^{+0.06}_{-0.14}$	$+0.13^{+0.08}_{-0.08}$	$+0.63 \pm 0.30$

\* What I consider reasonable limits (strict bounds worse, model calculations better)

Buchalla, Hiller, Nir, Raz and Beneke use QCDF;  $SU(3)$  bounds weaker [Grossman, ZL, Nir, Quinn]

- **Estimates model dependent:** theory has to develop further to firm up predictions  
There are also SM predictions with  $S_{\eta' K^0} - \sin 2\beta < 0$  [Williamson & Zupan, hep-ph/0601214]
- Will significance of hints of deviations from SM increase or decrease...?

# $\alpha$ from $B \rightarrow \rho\rho, \rho\pi, \pi\pi$

●  $S_{\rho^+\rho^-} = \sin[(B\text{-mix} = -2\beta) + (\bar{A}/A = -2\gamma + \dots) + \dots] = \sin(2\alpha) + \text{small}$

(1) Longitudinal polarization dominates (could be mixed  $CP$ -even/odd)

(2) Small rate:  $\mathcal{B}(B \rightarrow \rho^0\rho^0) < 1.1 \times 10^{-6}$  (90% CL)  $\Rightarrow$  small  $\Delta\alpha$

$$\frac{\mathcal{B}(B \rightarrow \pi^0\pi^0)}{\mathcal{B}(B \rightarrow \pi^+\pi^0)} = 0.26 \pm 0.06 \quad \text{vs.} \quad \frac{\mathcal{B}(B \rightarrow \rho^0\rho^0)}{\mathcal{B}(B \rightarrow \rho^+\rho^0)} < 0.06 \quad (90\% \text{ CL})$$

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This year the penguins started to bite

$\Rightarrow$  Need more data



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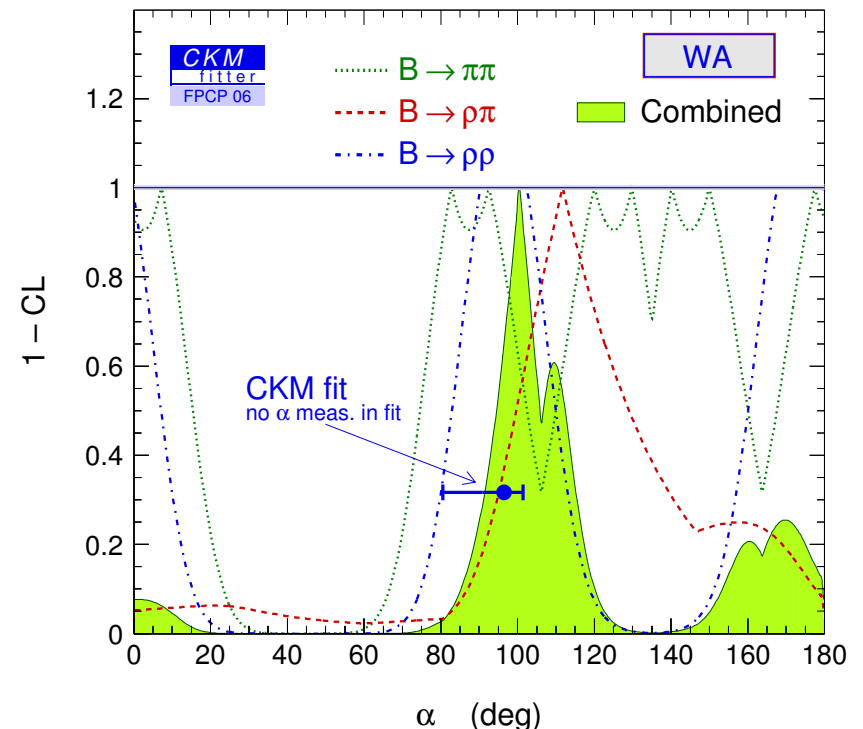
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- Isospin bound:  $|\Delta\alpha| < 17^\circ$

$$S_{\rho^+\rho^-} \text{ yields: } \alpha = (100^{+13}_{-20})^\circ$$

More complicated than  $\pi\pi$ ,  $I = 1$  possible due to  $\Gamma_\rho \neq 0$ ; its  $\mathcal{O}(\Gamma_\rho^2/m_\rho^2)$  effects can be constrained with more data [Falk, ZL, Nir, Quinn]

- All measurements combined:  $\alpha = (102^{+15}_{-9})^\circ$



# $\gamma$ from $B^\pm \rightarrow DK^\pm$

- **Tree level:** interfere  $b \rightarrow c$  ( $B^- \rightarrow D^0 K^-$ ) and  $b \rightarrow u$  ( $B^- \rightarrow \bar{D}^0 K^-$ )  
Need  $D^0, \bar{D}^0 \rightarrow$  same final state; determine  $B$  and  $D$  decay amplitudes from data

**Sensitivity driven by:**  $r_B = |A(B^- \rightarrow \bar{D}^0 K^-)/A(B^- \rightarrow D^0 K^-)| \sim 0.1 - 0.2$

Many variants according to  $D$  decay:  $D_{CP}$  [GLW], DCS/CA [ADS], CS/CS [GLS]

- **Best measurement was:**  $D^0, \bar{D}^0 \rightarrow K_S \pi^+ \pi^-$   
[Giri, Grossman, Soffer, Zupan; Bondar]

– Both amplitudes Cabibbo allowed

– Can integrate over regions in

$m_{K\pi^+} - m_{K\pi^-}$  Dalitz plot

Also got a lot harder this year!

Each of these methods satisfies the NIMSBHO principle:  
Not Inherently More Sensitive But Helps Overall  
(despite possible claims to the contrary...)

[Soffer @ 2004 Hawaii Super-B workshop]

$\Rightarrow$  Need a lot more data

- **Average of all measurements:**  $\gamma = (62_{-25}^{+35})^\circ$



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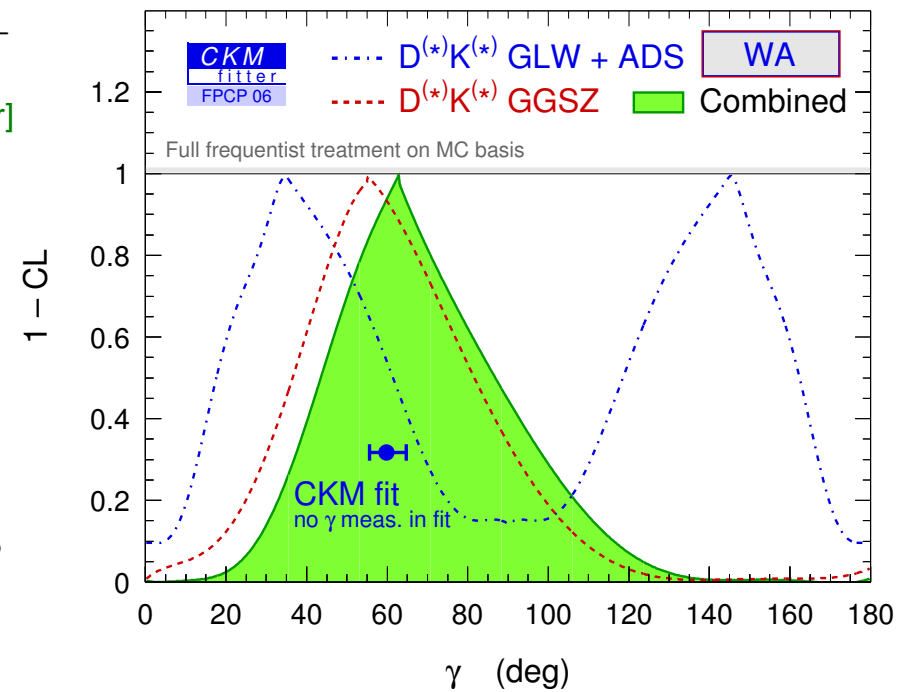
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- **Average of all measurements:**  $\gamma = (62^{+35}_{-25})^\circ$





# Rare $B$ decays

- Important probes of new physics

- $B \rightarrow K^* \gamma$  or  $X_s \gamma$ : Best  $m_{H^\pm}$  limits in 2HDM — in SUSY many param's
- $B \rightarrow K^{(*)} \ell^+ \ell^-$  or  $X_s \ell^+ \ell^-$ :  $bsZ$  penguins, SUSY, right handed couplings

A crude guide ( $\ell = e$  or  $\mu$ )

Decay	$\sim$ SM rate	physics examples
$B \rightarrow s \gamma$	$3 \times 10^{-4}$	$ V_{ts} , H^\pm, \text{SUSY}$
$B \rightarrow \tau \nu$	$1 \times 10^{-4}$	$f_B  V_{ub} , H^\pm$
$B \rightarrow s \nu \nu$	$4 \times 10^{-5}$	new physics
$B \rightarrow s \ell^+ \ell^-$	$6 \times 10^{-6}$	new physics
$B_s \rightarrow \tau^+ \tau^-$	$1 \times 10^{-6}$	
$B \rightarrow s \tau^+ \tau^-$	$5 \times 10^{-7}$	:
$B \rightarrow \mu \nu$	$5 \times 10^{-7}$	
$B_s \rightarrow \mu^+ \mu^-$	$4 \times 10^{-9}$	
$B \rightarrow \mu^+ \mu^-$	$2 \times 10^{-10}$	

Replacing  $b \rightarrow s$  by  $b \rightarrow d$  costs a factor  $\sim 20$  (in SM); interesting to test in both: rates,  $CP$  asymmetries, etc.

In  $B \rightarrow q l_1 l_2$  decays expect 10–20%  $K^*/\rho$ , and 5–10%  $K/\pi$  (model dept)

Many of these (cleanest inclusive ones) impossible at hadron colliders

# Some theory excitements

*B* physics has been and continues to be fertile ground for theoretical developments

HQET, ChPT, SCET, Lattice QCD, ...

# Charmless $B \rightarrow M_1 M_2$ decays

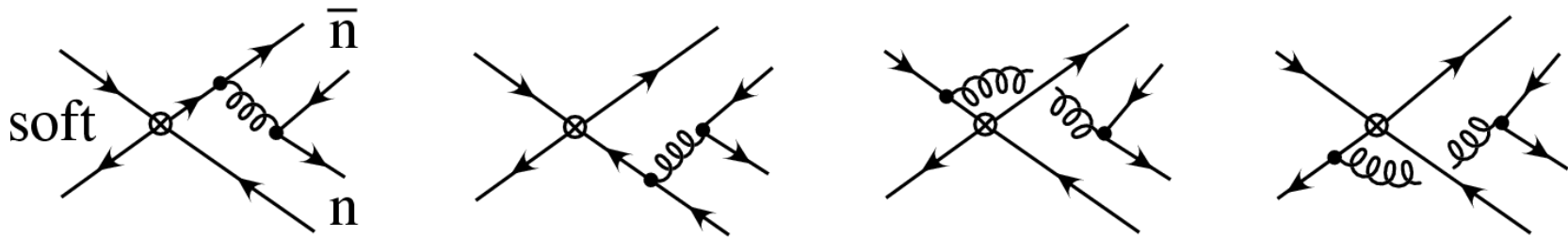
- BBNS (QCDF) factorization proposal:

$$\langle \pi\pi | O_i | B \rangle \sim F_{B \rightarrow \pi} T(x) \otimes \phi_\pi(x) + T(\xi, x, y) \otimes \phi_B(\xi) \otimes \phi_\pi(x) \otimes \phi_\pi(y)$$

The KLS (pQCD) formulae involve only  $\phi_B, \phi_{M_1}, \phi_{M_2}$ , with  $k_\perp$  dependence

- SCET:  $\langle \pi\pi | O_i | B \rangle \sim \sum_{ij} T(x, y) \otimes \left[ J_{ij}(x, z_k, k_\ell^+) \otimes \phi_\pi^i(z_k) \phi_B^j(k_\ell^+) \right] \otimes \phi_\pi(y)$

- Weak annihilation (WA) gives power suppressed ( $\Lambda/E$ ) corrections



Yields convolution integrals of the form:  $\int_0^1 \frac{dx}{x^2} \phi_\pi(x), \quad \phi_\pi(x) \sim 6x(1-x)$

- BBNS: interpret as IR sensitivity  $\Rightarrow$  modelled by complex parameters

KLS: rendered finite by  $k_\perp$ , but sizable and complex contributions

# Subtractions for divergent convolutions

- Choose interpolating field for pion to be made of collinear quarks ( $p_i^- \neq 0$ )

$$\langle \pi_n^+(p_\pi) | \bar{u}_{n,p_1^-} \not{n} \gamma_5 d_{n,-p_2^-} | 0 \rangle = -i f_\pi \delta(\bar{n} \cdot p_\pi - p_1^- - p_2^-) \phi_\pi(x_1, x_2, \mu)$$

**Zero-bin:**  $p_i^- \neq 0$  (collinear quark with  $p_i^- = 0$  is not a collinear quark)

Divergence in  $\int_0^1 \phi_\pi(x)/x^2$  related to one of the quarks becoming soft near  $x = 0$

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- Zero-bin ensures there is no contribution from  $x_i = p_i^- / (\bar{n} \cdot p_\pi) \sim 0$

Subtractions implied by zero-bin depend on the singularity of integrals, e.g.:

$$\int_0^1 dx \frac{1}{x^2} \phi_\pi(x, \mu) \quad \Rightarrow \quad \int_0^1 dx \frac{\phi_\pi(x, \mu) - x \phi'_\pi(0, \mu)}{x^2} + \phi'_\pi(0, \mu) \ln \left( \frac{\bar{n} \cdot p_\pi}{\mu_-} \right)$$

= finite

[Manohar & Stewart, hep-ph/0605001]

# Weak annihilation

- Match onto six-quark operators of the form (only hard contributions, no jet scale):

$$O_{1d}^{(ann)} = \sum_q \underbrace{[\bar{d}_s \Gamma_s b_v]}_{\text{gives } f_B} \underbrace{[\bar{u}_{\bar{n}, \omega_2} \Gamma_{\bar{n}} q_{\bar{n}, \omega_3}]}_{\pi \text{ in } \bar{n} \text{ direction}} \underbrace{[\bar{q}_{n, \omega_1} \Gamma_n u_{n, \omega_4}]}_{\pi \text{ in } n \text{ direction}} \quad [\text{Arnesen, ZL, Rothstein, Stewart}]$$

Similar to leading order contributions to the amplitude

- At leading nonvanishing order in  $\Lambda/m_b$  and  $\alpha_s$ :
  - **Real**, because there is no way for these matrix elements to be complex
  - **Calculable**, and do not introduce nonperturbative inputs beyond those that occur in leading order factorization formula

- 
- Constrain parameters in QCDF and pQCD to be real, which have been taken to be complex  $\Rightarrow$  fewer unknowns
  - Can try to disentangle charm penguin amplitudes from weak annihilation, etc.

**Final comments**

# Outlook

- If there are new particles at TeV scale, new flavor physics could show up any time

- Goal for further flavor physics experiments:

If NP is seen in flavor physics: study it in as many different operators as possible

If NP is not seen in flavor physics: achieve what is theoretically possible

could teach us a lot about the NP seen at LHC

The program as a whole is a lot more interesting than any single measurement

- Try to distinguish: One / many sources of CPV? Only in CC interactions?

NP couples mostly to up / down sector? 3rd / all generations?  $\Delta(F) = 2$  or 1?

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- Political and technical realities aside, I think the case is compelling

Many interesting measurements, complementarity with high energy frontier

# Theoretical limitations (continuum methods)

- Many interesting decay modes will not be theory limited for a long time

Measurement (in SM)	Theoretical limit	Present error
$B \rightarrow \psi K$ ( $\beta$ )	$\sim 0.2^\circ$	$1.3^\circ$
$B \rightarrow \eta' K, \phi K$ ( $\beta$ )	$\sim 2^\circ$	5, $10^\circ$
$B \rightarrow \rho\rho, \rho\pi, \pi\pi$ ( $\alpha$ )	$\sim 1^\circ$	$\sim 13^\circ$
$B \rightarrow DK$ ( $\gamma$ )	$\ll 1^\circ$	$\sim 20^\circ$
$B_s \rightarrow \psi\phi$ ( $\beta_s$ )	$\sim 0.2^\circ$	—
$B_s \rightarrow D_s K$ ( $\gamma - 2\beta_s$ )	$\ll 1^\circ$	—
$ V_{cb} $	$\sim 1\%$	$\sim 2\%$
$ V_{ub} $	$\sim 5\%$	$\sim 10\%$
$B \rightarrow X_s \gamma$	$\sim 5\%$	$\sim 10\%$
$B \rightarrow X_s \ell^+ \ell^-$	$\sim 5\%$	$\sim 20\%$
$B \rightarrow K^{(*)} \nu \bar{\nu}$	$\sim 5\%$	—

For some entries, the shown theoretical limits require more complicated analyses  
 It would require major breakthroughs to go significantly below these theory limits



# Conclusions

- Despite tremendous progress, new physics in neutral meson mixings may still be comparable to the SM contributions (sensitive to scales  $\gg$  LHC)
- Measurement of  $S_{\psi\phi}$ , etc., at LHC(b) will constrain  $B_s$  sector much better  
Precise measurements in  $B_{u,d}$  sector is crucial for this as well
- Exciting theory progress: zero-bin factorization  $\Rightarrow$  no divergent convolutions  
Annihilation & “chirally enhanced” hard scattering contributions better understood
- If new physics shows up in the flavor sector, pursuing this program is a no-brainer  
If no unambiguous sign of NP is found in the flavor sector, constraints may still provide important clues to model building in the LHC era



**Backup slides**