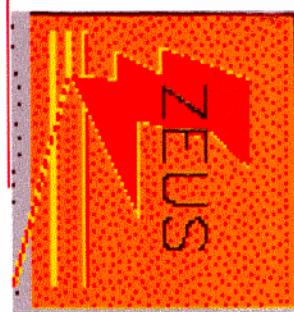


# Recent QCD results from HERA

J.J. Engelen (NIKHEF-Amsterdam)

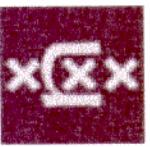
(for the H1 and ZEUS collaborations)



- Proton Structure Functions and Scaling Violations
  - $F_2$  (including reference to possible manifestation of non-pert. physics)
  - $F_2$  charm
- Diffractive deep inelastic scattering (very briefly)
- $\alpha_S$  measurement from jet rates and from scaling violations
- Photoproduction
- NC and CC cross sections and structure functions up to very high  $Q^2$

---

SLAC Summer Institute, Topical Conference, August 23-25, 2000



**HERA**:  $e^+$  p collider,  $27.5 \times 820$  ( $920$ ) GeV  
Instantaneous luminosity  $\sim 1.5 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$

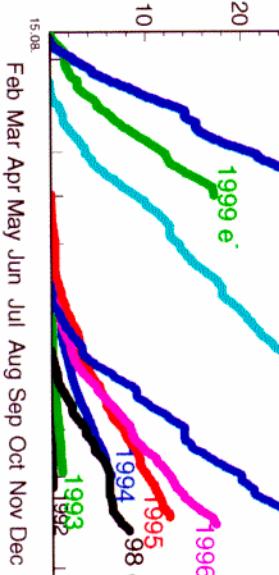
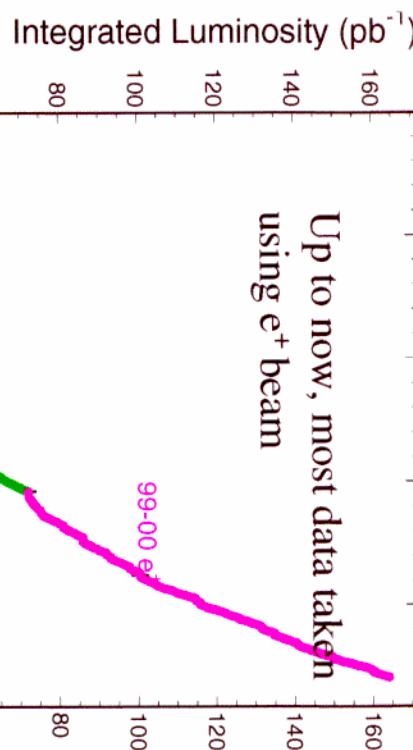
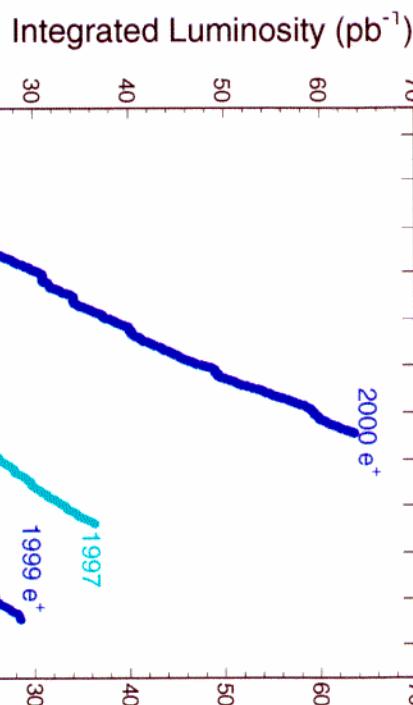
## Two 'general purpose' colliding beam experiments: **H1, ZEUS**

- One fixed target experiment, using polarized electron beam (Hermes)
- One fixed target experiment using proton beam (HERA-B)

HERA luminosity 1992 – 2000

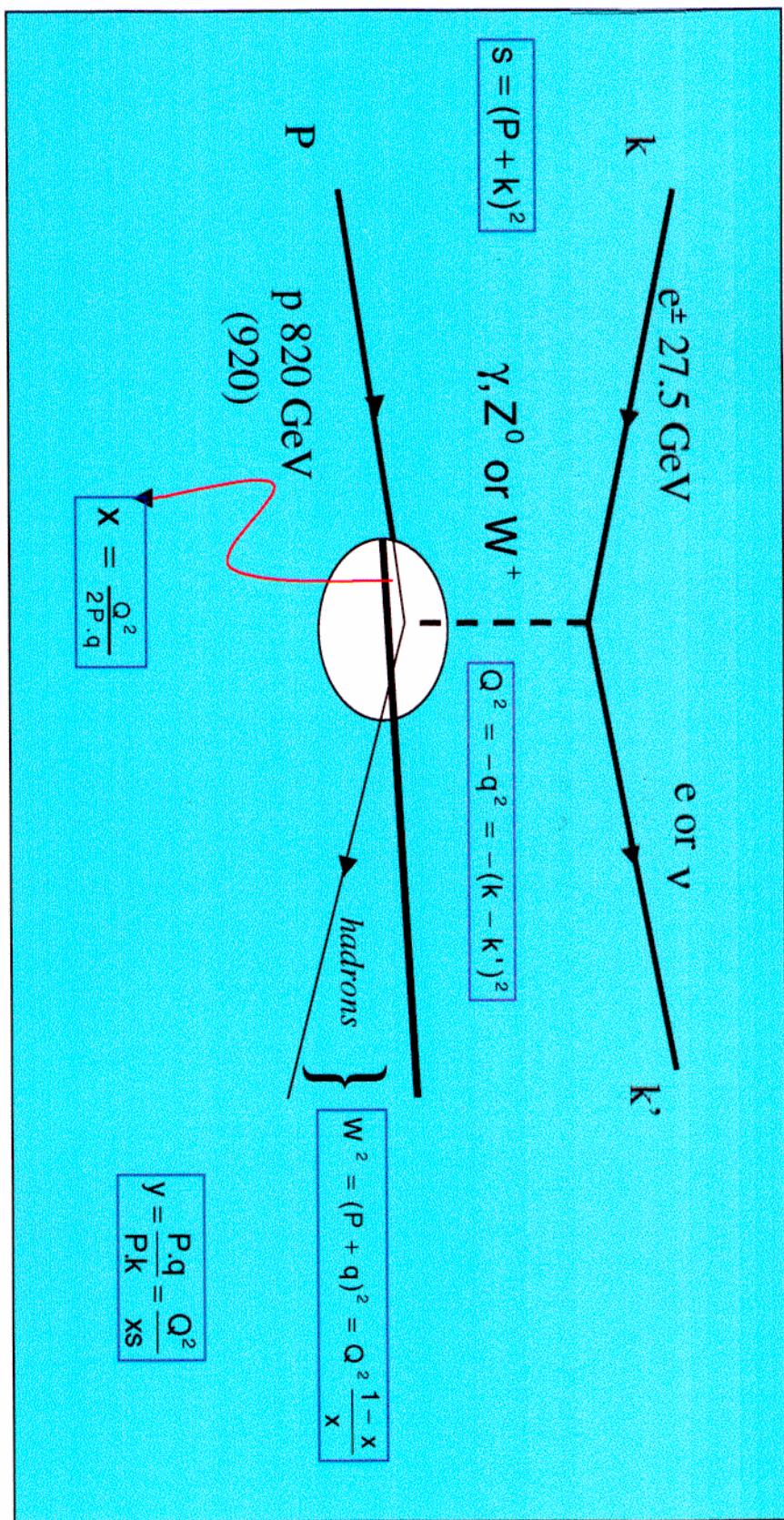
HERA luminosity 1994 – 2000

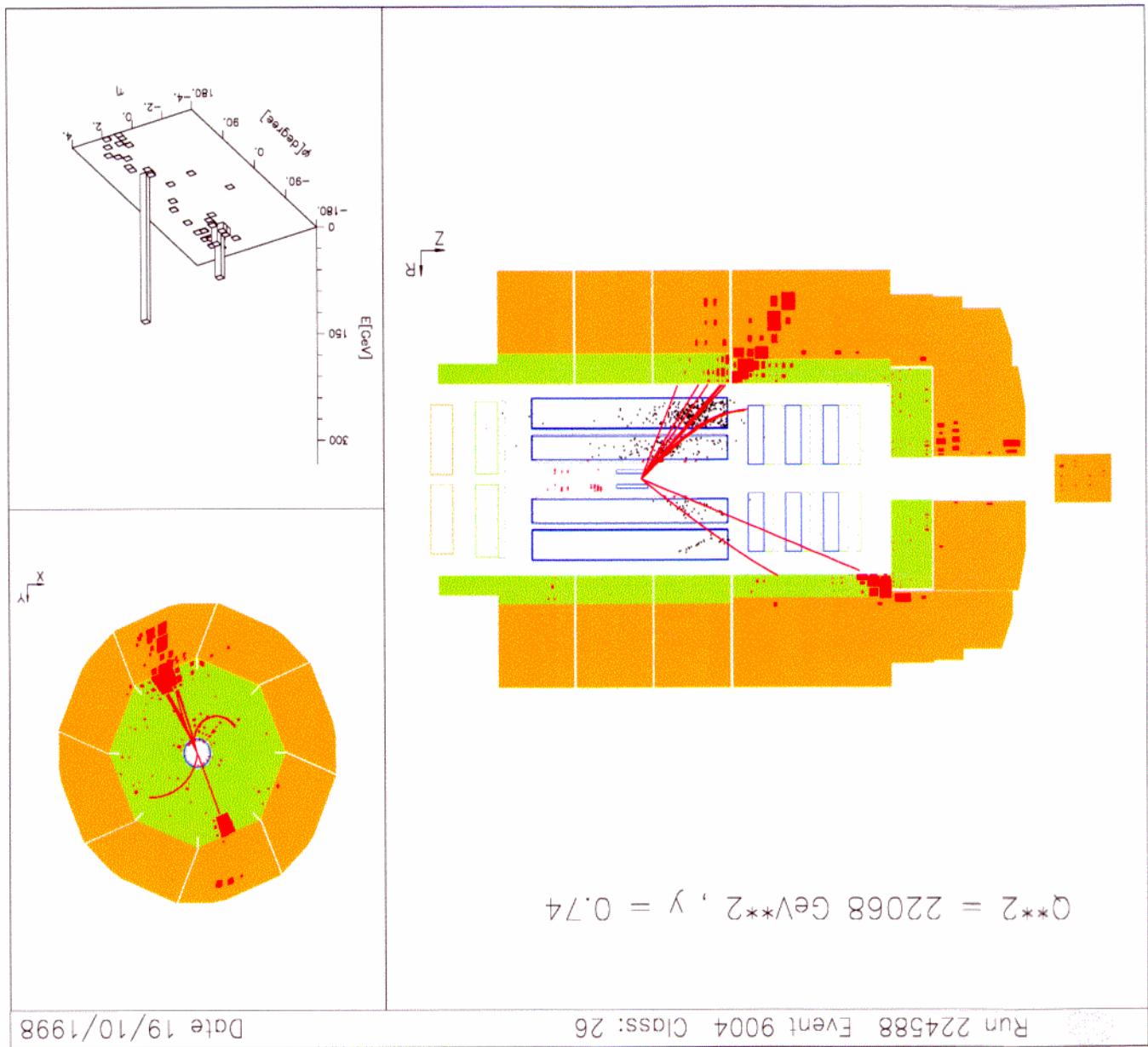
Up to now, most data taken  
using  $e^+$  beam

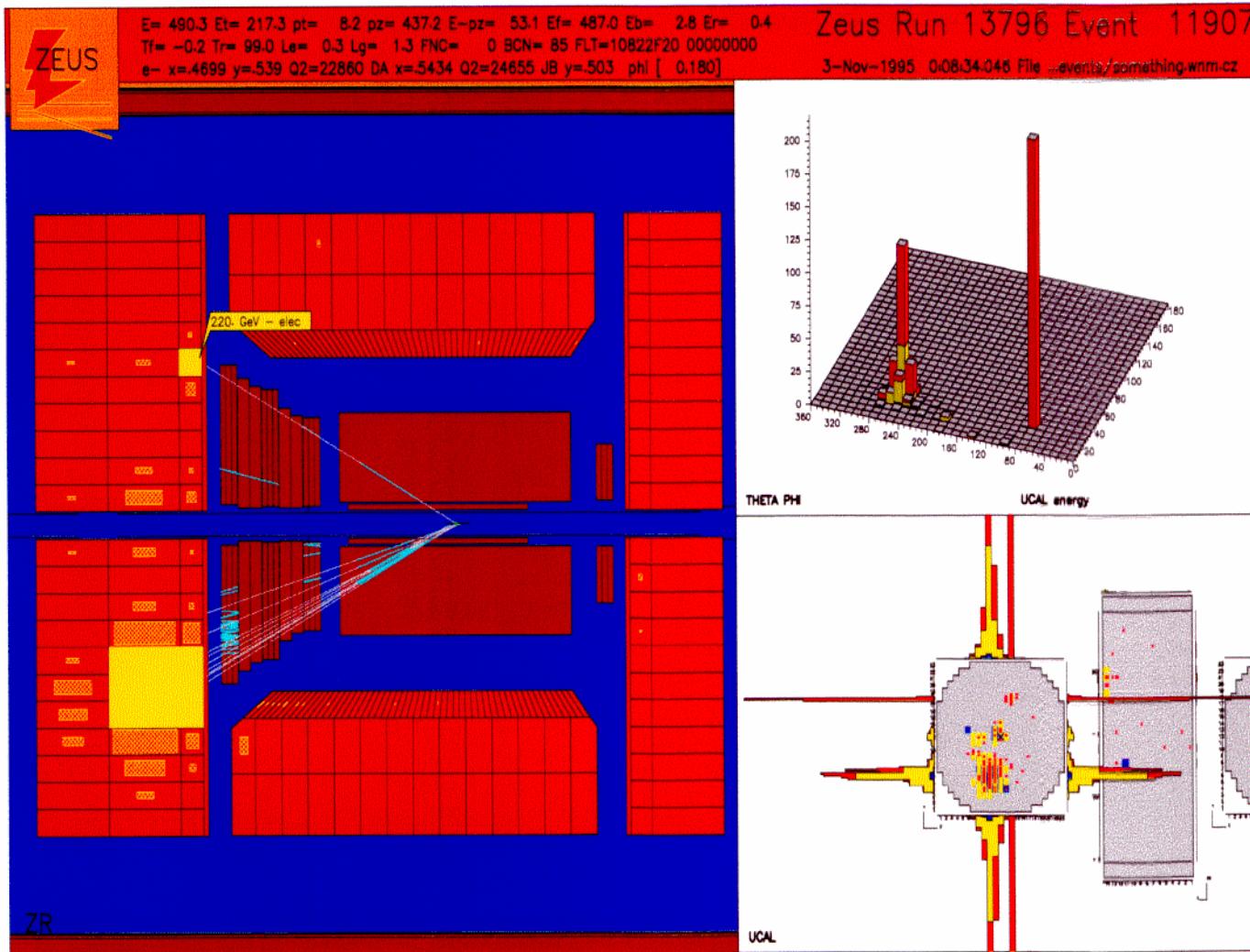


Days of running

- Structure Functions  $F_i(x, Q^2)$ :  $Q^2$  evolution described by pert. QCD
- Hadronic final state: governed by hard (#jets) and soft QCD (hadronization)
- $Q^2 \sim 0$ : photoproduction; if hard scale present ( $p_T, m_Q$ ): pert. QCD
- Hard ( $Q^2 \gg 1 \text{ GeV}^2$ ) diffraction







Neutral current  $e^+p$  scattering:

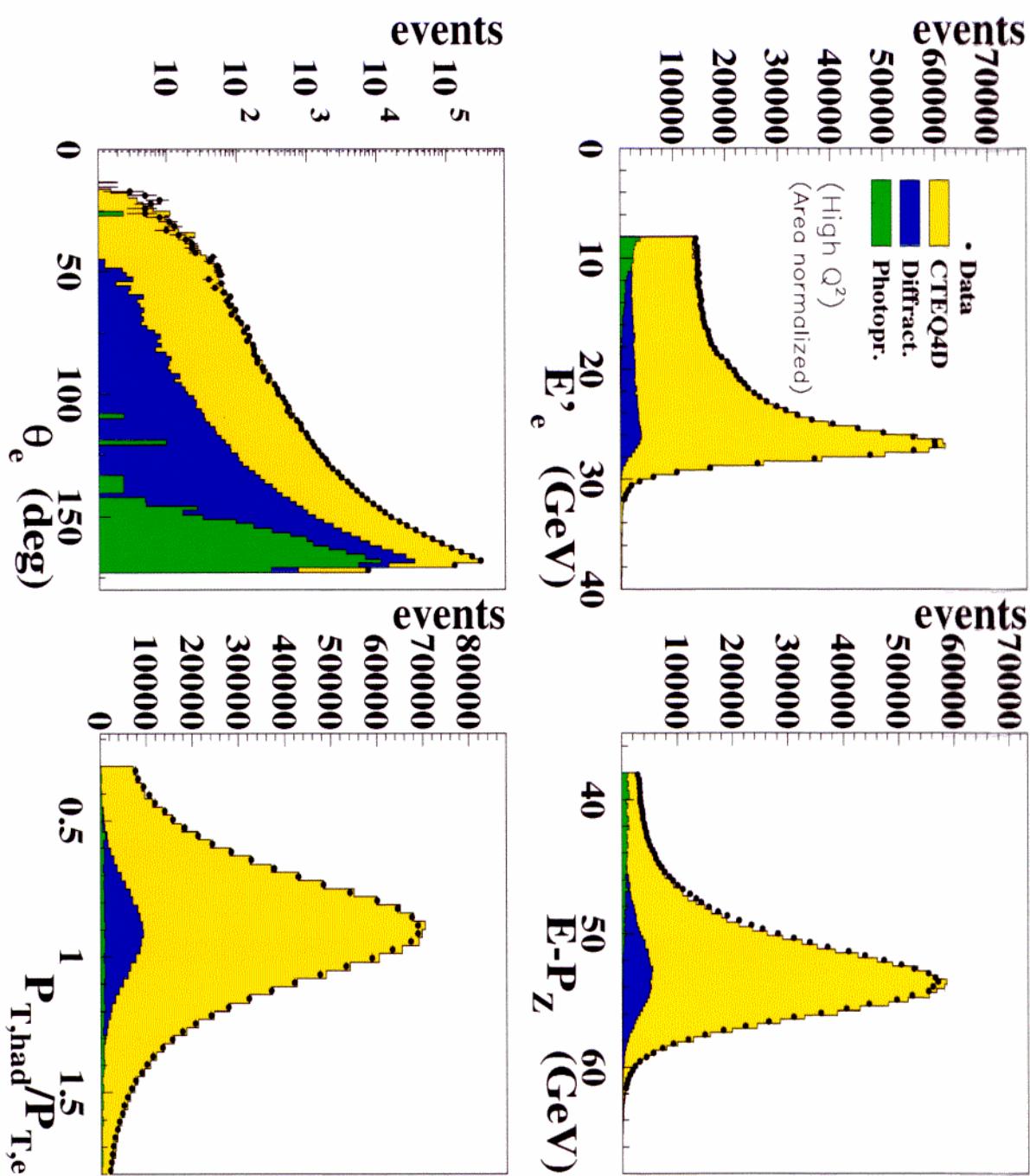
$$\frac{d^2\sigma}{dxdQ^2} = \frac{2\pi\alpha^2}{xQ^4} [Y_+F_2(x,Q^2) - y^2F_L(x,Q^2) - Y_-xF_3(x,Q^2)](1 + \delta_r(x,Q^2))$$

$$Y_{\pm} = 1 \pm (1-y)^2$$

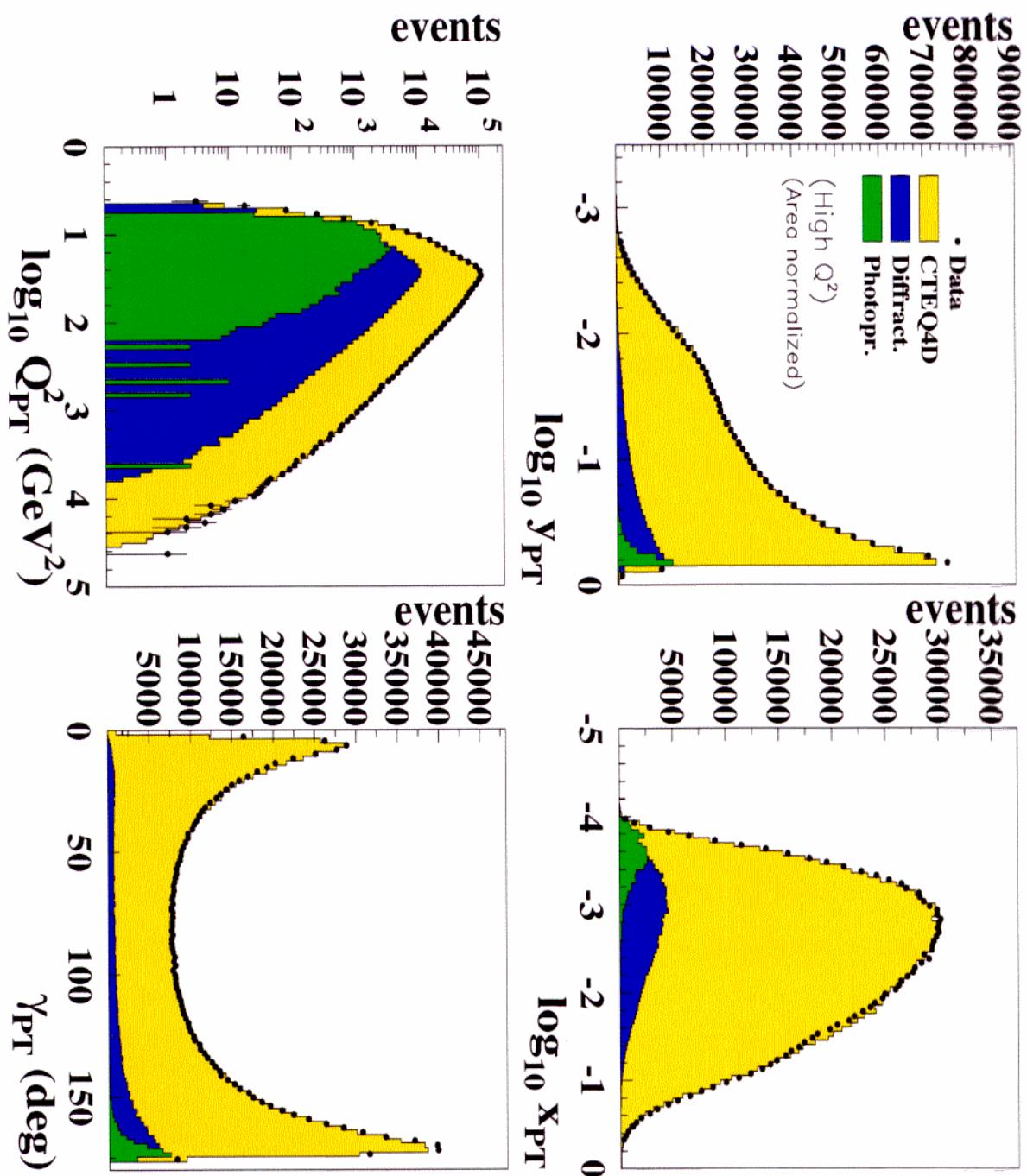
$$F_2 = F_2^{em} + \frac{Q^2}{(Q^2 + M_Z^2)} F_2^{\text{int}} + \frac{Q^4}{(Q^2 + M_Z^2)^2} F_2^{\text{wk}} = F_2^{em}(1 + \delta_Z)$$

$$\frac{d^2\sigma}{dxdQ^2} = \frac{2\pi\alpha^2 Y_+}{xQ^4} F_2^{em} (1 + \delta_z)(1 - \delta_L - \delta_3)(1 + \delta_r)$$

# ZEUS Preliminary 1996-97



# ZEUS Preliminary 1996-97



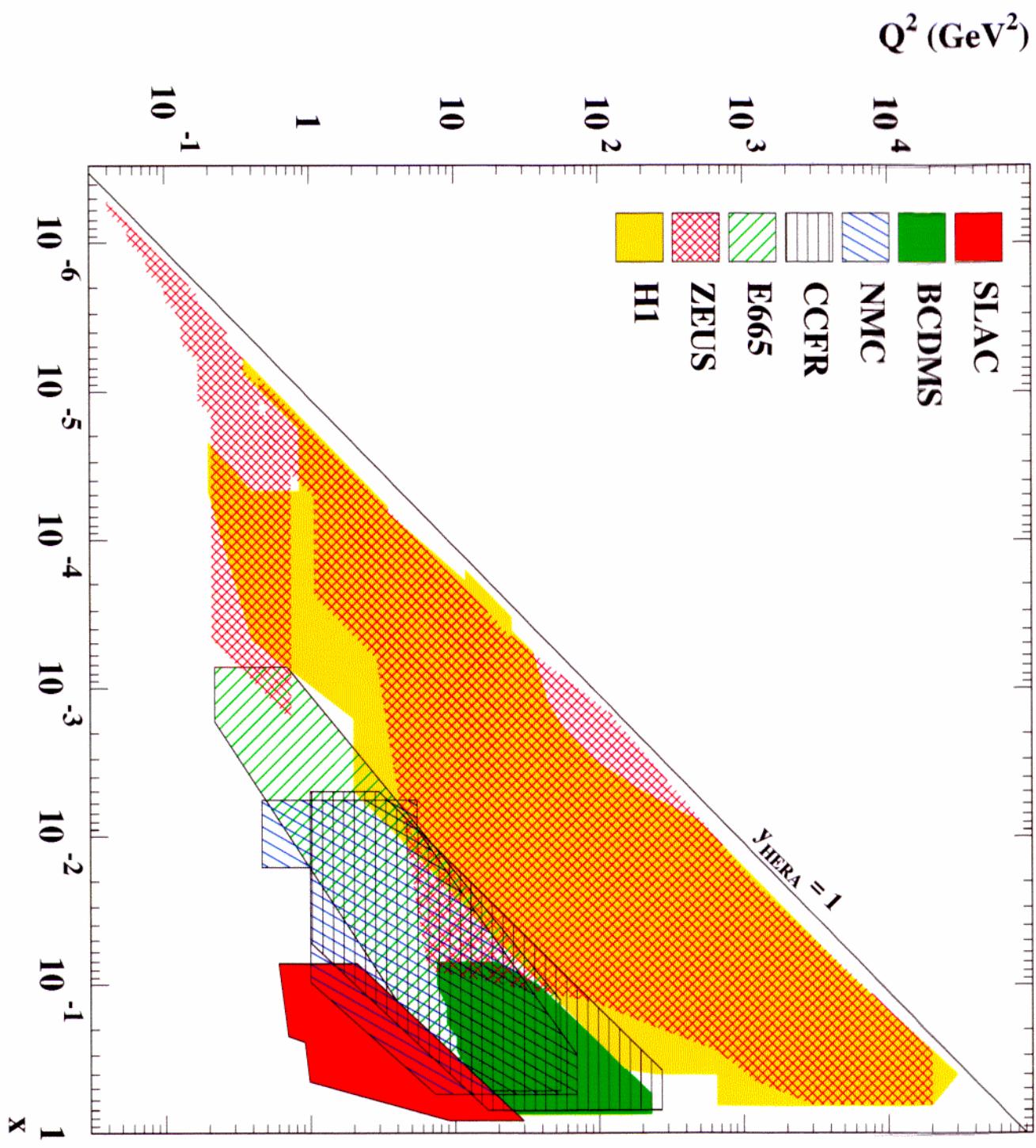
The DGLAP equations govern the  $Q^2$  evolution of the structure functions:

$$Q^2 \frac{\partial F^{NS}}{\partial Q^2} = \frac{\alpha_s(\ln Q^2)}{2\pi} P^{qq} * F^{NS}$$

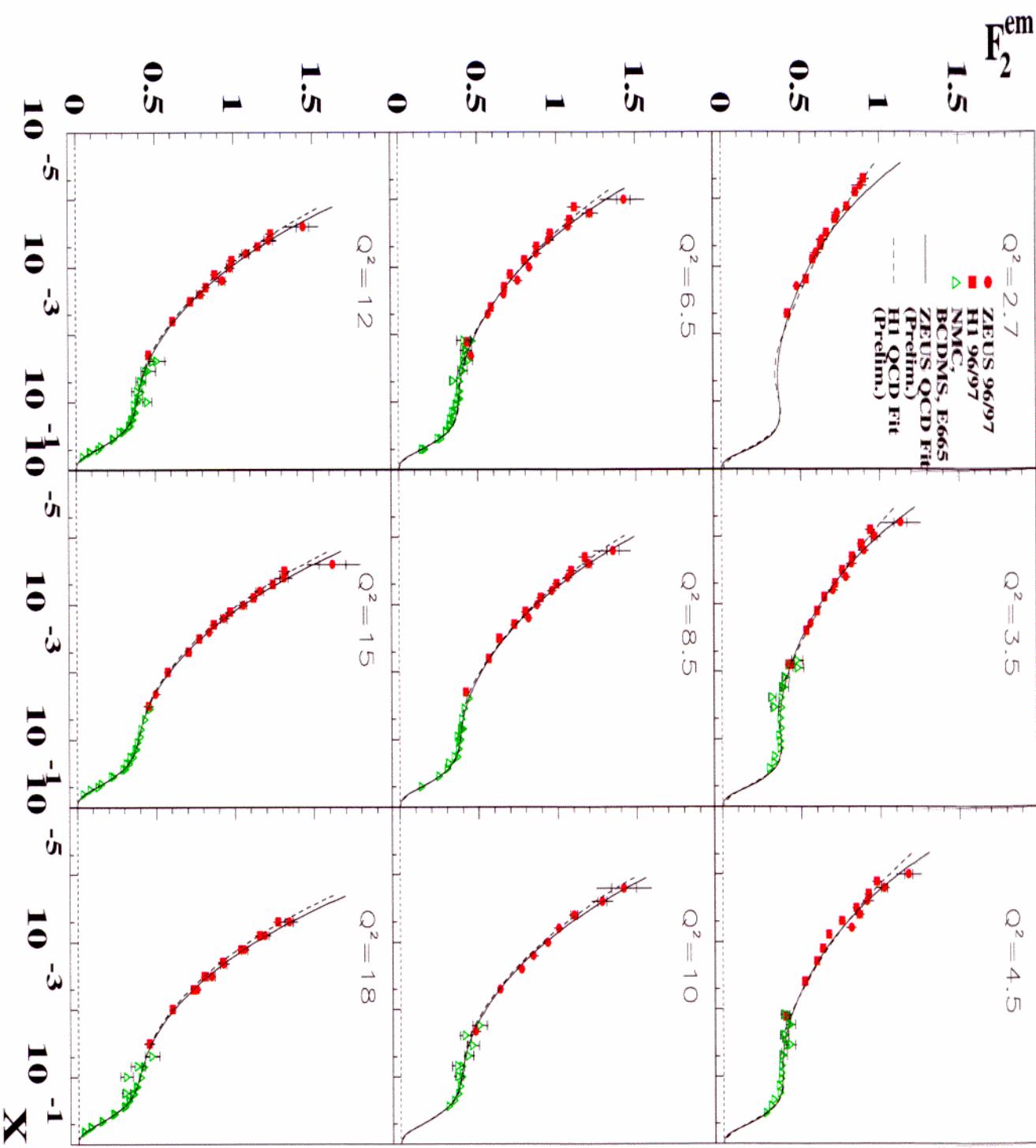
$$Q^2 \frac{\partial}{\partial Q^2} \begin{pmatrix} F^S \\ G \end{pmatrix} = \frac{\alpha_s(\ln Q^2)}{2\pi} \begin{pmatrix} P^{qq} & 2n_f P^{qg} \\ P^{gq} & P^{gg} \end{pmatrix} * \begin{pmatrix} F^S \\ G \end{pmatrix}$$

$$F^{NS} = q_i - q_j \quad ; \quad F^S = \sum_i (q_i + \bar{q}_i)$$

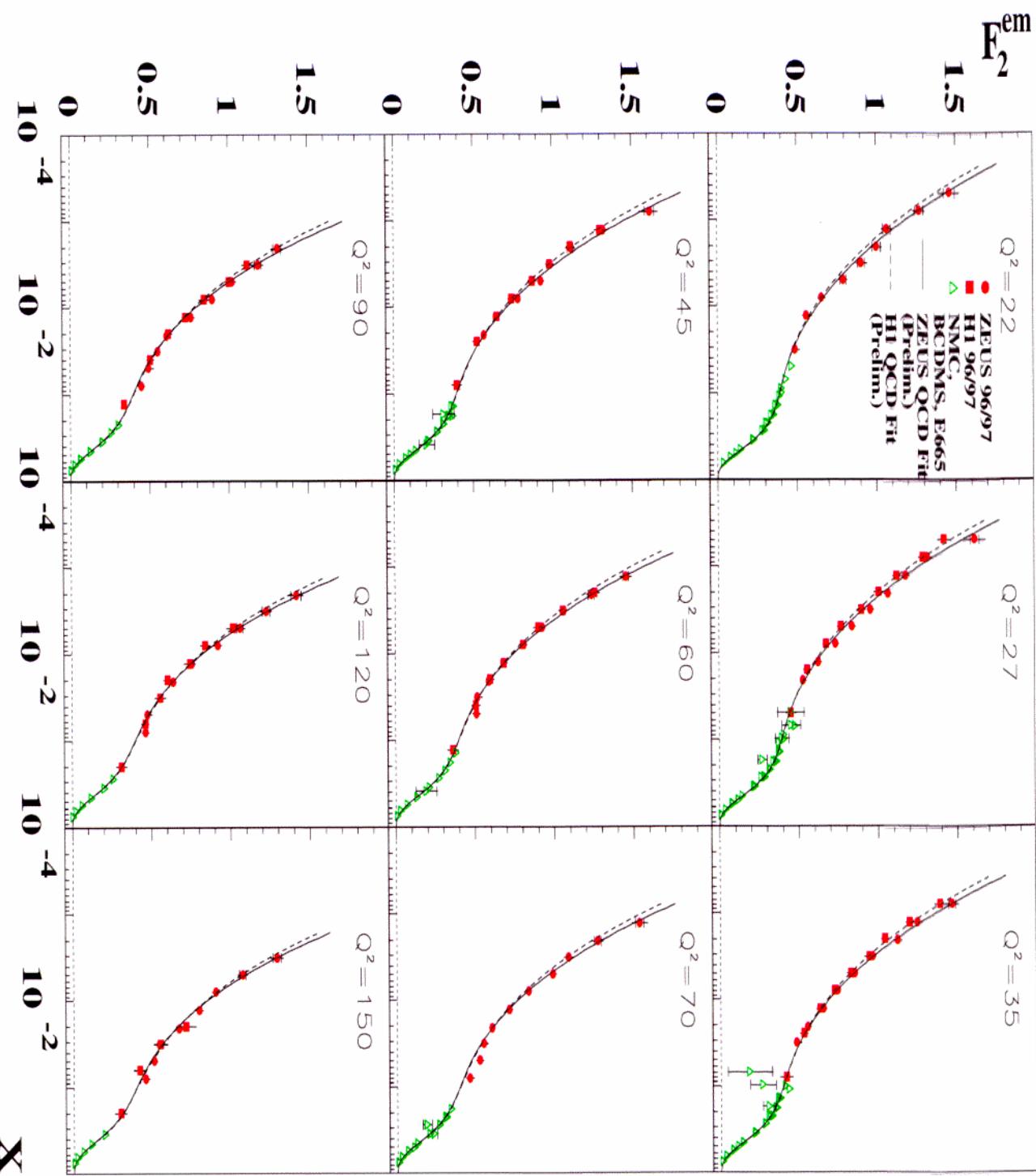
$$P * F = \int_x^1 \frac{dy}{y} P(y) F\left(\frac{x}{y}\right)$$



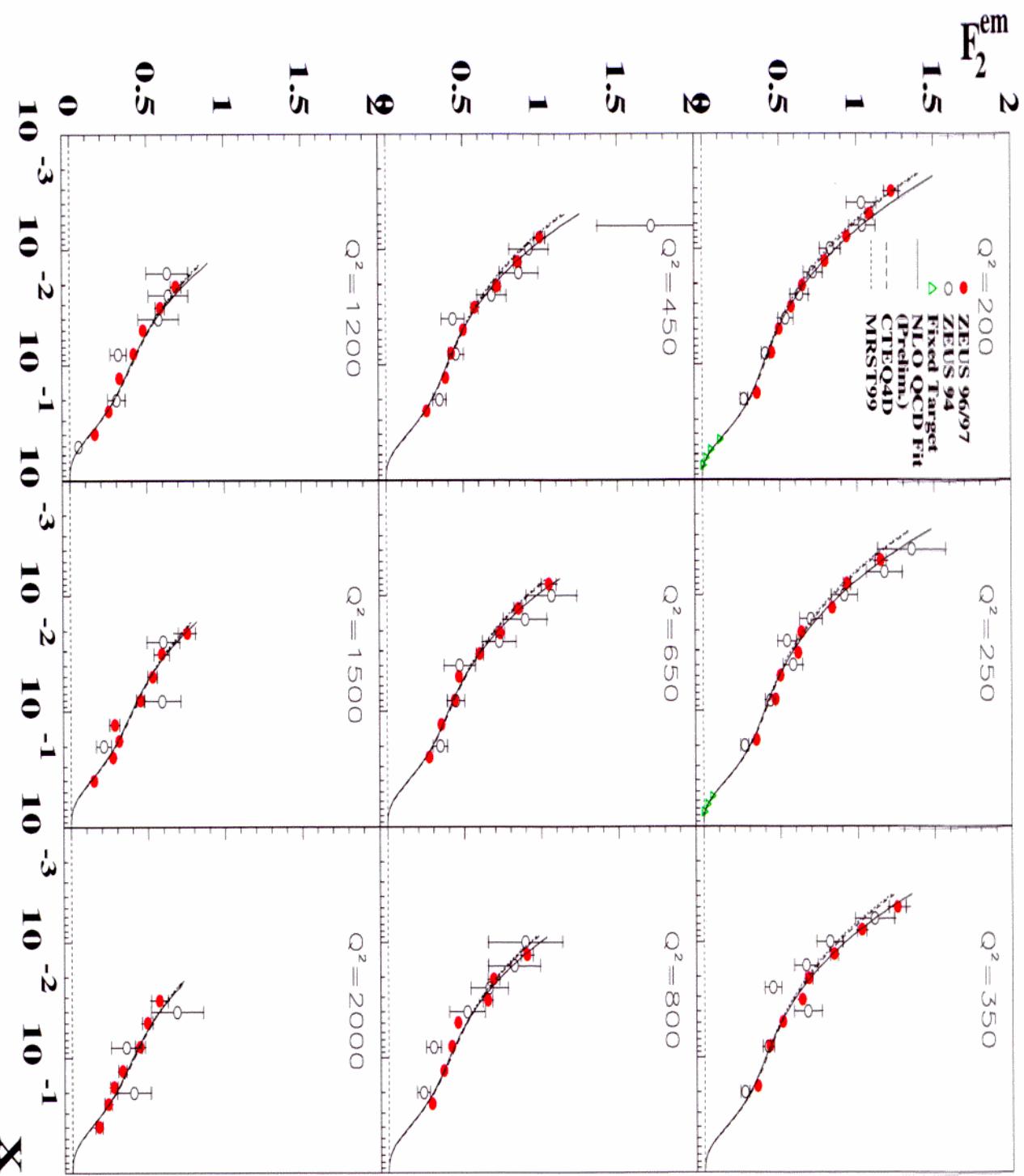
# ZEUS+H1 Preliminary 96/97



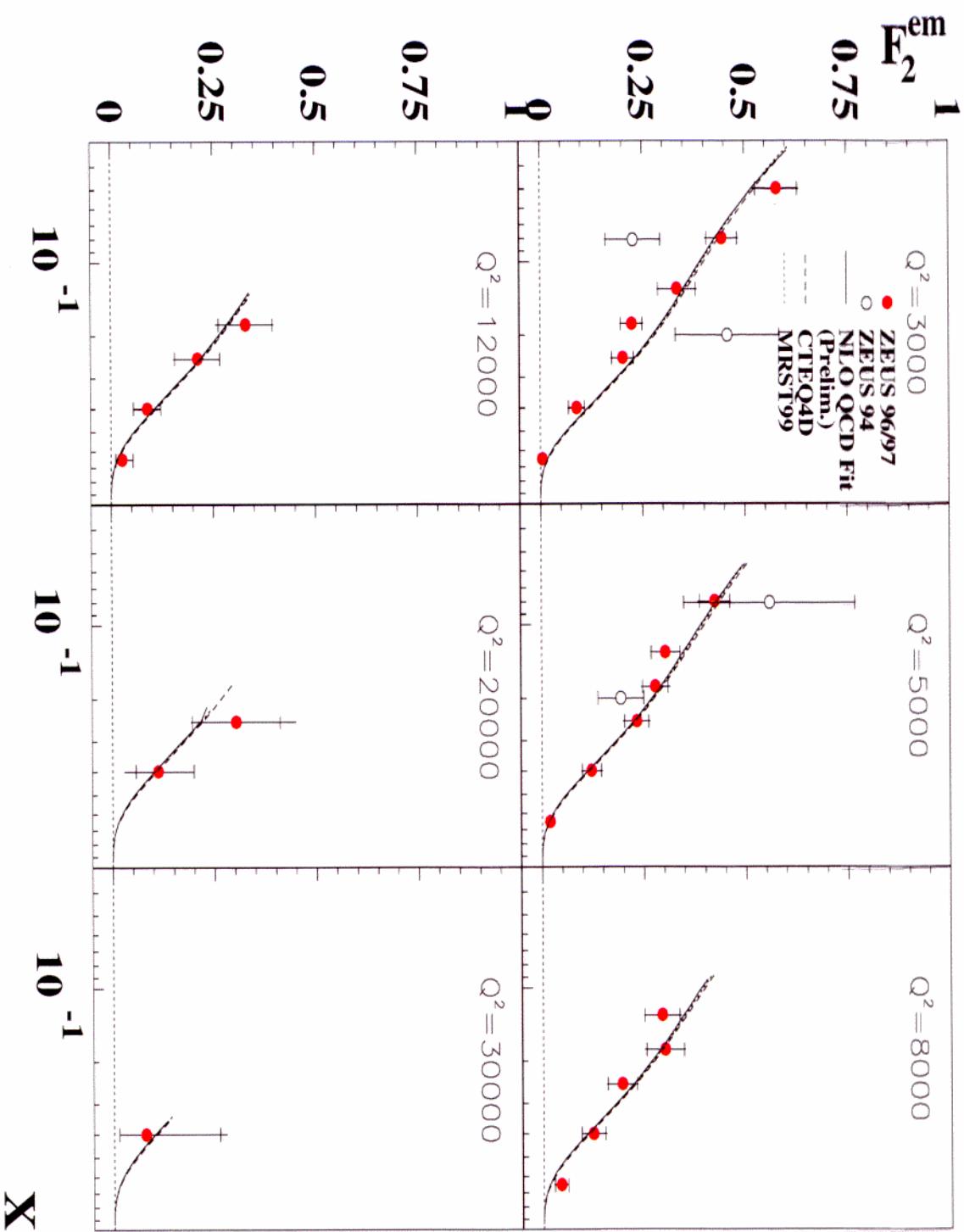
# ZEUS+H1 Preliminary 96/97



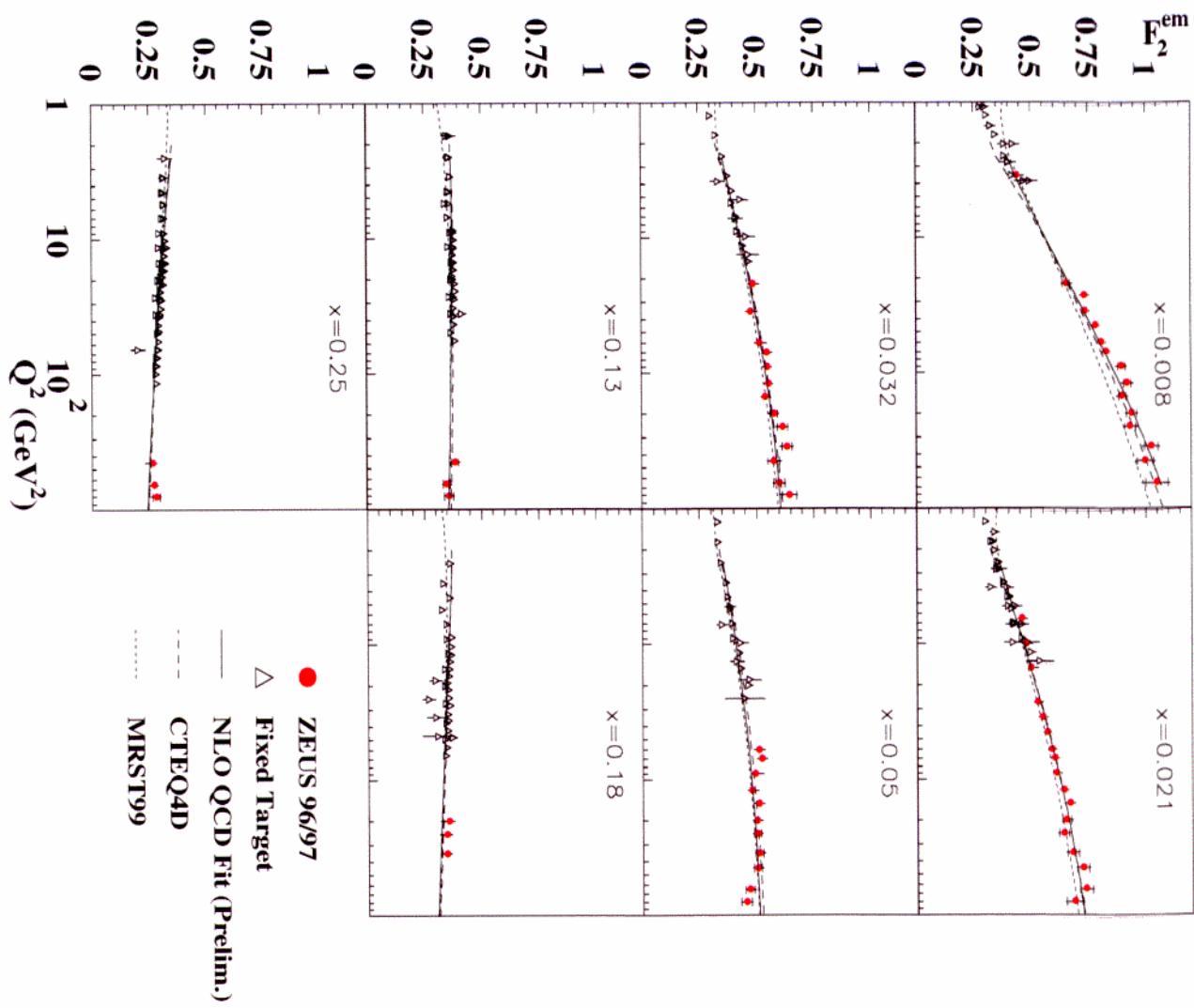
# ZEUS Preliminary 96/97

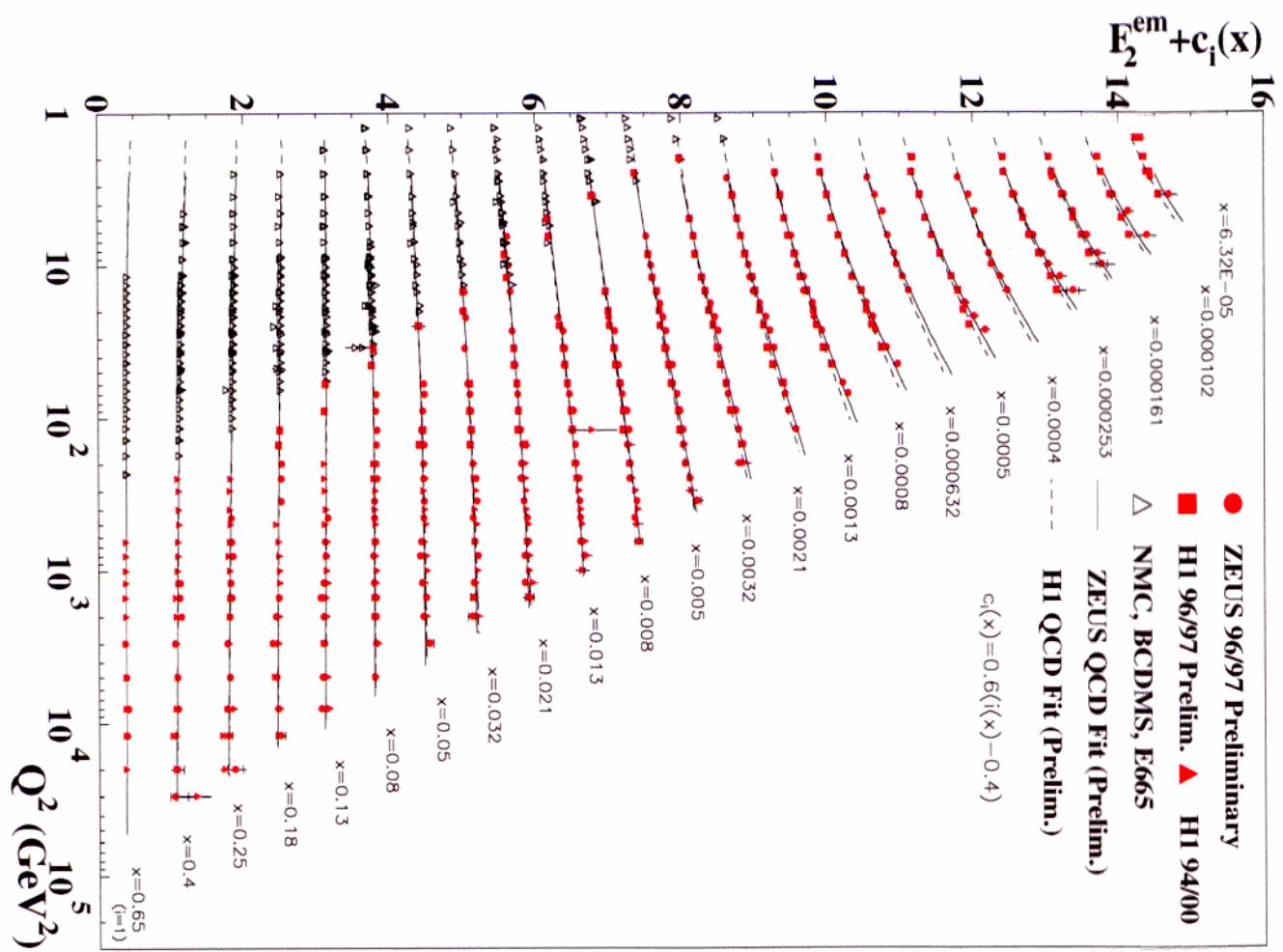


# ZEUS Preliminary 96/97



# ZEUS Preliminary 1996-97





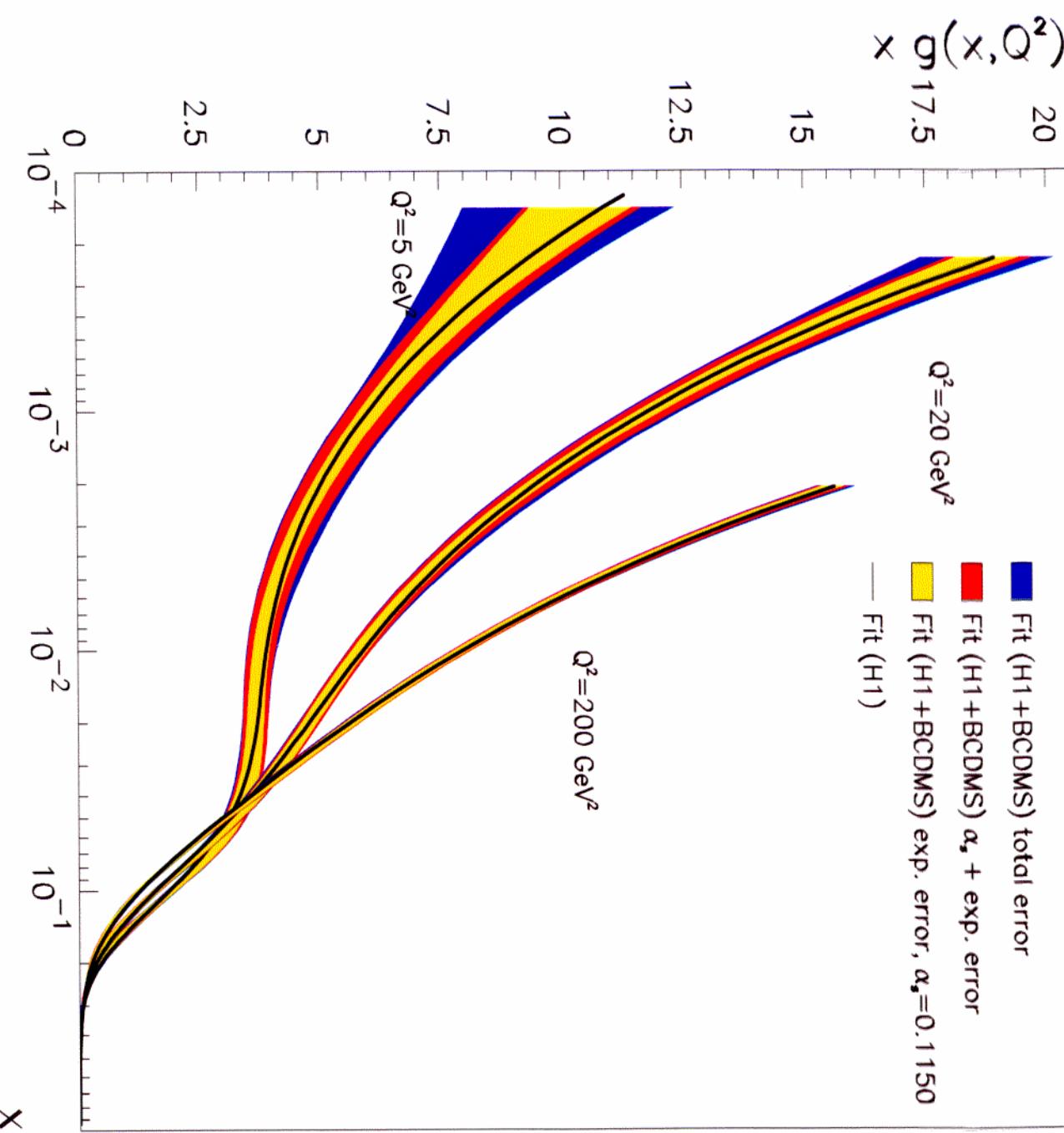
## $F_2$ fits in the framework of DGLAP $Q^2$ evolution

- 19 parameters to parameterise the parton densities as a function of  $x$ ;  
typically:  $xq(x, Q_0^2) = Ax^\delta(1-x)^\eta(1+\gamma x)$
- 16 free parameters after imposing sum rules

Need high  $x$  (i.e. fixed target - NMC,SLAC,BCDMS) data for properly constraining pdf's (valence) (need to be corrected for higher twist contributions etc.)

Beautiful description of data - extraction of gluon density; delicate fit, very sensitive to scaling violations at low  $x$  - how low can one go?

H1 preliminary



## Conclusions on $F_2$

- $F_2$  determined at (better than) 5% up to  $Q^2 \sim 800 \text{ GeV}^2$
- some overlap with fixed target data
- systematics dominated
- scaling violations in agreement with QCD (DGLAP)
- extraction of gluon density and  $\alpha_s(\text{H1; ZEUS very soon})$
- $F_2$  measured all the way up to  $Q^2 \sim 30,000 \text{ GeV}^2$

Remarks:

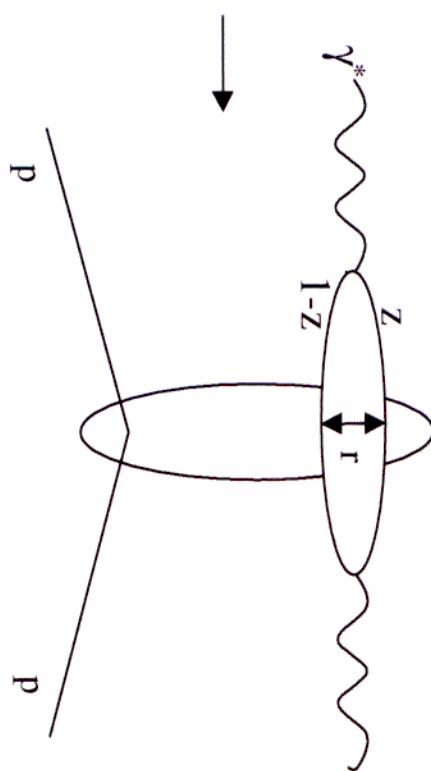
- measurement includes diffractive DIS; how ‘universal’ is  $F_2$  (cf. pp scattering) ?
- transition into ‘non-perturbative’ region: where, how? } → *next*
- low  $x$  region (saturation model & geometric scaling:  
 $\gamma^* \rightarrow q \bar{q}$  dipole interacting with the proton; dipole cross section saturates for  $x \rightarrow 0$ ;  
 $\gamma^* p$  cross section function of only one dimensionless variable :  $Q^2 R_0(x)$ )  
(Stasto, Golec-Biernat, Kwiecinski))

The transition into the non-perturbative regime: not a priori clear at which  $Q^2$ .

DGLAP fits can be made to work down to  $Q^2 \sim 1 \text{ GeV}^2$ ; vanishing

(or negative gluon distribution)...

$F_2$  slopes,  $dF_2/d(\log Q^2)$ , track the scaling violations and may be sensitive to non-perturbative effects; these slopes show a behaviour in qualitative agreement with a ‘saturation’ model (Golec-Biernat, Wuesthoff)



$$\sigma_{T,L}(x, Q^2) = \int d^2 r \int_0^1 dz |\psi_{T,L}(z, r)|^2 \hat{\sigma}(x, r^2)$$

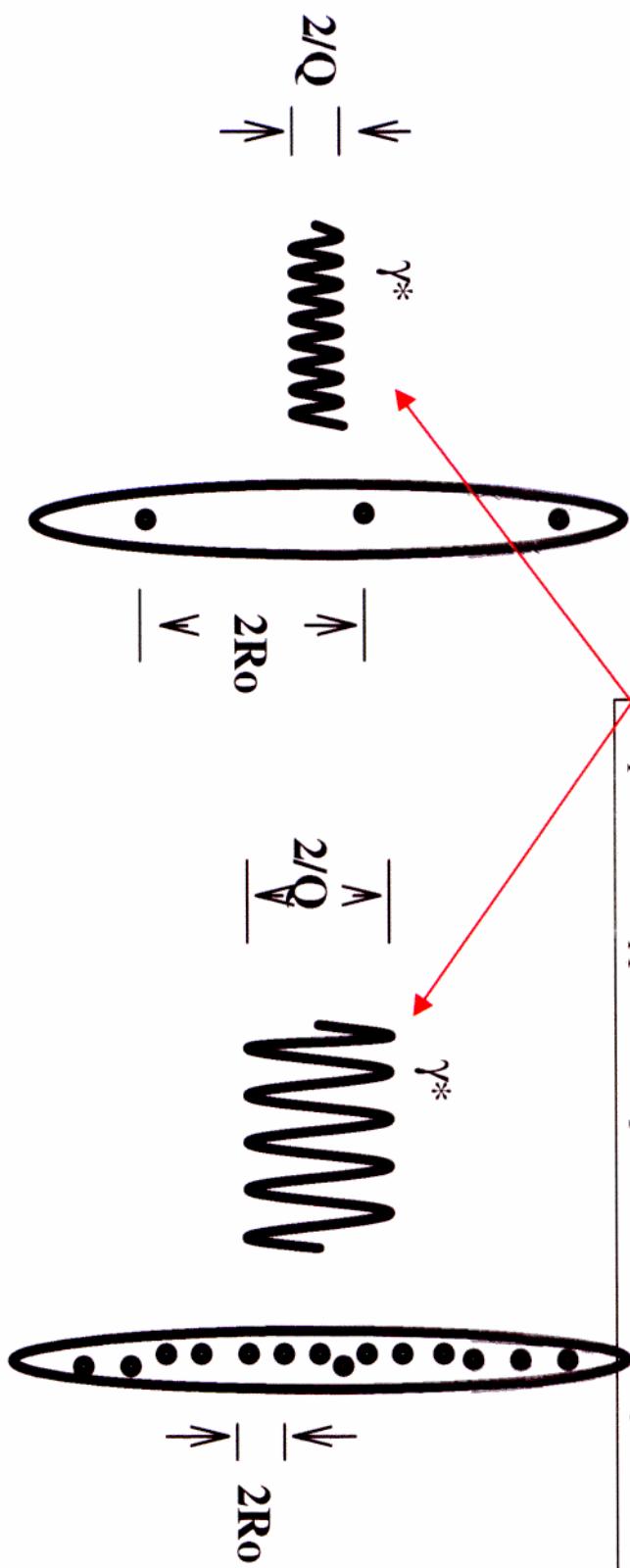
$$F_{T,L}(x, Q^2) = \frac{Q^2}{4\pi^2 \alpha_{em}} \sigma_{T,L}(x, Q^2)$$

Modeling of dipole cross section, adopting an  $x$  dependent radius:

$$R_0(x) = \frac{1}{Q_0} \left( \frac{x}{x_0} \right)^{\lambda/2}; \quad \hat{\sigma}(x, r^2) = \sigma_0 g(\hat{r}^2)$$

$$\hat{r} = \frac{r}{2R_0(x)} \quad ; \quad g(\hat{r}^2) = 1 - e^{-\hat{r}^2}$$

The cartoon is somewhat misleading; what we draw as an amplitude is supposed to represent the wavelength



## SCALING

$$1/Q^2 \ll R_0^2 ; dF_2/d \log(Q^2) \sim x^{-\lambda}$$

## SATURATION

$$1/Q^2 \gg R_0^2 ; dF_2/d \log(Q^2) \sim Q^2 \sigma_0$$

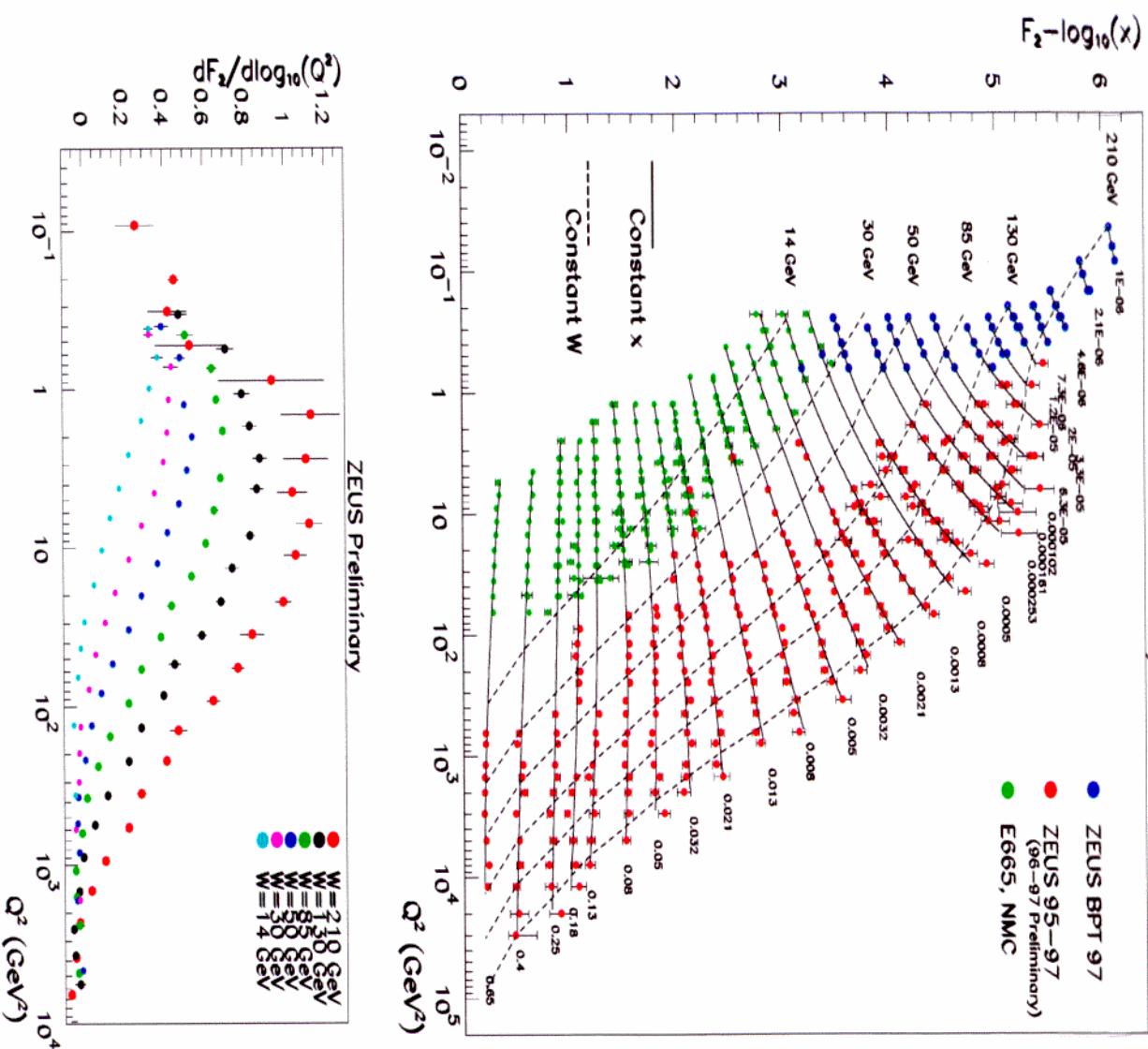
(and  $1/R_0^2 \sim x^{-\lambda}$ ; cf. gluon density)

**Model can also be made to work ‘naturally’ for diffraction: probability of hitting 2 gluons in a color singlet state**

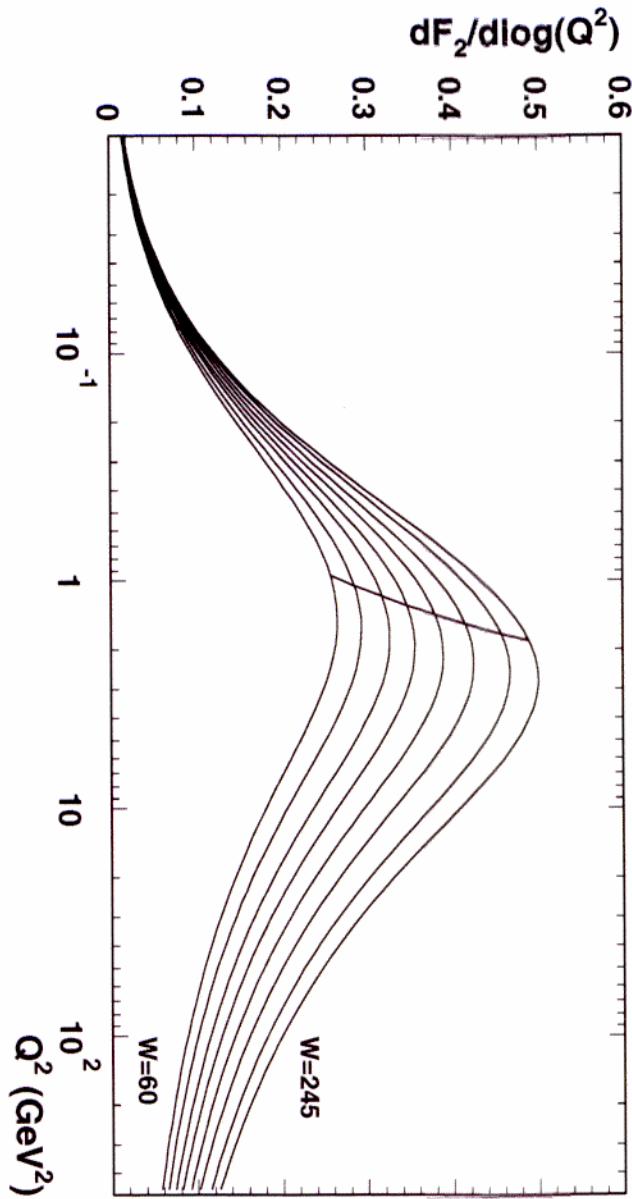
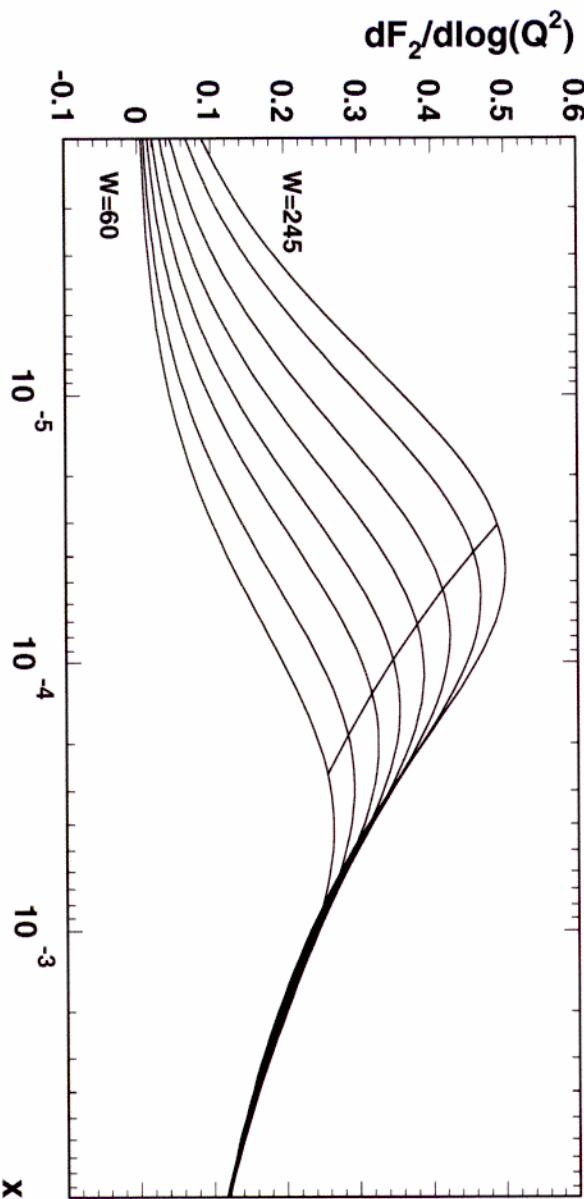
## Proton $F_2$ scaling

Behaviour changes at low  $x$ ,  $Q^2 \approx 2\text{--}6 \text{ GeV}^2$

ZEUS Preliminary



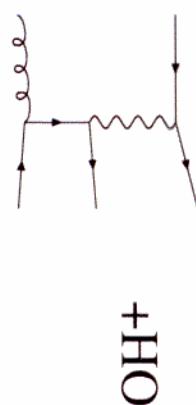
+



From Golec-Biernat, Wüsthof  
Change of slopes in qualitative  
agreement with data

## Charm production in DIS

- consistent with photon-gluon fusion



Two approaches:

- select  $D^{*\pm}$  events in the ‘usual’ way
- select events with ‘direct electrons’

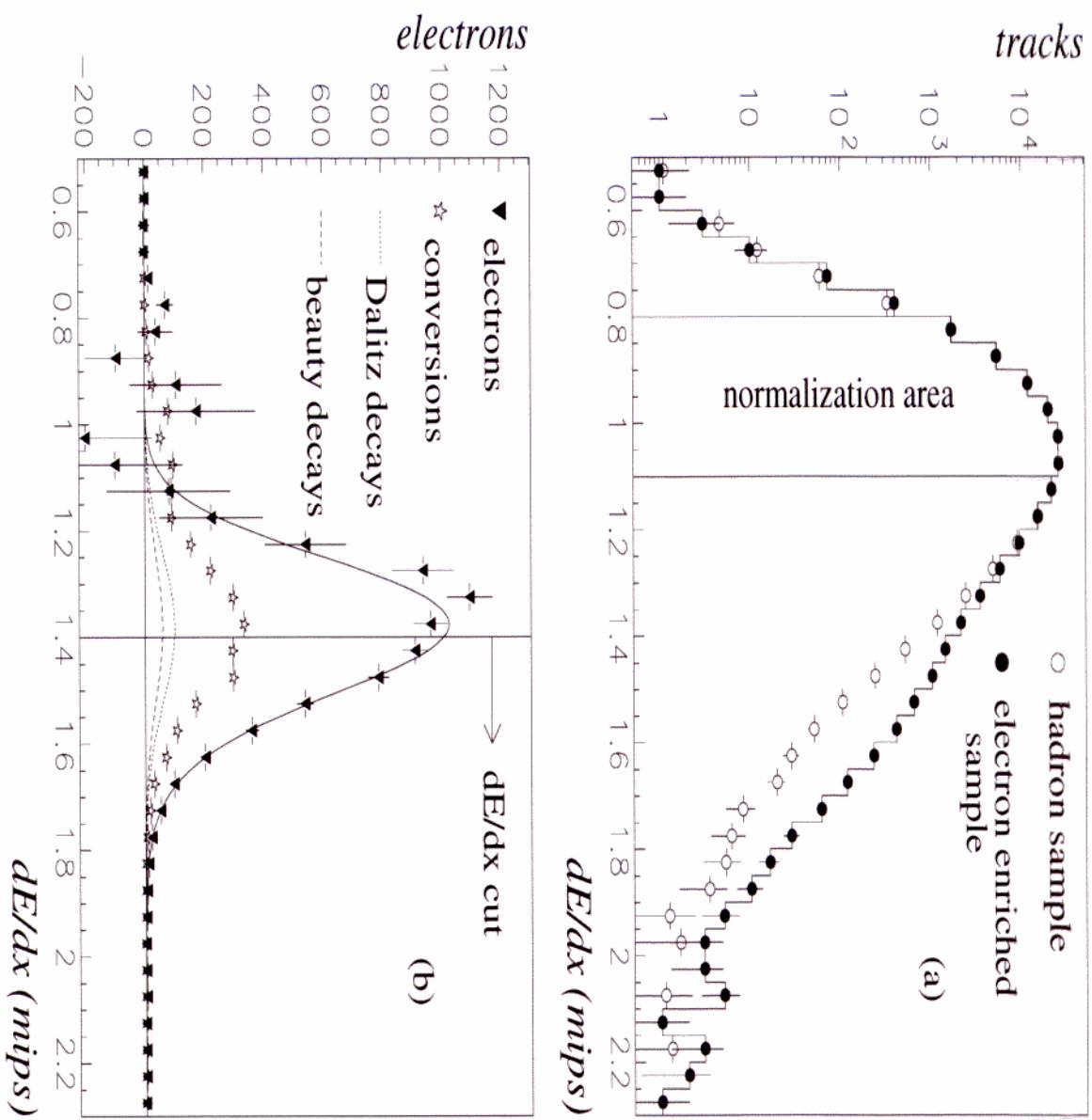
Large extrapolations required in both cases

NLO calculations implemented  
in HVQDIS; treatment  $m_Q$

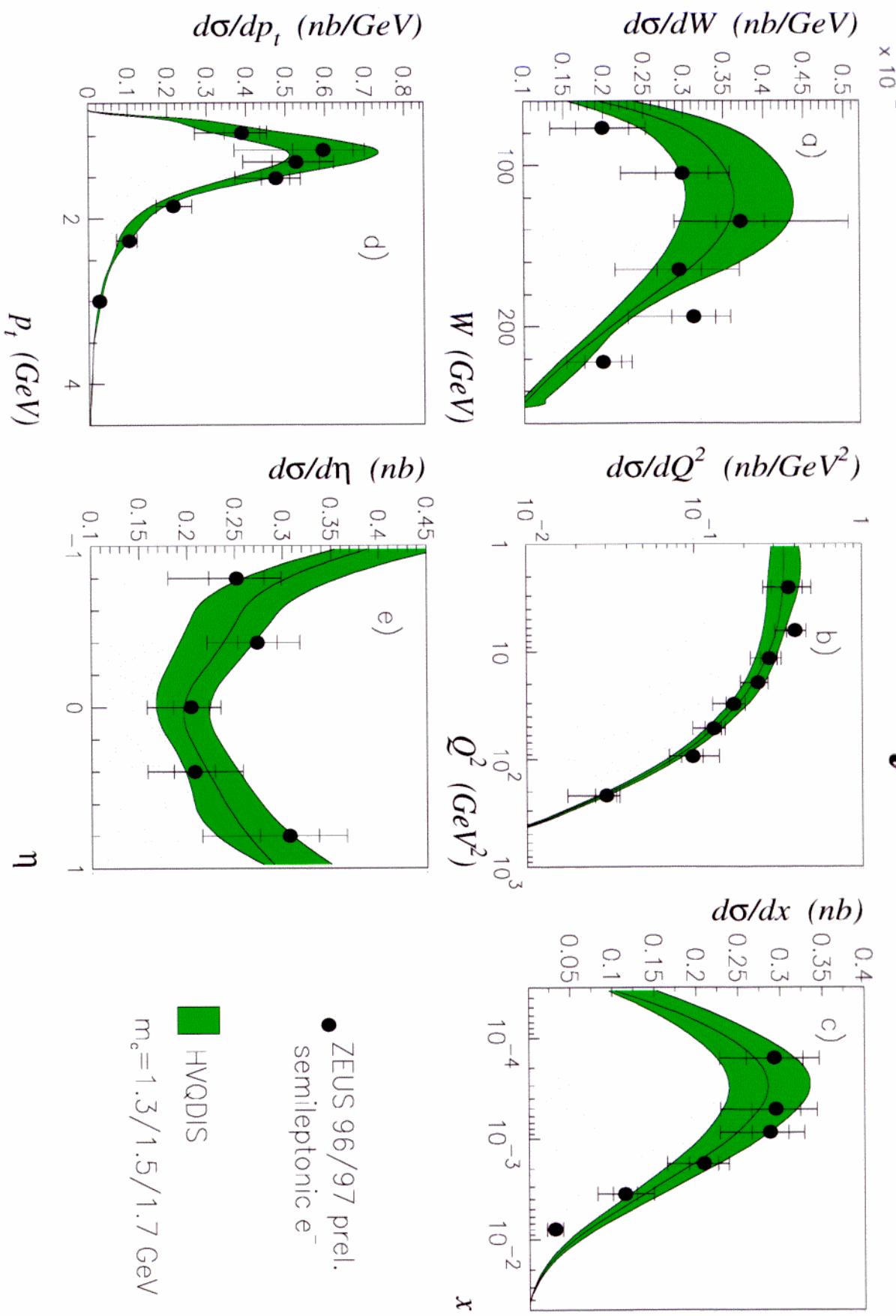
Harris, Smith + refs. to earlier work

$$\frac{d^2\sigma^c}{dxdQ^2} = \frac{2\pi\alpha^2}{Q^4 x} (1 + (1 - y)^2) F_2^c(x, Q^2)$$

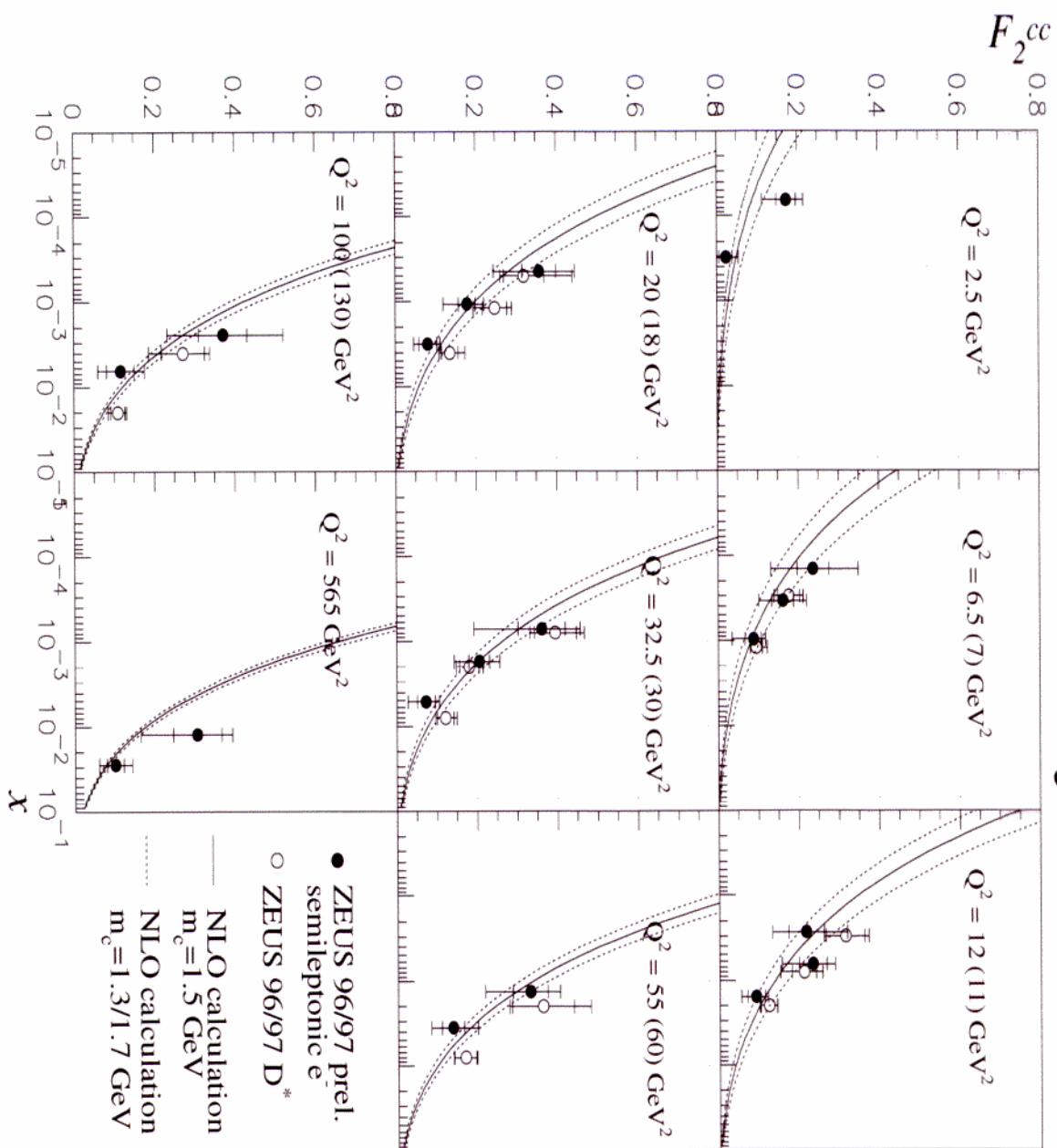
# ZEUS Preliminary 1996-97



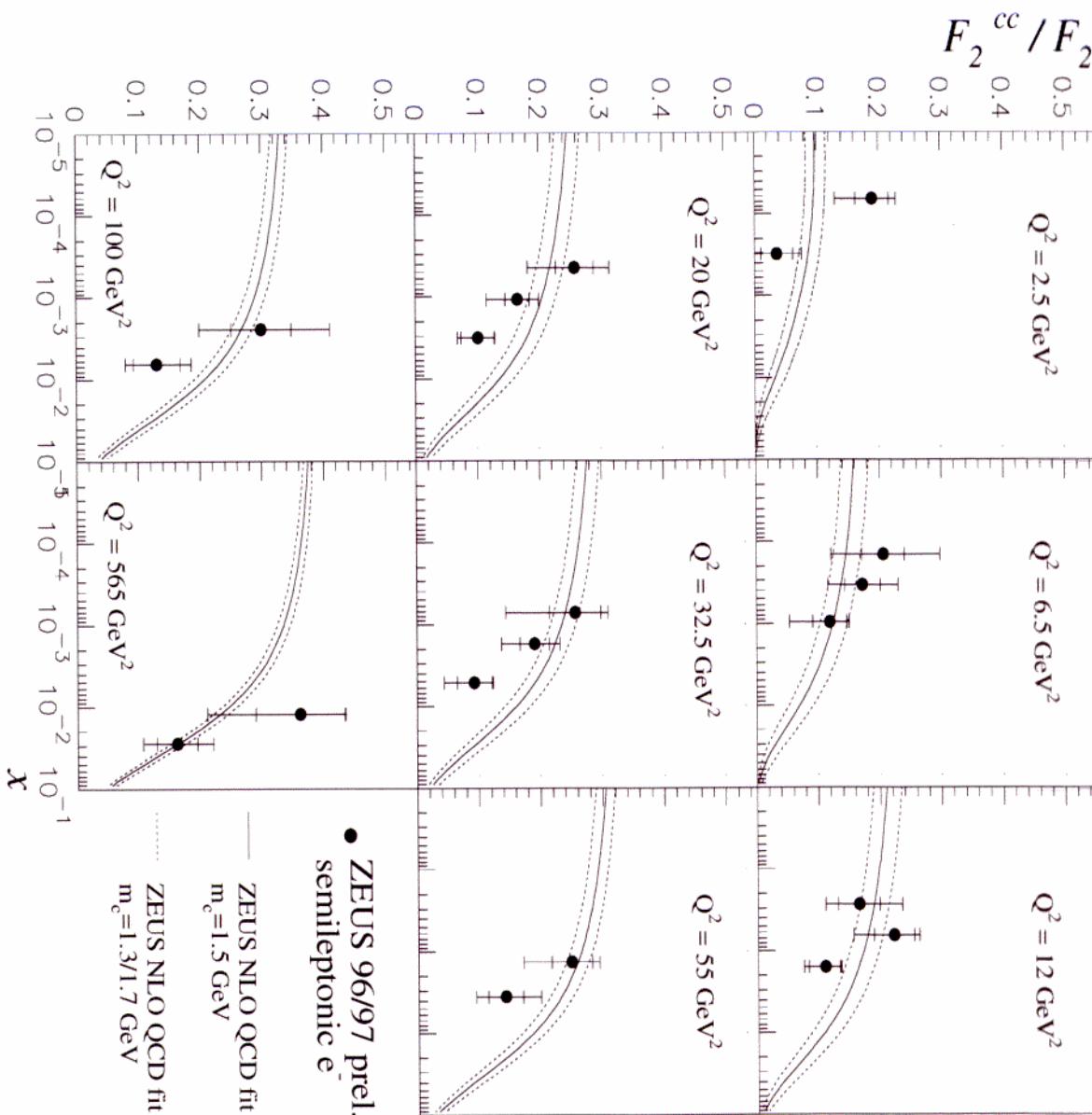
# ZEUS Preliminary 1996-97



# ZEUS Preliminary 1996-97

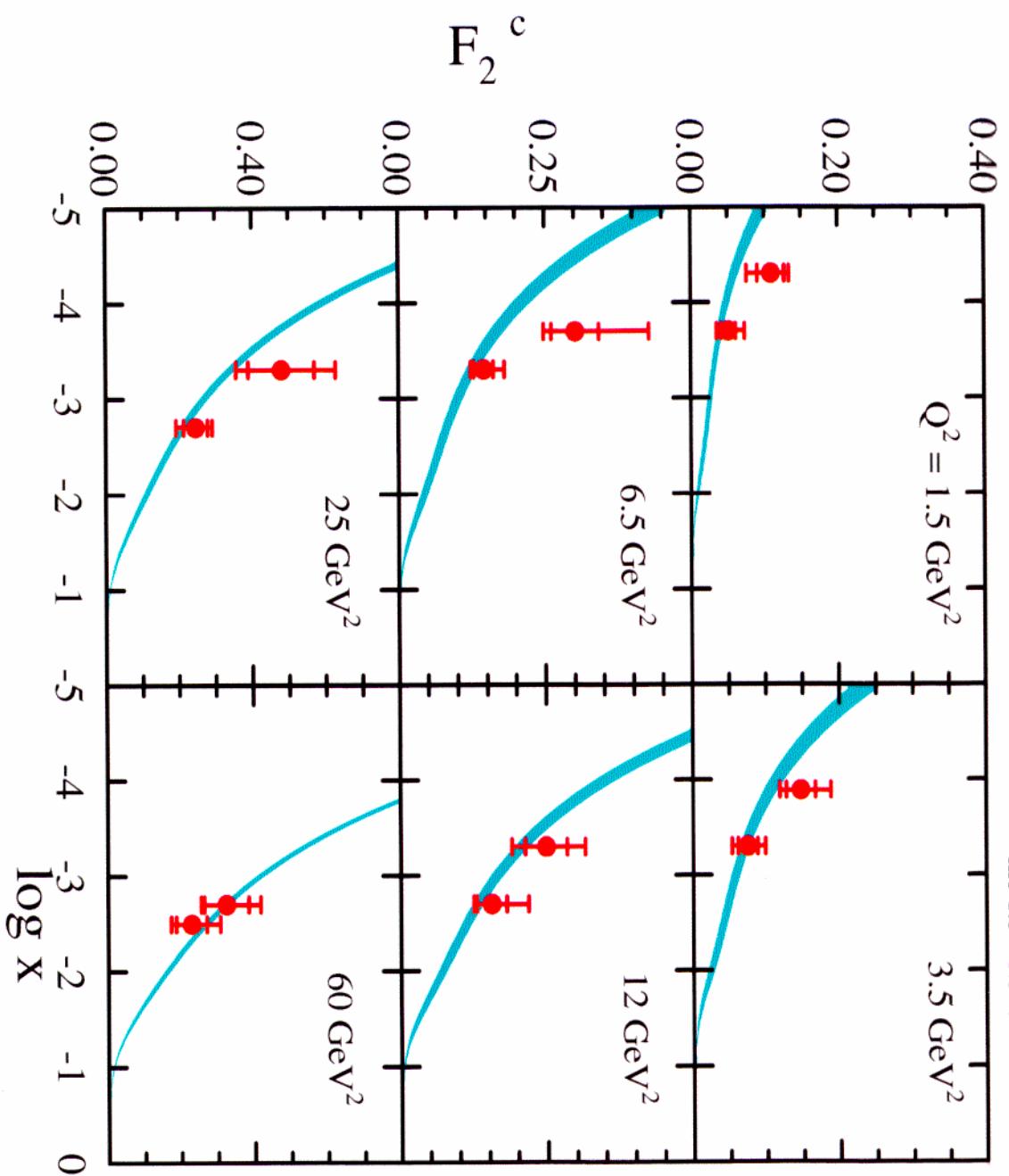


# ZEUS Preliminary 1996-97

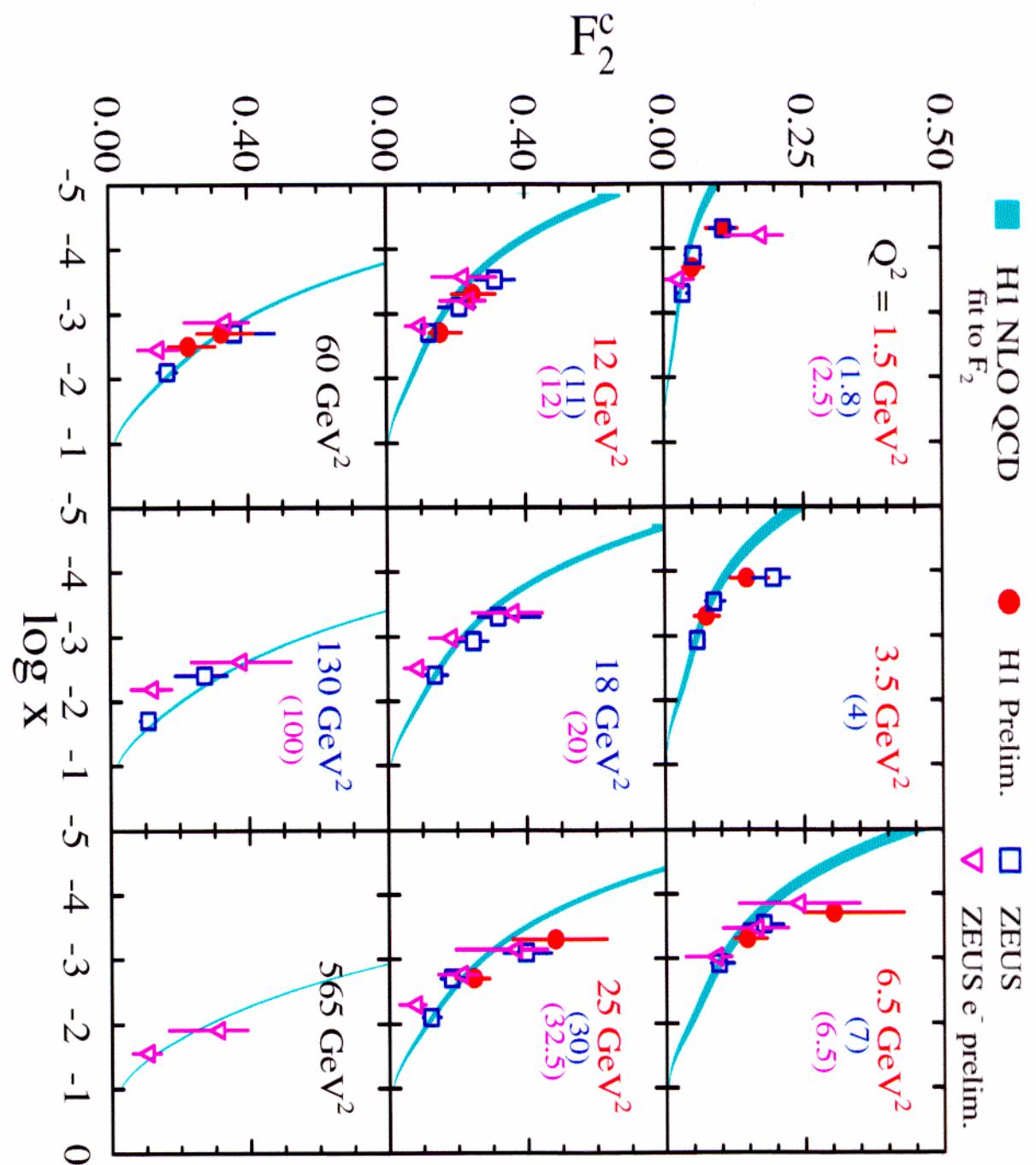


# $F_2^c$ in the NLO DGLAP scheme

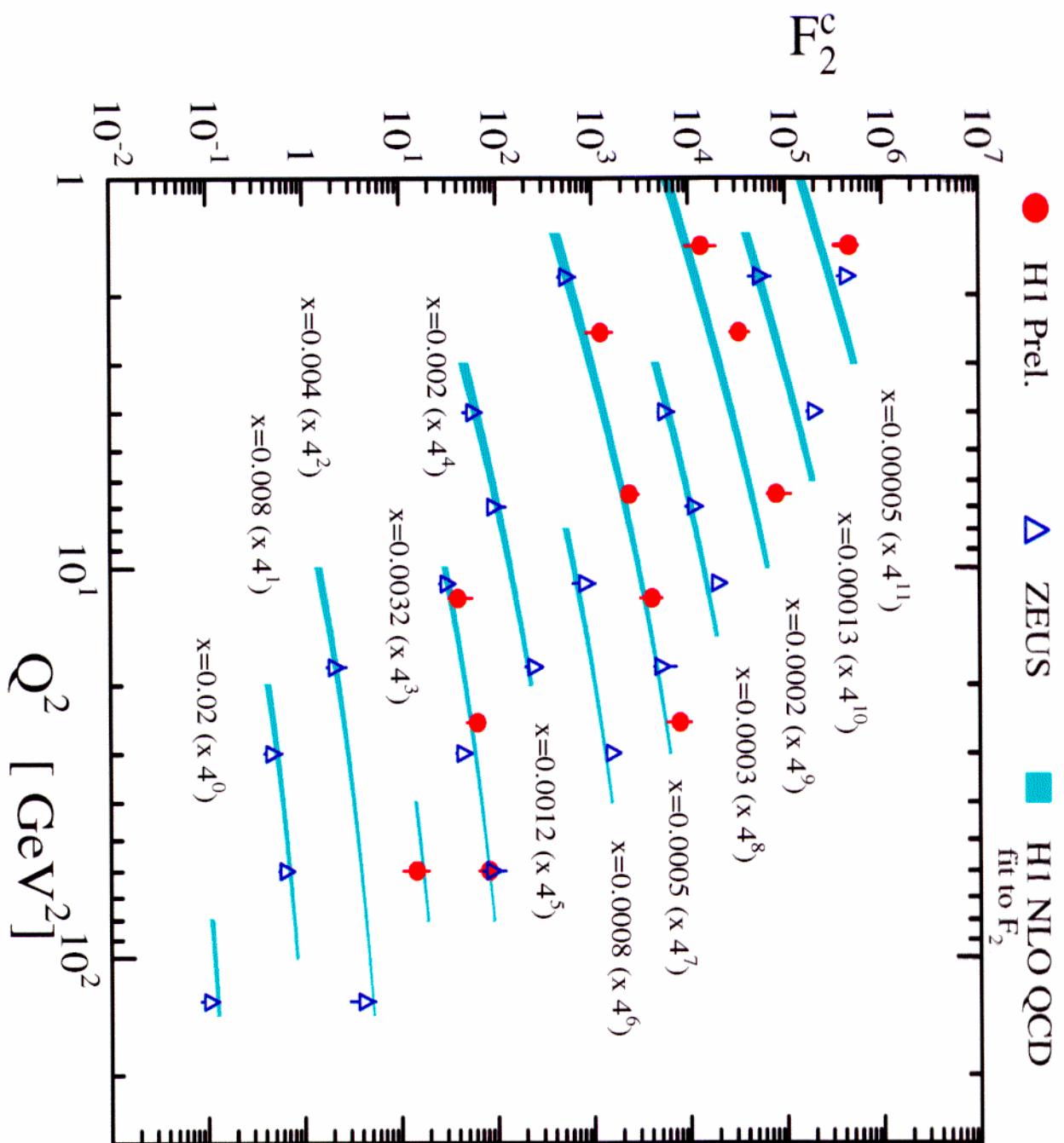
● H1 Preliminary ■ H1 NLO QCD fit to  $F_2$   
mc 1.3 - 1.5 GeV



## $F_2^c$ in the NLO DGLAP scheme



## $F_2^c$ in the NLO DGLAP scheme



H1 has performed an analysis of charm production in DIS in the framework of CCFM evolution, as implemented in the CASCADE programme

Ciaffeloni, Catani, Fiorani, Marchesini

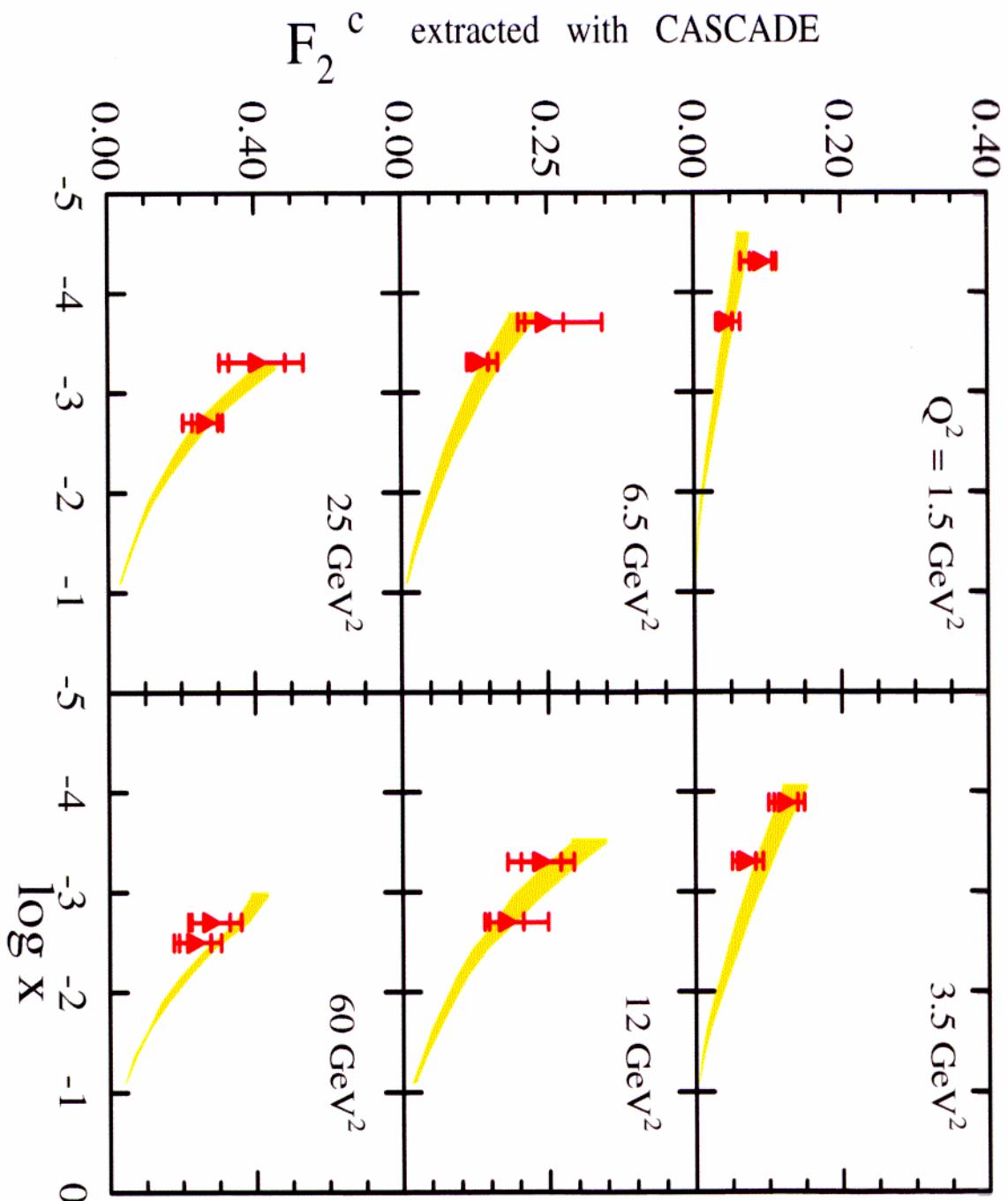
Jung

CCFM: evolution in both  $Q^2$  and  $1/x$

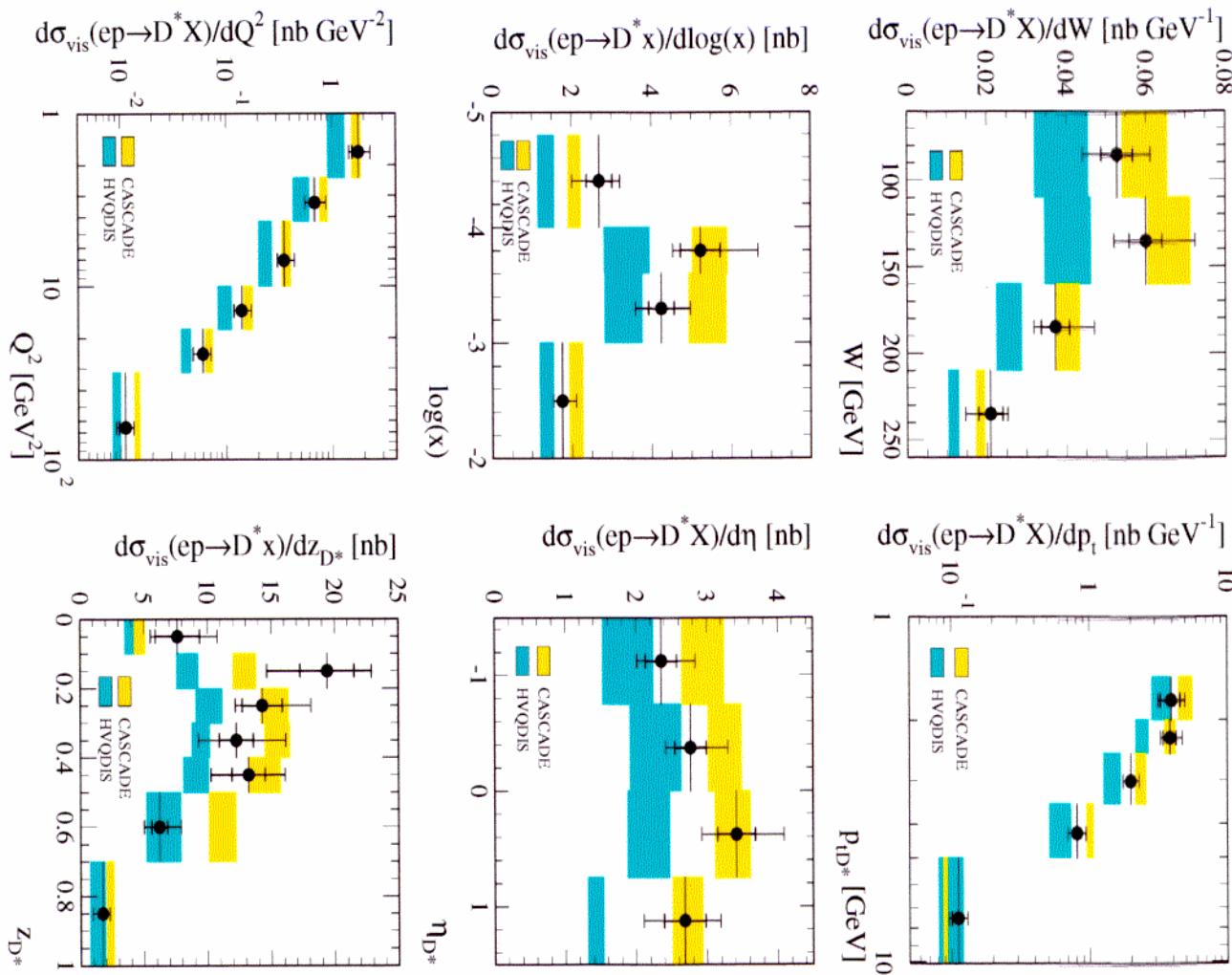
Good (better) description of charm production in DIS, in particular in the lower  $p_T$  region

$F_2^c$  in the CCFM scheme

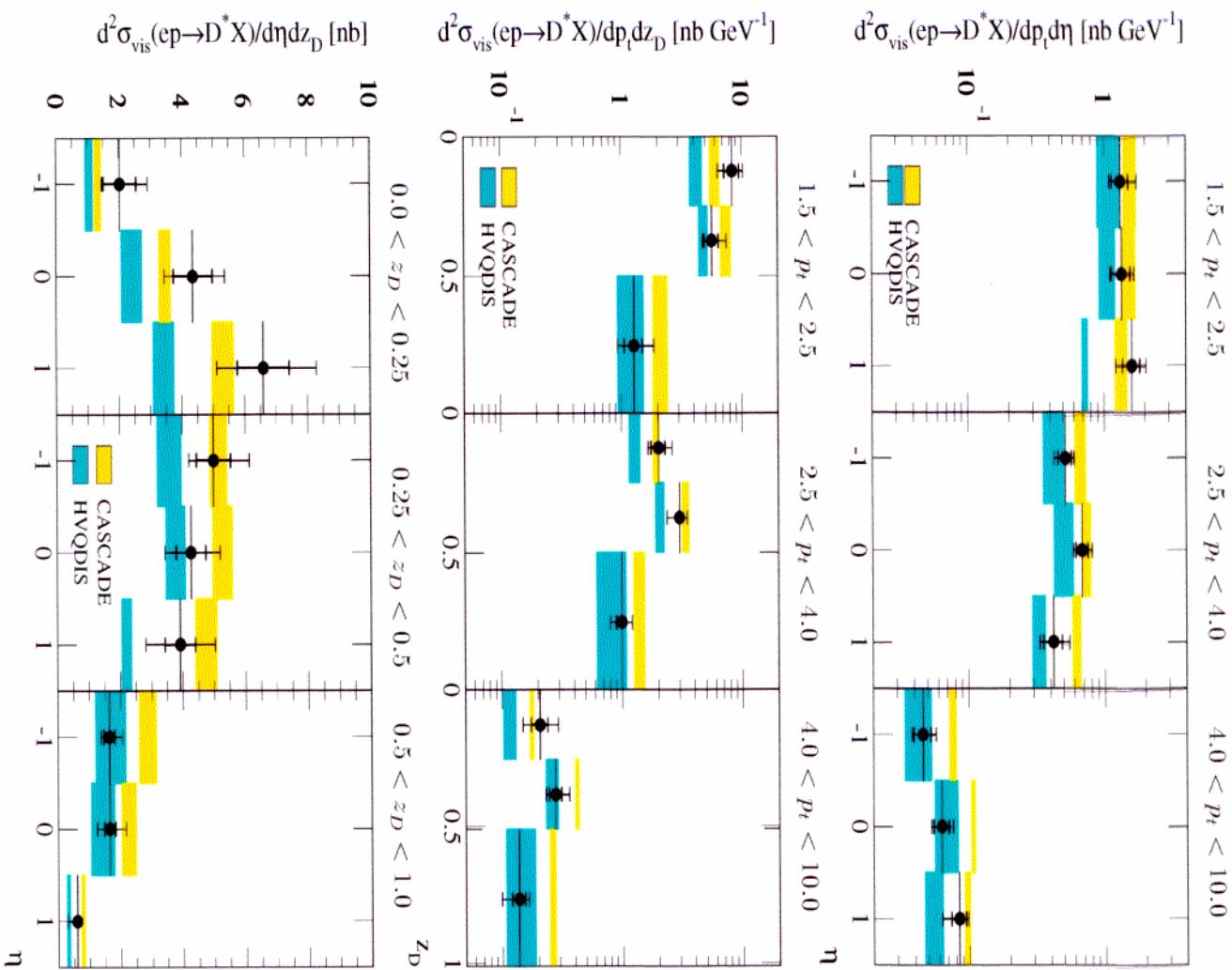
▲ H1 Preliminary      ■ CCFM



# H1 preliminary



# H1 preliminary



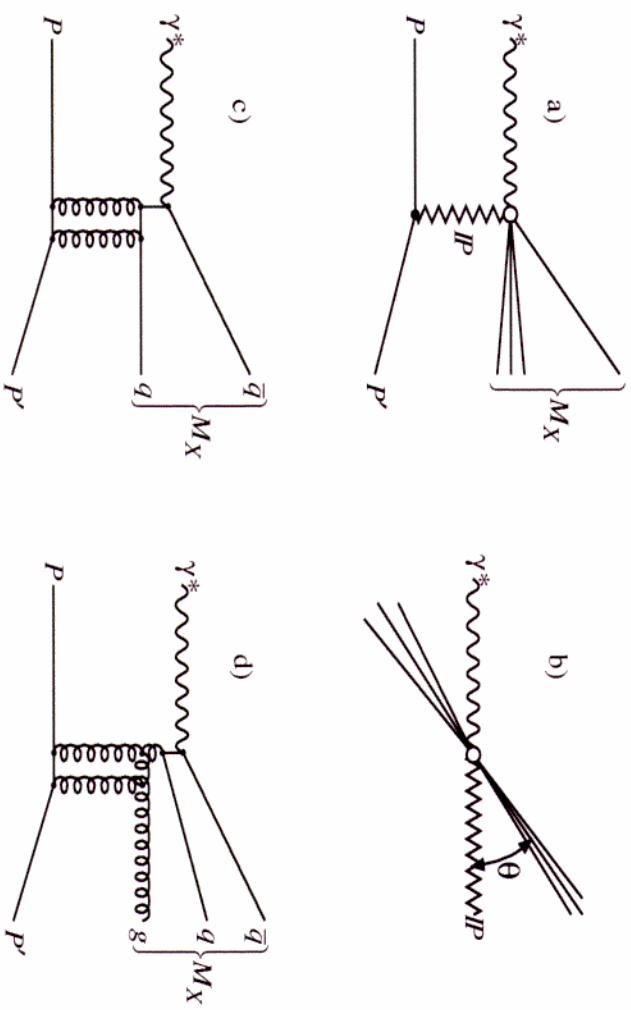
## Conclusions on $F_2^{\text{charm}}$

- only initial measurements; large extrapolations
- probes gluon density function
- agreement with HO pQCD calculations; various approaches to treatment of charm quark mass
- H1: indications that CFFM scheme as implemented in CASCADE gives better description of the data (at low  $p_T$ )

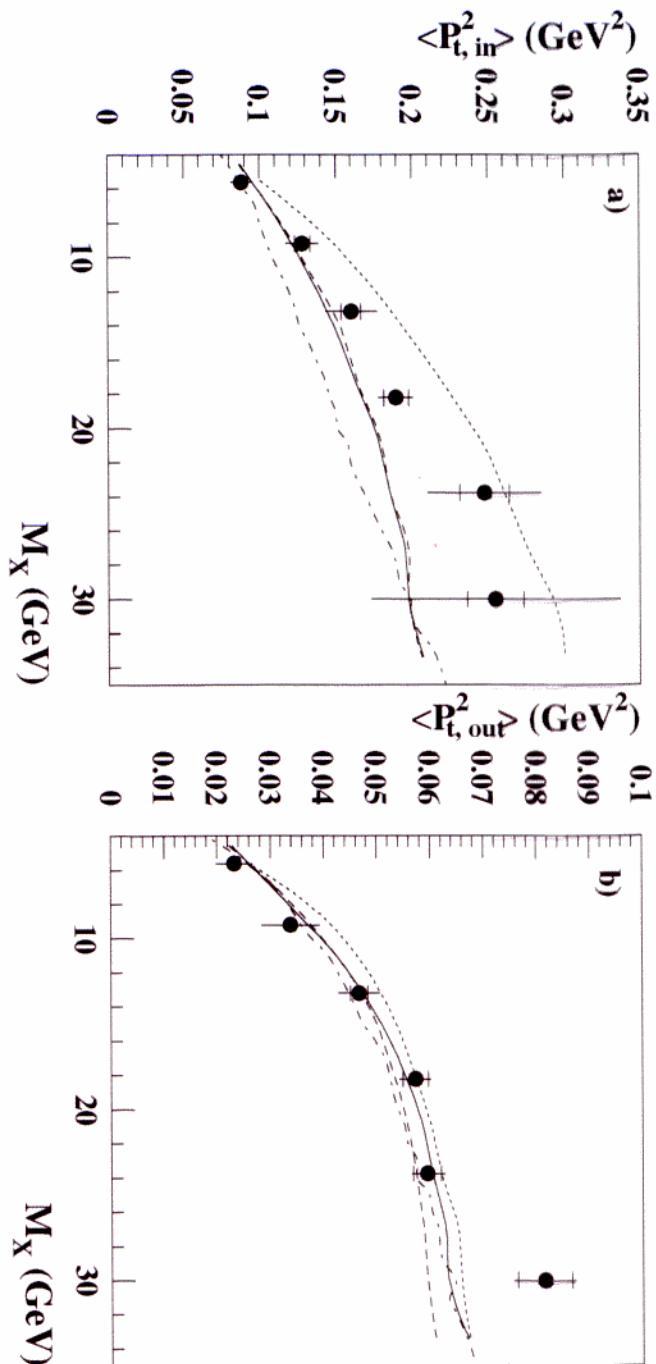
Diffractive DIS has been discovered at HERA; ‘Pomeron’ pdf’s have been extracted (‘gluonic’); now trying to get insight in DDIS by studying final states.

### Three approaches:

- RAPGAP -  $\gamma^*$  IP scattering + Pomeron structure functions (H1)  
Ingelman, Schlein; Jung
- SATRAP -  $\gamma^*$  dissociation + coupling to proton via 2g exchange  
Bartels, Ellis, Kowalski, Wuesthoff + saturation of parton densities in proton plus saturation
- RIDI - LLA;  $\sigma \sim G^2$   
Ryskin; Ryskin, Solano



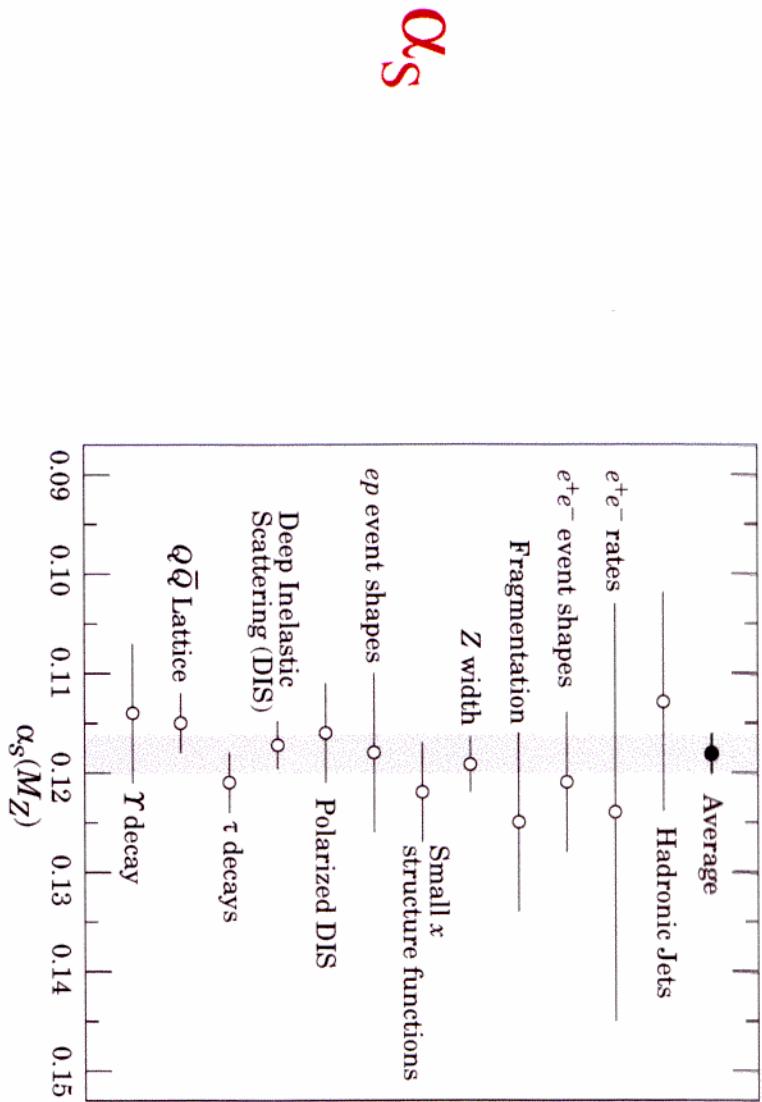
## ZEUS 1997 Preliminary



Extensive studies have been made, but definitive conclusions in favor of or against one of the models cannot be drawn yet

## 9. Quantum chromodynamics 9

relevant event data [59]. In particular, data from purely hadronic initial states are used as they can provide important constraints on the gluon distributions.

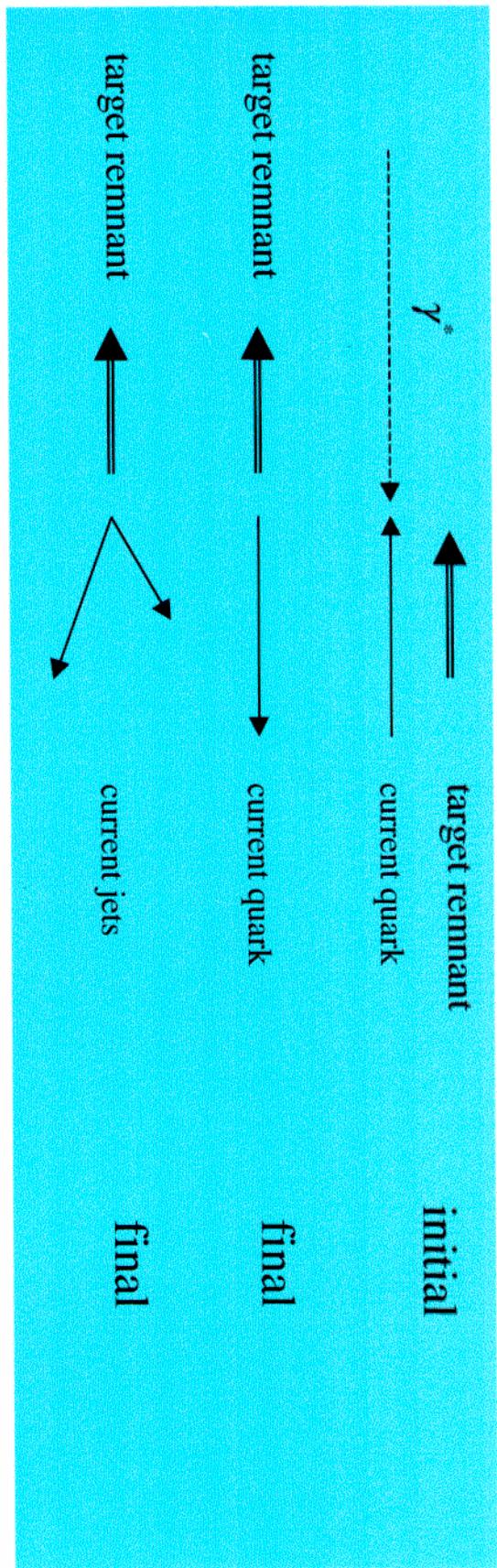


**Figure 9.1:** Summary of the values of  $\alpha_s(M_Z)$  and  $\Lambda^{(5)}$  from various processes. The values shown indicate the process and the measured value of  $\alpha_s$  extrapolated up to  $\mu = M_Z$ . The error shown is the *total* error including theoretical uncertainties.

### 9.4. QCD in decays of the $\tau$ lepton

The semi-leptonic branching ratio of the tau ( $\tau \rightarrow \nu_\tau + \text{hadrons}$ ,  $R_\tau$ ) is an inclusive quantity. It is related to the contribution of hadrons to the imaginary part of the  $W$  self

## Analysis of DIS final states in Breit frame



Jet search via  $k_T$  cluster algorithm

## $\alpha_s$ measurement at HERA

$$\text{PDG: } \alpha_s(M_z) = 0.1185 \pm 0.0020$$

Di-jets in NC DIS

DISENT (NLO QCD); Catani, Seymour

ZEUS:  $\alpha_s(M_z) = 0.1166 \pm 0.0019(\text{stat})$

$$\begin{array}{ll} \pm 0.0034 & 0.0057 \\ \pm 0.0043 & (\text{exp}) \pm 0.0044 (\text{th}) \end{array}$$

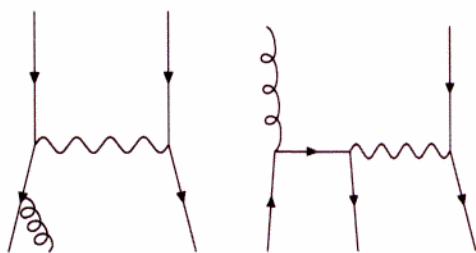
H1:

$$\alpha_s(M_z) = 0.1181 \pm 0.0030(\text{exp})$$

$$\boxed{\mu_r = E_T}$$

$$\begin{array}{ll} \pm 0.0039 & 0.0036 \\ \pm 0.0046 & (\text{th}) \pm 0.0015 (\text{pdf}) \end{array}$$

$$\begin{array}{ll} \alpha_s(M_z) = 0.1221 \pm 0.0034(\text{exp}) & \\ \pm 0.0054 & 0.0033 \\ \pm 0.0059 & (\text{th}) \pm 0.0016 (\text{pdf}) \end{array}$$



1

From scaling violations (low x):  $\alpha_s(M_z) = 0.1150 \pm 0.0017$  (exp)

$$\begin{array}{ll} \pm 0.0011 & \\ \pm 0.0012 & (\text{mod}) \pm 0.005 (\text{scale}) \end{array}$$

## H1 preliminary

correlation:  $\alpha_s$  – gluon density  
in a simultaneous NLO QCD fit

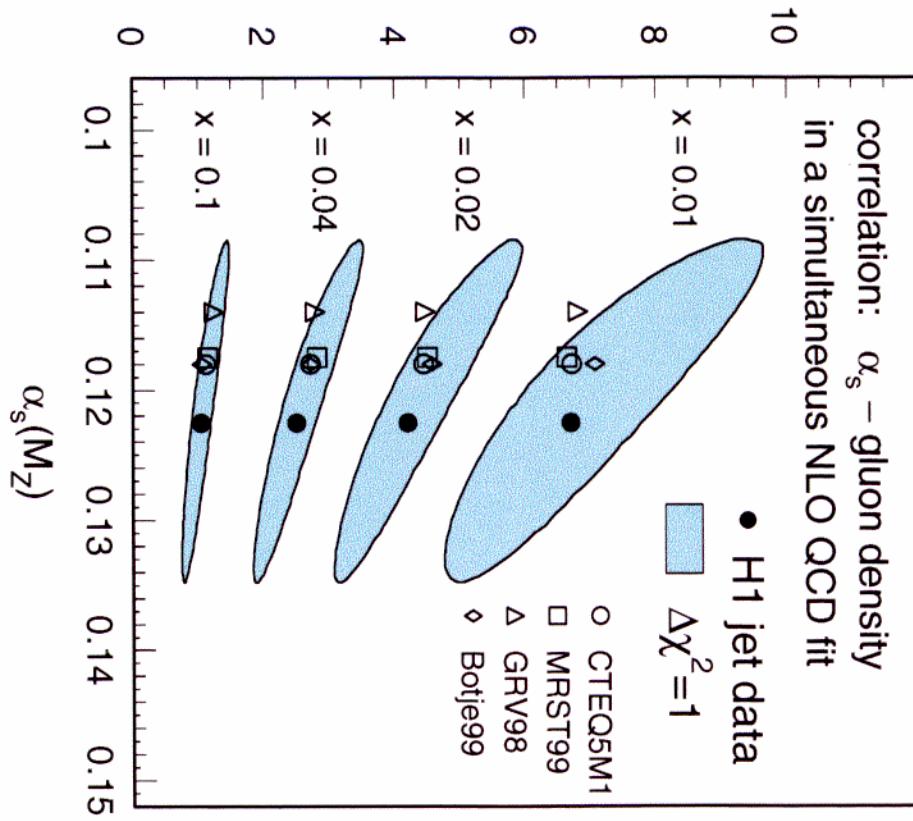
$x = 0.01$   
 $x = 0.02$   
 $x = 0.04$   
 $x = 0.1$

• H1 jet data  
 $\Delta\chi^2 = 1$

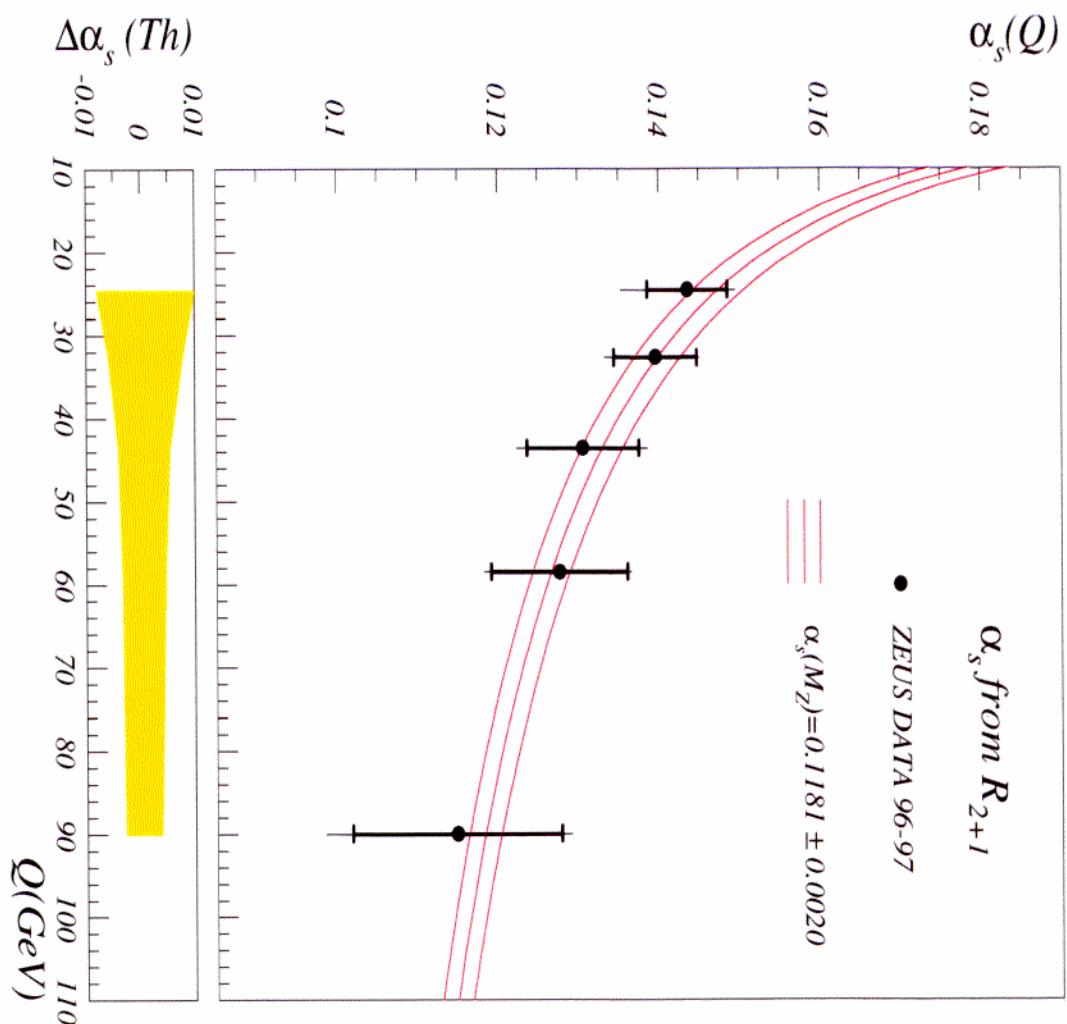
○ CTEQ5M1  
□ MRST99  
△ GRV98  
◊ Botje99

$x G(x, \mu_f^2 = 200 \text{ GeV}^2)$

Using HERA (i.e. H1)  
data only



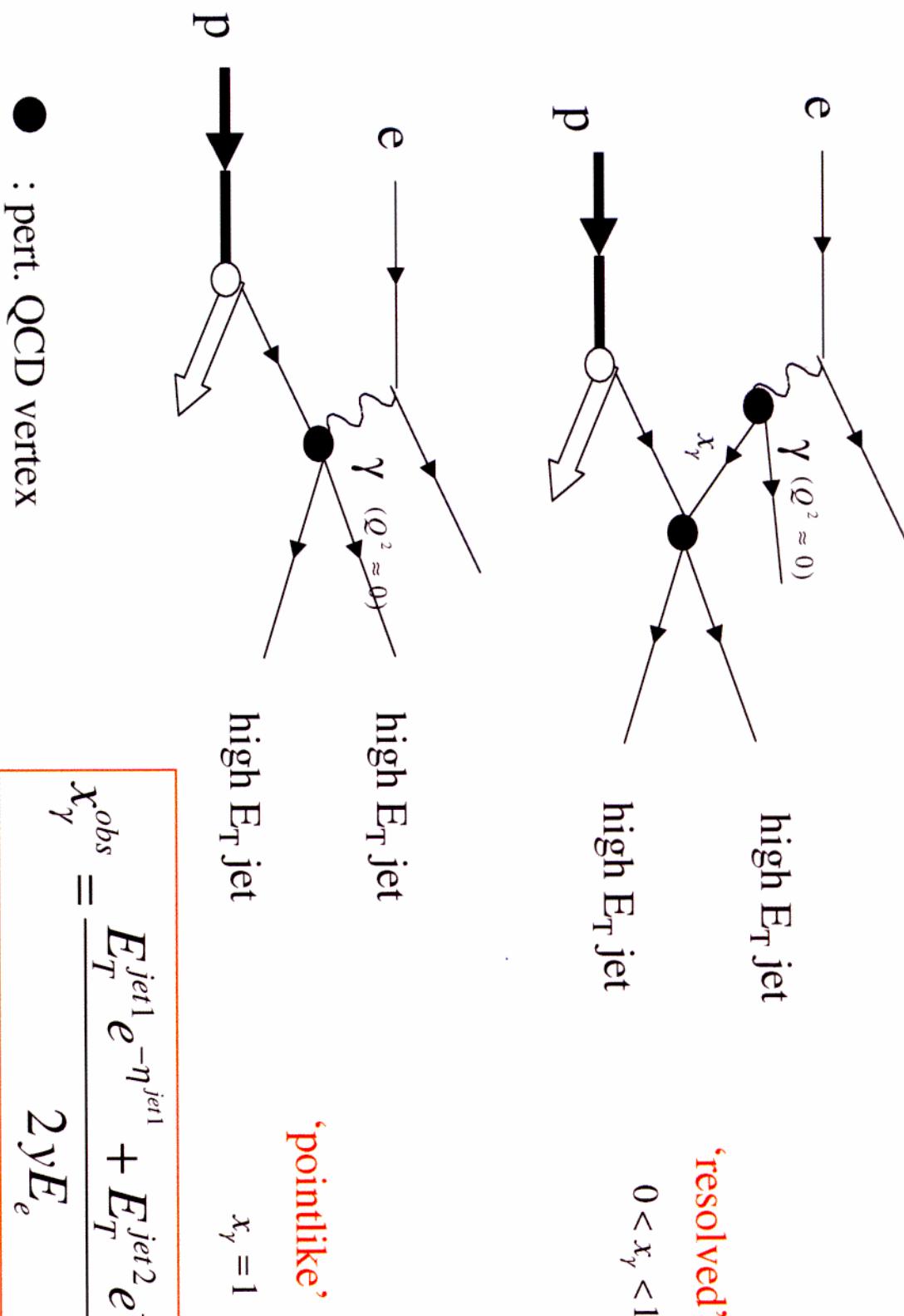
# ZEUS 96-97 PRELIMINARY



## Conclusions on $\alpha_s$

- Precision measurements possible and achieved, both from  
 $(\geq)$  2-jet production and from  $F_2$  scaling violations and from  
a combined analysis.
- Main sources of uncertainty: choice of scale (need higher order  
calculations?) and the correlation of  $\alpha_s$  and the gluon density  
(to be measured independently!)

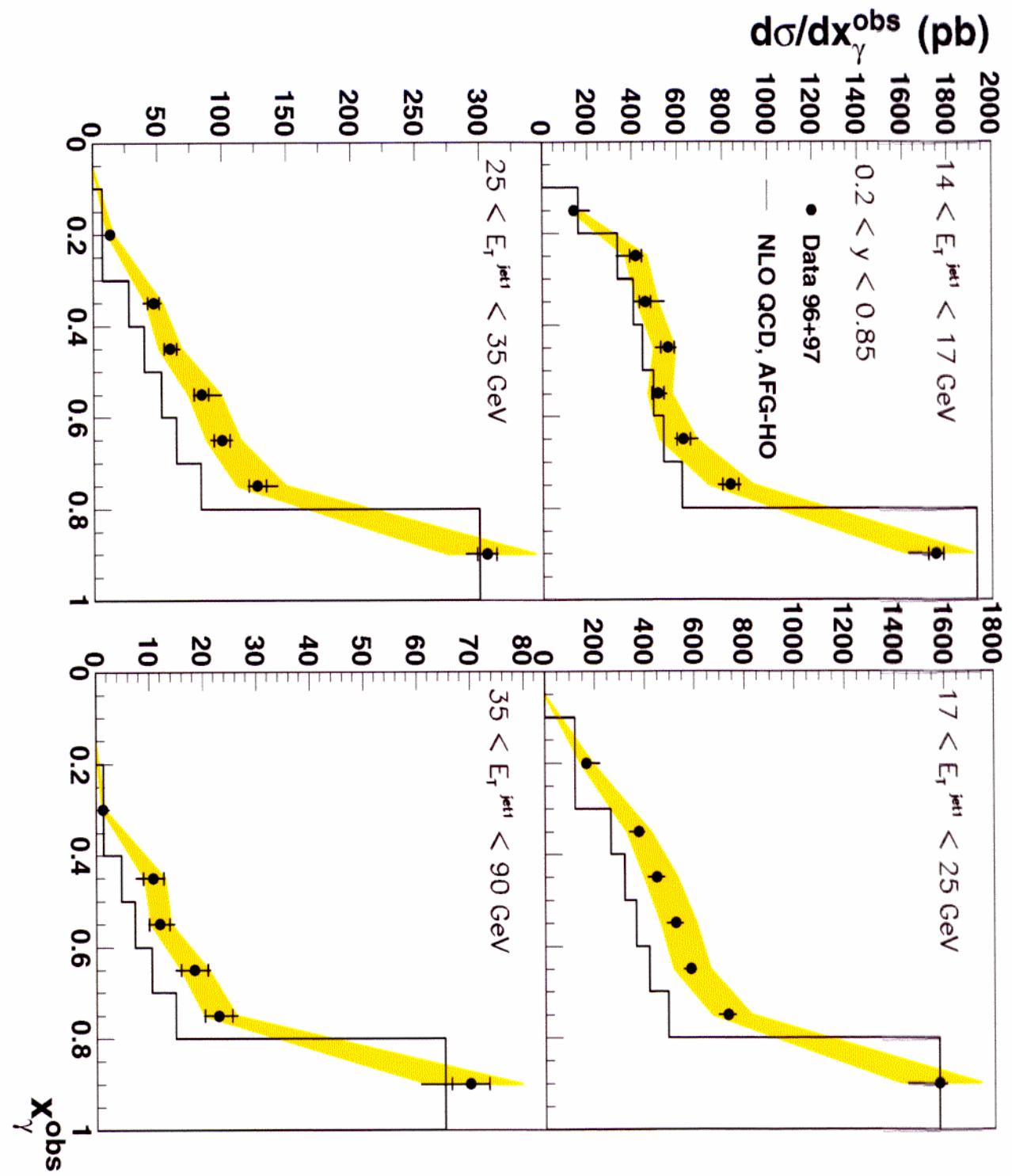
## Photoproduction



$$x_\gamma^{obs} = \frac{E_T^{jet1} e^{-\eta_{jet1}} + E_T^{jet2} e^{-\eta_{jet2}}}{2yE_e}$$

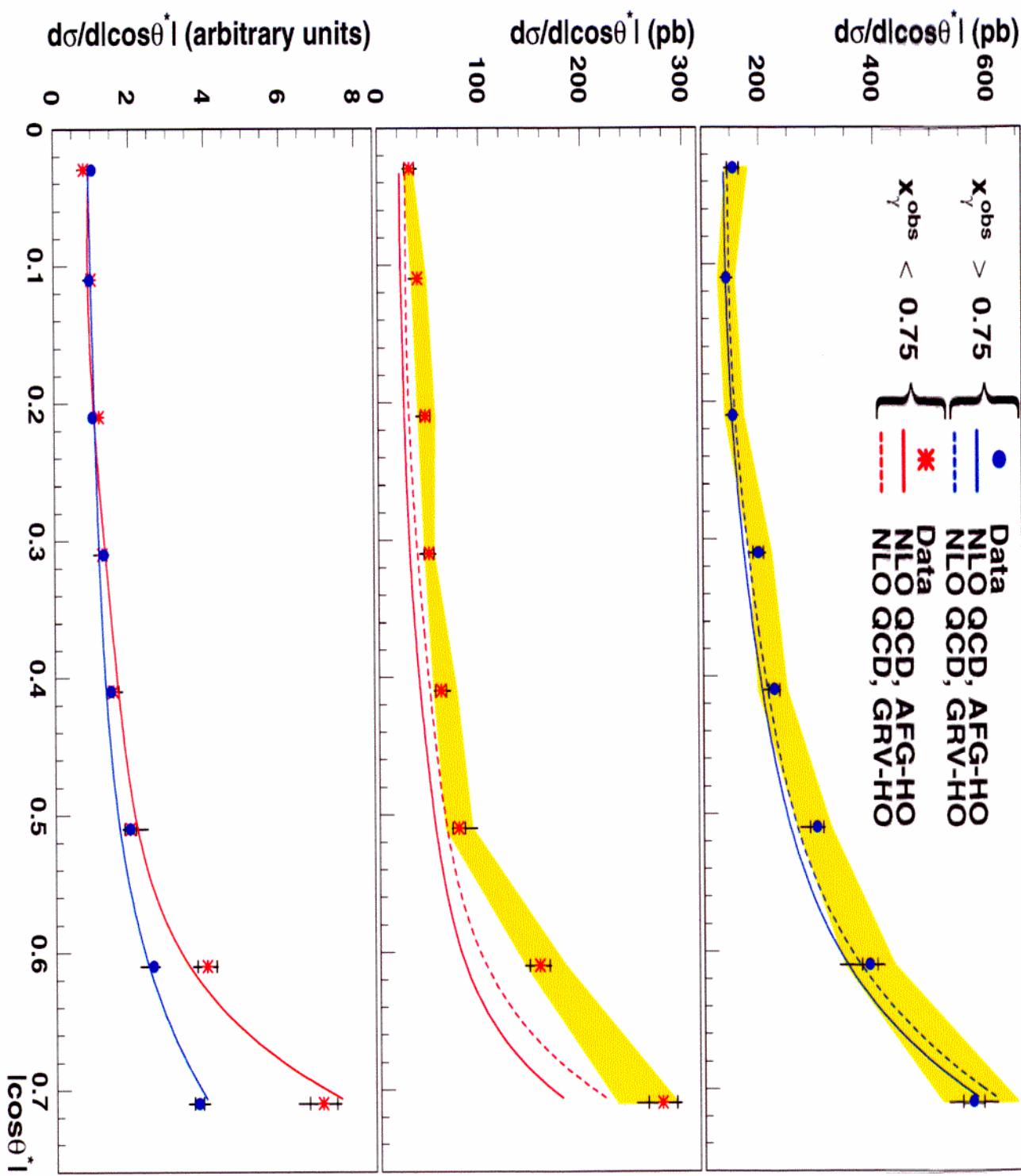
● : pert. QCD vertex

# ZEUS Preliminary



NLO QCD calculations  
reviewed by Harris,  
Klasen, Vossebeld  
[hep-ph/9905348](https://arxiv.org/abs/hep-ph/9905348)

# ZEUS Preliminary 96-97

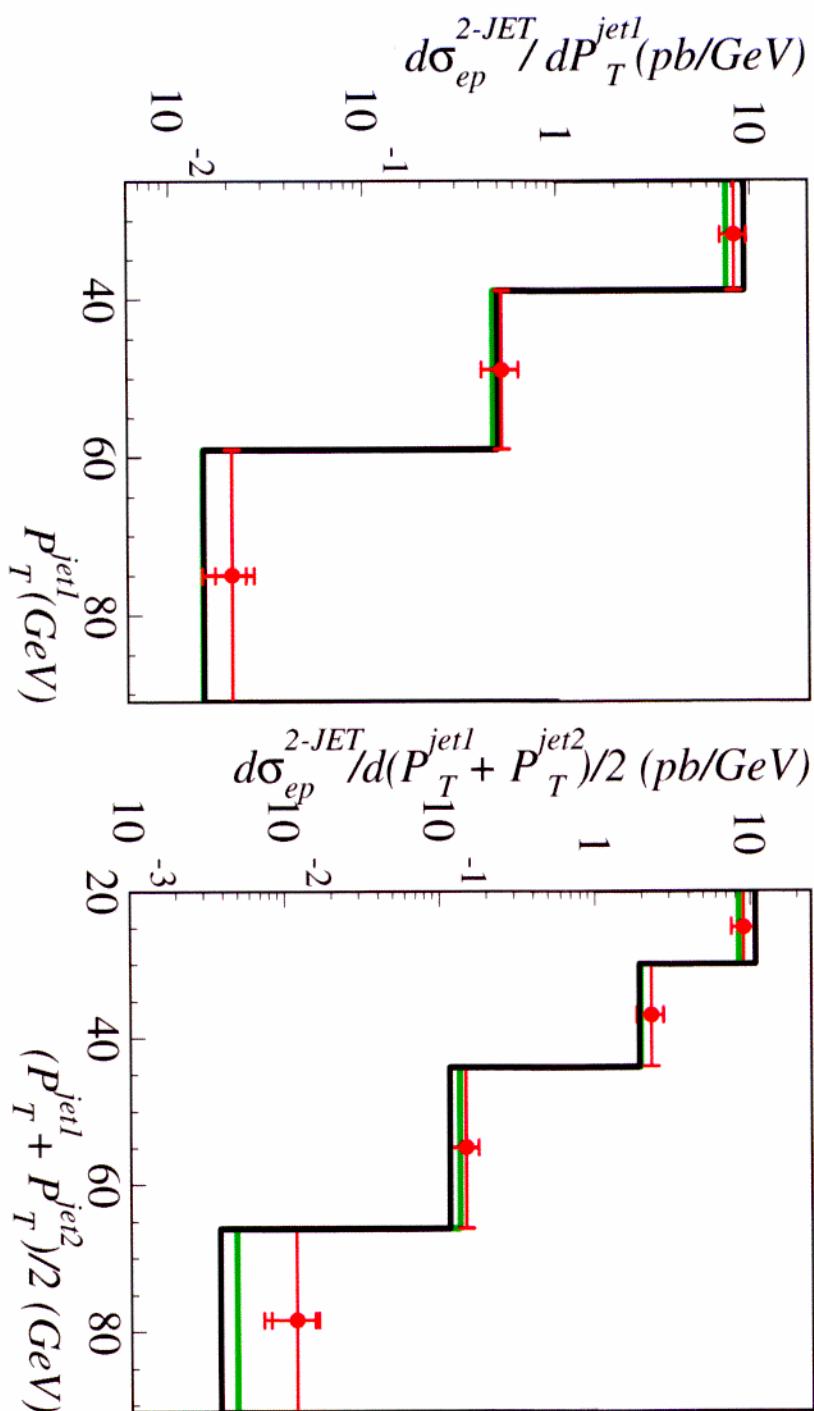


- H1 preliminary
- PYTHIA 5.7 (GRV LO)
- JETVIP NLO (GRV HO)

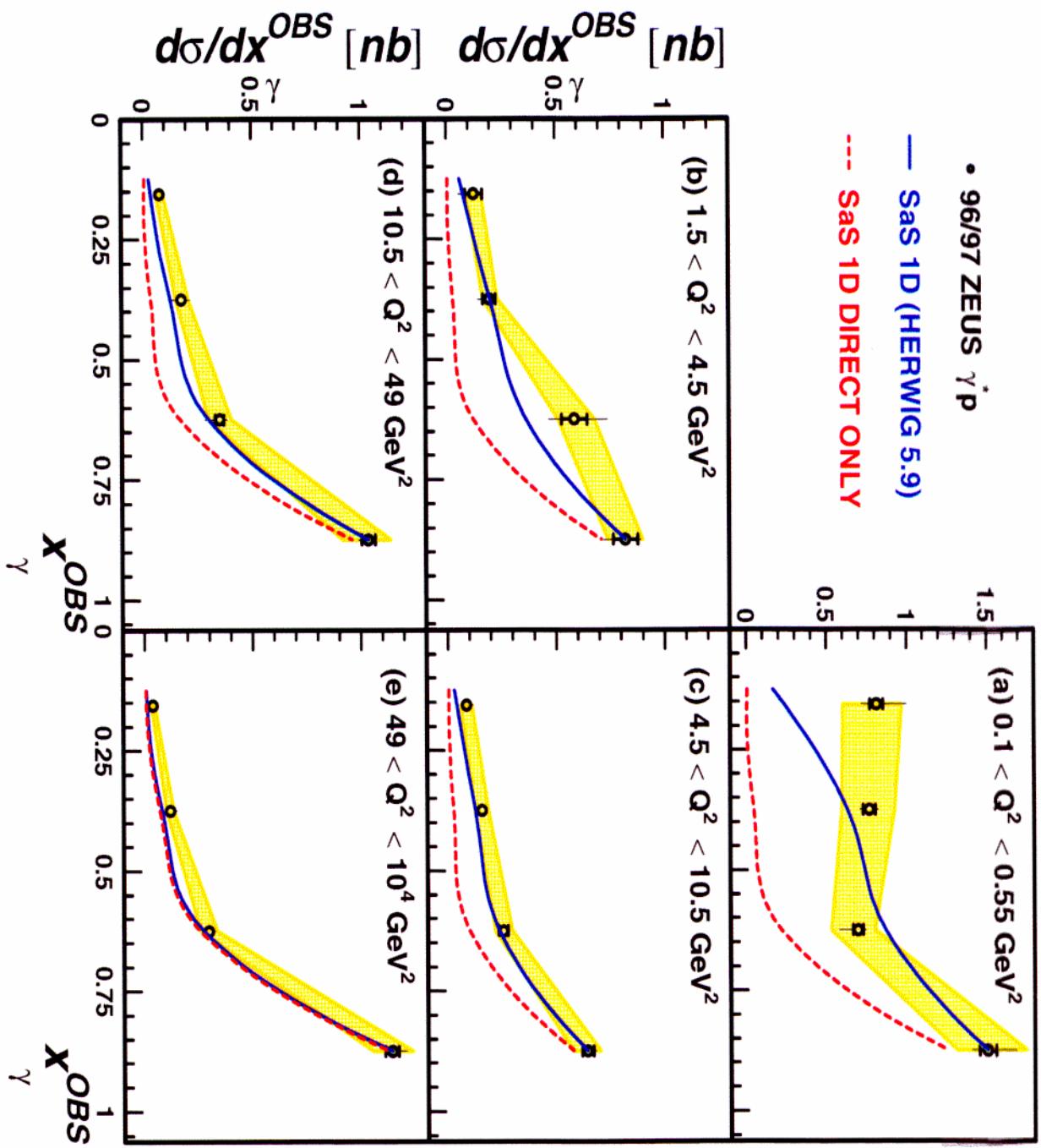
$Q^2 < 4 \text{ GeV}^2, y < 0.9, N^{\text{JETS}} \geq 2$

$P_T^{\text{jet1}} > 25 \text{ GeV}$

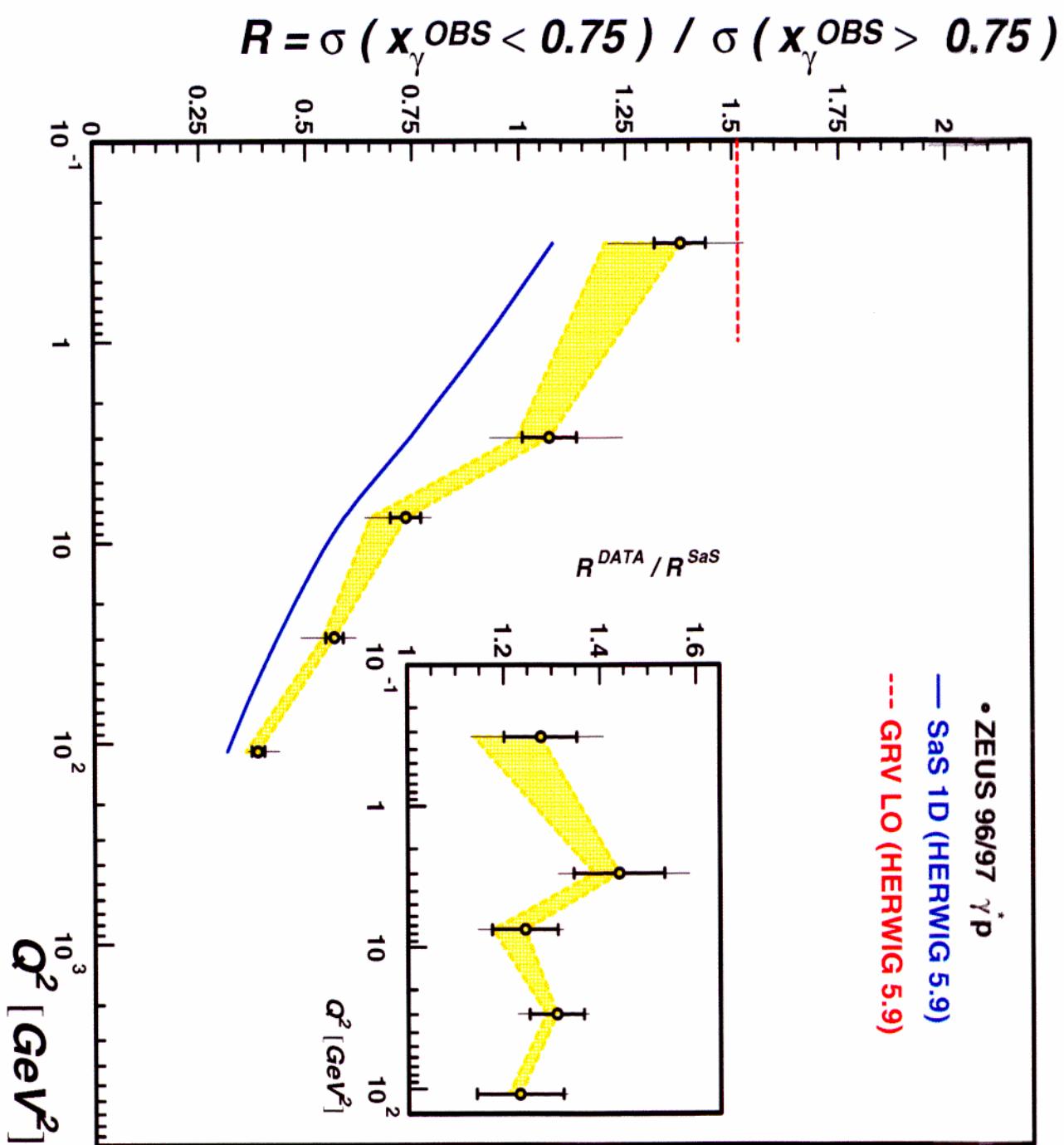
$P_T^{\text{jet2}} > 15 \text{ GeV}$



# ZEUS PRELIMINARY



**ZEUS PRELIMINARY**



## Beauty Photoproduction

(in lowest order: photon-gluon fusion; NLO calculations available)

Frixione, Mangano, Nason, Ridolfi

- H1: inclusive muons in di-jets; impact parameter distribution**  
in limited kinematic range,  $\sigma_{vis}(ep \rightarrow b\bar{b} X \rightarrow \mu X) = 170 \pm 25$  pb  
as compared to NLO QCD prediction  $104 \pm 17$  pb
- ZEUS: inclusive electrons in di-jets**

UA1, CDF, D0 find larger b cross section at colliders than predicted.

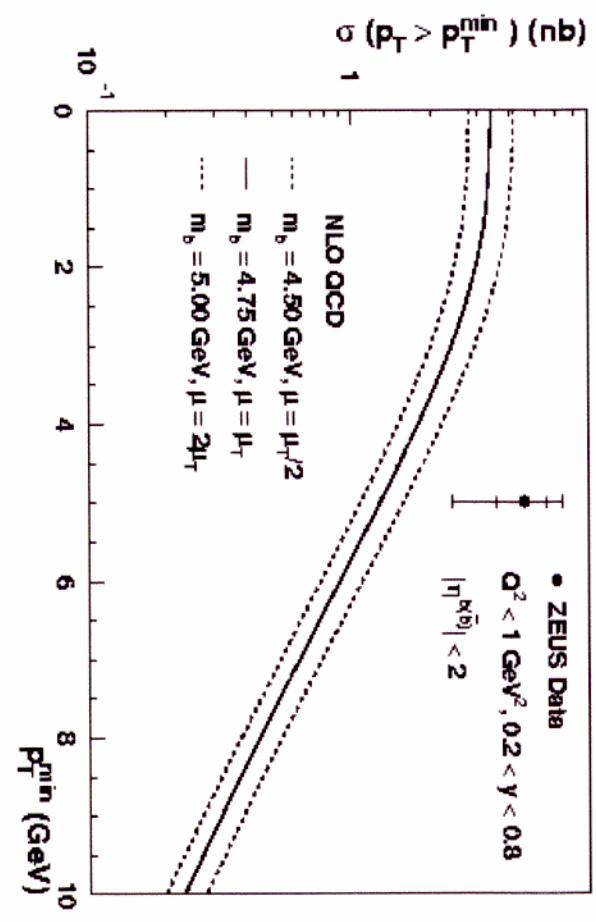


Figure 1.1: The extrapolated  $b\bar{b}$  cross section as a function of the minimum transverse momentum  $p_T^{min}$ . The data point is shown with statistical error (inner bar) and statistical, systematic and extrapolation errors added in quadrature and is compared with predictions from NLO-QCD.

## Conclusions on Photoproduction

- Jet  $p_T$  spectra well described (H1) (at high  $p_T$ , no contradiction with)
  - GRV pdf's for proton and photon      Glueck, Reya, Vogt
- PYTHIA 5.7 event generator (LO)
- JetVip calculations (HO)      Potter
- NLO QCD predictions agree with data for ‘pointlike’ photon (ZEUS)
- NLO QCD predictions below the data for ‘resolved’ photon (ZEUS)
  - AFG(HO) and GRV(HO) photon pdf's
- Aurenche, Fontannaz, Guillet
  - shape of angular distributions correct, normalization not → need improved photon pdf's (i.e. include these data in future fits)
- Di-jet production in  $\gamma^* p$  interactions reveals virtual photon structure
  - SaS photon pdf's   Schuler, Sjostrand
- resolved virtual photon component up to  $Q^2 \sim E_T^2 \sim 49 \text{ GeV}^2$
- $0.1 < Q^2 < 0.55 \text{ GeV}^2$  not well described
  - resolved virtual photon component decreases with  $Q^2$
- Indications that cross section for photoproduction of beauty is larger than theoretical predictions      Frixione, Mangano, Nason, Ridolfi

Neutral current  $e^\pm p$  scattering:

$$\frac{d^2\sigma^{e^\pm p}}{dxdQ^2} = \frac{2\pi\alpha^2}{xQ^4} [Y_+ F_2(x, Q^2) \mp Y_- x F_3(x, Q^2) - y^2 F_L(x, Q^2)]$$

$$F_2(x, Q^2) = x \sum_f A_f(Q^2) [q_f(x, Q^2) + \bar{q}_f(x, Q^2)]$$

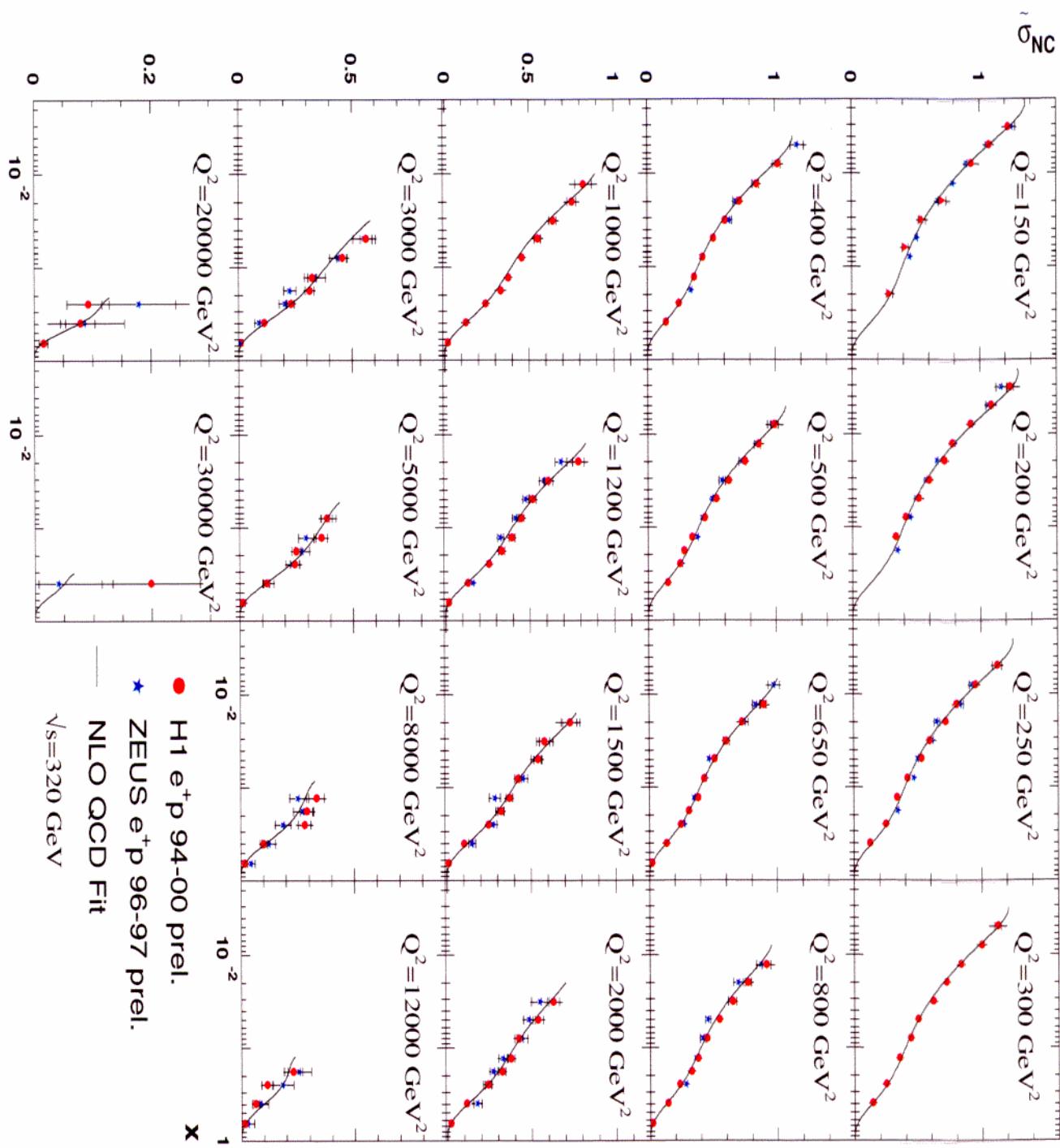
$$xF_3(x, Q^2) = x \sum_f B_f(Q^2) [q_f(x, Q^2) - \bar{q}_f(x, Q^2)]$$

$$A_f(Q^2) = e_f^2 - 2\nu_e \nu_f e_f P_Z + (\nu_e^2 + a_e^2)(\nu_f^2 + a_f^2) P_Z^2$$

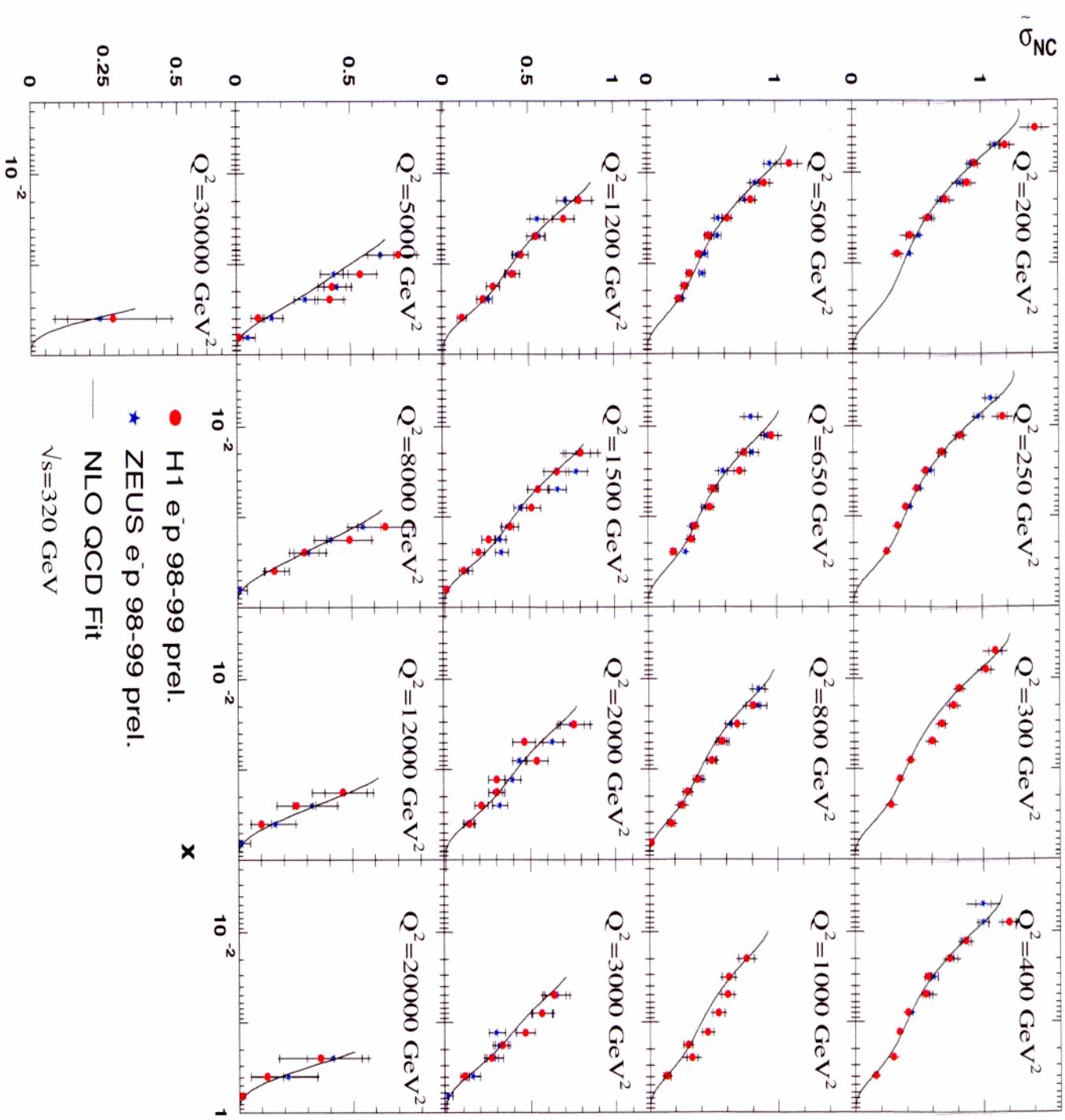
$$B_f(Q^2) = -2a_e a_f e_f P_Z + 4\nu_e \nu_f a_f P_Z^2$$

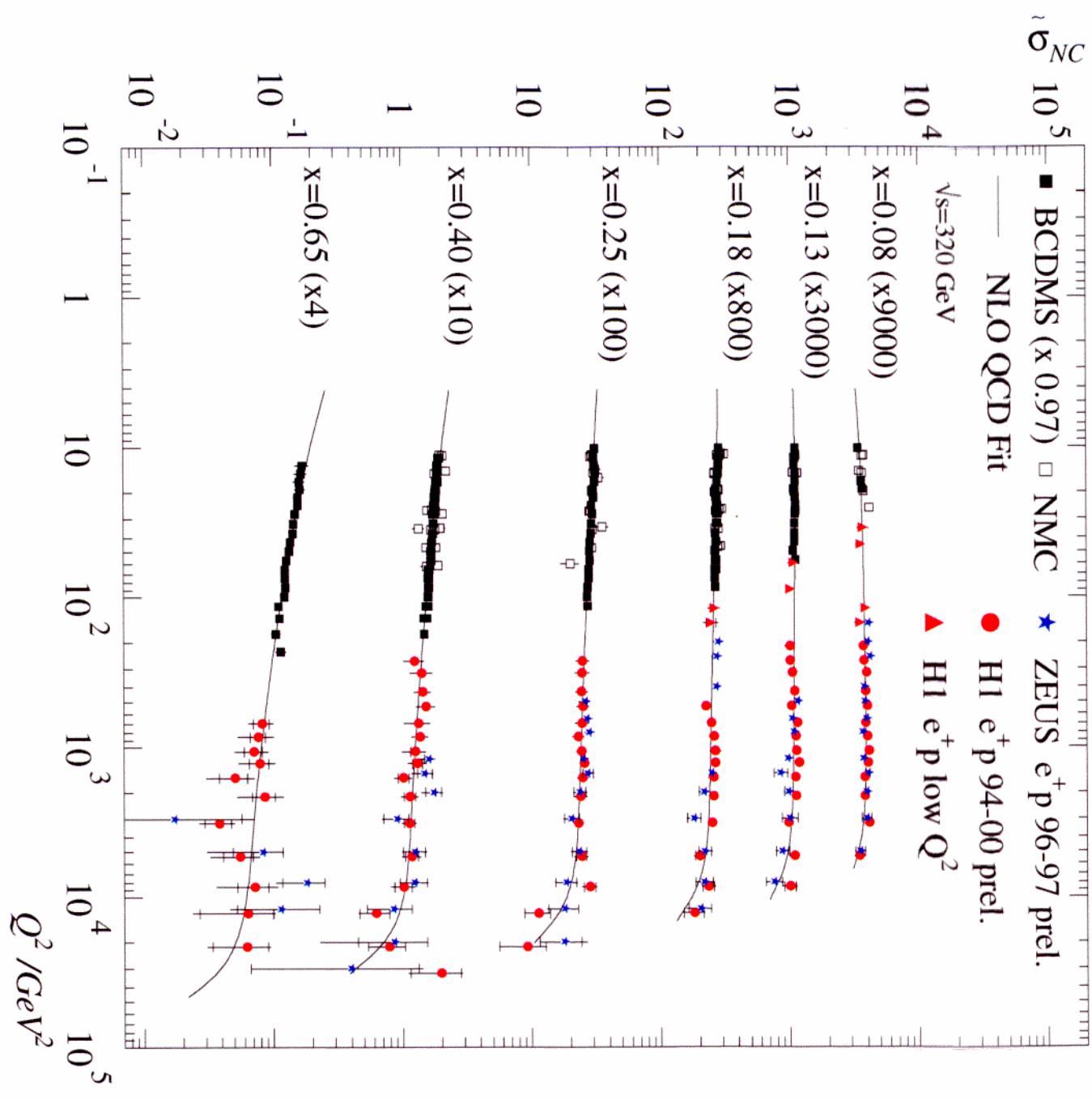
$$P_Z = \frac{1}{4\sin^2\theta_W \cos^2\theta_W} \frac{Q^2}{Q^2 + M_Z^2}$$

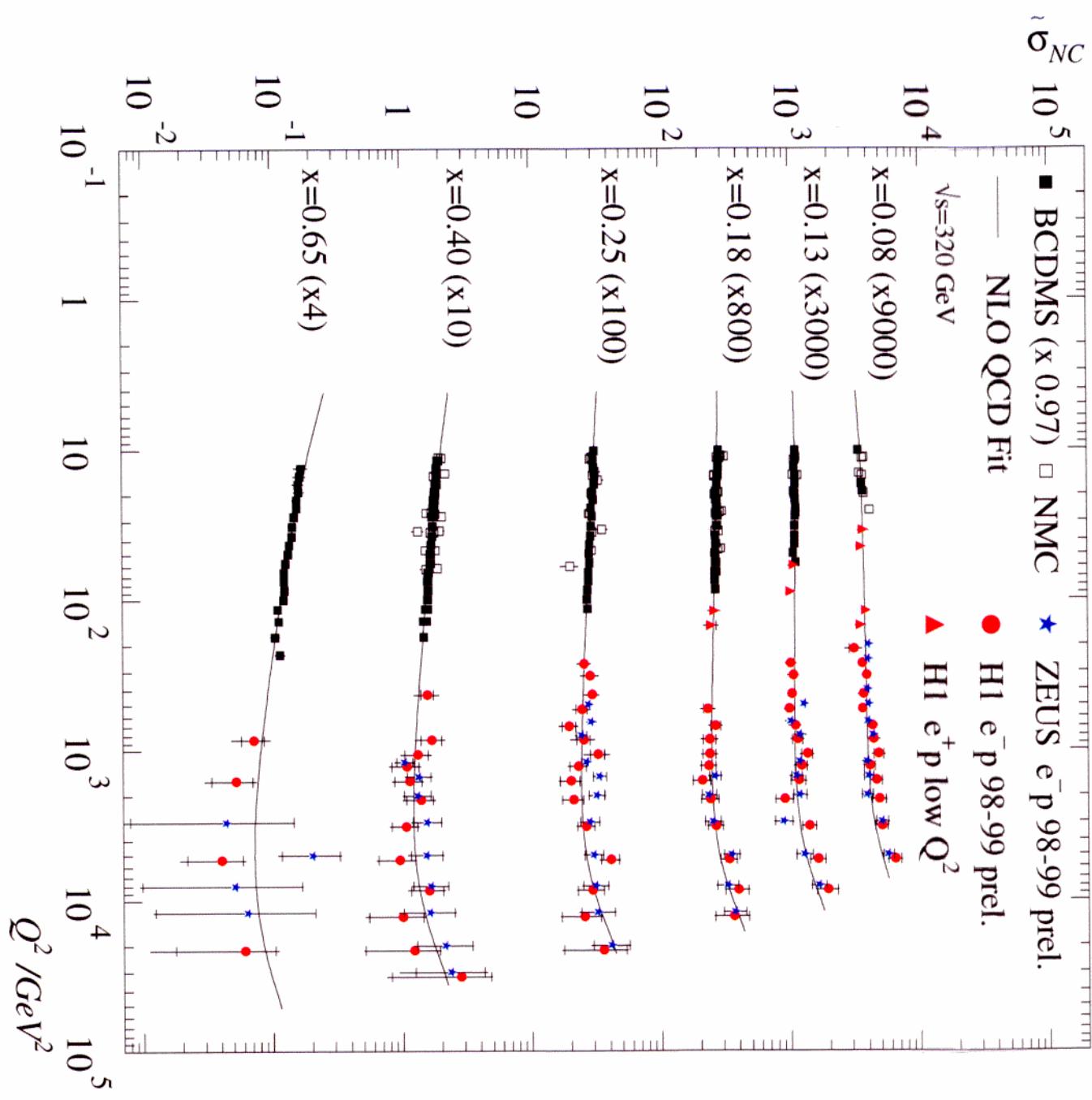
## Reduced cross section



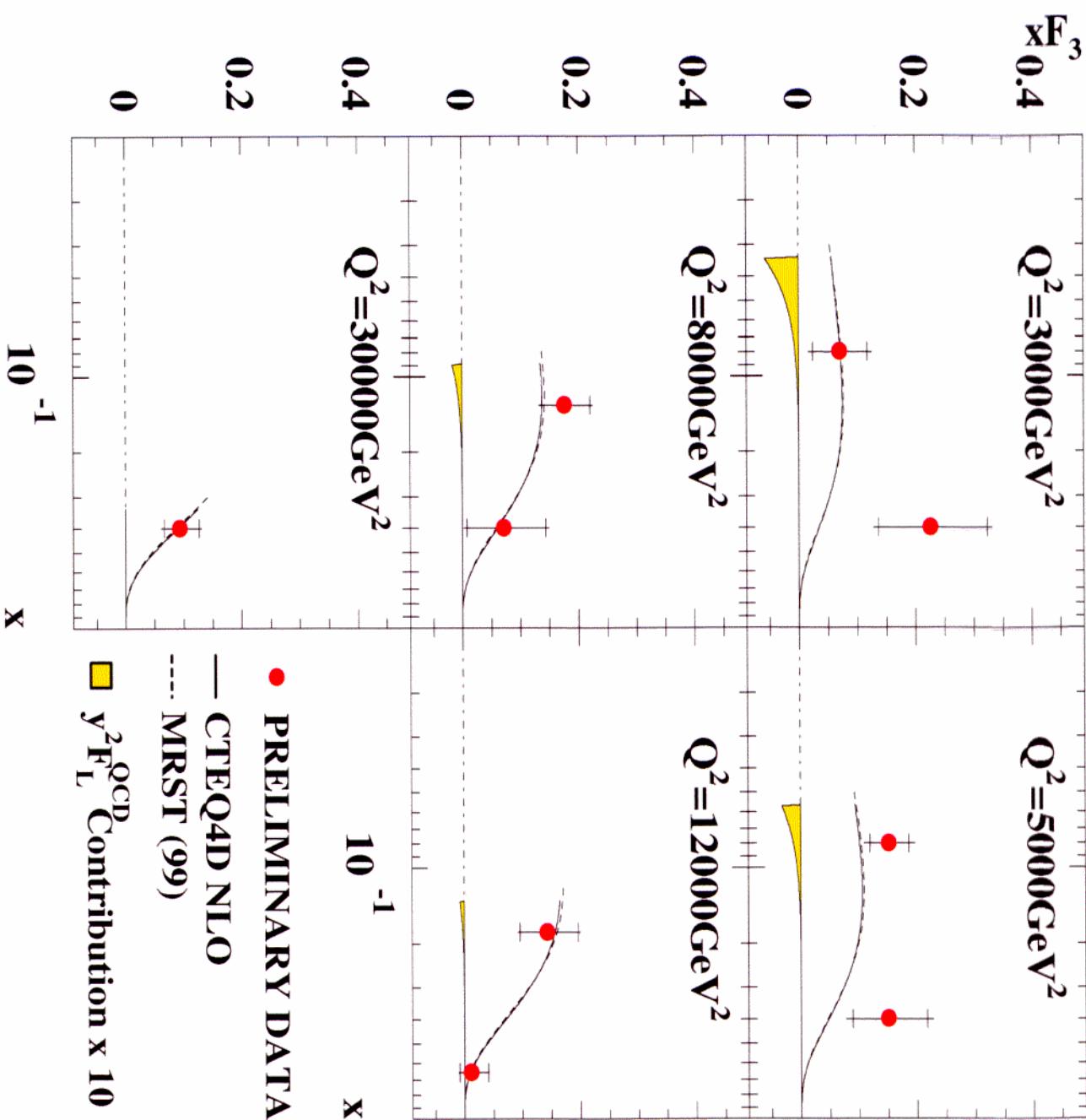
## Reduced cross section



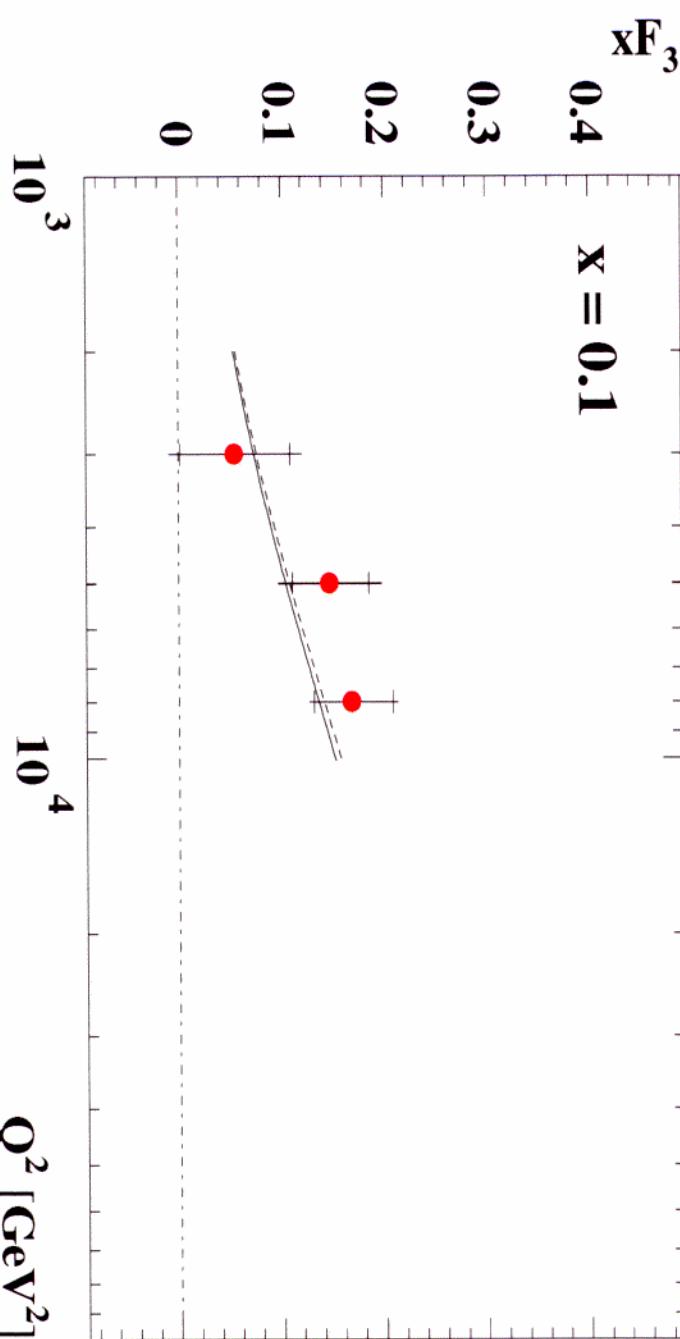
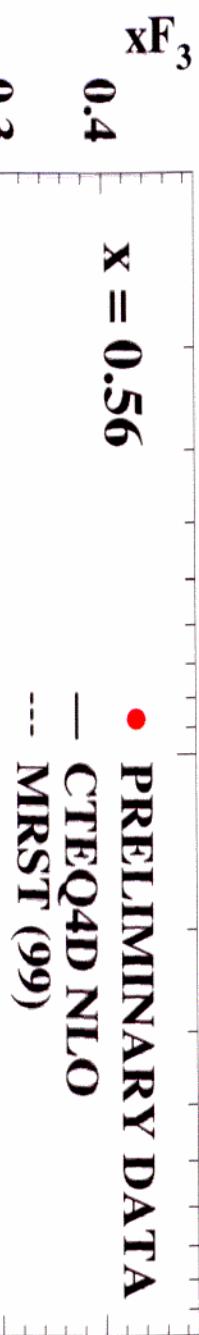




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## Charged Current Scattering:

$$\frac{d^2\sigma^{e^- p \rightarrow \nu_e X}}{dxdQ^2} = \frac{G_F^2}{2\pi x} \left( \frac{M_W^2}{M_W^2 + Q^2} \right)^2 [xu + xc + (1-y)^2(x\bar{d} + x\bar{s})]$$

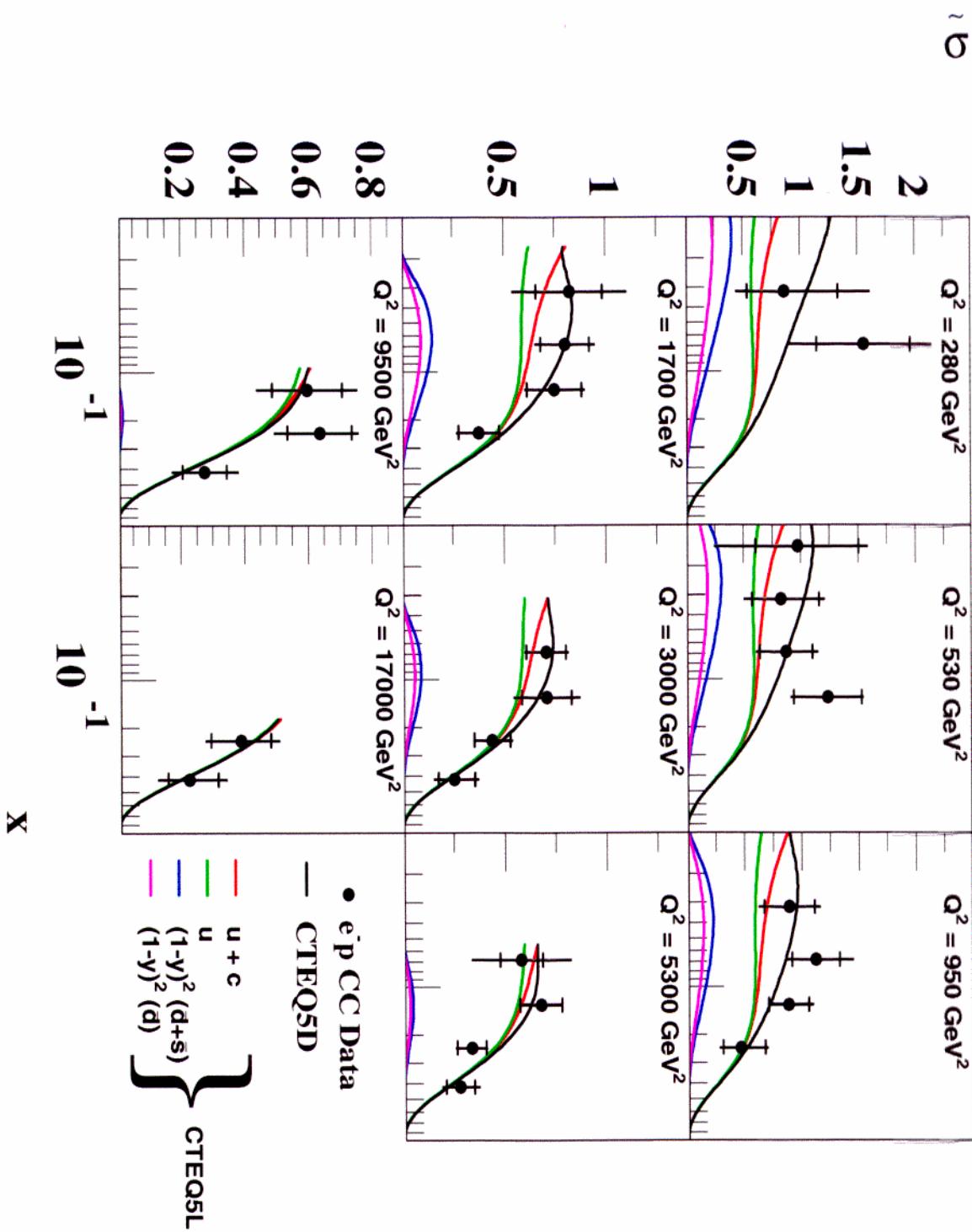
For  $e^+p$  CC scattering replace (u,c) by anti-(u,c) and anti-(d,s) by (d,s)

Reduced double-differential cross-sections:

$$\tilde{\sigma}^{e^- p \rightarrow \nu_e X} = \left[ \frac{G_F^2}{2\pi x} \left( \frac{M_W^2}{M_W^2 + Q^2} \right)^2 \right]^{-1} \frac{d^2\sigma}{dxdQ^2} = x[u + c + (1-y)^2(\bar{d} + \bar{s})]$$

$$\tilde{\sigma}^{e^+ p \rightarrow \bar{\nu}_e X} = x[\bar{u} + \bar{c} + (1-y)^2(d + s)]$$

# ZEUS Preliminary 1998-99



## Conclusions

HERA offers excellent possibilities for studying (p)QCD

- measurements of structure functions over large range in  $x$  (down to  $\leq 10^{-5}$ ) and  $Q^2$  (up to  $10^5 \text{ GeV}^2$ )
- quantitative study of scaling violations
- measurement of gluon density function
- charm production in DIS
- diffractive DIS
- jet production in DIS and measurement of  $\alpha_s$
- photoproduction and photon structure

Progress in modeling of transition into low  $x$ , low  $Q^2$  region: CFFM evolution;  
 $\gamma^*(\text{dipole})p$  cross section & saturation

## Outlook

HERA upgrade during shutdown 2000-2001 (luminosity \*5)

Detector upgrades (Si  $\mu$ VTX)

- charm (beauty) in photoproduction and DIS
- high  $Q^2$  (and high  $x$ ) structure functions and pdf's
- $\rightarrow$  and  $\leftarrow$  polarised  $e^+$  and  $e^-$  beams