

New apparatus for precise synchronous phase shift measurements in storage rings¹

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Measuring a synchronous phase shift as a function of beam current is commonly done in accelerator physics to estimate the longitudinal impedance of a storage ring vacuum chamber. This measurement is normally done with RF techniques that don't have enough accuracy to detect small phase shifts typical to the newer storage rings. In this paper we report results from a new method for precise measurement of a synchronous phase shift. Our method involves downmixing from the RF frequency to a kHz range and then using an audio DSP lock-in amplifier for the actual phase detection. This paper describes the idea and the advantages of a new method as well as its practical implementation in the apparatus we build for precise synchronous phase measurements in the Stanford Linear Collider damping rings. The results of those measurements are also presented.

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1.0 Introduction

Measuring synchronous phase shift as a function of beam current gives the so-called loss factor, which is related to the ring impedance and affects the longitudinal beam dynamics. There are elaborate computational methods to calculate the impedance by summing up the contributions of individual vacuum chamber elements and the measurement of the loss factor provides a check of the calculations and the vacuum chamber manufacturing and assembly procedure.

Although conceptually simple the synchronous phase shift measurement can be difficult in practice especially for the newer storage rings. The loss factor tends to be small, resulting in a total phase shift on the order of a degree or less which is hard to measure accurately with traditional experimental techniques. In this paper we introduce a new low cost apparatus that offers significantly higher precision and flexibility than commonly used ones. We will also describe our successful use of this apparatus to measure the synchronous phase shift in the Stanford Linear Collider (SLC) damping rings.

2.0 Physics of a synchronous phase shift and predictions for the SLC damping rings

The energy balance of the stored beam can be written as

$$eV_{RF} \cos(\varphi_0 + \Delta\varphi) = U_0 + ke^2N, \quad (\text{EQ 1})$$

where V_{RF} is the accelerating voltage, φ_0 is the zero current synchronous phase, U_0 is the synchrotron radiation energy loss per turn, eN is the total beam charge, k is the loss factor and $\Delta\varphi$ is the synchronous phase shift. When the latter is small we get for the loss factor

$$k = -\frac{\Delta\varphi}{eN} V_{RF} \sin \varphi_0. \quad (\text{EQ 2})$$

For a given longitudinal beam density $\rho(z)$ the loss factor can be related to the total wake-field $W(z)$ or to the real part of the impedance $Z(\omega)$ as¹

$$k = \int_{-\infty}^{\infty} W(z)\rho(z)dz = \frac{1}{2\pi} \int_{-\infty}^{\infty} \text{Re}(Z(\omega))|\tilde{\rho}(\omega)|^2 d\omega, \quad (\text{EQ 3})$$

where $\rho(z)$ is normalized to one and $\tilde{\rho}(\omega)$ is the Fourier transform of $\rho(z)$. For short Gaussian bunches the ω dependence of Z can be neglected above so that we get for the

real part of the impedance

$$R = \frac{2\sqrt{\pi}\sigma k}{c}, \quad (\text{EQ 4})$$

where σ is the rms bunch length and c is the velocity of light. For the SLC damping rings the longitudinal wake-field $W(z)$ has been calculated numerically^{2,3} for a 1 mm rms Gaussian bunch. For the low current bunch length of $\sigma_0 = 5.3$ mm corresponding to 800 kV nominal RF voltage this calculation yields the total loss factor of 15 V/pC which corresponds to 950 Ω resistive impedance. This loss factor substituted into EQ 2 where $\phi_0 = 84^\circ$ calls for the phase shift of 1.7° per 10^{10} particles. This is the value we have to be able to measure.

3.0 Traditional way to measure the synchronous phase shift and its limitations

Although other signals carrying beam phase information exist the simplest one to use is a beam position monitor (BPM) pickup signal. It includes the fundamental harmonic of the RF frequency the phase of which relative to the RF in the accelerating cavity defines the synchronous phase up to some constant offset. For large phase shifts the synchronous phase can be simply measured with an oscilloscope or a mixer-based phase detector. Smaller phase shifts require more accurate tools. The most precise, general-purpose instrument to measure the phase of RF signals is the vector voltmeter. It is traditionally the instrument of choice for synchronous phase shift measurements.^{4,5,6}

However, as we found out in our experiments we could not measure the synchronous phase shift reliably with a Hewlett-Packard 8508A vector voltmeter. This is not surprising because the accuracy standard vector voltmeters provide is not sufficient for the SLC damping rings. For example, the specifications for the HP 8508A state an 0.8° phase accuracy within 1 mV to 100 mV input signal range and several times lower accuracy outside of it.⁷ Another disadvantage of this device is the lack of convenient control over the averaging constant which is important for synchronous phase measurement. Indeed, in a noisy environment a significant increase in sensitivity can be achieved from averaging the phase over the interval comparable to the sampling time.

To overcome these limitations of the vector voltmeter we came up with the following solution.

4.0 New Apparatus

In our apparatus we modify the approach described above in two ways. First, we do not perform the phase comparison at the fundamental RF frequency but rather downmix both beam and RF cavity signals to roughly 25 kHz where audio measurement techniques are available. Second, for the actual phase measurement we use the SR830 DSP Lock-in Amplifier manufactured by Stanford Research Systems. This device has a relative phase error of 0.01° , adequate input sensitivity and temperature stability, and it provides complete control over the time averaging constant. Other features we found useful for this measurement include power line notch filters in the signal arm, auxiliary ADC channels and complete GPIB capability.

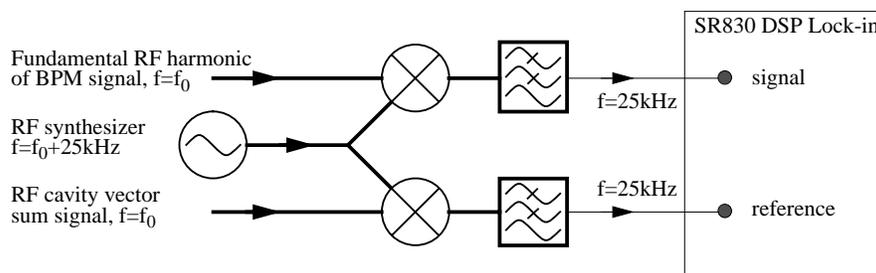


Figure 1. The idea of the apparatus.

The basic idea of our apparatus is shown in Fig. 1. To provide an LO arm for the downmixing, we use an RF synthesizer. The low pass filters cut the higher frequency mixing products out. Since a bridge is implemented synthesizer frequency drift should not in the first order result in a phase error. Note that the total cost of this setup is a fraction of that for the vector voltmeter. Also, the system is rather flexible. Indeed, to switch to another RF frequency one needs to either reprogram the synthesizer or replace it when the frequency is substantially different. Finally, this setup can be used in other experiments that require phase measurement of RF signals of practically any frequency. For example, a similar approach was used in a home-made W-band vector network analyzer where phase and amplitude of a 92 GHz signal were measured.⁸ Finally, filtering a beam signal at the fundamental harmonic can be hard for larger rings where a very high-Q RF filter may be needed. However, with this setup we can easily insert one more stage of downmixing to some common frequency where appropriate off-the-shelf crystal filters are available.

5.0 Experimental Details

In order to accurately measure the phase it is not enough to have a precise lock-in amplifier. Care has to be taken about other elements of the system as well as the machine conditions. Here we summarize our experience coming from the SLC measurements.

Input Cables. Typical electrical length change in cables runs from 150 PPM/°C (RG223) to ~6 PPM/°C (HELIAX). Therefore, a temperature drift during a measurement can significantly alter the result if the cable runs are long. In the SLC (~100 ft of RG223) we found out that using a temperature stabilized cable significantly improves measurement reproducibility. Unfortunately, this cable was only available for part of the distance needed and also the temperature in the room with our setup was not fully controlled. This may explain our experience of better reproducibility when the measurements were taken at night so that the outside temperature didn't change much.

BPM signal filter. To measure the phase correctly the input signal to the lock-in amplifier should not have significant amplitude modulation. Approximating a filter as an oscillator of a quality factor Q gives a requirement $Q/h \geq 1$, where h is the harmonic number. For the SLC damping rings ($f_{RF} = 714$ MHz, $h = 84$) we made a simple coaxial cavity filter with $Q \approx 300$.

Vector sum. EQ 1 includes the total accelerating voltage. To measure it the pickup voltages from the individual cells must be summed vectorially. This signal is available for the SLC since it is used in the so-called direct feedback loop.⁹

Signal levels. The SR830 specifications require at least 200 mV_{peak-peak} (into 1 MΩ) reference arm input signal. We had to use an audio amplifier to bring the reference signal above this level. To make sure that the amplitude stayed constant we monitored it by a home-made RMS detector with the output connected to one of the auxiliary inputs of SR830 (Fig. 2). A related issue here is the isolation of the power splitter that divides the LO signal. We had to make sure that it is high enough so that the cavity signal doesn't leak through the coupler and doesn't significantly distort the beam signal or vice versa.

Beam lifetime and the lock-in averaging constant. To get a significant current decay the store should be comparable to the beam lifetime. There are simple ways of shortening the lifetime (with scrapers, transverse detuning etc.) to accelerate the measurement and reduce the temperature drift effect. However, the decay has to be rather smooth because rapid drops in the input signal to the lock-in amplifier may result in phase measurement error. In the SLC (lifetime on the order of ten minutes and no scraper is available to reduce it) we tried the transverse detuning but couldn't make it smooth enough. We proceeded with our measurements using nominal lifetime stores. The data was sampled about every three seconds, and the lock-in time averaging constant was set to one second. Shorter settings resulted in noisier data but didn't lead to a different phase slope with the current.

Feedbacks. If the vector sum signal is properly derived then most feedback loops should not affect the measurement. For the SLC this is not true only for the so-called s-band feedback that adjusts the beam phase for subsequent injection to the linac as well as for the direct feedback loop that effectively changes the cavity shunt impedance. These two feedbacks had to be turned off for our measurements.

6.0 Damping ring measurement results

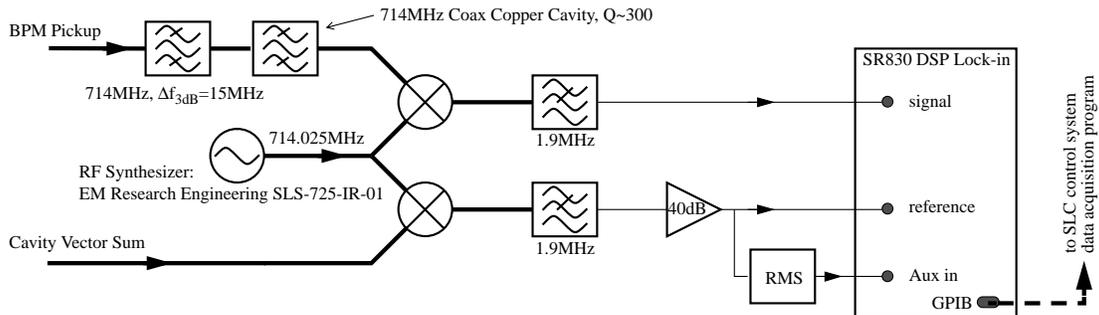


Figure 2. The setup for synchronous phase measurement in the SLC damping rings.

The measurements we describe here were done in the positron damping ring. Similar results were later obtained in the other (electron) damping ring that has almost identical vacuum chamber. The setup we used is shown schematically in Fig. 2. Single beam stores were done at different values of accelerating voltage clustered near 600 kV, 800 kV and 1000 kV. The total beam charge was 1 to 1.5×10^{10} particles per bunch at the beginning of each store, which is below the known longitudinal instability threshold. The stores lasted ten to fifteen minutes, so that the current decayed roughly a factor of two (Fig. 3a). Since many systematic errors could show up as a linear change of phase with time, which could hide real effects, we did several measurements at every value of accelerating voltage. The total number of stores was seventeen.

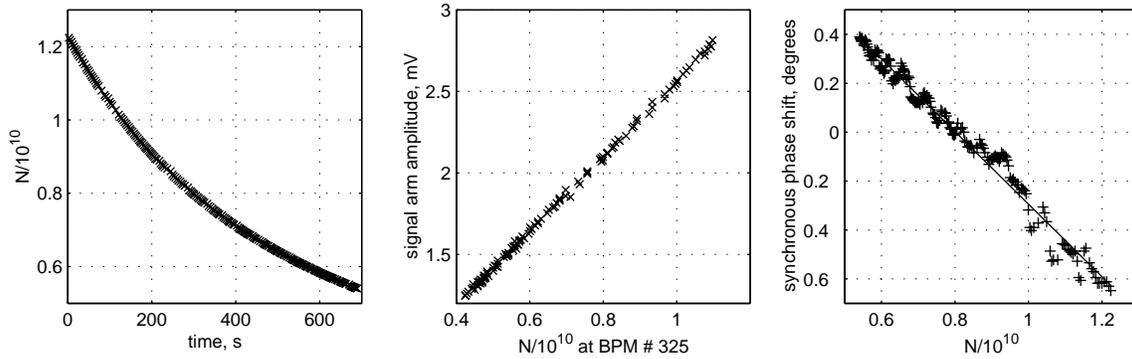


Figure 3. Typical data sample (left to right) a) Charge stored vs. time b) Lock-in signal amplitude vs. BPM current reading c) Phase shift vs. charge stored (data and linear fit).

For each store we were recording some of the RF system parameters as well as the beam current; these values are routinely available from the SLC control system. Simultaneously we sampled five values with the lock-in amplifier namely the lock status bit, reference arm amplitude, reference arm frequency, signal arm amplitude and signal arm phase. All but the last were recorded for diagnostic purposes to ensure solid lock to the external reference with stable frequency and amplitude. The signal arm amplitude was proportional to the beam current (Fig. 3b) which argues that the signal was largely beam induced. The phase shift measured by the lock-in was the actual synchronous phase shift and as expected it turned out to be linear with the beam current (Fig. 3c). The phase shift slope with current substituted in EQ 2 allowed us to extract the value for the loss factor. The results for seventeen stores at different RF voltages are shown in Fig. 4. The data are consistent with a constant justifying the assumptions made in EQ. 4 together with $\sigma^2 \sim V_{RF}$ scaling. Using these assumptions we found the average nominal value for the loss factor $k_0 = 16.5 \text{ V/pC} \pm 15\%$ which corresponds to about $1 \text{ k}\Omega$ resistive component in the longitudinal impedance. This measured value is in good agreement with calculations.^{2,3} The error is largely systematic and comes from the uncertainty in absolute values of beam current and accelerating voltage; the error in the mean from the data points in Fig. 4 is less than 3%. It is also possible to estimate the loss factor for a given accelerating voltage without making any assumptions on bunch length scaling. For example, for $V_{RF} = 760 \text{ kV}$ the loss factor $k(760 \text{ kV}) = 16 \text{ V/pC}$ which is consistent with k_0 .

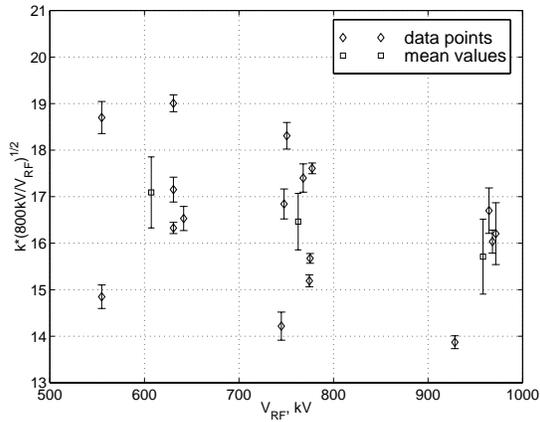


Figure 4. Scaled loss factor vs. accelerating voltage. The results from each store are plotted with the statistical error of the fit (diamonds). Also plotted are the mean values within each group (squares) with their errors derived from the rms spread of the individual stores.

7.0 Summary

We have designed and built a new apparatus that allows for precise synchronous phase measurement in the storage rings. Our apparatus compares favorably with other techniques due to increased accuracy and flexibility and also lower cost. We have successfully used our apparatus in the SLC damping rings where the total phase shifts measured were about one degree. The loss factor value was obtained from our measurement and it turned out to agree well with calculations.

8.0 Acknowledgements

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