

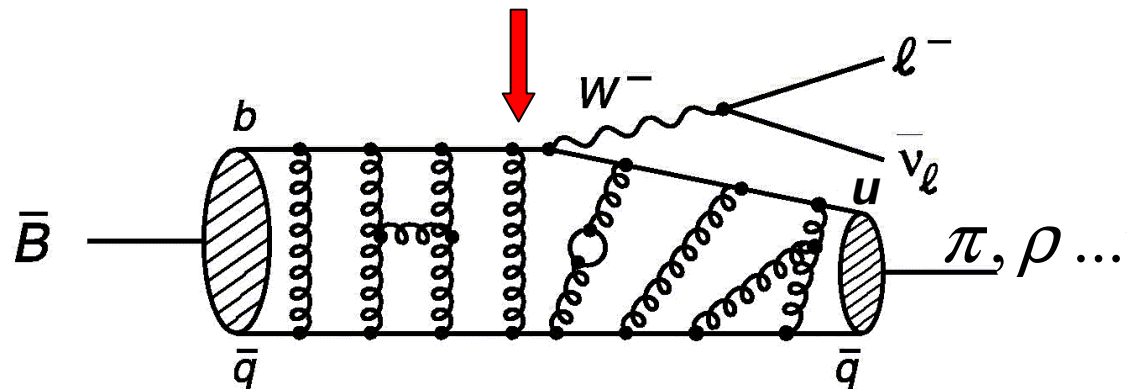
Measurement of $|V_{ub}|$

Tom Browder (University of Hawaii)

Inclusive approaches (endpoint, M_X , q^2)

Exclusive approaches ($B \rightarrow \pi l \nu$, $B \rightarrow \rho l \nu$)

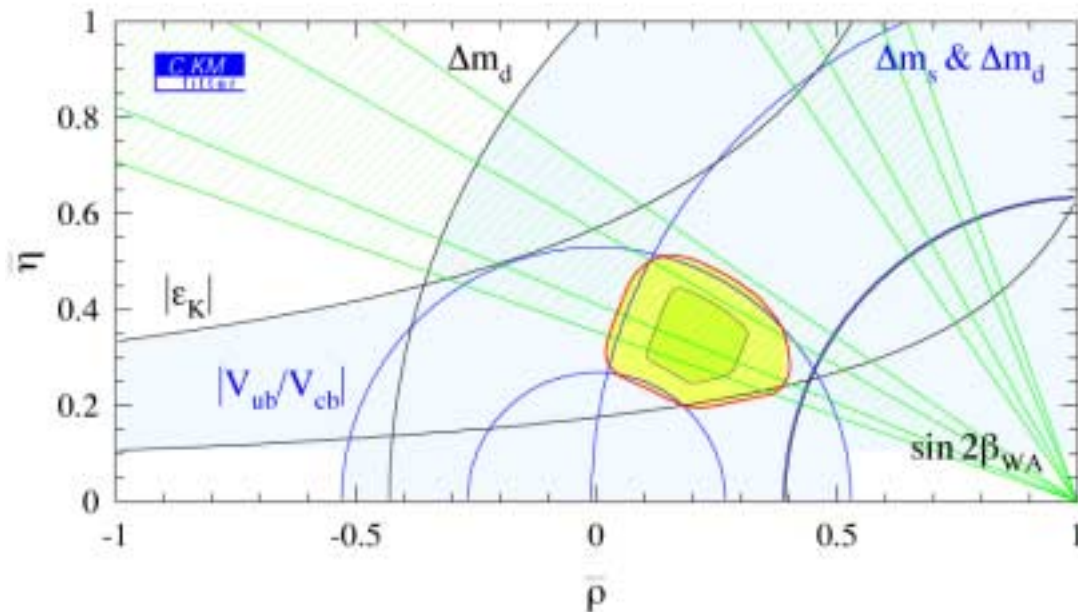
Conclusion



The V_{ub} element of the CKM matrix

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

$|V_{ub}|$ determines a circle of radius² = $\rho^2 + \eta^2$ for the apex of the Bjorken triangle. *Very important for indirect constraints on the CKM triangle and for detecting New Physics.*

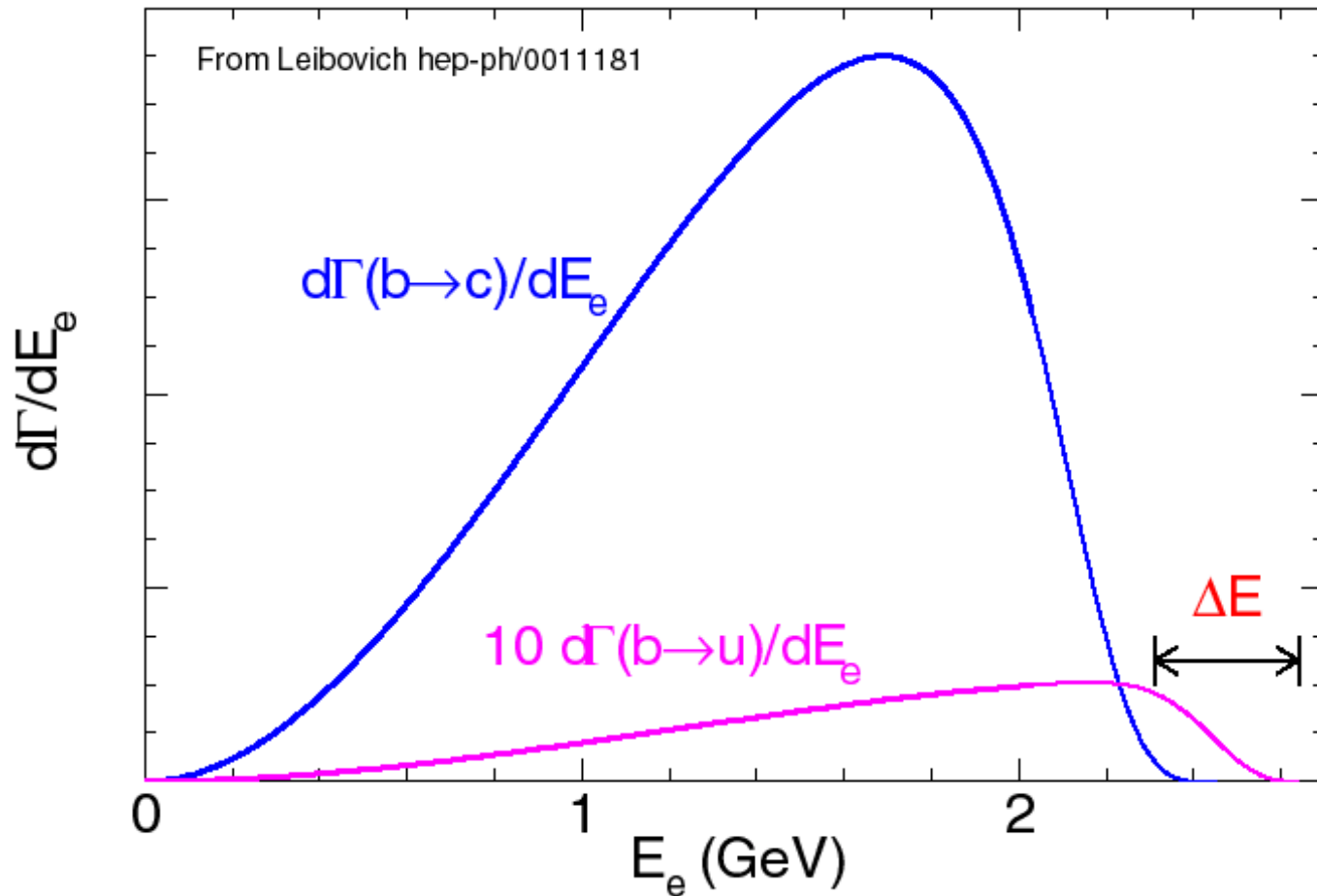


How are $|V_{ub}|$ measurements different from $|V_{cb}|$ measurements?

Cannot observe the whole spectrum of $b \rightarrow u l \nu$ unlike $b \rightarrow c l \nu$. Backgrounds are too large hence restricted to small portions of phase space.

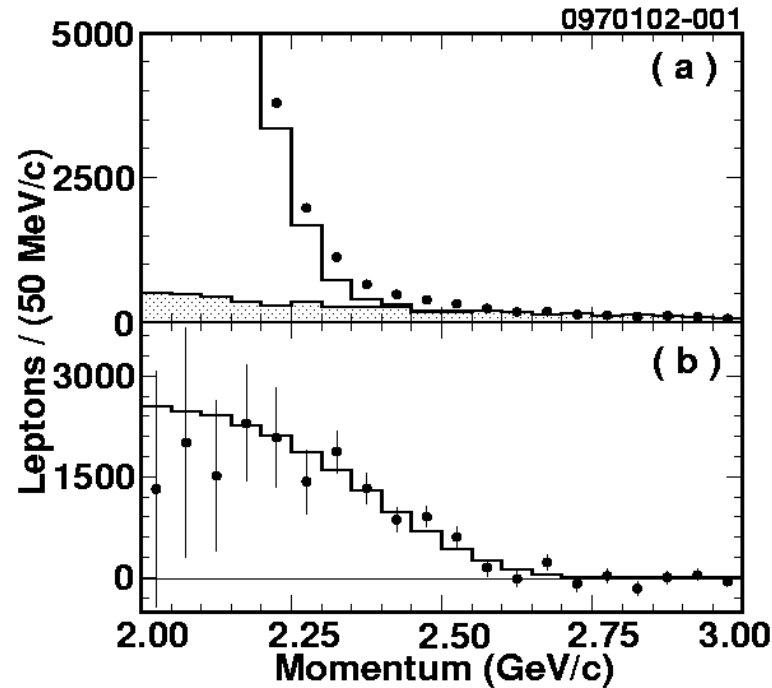
Heavy \rightarrow light FF not Heavy \rightarrow Heavy FF: very little simplification from HQET. W or q^2 range is much larger (dependence on FF is much greater).

$|V_{ub}|$ from the Lepton Endpoint



A large theoretical extrapolation is required to obtain $|V_{ub}|$

CLEO 2001: $|V_{ub}|$ from leptons beyond the $b \rightarrow c$ endpoint



$$1901 \pm 127 \pm 256$$

Large cont subtr.

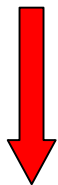
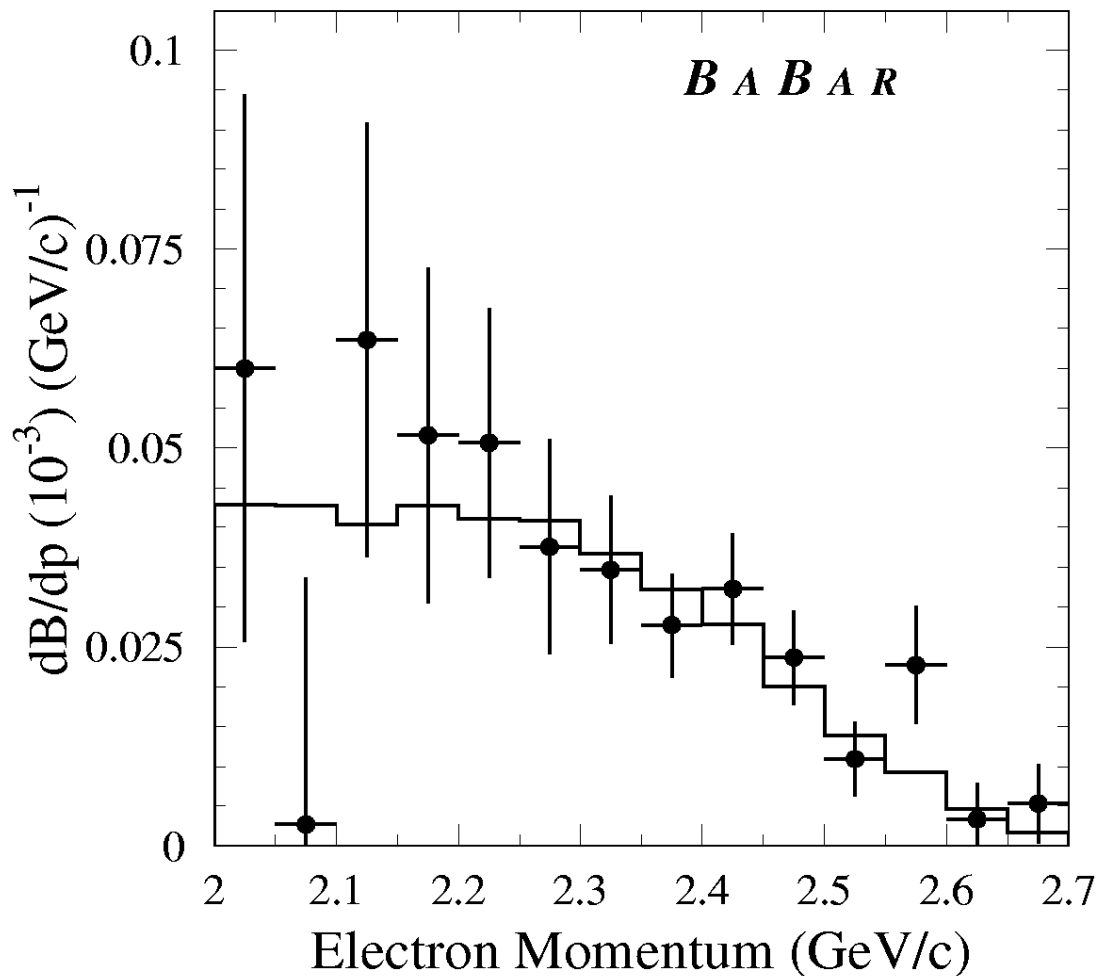


TABLE I: Lepton yields and backgrounds in the momentum interval 2.2 – 2.6 GeV/c.

	e	μ	Sum
N_{ON}	4110	4857	8967
N_{OFF}	410	573	983
Excess	$3265 \pm 77 \pm 8$	$3673 \pm 85 \pm 12$	$6938 \pm 115 \pm 20$
Fakes	$15 \pm 6 \pm 4$	$194 \pm 13 \pm 58$	$209 \pm 19 \pm 58$
J/ψ	$68 \pm 4 \pm 7$	$90 \pm 5 \pm 9$	$158 \pm 6 \pm 16$
Other Backgrounds	$40 \pm 8 \pm 10$	$67 \pm 6 \pm 18$	$107 \pm 10 \pm 29$
$B \rightarrow X_c l \nu$	$2147 \pm 23 \pm 116$	$2415 \pm 24 \pm 130$	$4562 \pm 33 \pm 246$
$B \rightarrow X_u l \nu$	$995 \pm 81 \pm 117$	$906 \pm 106 \pm 133$	$1901 \pm 122 \pm 256$

BABAR 2002: $|V_{ub}|$ from leptons beyond the endpoint



Bkg subtracted
yield and
ISGW2 model

1696 ± 133

$$BF(b \rightarrow u l \nu, 2.3-2.6 \text{ GeV}) = (0.152 \pm 0.014 \pm 0.014) \times 10^{-3}$$

Agrees well with CLEO $(0.143 \pm 0.010 \pm 0.014) \times 10^{-3}$

Model Dependence in $|V_{ub}|$ from inclusive decay.

CLEO 1993: Model dependence

TABLE IV. Partial branching fractions and corresponding values of $|V_{ub}/V_{cb}|^2$ and $|V_{ub}/V_{cb}|$ for the strict-cut analysis in the momentum interval 2.3 to 2.6 GeV/c.

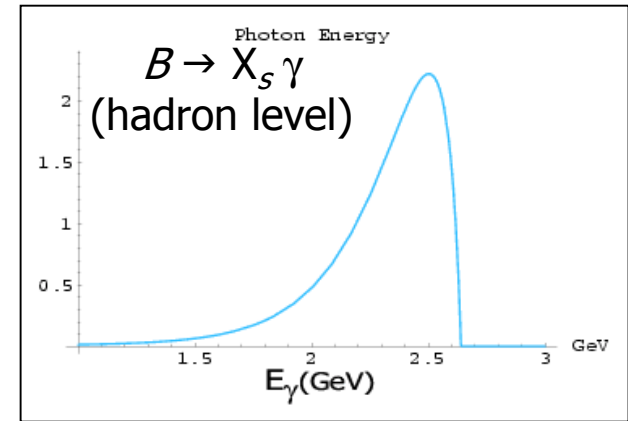
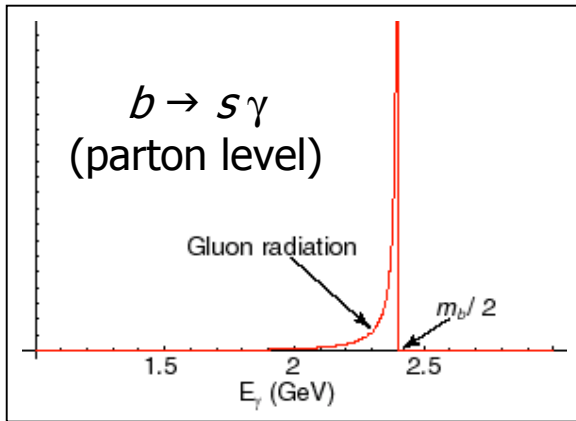
Model	$10^6 \Delta B_{ub}(p)$	$10^2 V_{ub}/V_{cb} ^2$	$ V_{ub}/V_{cb} $
ISGW	$121 \pm 17 \pm 15$	1.02 ± 0.20	0.101 ± 0.010
KS	$115 \pm 16 \pm 15$	0.31 ± 0.06	0.056 ± 0.006
WSB	$122 \pm 17 \pm 16$	0.53 ± 0.11	0.073 ± 0.007
ACCMM	$154 \pm 22 \pm 20$	0.57 ± 0.11	0.076 ± 0.008



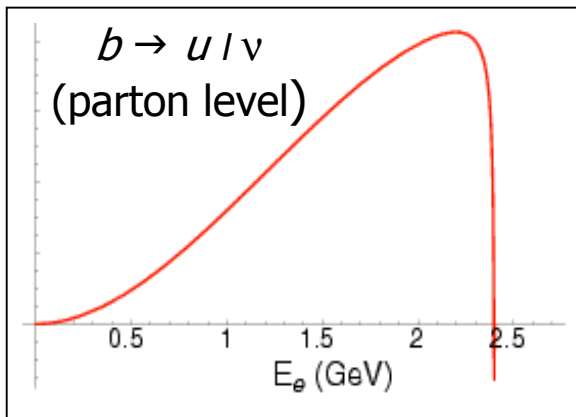
CLEO 2001, BABAR 2002: No longer use a model for extrapolation. Instead rely on the $b \rightarrow s \gamma$ shape function..

(Discussed in lectures by Ligeti)

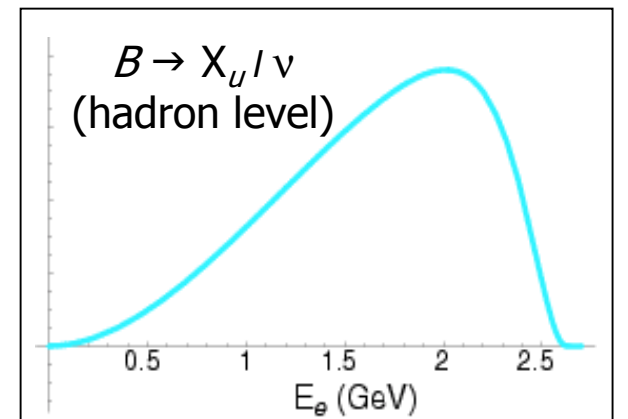
$B \rightarrow$ light quark shape function, SAME (to lowest order in Λ_{QCD}/m_b) for $b \rightarrow s \gamma$ ($B \rightarrow X_s \gamma$) and $b \rightarrow u l \nu$ ($B \rightarrow X_u l \nu$).



Convolute with light cone shape function.



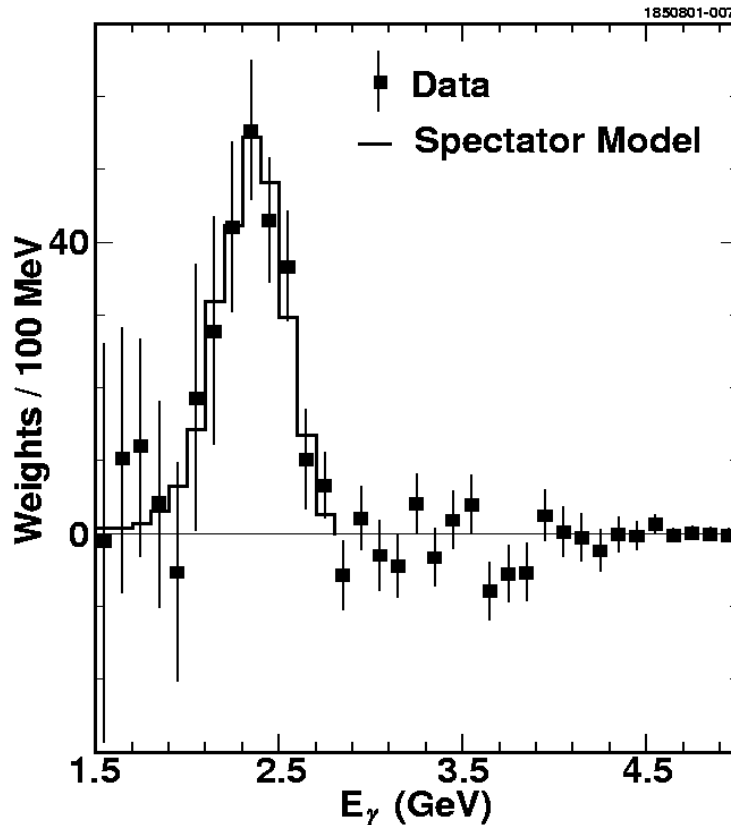
Fraction of $b \rightarrow u l \nu$
spectrum above 2.2 is
 0.13 ± 0.03



Extrapolation from endpoint region using $b \rightarrow s \gamma$

Idea: Use the shape function in $b \rightarrow s \gamma$ to determine the $b \rightarrow u l \nu$ shape function. Then get the fraction of events in the $b \rightarrow u l \nu$ endpoint region.

CLEO



Idea introduced by Neubert; Leibovich, Low, and Rothstein.

$f_u(2.2-2.6 \text{ GeV})$
 $= 0.130 \pm 0.024 \pm 0.05$

V_{ub} Extrapolation from endpoint region using $b \rightarrow s \gamma$

TABLE II: Results for five momentum intervals. Uncertainties on yields, f_u , and branching fractions are statistical and systematic. The first uncertainty on the total branching fraction is from the measurement of $\Delta\mathcal{B}_u(p)$ and the second is from f_u . The first two uncertainties on $|V_{ub}|$ are from the branching fraction and the third and fourth are from theory.

p (GeV/c)	Yield	$\Delta\mathcal{B}_u(p)(10^{-4})$	f_u	$\mathcal{B}(B \rightarrow X_u \ell \nu) (10^{-3})$	$ V_{ub} (10^{-3})$
2.0-2.6	$3538 \pm 279 \pm 1470$	$4.22 \pm 0.33 \pm 1.78$	$0.266 \pm 0.041 \pm 0.024$	$1.59 \pm 0.68 \pm 0.28$	$3.87 \pm 0.83 \pm 0.35 \pm 0.15 \pm 0.12$
2.1-2.6	$2751 \pm 191 \pm 584$	$3.28 \pm 0.23 \pm 0.73$	$0.198 \pm 0.035 \pm 0.020$	$1.66 \pm 0.39 \pm 0.34$	$3.95 \pm 0.46 \pm 0.40 \pm 0.16 \pm 0.16$
2.2-2.6	$1901 \pm 122 \pm 256$	$2.30 \pm 0.15 \pm 0.35$	$0.130 \pm 0.024 \pm 0.015$	$1.77 \pm 0.29 \pm 0.38$	$4.08 \pm 0.34 \pm 0.44 \pm 0.16 \pm 0.24$
2.3-2.6	$1152 \pm 80 \pm 61$	$1.43 \pm 0.10 \pm 0.13$	$0.074 \pm 0.014 \pm 0.009$	$1.94 \pm 0.22 \pm 0.43$	$4.27 \pm 0.24 \pm 0.47 \pm 0.17 \pm 0.34$
2.4-2.6	$499 \pm 57 \pm 14$	$0.64 \pm 0.07 \pm 0.05$	$0.037 \pm 0.007 \pm 0.003$	$1.74 \pm 0.24 \pm 0.38$	$4.05 \pm 0.28 \pm 0.45 \pm 0.16 \pm 0.45$

Optimal interval is $2.2 < p_L < 2.6$ GeV

$$\text{BF}(2.2-2.6 \text{ GeV}) = (2.30 \pm 0.15 \pm 0.35) \times 10^{-4}$$

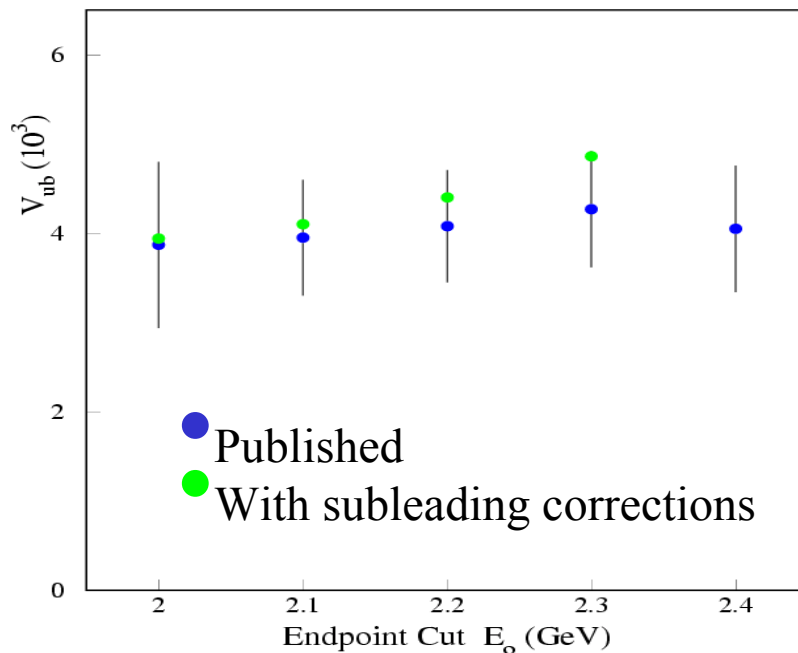
$$f_u(2.2-2.6 \text{ GeV}) = 0.130 \pm 0.024 \pm 0.05$$

$$|V_{ub}| = (3.07 \pm 0.12) \times 10^{-3} \times \left[\frac{\mathcal{B}(B \rightarrow X_u e \nu) 1.6 \text{ ps}}{0.001 \tau_B} \right]^{\frac{1}{2}}.$$

CLEO: $|V_{ub}|$ from Lepton Endpoint (using $b \rightarrow s \gamma$)

$$|V_{ub}| = (4.08 \pm 0.34 \pm 0.44 \pm 0.16 \pm 0.24) \times 10^{-3}$$

stat $b \rightarrow s \gamma$ Γ theory Λ/M_B theory



➤ *Subleading corrections large*

*C. Bauer, M. Luke, T. Mannel
A. Leibovich, Z. Ligeti, M. Wise*

➤ Method for partial inclusion of subleading corrections:
Neubert

➤ *Quark-hadron duality ?*

How can we improve our knowledge of $|V_{ub}|$ from inclusive decays ?

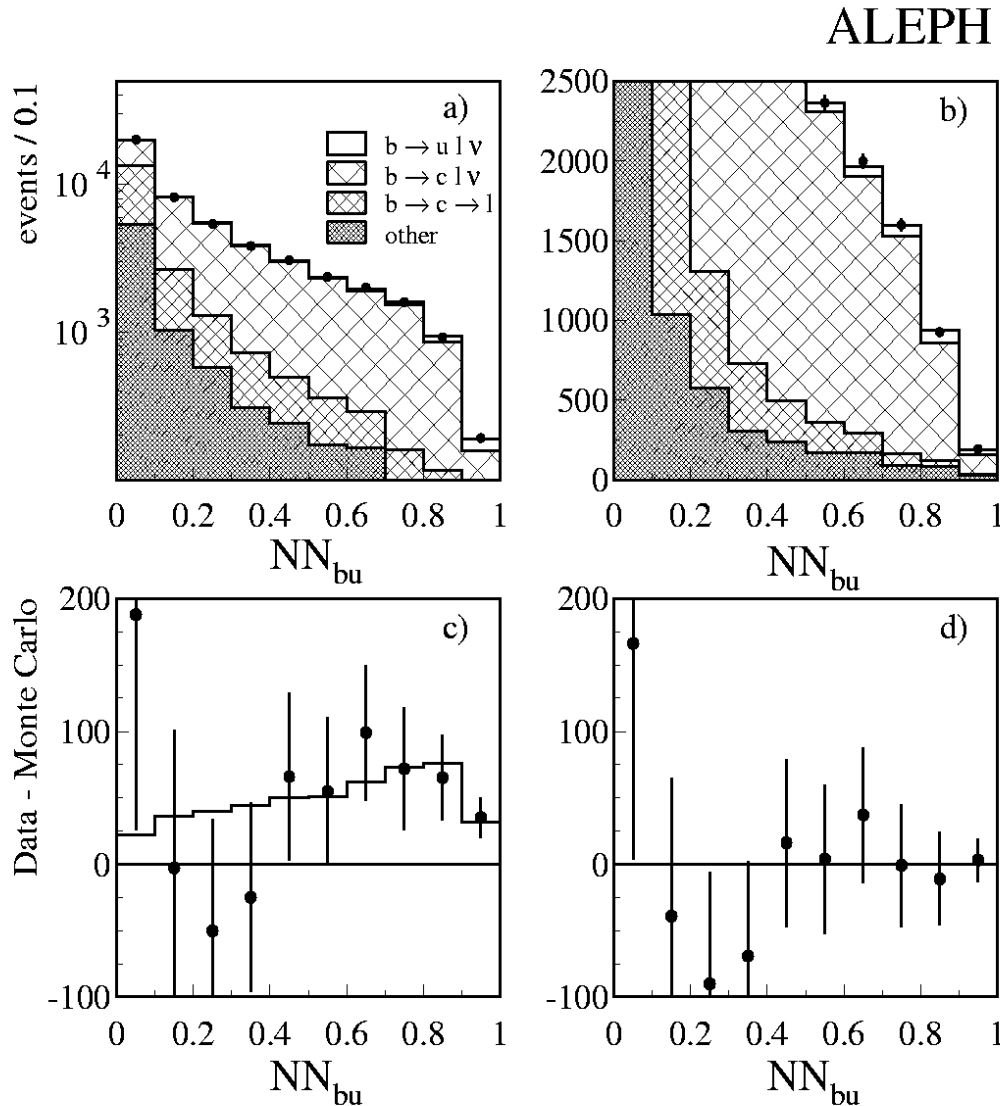
Use all of phase space (LEP)

*Use favorable regions of M_X or q^2
(DELPHI, CLEO) and new
theoretical strategies*

**Fraction with $E_L > 2.2$ GeV ($\sim 15\%$);
fraction with $M_X < M_D$ ($\sim 70\%$), fraction
with $q^2 > (M_B - M_D)^2$ ($\sim 20\%$)**

ALEPH $|V_{ub}|$ Measurement

$S/B=0.07$

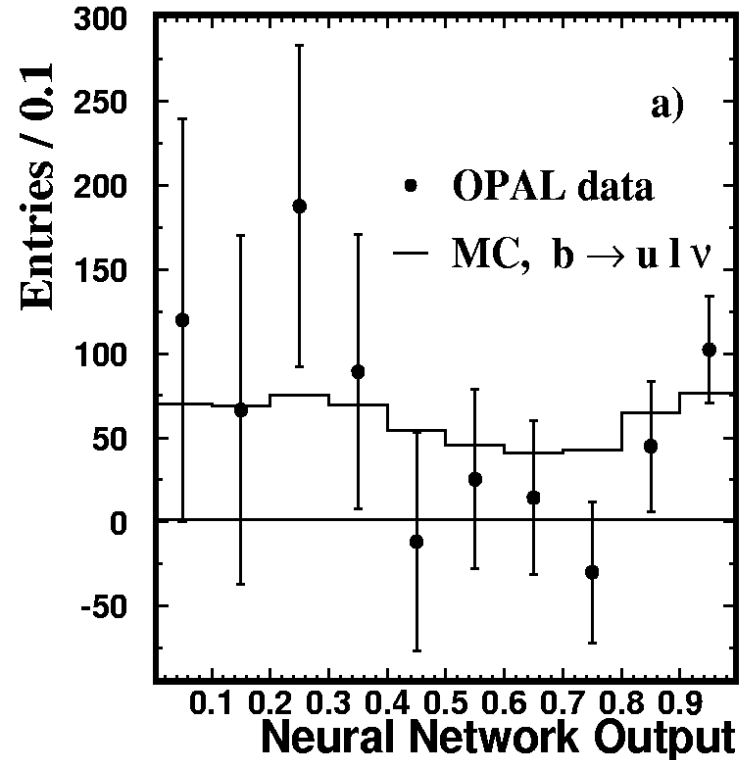
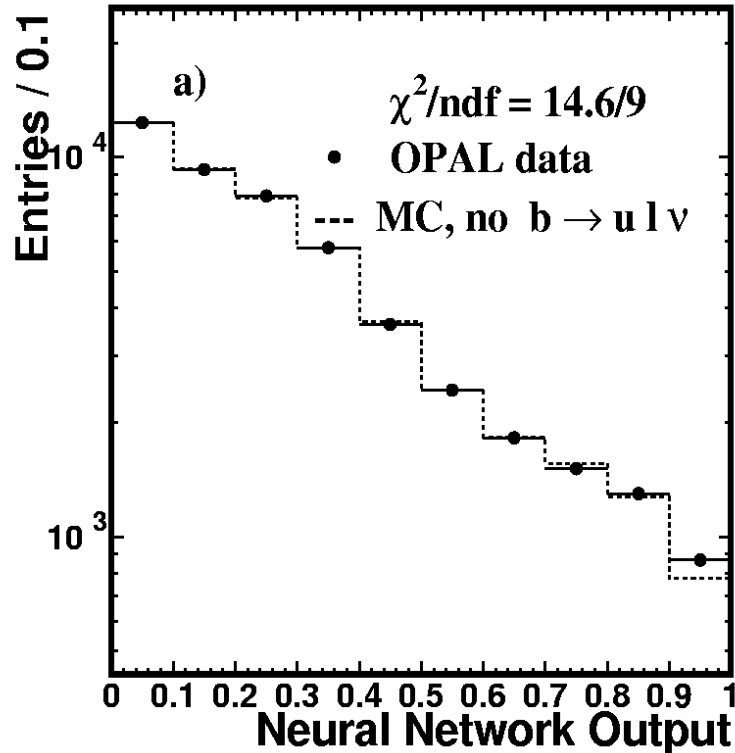


20 kinematic variables in a NN

$b \rightarrow u$ enriched

$b \rightarrow u$ depleted

OPAL $|V_{ub}|$ Measurement



Huge background suppressed with 7 variable Neural Net

Small signal extraction depends on $b \rightarrow c l \nu$ model! $S/B = 0.05$

Published Inclusive $|V_{ub}|$ Determinations

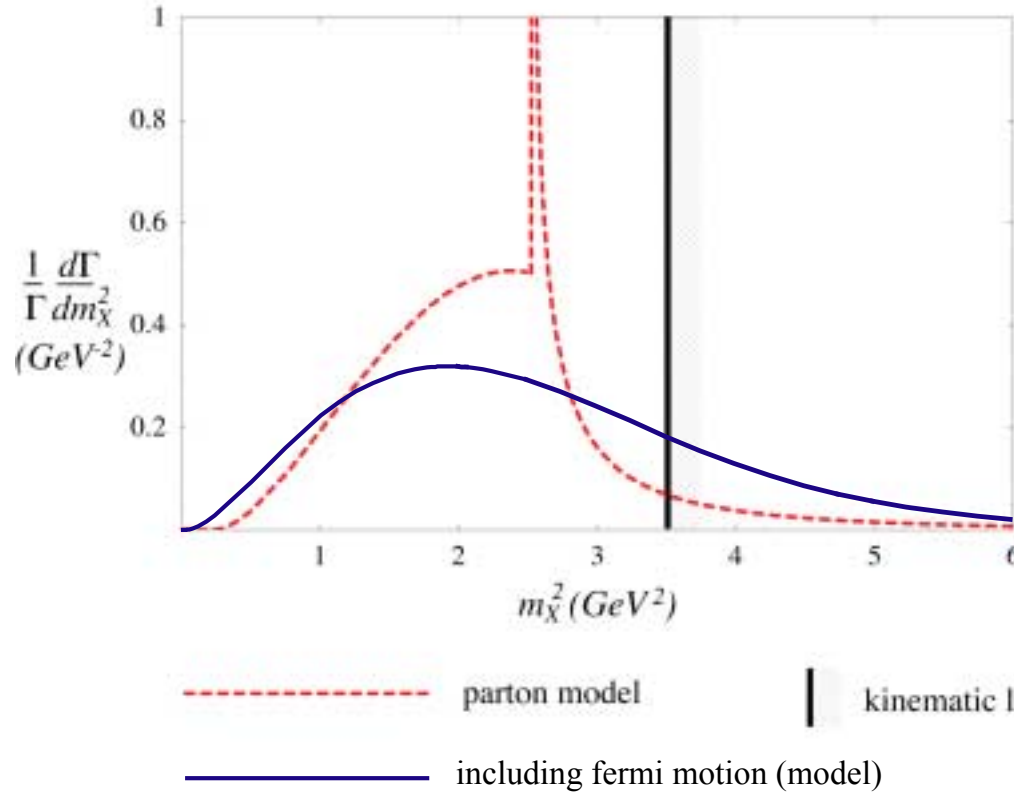


Exp.	Method	S/B	$ V_{ub} $ [10^{-3}]	$\sigma_{b \rightarrow c}$ ($ V_{ub} $)	σ_{th} ($ V_{ub} $)
ALEPH	Neural Net	0.07	$4.12 \pm .67 \pm .62 \pm 0.35$	15%	9%
OPAL	Neural Net	0.05	$4.00 \pm .71 \pm .59 \pm 0.40$	15%	10%
DELPHI	M_X	0.10	$4.07 \pm .65 \pm .47 \pm 0.39$	12%	10%
L3	$\pi - \ell$ Cut	0.22	$5.7 \pm 1.0 \pm 1.3 \pm 0.5$	22%	10%
LEP	Average		$4.09 \pm 0.37 \pm 0.44 \pm 0.34$		9–15%
CLEO	E_ℓ endpoint	0.39	$4.12 \pm 0.34 \pm 0.44 \pm 0.33$	7%	10–15%

LEP

Battaglia and Gibbons

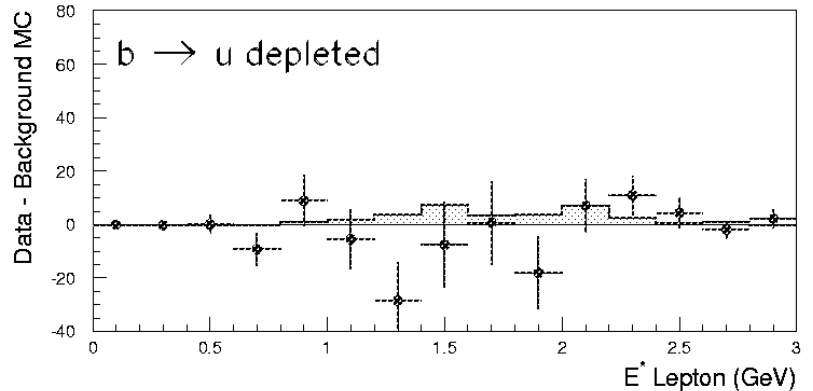
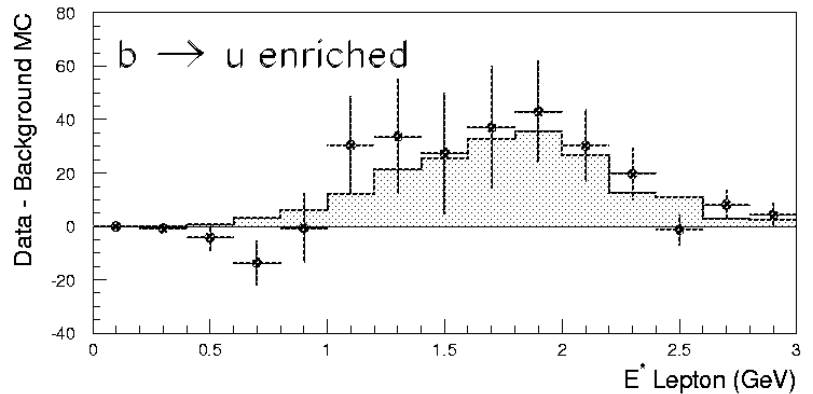
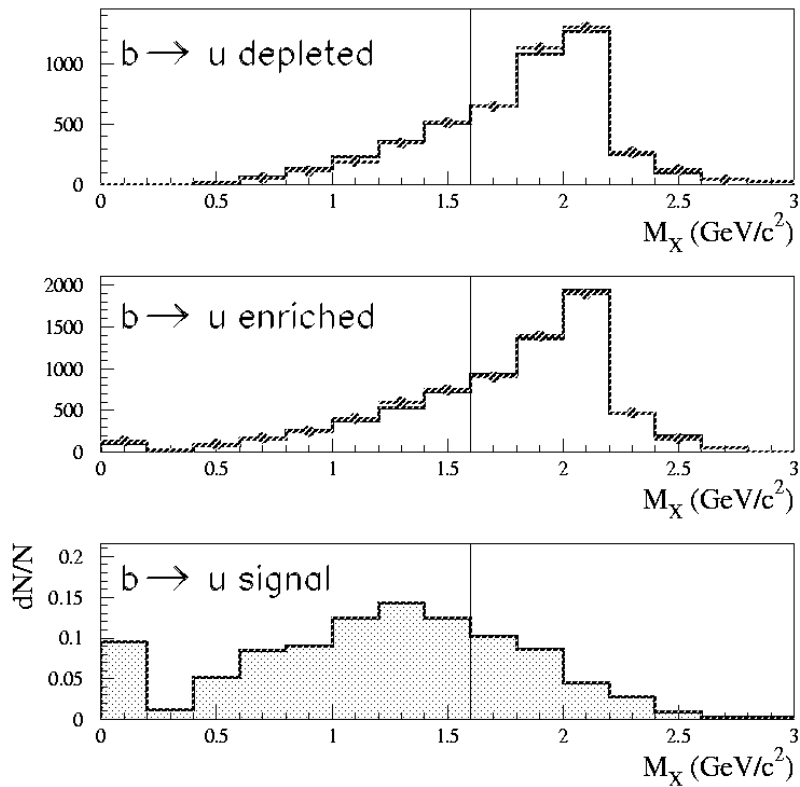
Hadronic Invariant Mass Spectrum for $b \rightarrow u$ Decay



See lectures
by Ligeti

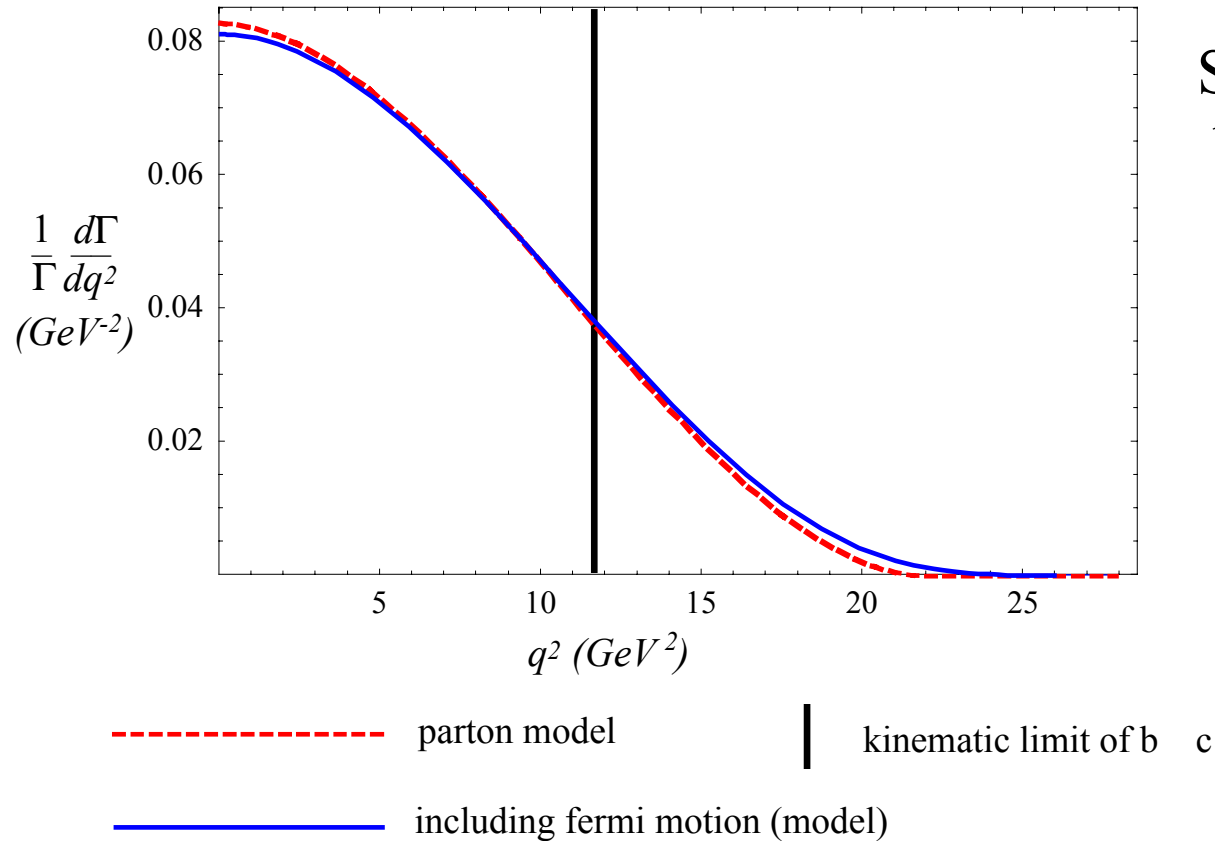
- singularity is smeared out by b quark light-cone distribution function $f(k_+)$
- rate is sensitive to details of $f(k_+)$ unless $m_X^2 \gg \Lambda_{QCD} m_b$ (bad for $m_X < m_D$!) - introduces model dependence unless we know $f(k_+)$

DELPHI 2000: Analysis with $M_X < 1.6 \text{ GeV}$



$$|V_{ub}| = (4.07 \pm 0.65(\text{exp}) \pm 0.47(\text{b} \rightarrow \text{c}) \pm 0.39(\text{theo})) \times 10^{-3}$$

Lepton Invariant Mass Spectrum for $b \rightarrow u$ Decay



Lepton q^2 spectrum is insensitive to Fermi motion (and has less model dependence.)

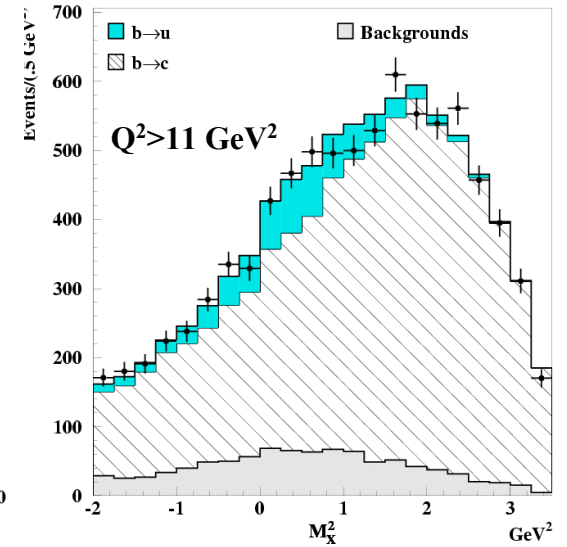
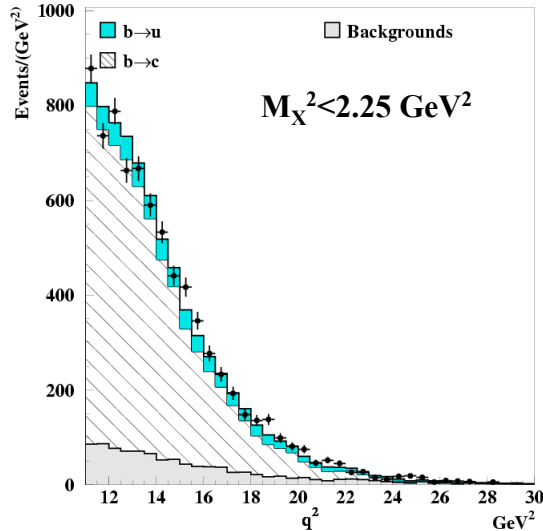
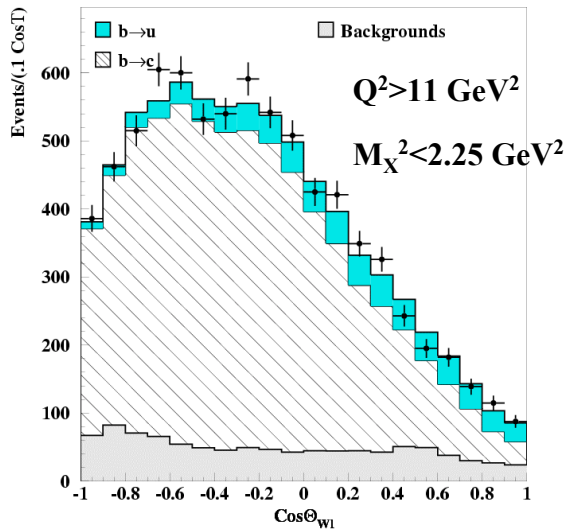
M.Luke:

Representative cuts:

- | | | |
|-----|---|-------------|
| (a) | $q^2 > 6 \text{ GeV}^2, m_X < m_D$ | 46% of rate |
| (b) | $q^2 > 8 \text{ GeV}^2, m_X < 1.7 \text{ GeV}$ | 33% of rate |
| (c) | $q^2 > 11 \text{ GeV}^2, m_X < 1.5 \text{ GeV}$ | 18% of rate |

Uncertainty	Size (in V_{ub})	Improvement?
Δm_b	$\pm 80 \text{ MeV}$: 7%, 8%, 10% $\pm 30 \text{ MeV}$: 3%, 3%, 4%	RG improved \mathcal{Y} sum rules, moments of B decay spectra, lattice
α_s	2%, 3%, 7%	full two-loop calculation
$1/m_b^3$ (weak annihilation)	3%, 4%, 8%	compare B^\pm, B^0 compare S.L. width of D^0, D_S , lattice

CLEO: $B \rightarrow X \ell \nu$ with Neutrino Reconstruction



$$|V_{ub}| = (4.05 \pm 0.18 \pm 0.58 \pm 0.25 \pm 0.21 \pm 0.56) 10^{-3}$$

stat
sys
 $b \rightarrow c$
 $b \rightarrow u$
theory

$|V_{ub}|$ from M_X or q^2 with fully reconstructed B tags (MC)

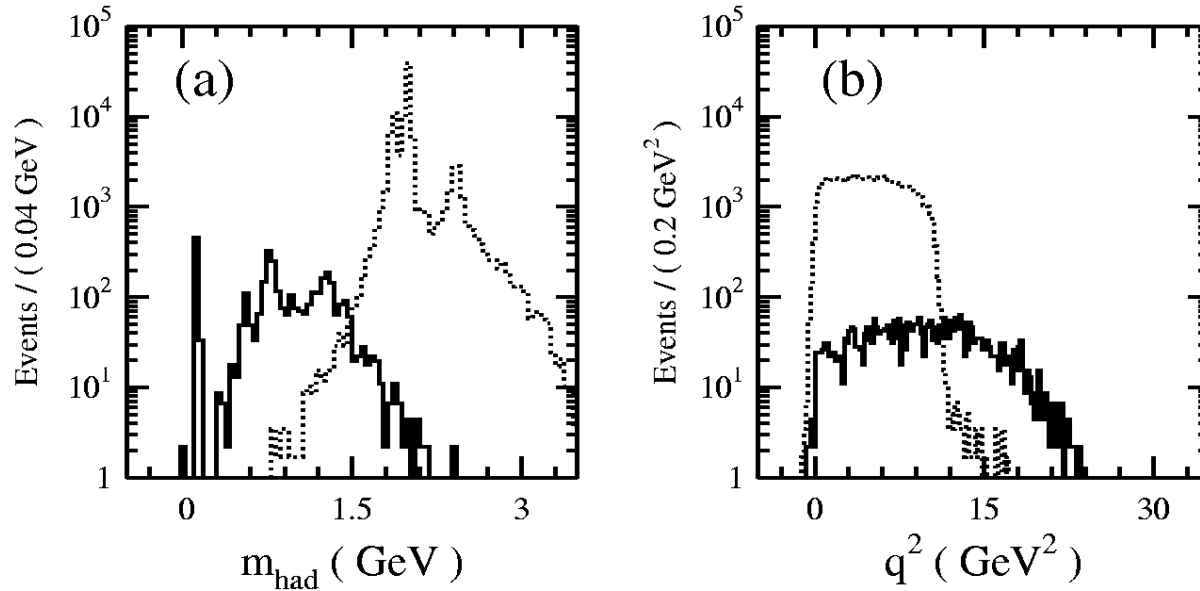


FIG. 1: (a) Hadronic mass (m_{had}) distribution for 1000 fb^{-1} data found with CLEO III fast MC. The solid histogram is the m_{had} distribution of $b \rightarrow ul\nu$, and the dashed histogram is the m_{had} distribution of $b \rightarrow cl\nu$. (b) q^2 distribution for 1000 fb^{-1} data found with CLEO III fast MC. The solid histogram is the q^2 distribution of $b \rightarrow ul\nu$, and the dashed histogram is the q^2 distribution of $b \rightarrow cl\nu$.

year	$\mathcal{L}_{\text{int}}(fb^{-1})$	m_{had}					q^2				
		S	B	$\delta V_{ub}^{\text{expt.}} (\%)$			S	B	$\delta V_{ub}^{\text{expt.}} (\%)$		
				stat.	sys.	tot.			stat.	sys.	tot.
2002	100	335	127	3.2	2.2	3.9	127	7	4.6	3.0	5.5
2005	500	1675	635	1.5	1.5	2.1	635	36	2.0	1.2	2.3
2010	2000	6700	2540	0.7	1.5	1.7	2538	144	1.0	1.2	1.6

Shipsey
and Lee

Exclusive Approaches to $|V_{ub}|$

Measure $BF(B \rightarrow \pi l \nu)$, $BF(B \rightarrow \rho l \nu)$ or $BF(B \rightarrow \omega l \nu)$.

With more statistics, can then measure $d\Gamma/dq^2$ ($B \rightarrow \pi l \nu$) or even form factors for $BF(B \rightarrow \rho l \nu)$.

A key experimental ingredient is the use of detector hermiticity to deduce the ν momentum

Variables for ν reconstruction of exclusive semileptonic decays (used for $B \rightarrow \pi (\rho) l \nu$)

$$p_{miss} = - \sum p_i$$

$$E_{miss} = 2 E_{beam} - \sum E_i$$

$$M_{miss}^2 = E_{miss}^2 - P_{miss}^2$$

$$p_\nu = (p_{miss}, |p_{miss}|)$$

$$\Delta E \equiv E_{beam} - (E_\pi + E_l + E_\nu)$$

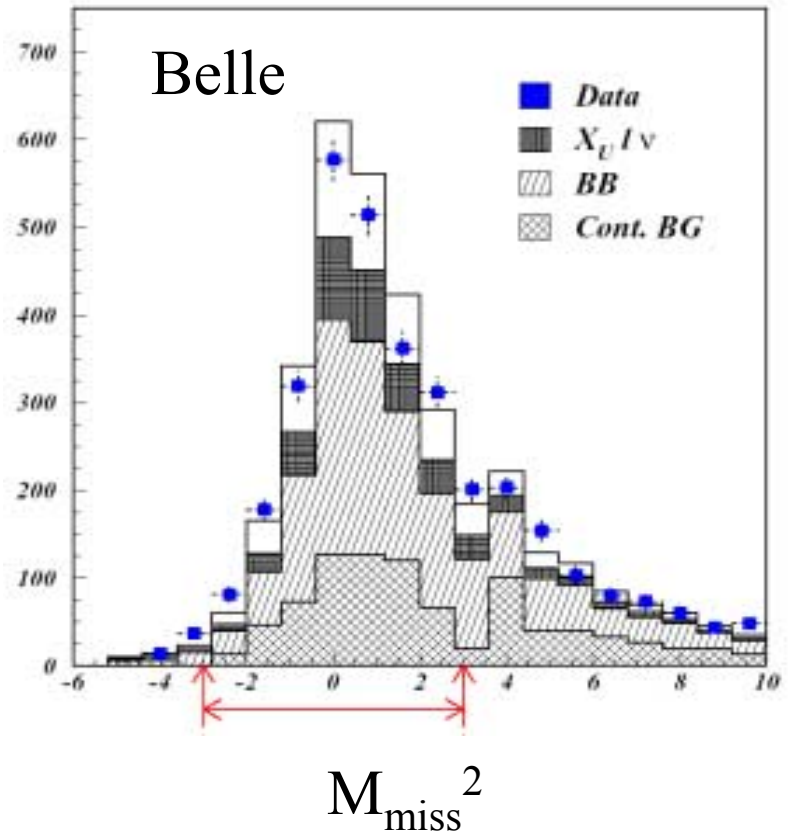
$$M_B \equiv \sqrt{E_{beam}^2 - |p_\pi + p_l + p_\nu|^2}$$

where $E_{beam} = 5.29 \text{ GeV}$

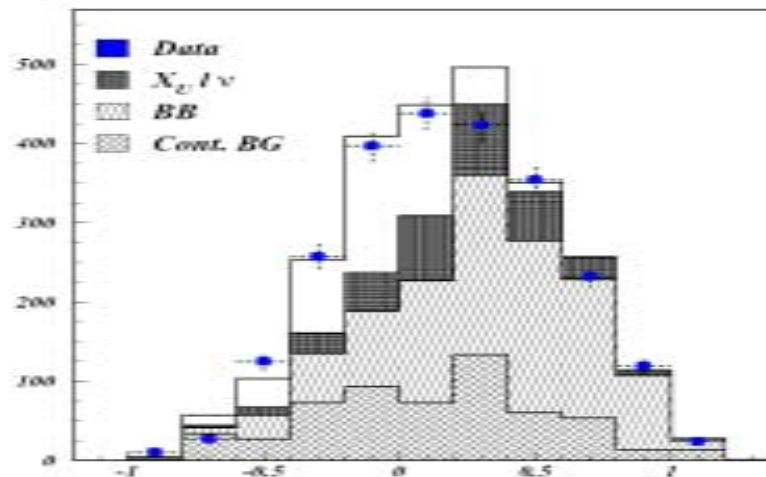
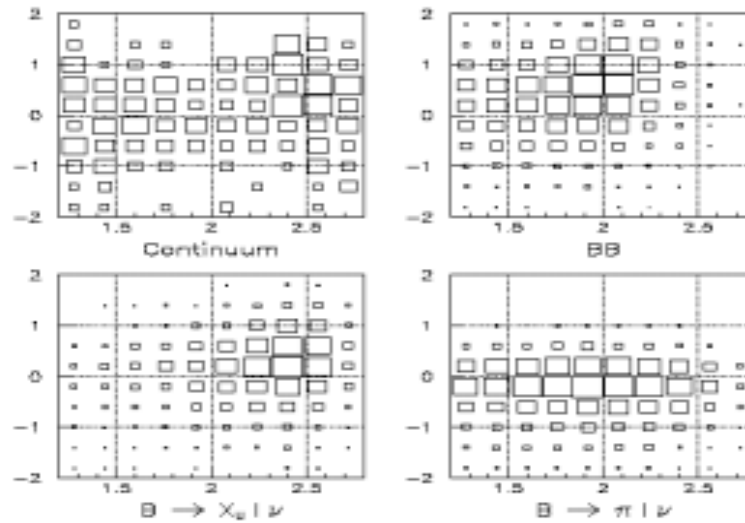
Detector hermiticity requirements (cont'd)

e.g. Only one lepton and
 $|Q_{\text{tot}}| = \pm 2$. Also require
 $|M_{\text{miss}}|^2 < 3.0 \text{ GeV}^2$

Fiducial cut on p_{miss} is
important at the B factories.
E.g. $170^\circ < \theta_{\text{miss}} < 150^\circ$



Belle: $B^0 \rightarrow \pi^+ l^- \nu$ signal



ΔE

Signal is extracted from a 2D fit to ΔE and p_L

Determination of $|V_{ub}|$ from $\text{BF}(B^0 \rightarrow \pi \ell \nu)$

Models or lattice calculations are needed to determine detection efficiency as well as convert the BF into a value of $|V_{ub}|$

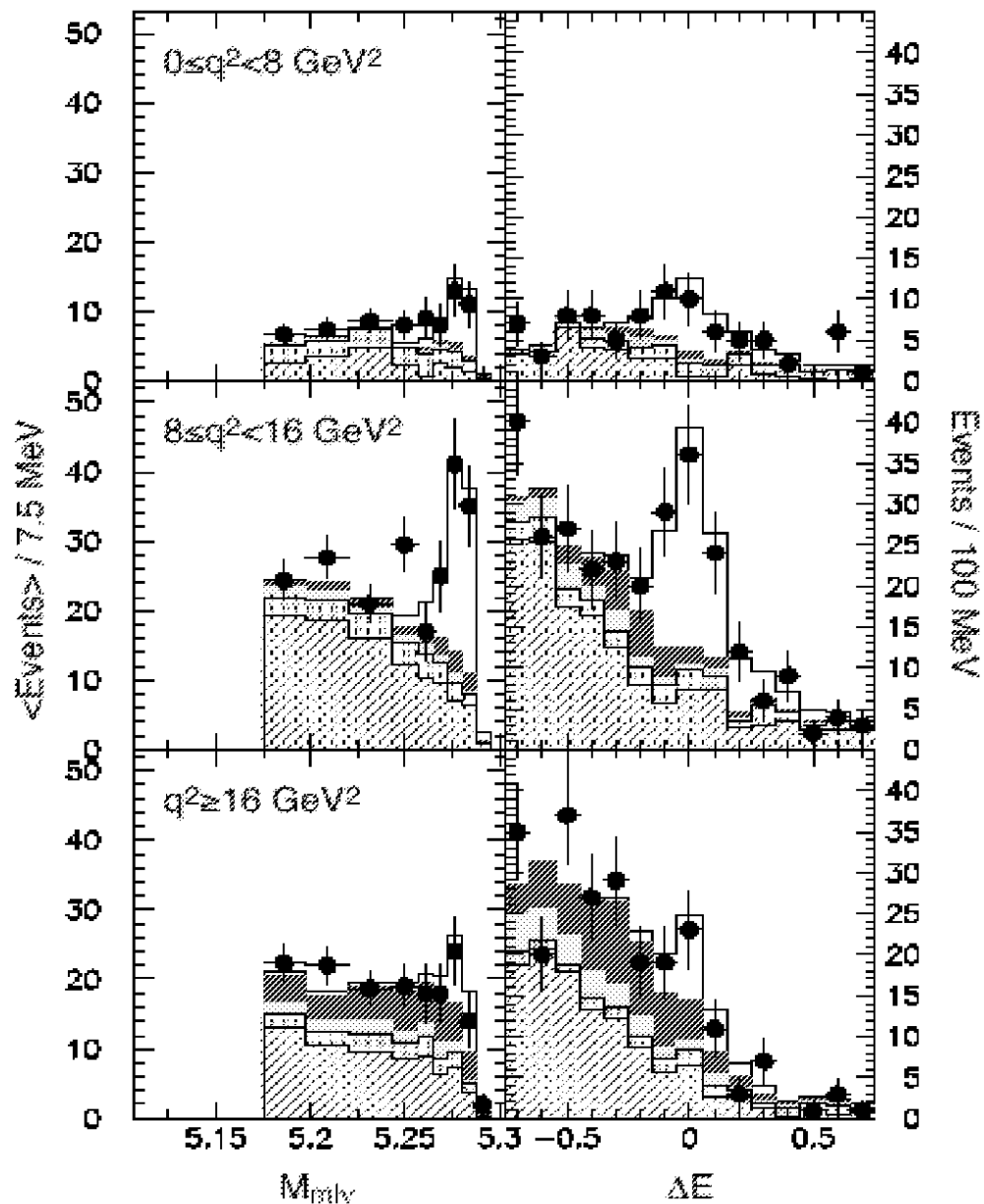
(Khodjamirian *et al.*)

model	UKQCD	LCSR
Reference	PLB 486, 111 (2000)	PRD 62, 114002 (2000)
good for	large q^2	small q^2
γ_π	9_{-2-2}^{+3+2}	7.3 ± 2.5
effi. (%)	2.9	3.1
$\mathcal{B}(B^0 \rightarrow \pi^- \ell^+ \nu_\ell)$	$(1.35 \pm 0.11 \pm 0.21) \times 10^{-4}$	$(1.31 \pm 0.11 \pm 0.20) \times 10^{-4}$
$ V_{ub} $	$(3.11 \pm 0.13 \pm 0.24 \pm 0.56) \times 10^{-3}$	$(3.58 \pm 0.15 \pm 0.28 \pm 0.63) \times 10^{-3}$



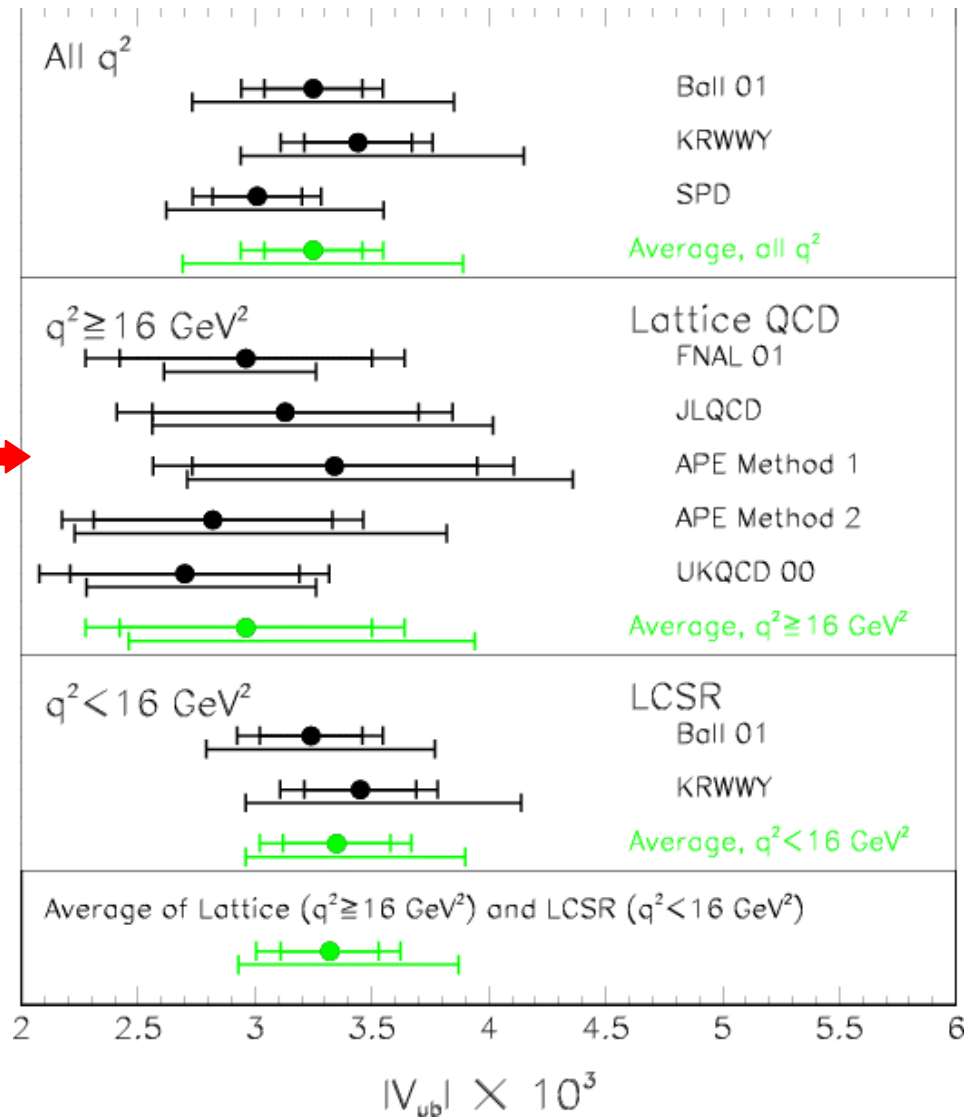
CLEO 2002:

$B^0 \rightarrow \pi^+ l^- \nu$ signal in bins of q^2 .



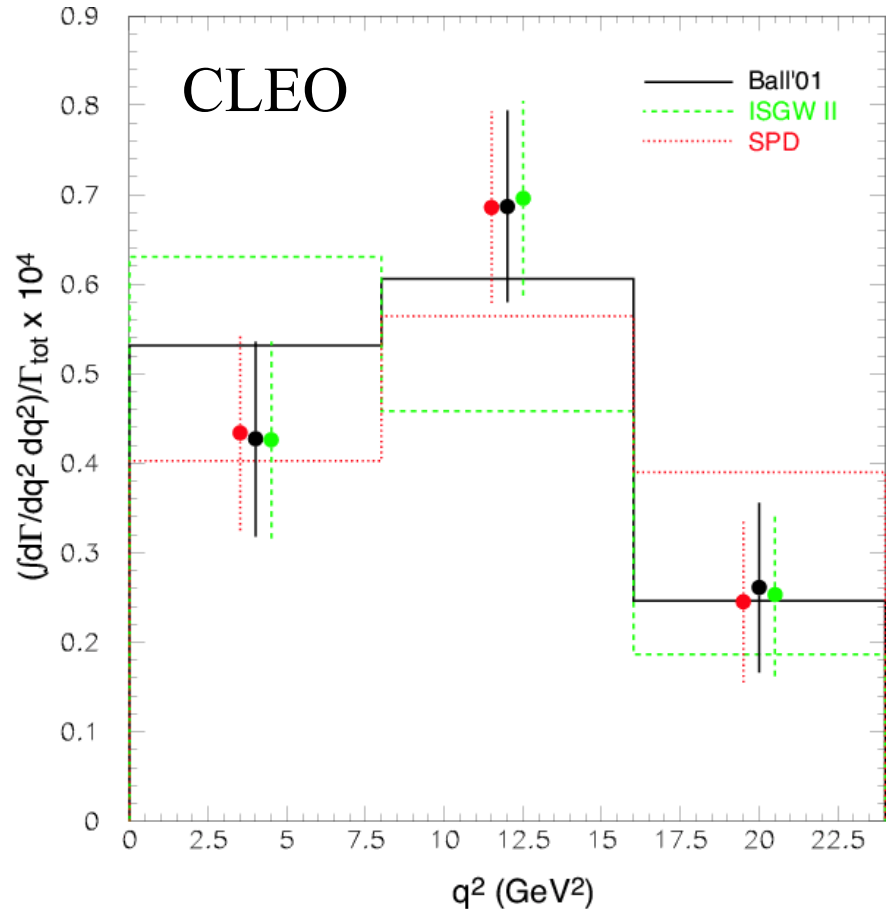
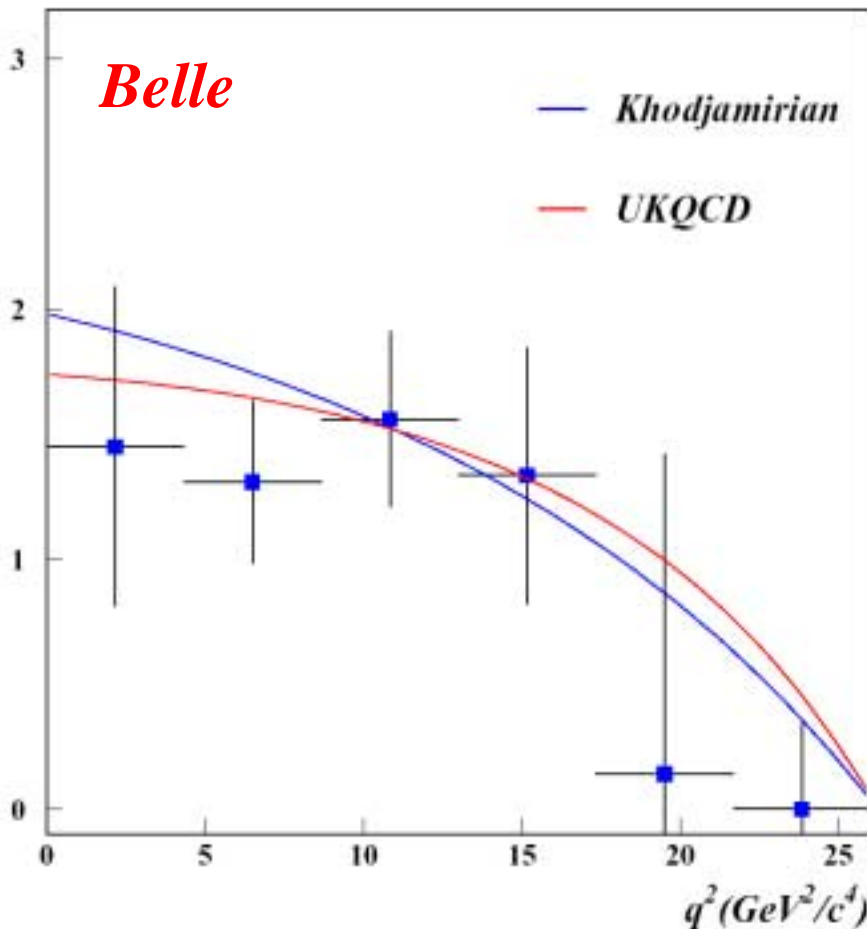
CLEO: Determination of $|V_{ub}|$ from $\text{BF}(B^0 \rightarrow \pi l \nu)$

Large errors →



q^2 distribution of $B \rightarrow \pi l \nu$

$$d\Gamma/dq^2 (/10^2 \text{ ns}^{-1} / 4.3 \text{ GeV}^2 / c^4)$$

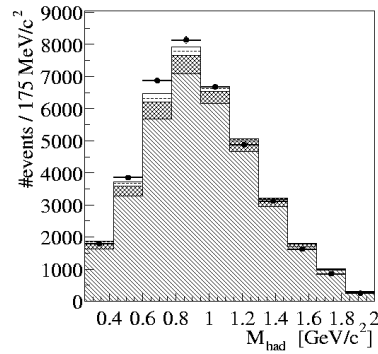


Find prob(ISGWII) $\sim 1\%$

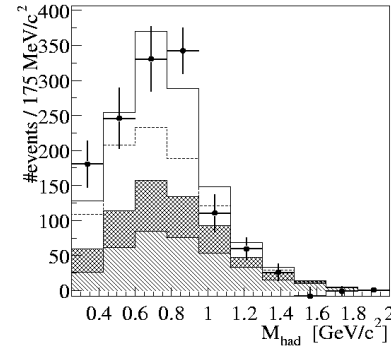
BABAR $B \rightarrow \rho^{0(+)} 1 \nu$ signal

LOLEP

$2.0 < p_L < 2.3$ GeV



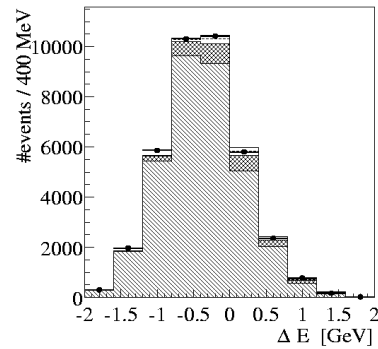
(a) $M_{\pi\pi}$ (LOLEP)



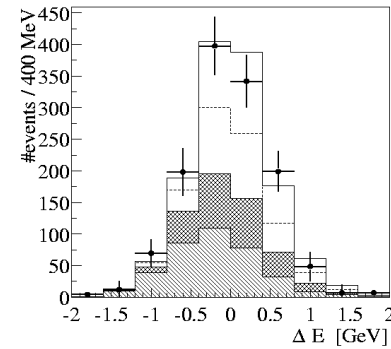
(b) $M_{\pi\pi}$ (HILEP)

HILEP

$2.3 < p_L < 2.7$ GeV



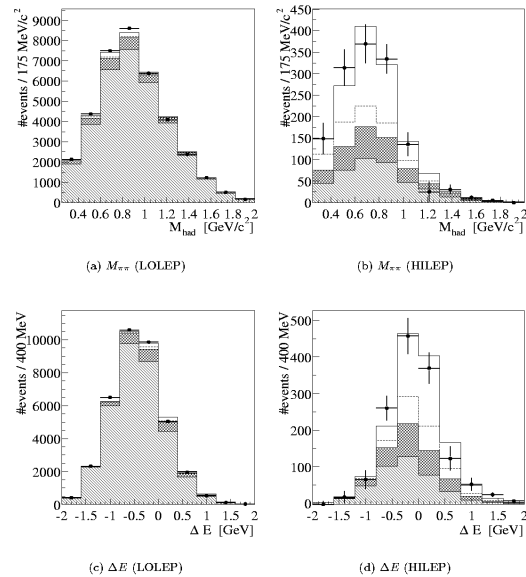
(c) ΔE (LOLEP)



(d) ΔE (HILEP)

Figure 3: Continuum-subtracted projections of the ISGW2 fit result for the $B^+ \rightarrow \rho^{0+} e^+$ channels in the LOLEP and HILEP electron energy regions; the contributions are the direct and crossfeed components of the signal (unhatched region, above and below the dashed line respectively); the background from $b \rightarrow ue\nu$ other than $B \rightarrow \rho e\nu$ and $B \rightarrow \omega e\nu$ modes (double hatched region); the background from $b \rightarrow ce\nu$ and other backgrounds (single-hatched region)

BABAR $B \rightarrow \rho^{0(+)} l \nu$ signal



LOLEP

$2.0 < p_L < 2.3$ GeV

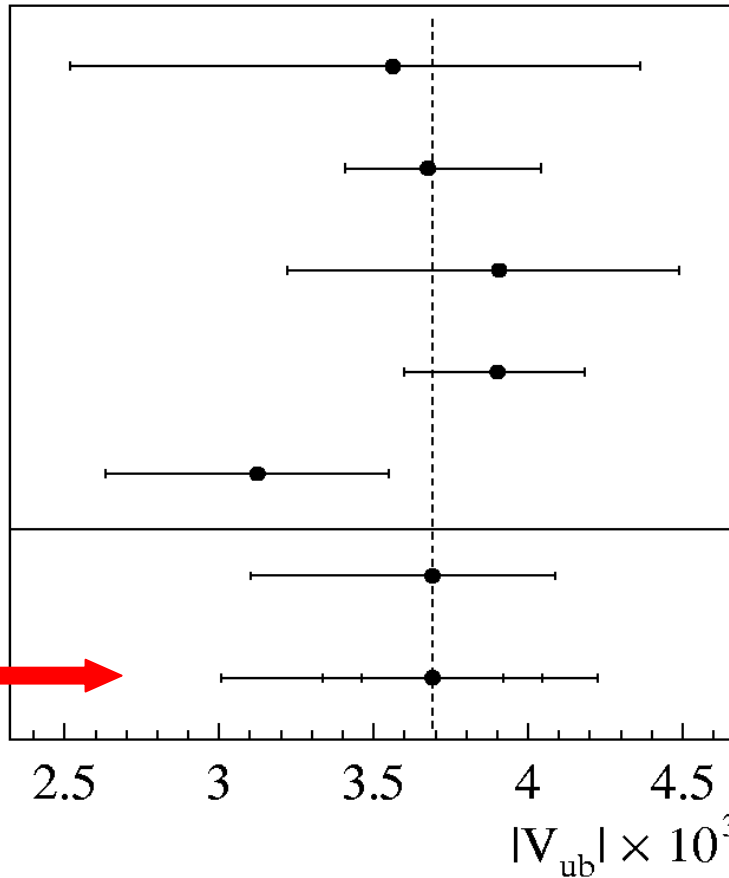
HILEP

$2.3 < p_L < 2.7$ GeV

Table 2: Summary of data yields for the $B^0 \rightarrow \rho^- e^+ \nu$ and $B^+ \rightarrow \rho^0 e^+ \nu$ modes with electron energies between 2.3 and 2.7 GeV (HILEP), and between 2.0 and 2.3 GeV (LOLEP). The yields presented in this table were obtained using the ISGW2 form-factor. The downfeed background includes all $B \rightarrow X_u e \nu$ modes except for ρ , ω , and π . The crossfeed signal contribution corresponds to events from the other signal modes with ρ^0 , ω , or π and is constrained to the signal in the fit. All errors are statistical only.

	$B^0 \rightarrow \rho^- e^+ \nu$		$B^+ \rightarrow \rho^0 e^+ \nu$	
	HILEP	LOLEP	HILEP	LOLEP
On-resonance yield	2302	39349	2213	40155
Direct signal	510 ± 63	718 ± 89	324 ± 40	440 ± 55
Crossfeed signal	262 ± 32	538 ± 73	363 ± 42	725 ± 86
Downfeed	203 ± 55	2278 ± 403	226 ± 92	2435 ± 430
$b \rightarrow ce\nu$	414 ± 5	33859 ± 438	367 ± 5	34366 ± 458
$e^+ e^- \rightarrow q\bar{q}$	917 ± 73	1928 ± 106	912 ± 73	2063 ± 110
Fake electrons	12 ± 3	80 ± 9	18 ± 4	76 ± 9

Model dependence in $|V_{ub}|$ BABAR $B \rightarrow \rho l \nu$ signal



ISGW2:
 $3.56 \pm 0.22 \pm 0.27$ $^{+0.80}_{-1.04}$

UKQCD:
 $3.68 \pm 0.23 \pm 0.27$ $^{+0.37}_{-0.27}$

LCSR:
 $3.91 \pm 0.25 \pm 0.29$ $^{+0.58}_{-0.68}$

Beyer/Melikhov:
 $3.90 \pm 0.24 \pm 0.29$ $^{+0.28}_{-0.30}$

Ligeti/Wise:
 $3.12 \pm 0.21 \pm 0.23$ $^{+0.42}_{-0.49}$

Combined:
 $3.69 \pm 0.23 \pm 0.27$ $^{+0.40}_{-0.59}$

Includes spread
in models

Does it make sense to take the average of models ?

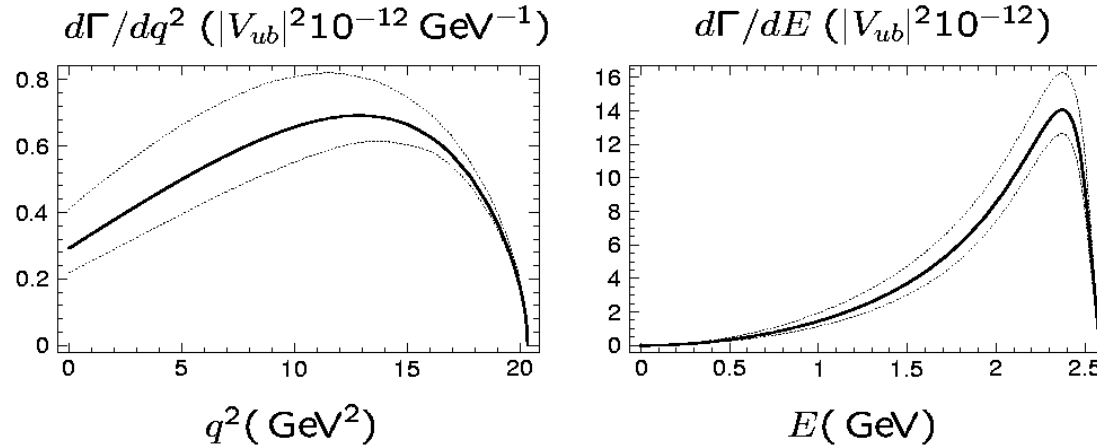
How can we improve our knowledge of V_{ub} from exclusive decays ?

A considerable amount of model dependence is due to FF uncertainties.

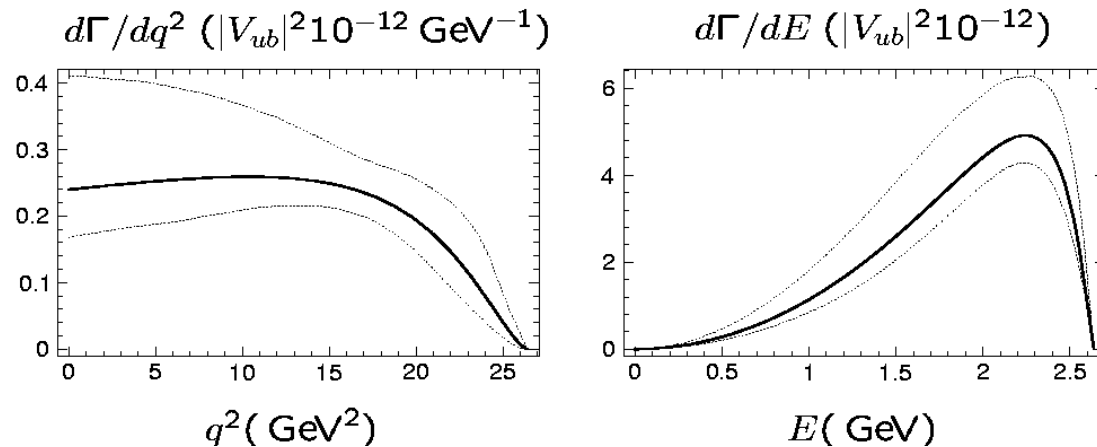
$$\boxed{\bar{B}^0 \rightarrow \rho^+ l^- \bar{\nu}_l}$$

Examples:

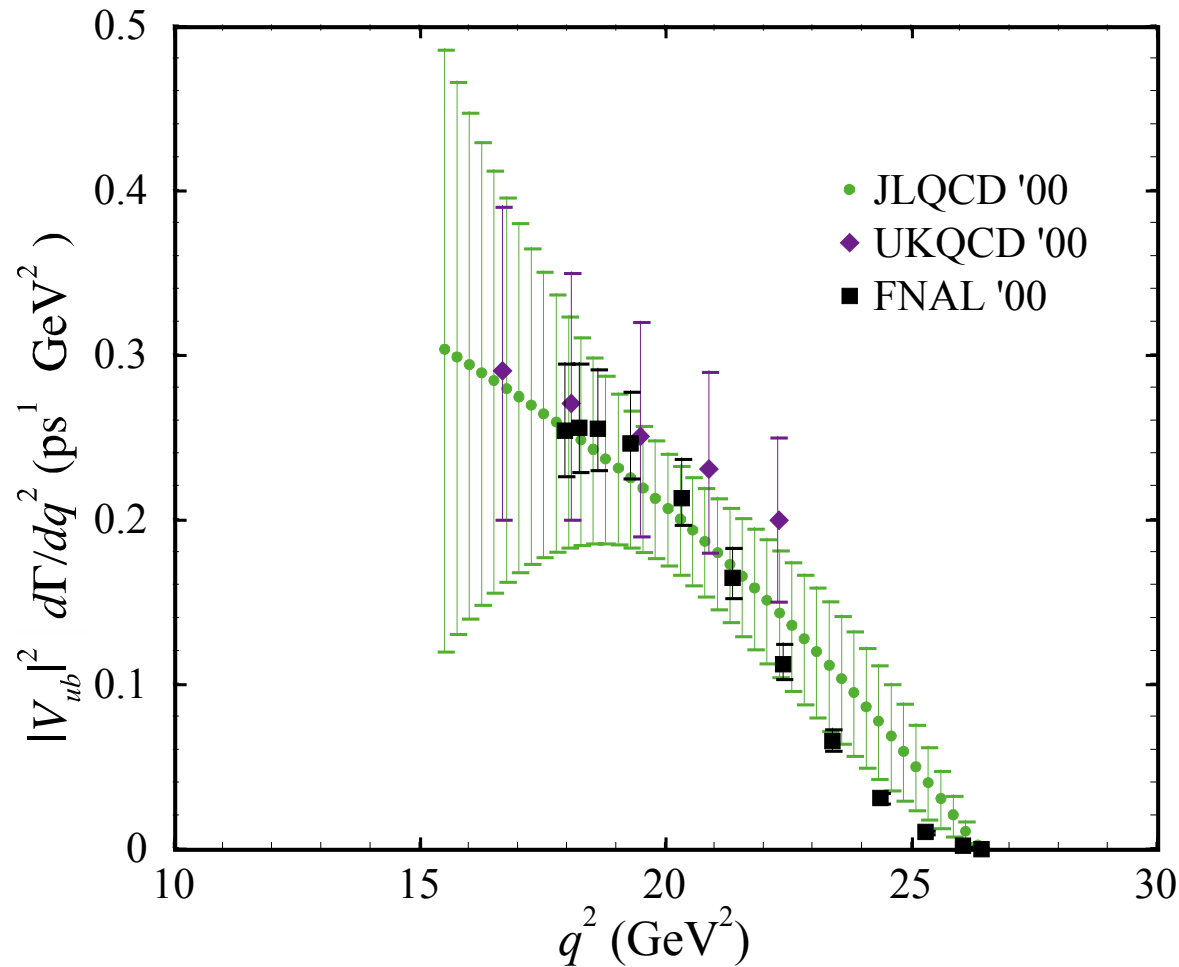
J. Flynn



$$\boxed{\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}_l}$$



Lattice Calculations of $B \rightarrow \pi l \nu$ Form Factor



(from A. Kronfeld, hep-ph/0010074)

Need to measure $d\Gamma/dq^2$ for $B \rightarrow \pi l \nu$ at high q^2 /low p_π

Future Improvements in $|V_{ub}|$ from the Lattice

$$|V_{ub}|^2 = \frac{12\pi^2}{G_F^2 m_B} \boxed{T_B(p_{\min}, p_{\max})} \int_{p_{\min}}^{p_{\max}} dp \frac{d\Gamma_{B \rightarrow \pi \ell \nu}}{dp}$$

$$T_B(0.4 \text{ GeV}, 1.0 \text{ GeV}) = 0.55^{+0.15}_{-0.05} \text{ }^{+0.09}_{-0.12} \text{ }^{+0.09}_{-0.02} \pm .06 \pm .09 \text{ GeV}^4$$

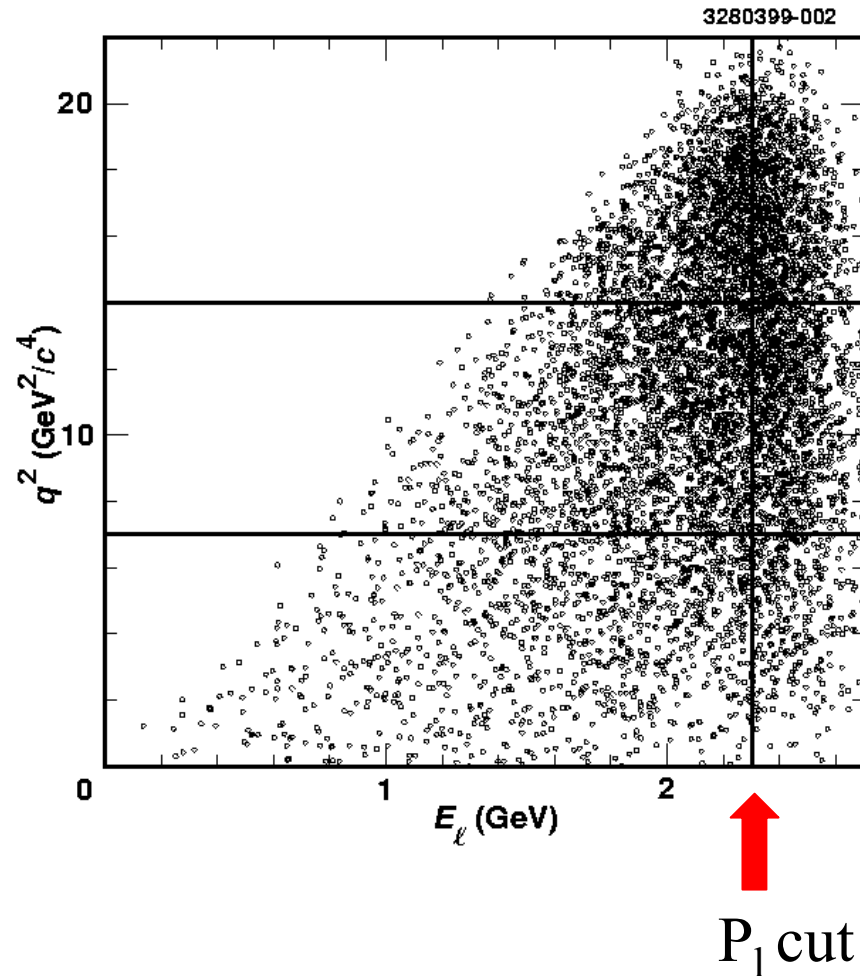
statistical chiral extrapolation lattice spacing matching misc. (lattice units, ...)

$\Delta V_{ub} \approx 15-18\% + \text{quenching error}$

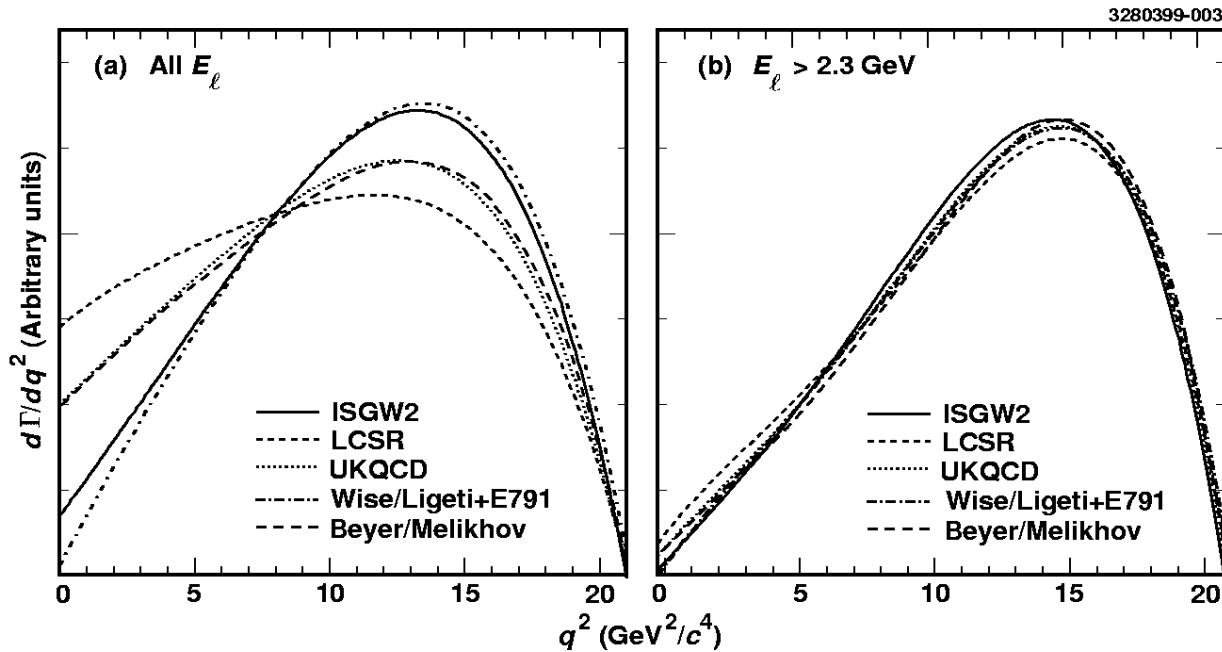
(A. El-Khadra et. al., PRD64, 014502)

To understand these errors: see Lectures by P. Lepage

MC simulation of the $B \rightarrow \rho l \nu$ Dalitz plot



Model dependence in $B \rightarrow \rho l \nu$ form factors



A tight p_L cut makes it difficult to distinguish models.

FF model	$\tilde{\Gamma}_{\text{thy}}$ (ps^{-1})	$\Gamma(E_\ell > 2.3 \text{ GeV})/\Gamma$ (%)	$\Gamma(2.0 < E_\ell < 2.3 \text{ GeV})/\Gamma$ (%)
ISGW2	14.2	35	33
LCSR	16.9	24	28
UKQCD	16.5	27	30
Wise/Ligeti+E791	19.4	31	34
Beyer/Melikhov	16.0	27	30

Model dependence of $B \rightarrow \rho l \nu$ form factors

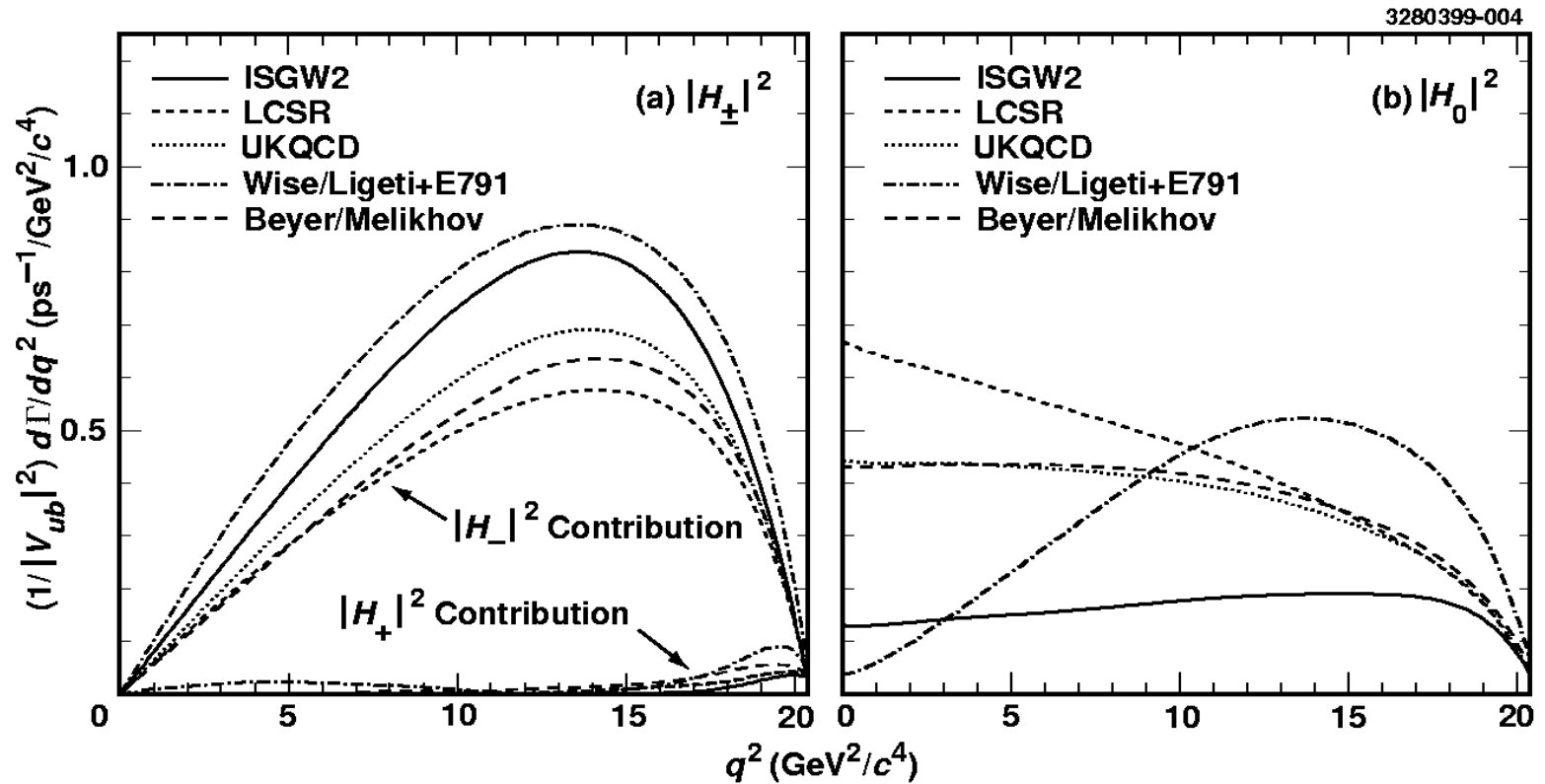
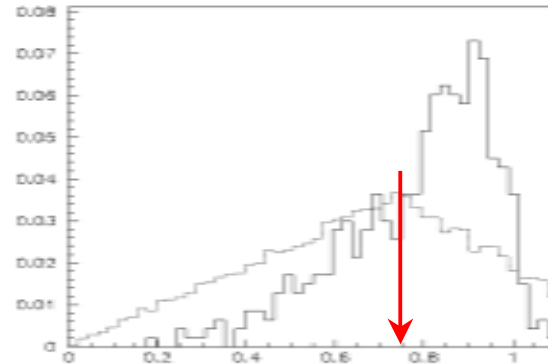


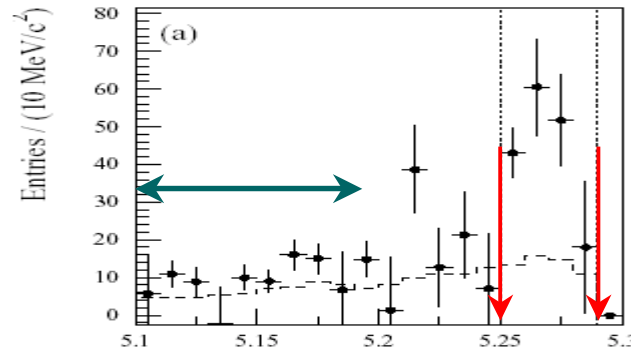
FIG. 4. $d\Gamma/dq^2$ distributions for each of the three terms in Eq. 9: (a) the terms proportional to $|H_-|^2$ and $|H_+|^2$ and (b) the $|H_0|^2$ term.

BELLE: $B^0 \rightarrow \omega e^+ \nu$ signal selection

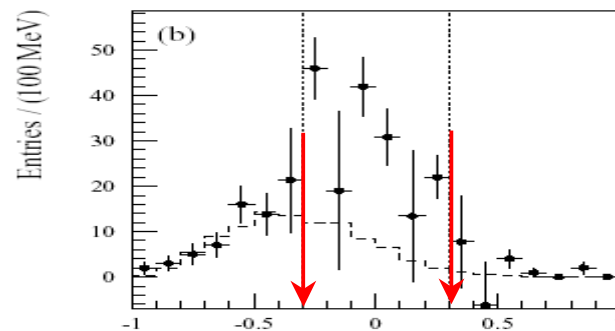
Lattice calcs of $B \rightarrow \rho$ FFs cannot handle the finite width of the ρ



$$|P_{\pi^+} \times P_{\pi^-}|$$



$$M_B$$



$$\Delta E$$

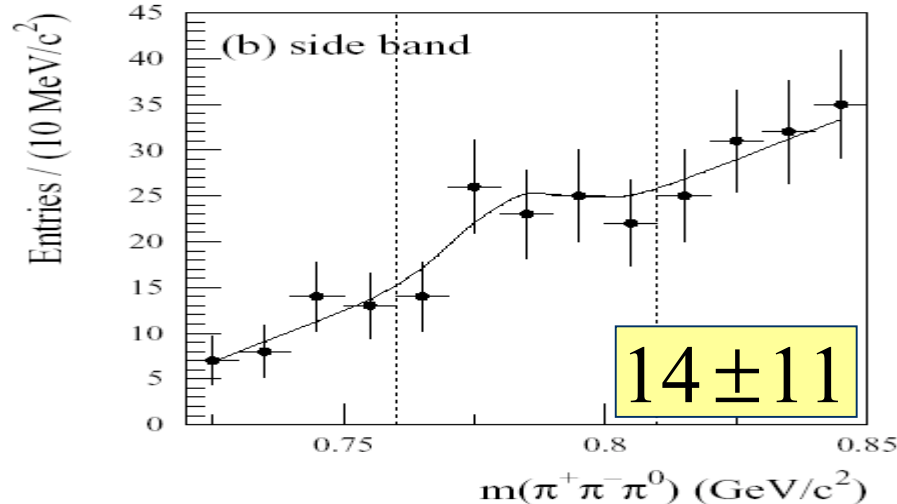
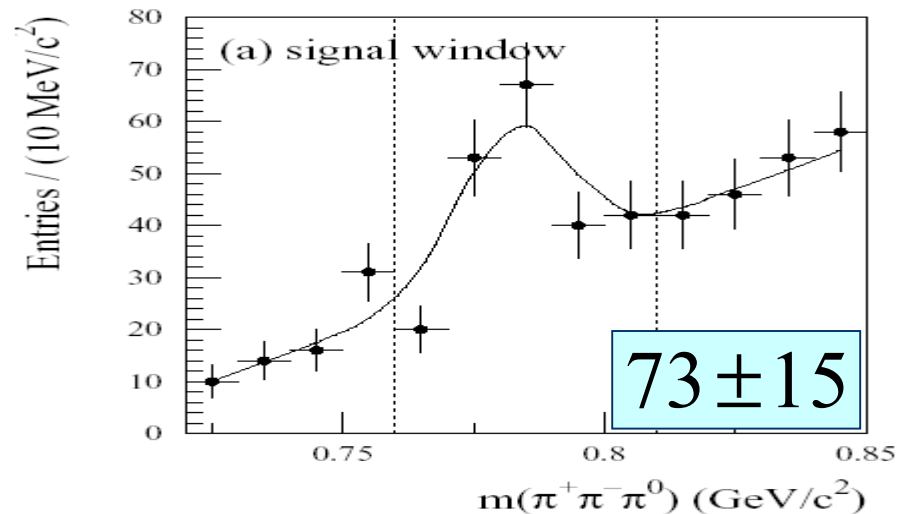
Less exp problem with $B \rightarrow \pi\pi 1 \nu$

BELLE: $B^0 \rightarrow \omega e^+ \nu$ signal

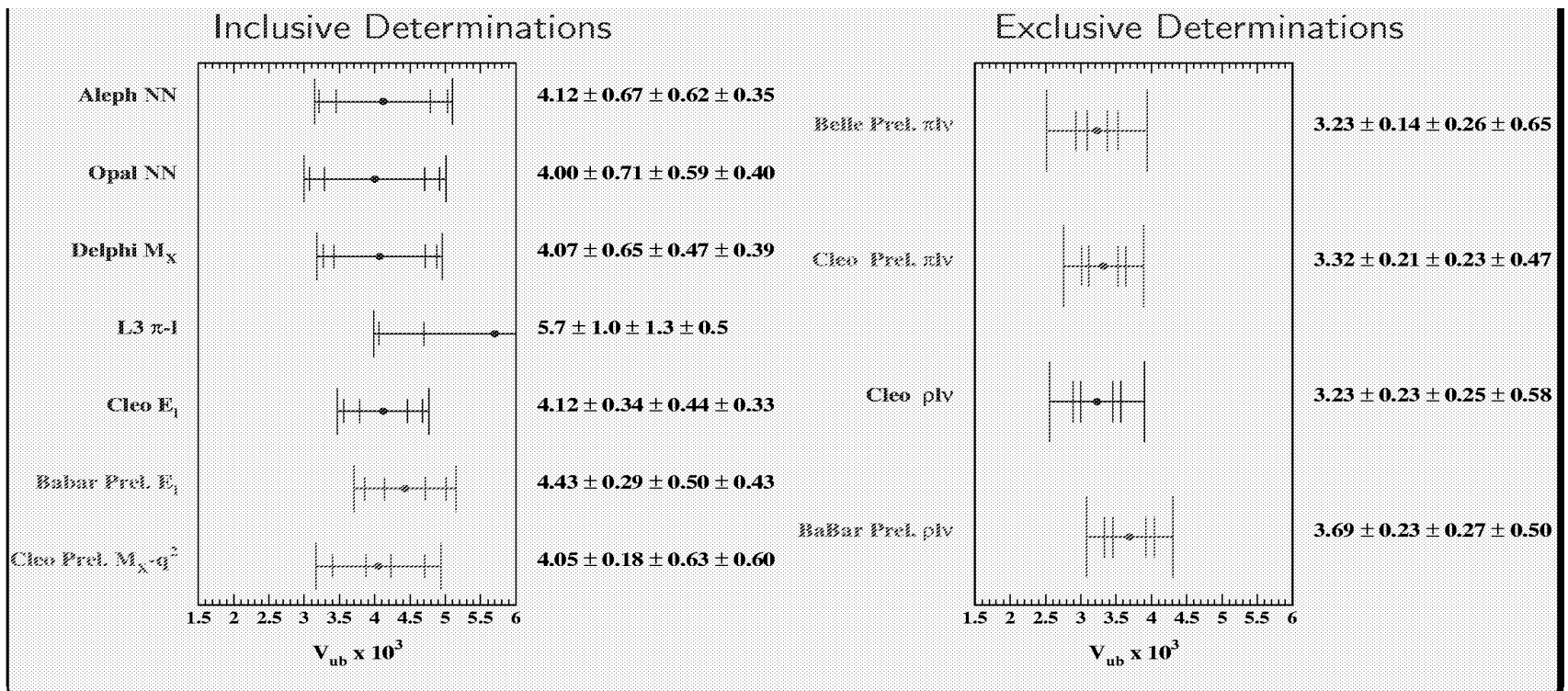
- N(events) in the signal region
with $0.76 < m(3\pi) < 0.81$

222 ± 15 (total)	} MC est.
48 ± 10 ($b \rightarrow c$)	
2 ± 2 (fake)	
47 ± 21 (cont.)	

- Excess in $m(3\pi)$
after side-band subtraction
= 59 ± 15 events



Summary of recent $|V_{ub}|$ determinations



Review by
Battaglia

Conclusions

An improved method for $|V_{ub}|$ determination using leptons in the endpoint region has been introduced. The uncertainty in the extrapolation is reduced by using the shape function measured in $b \rightarrow s \gamma$.

An inclusive method using optimized cuts on q^2 and M_X appears promising.

Prospects for improved $|V_{ub}|$ in $B \rightarrow \pi l \nu$ using high statistics measurements of $d\Gamma/dq^2$ and FFs determined from the lattice appear good.