

Dirac vs Majorana

Now that neutrinos appear massive



because $m_\nu \neq 0$, $v < c$



you can pass it
and look back



what is this state??

two possibilities:

Dirac neutrino

This is a new state:

"right-handed neutrino"

We didn't know this state existed
but it must be there.

Majorana neutrino

This is a known state:

"right-handed anti-neutrino"

We thought $\nu + \bar{\nu}$ are different, but
they must be the same particle (L violation)

What about massive particles? e, u, d, μ, \dots

CC weak interaction acts

only on left-handed particles

appears inconsistent if massive

Resolution in the Standard Model:

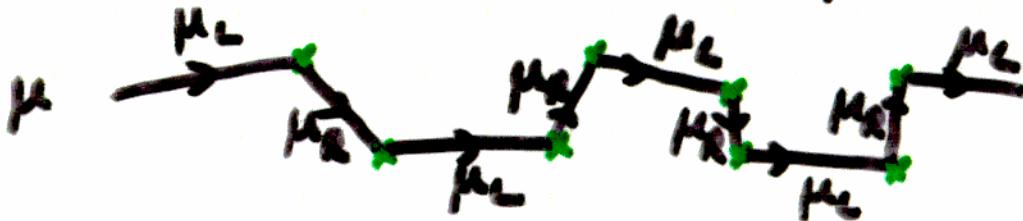
Universe is filled with Higgs boson

⇒ left-handed + right-handed mix

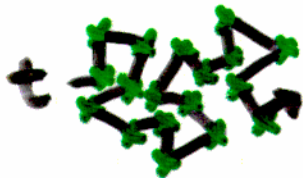


0.511 MeV/c²

doesn't bump too often

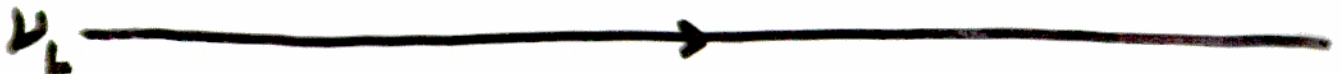


105 MeV/c²



175,000 MeV/c²

bumps all the time



no ν_R ⇒ no way to bump + mix
⇒ massless

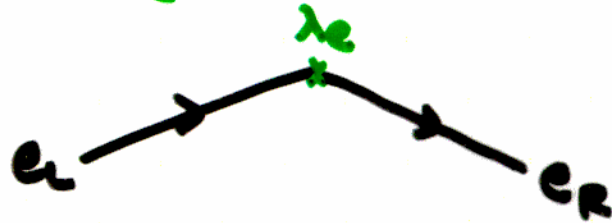
quarks, leptons:

e.g. $[(e^-)_L, (e^*)_R]$

$[(e^-)_R, (e^*)_L]$

mix due to Higgs

$$m_e = \lambda_e v$$



they are all Dirac type

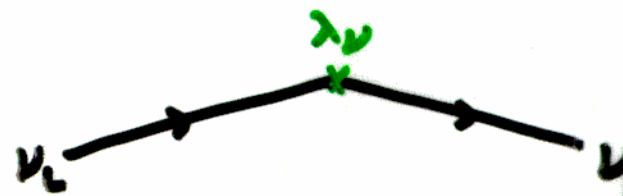
Dirac neutrinos?

$$[(\nu)_L, (\bar{\nu})_R]$$

NEW: $[(\nu)_R, (\bar{\nu})_L]$

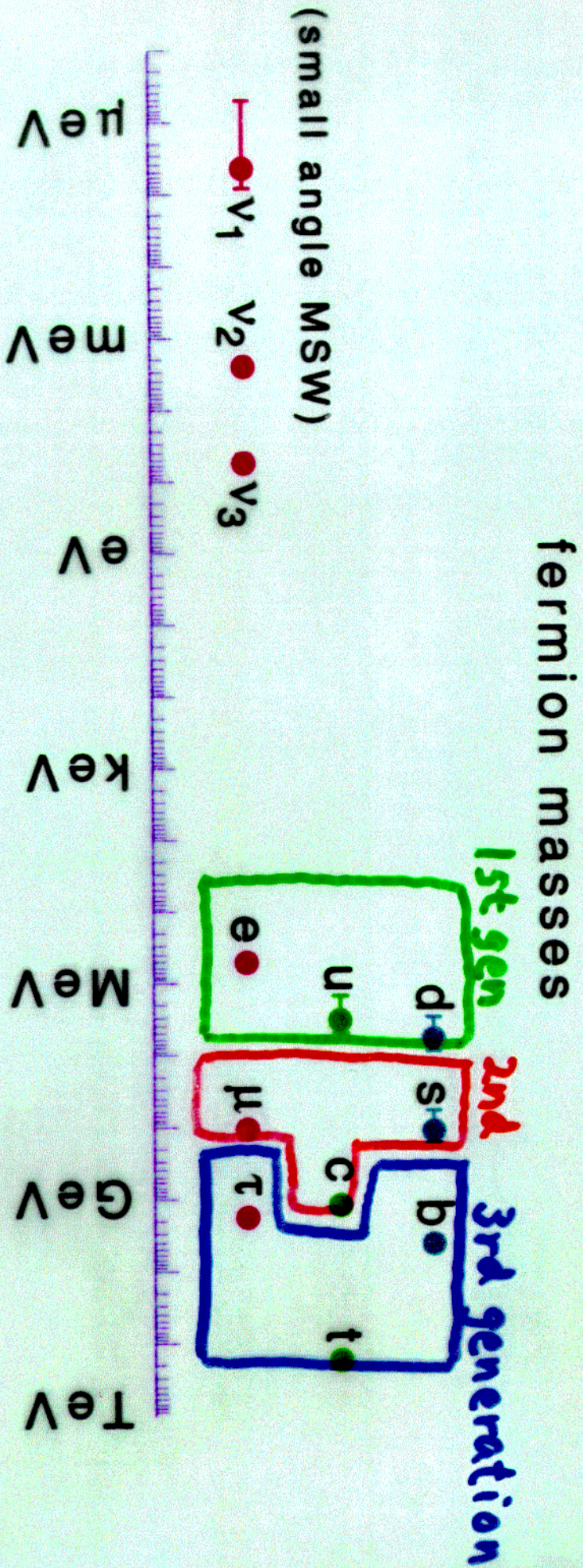
↕ mix

$$m_\nu = \lambda_\nu \bar{\nu}$$



⇒ naively, we expect

$$m_\nu \sim m_e \sim m_\mu$$



$< 10^{-12}$

\times
 \ll

hard to accept this unless
 \exists reason why $h_\nu \ll h_e, h_g$ esp. 3rd gen

Theoretical bias against light ν_R

$SU(3)_C \times SU(2)_L \times U(1)_Y$ gauge int.

$$Q_L \quad (3, 2, \frac{1}{6})$$

$$u_R \quad (3, 1, \frac{2}{3})$$

$$d_R \quad (3, 1, -\frac{1}{3})$$

$$L_L \quad (1, 2, -\frac{1}{2})$$

$$e_R \quad (1, 1, -1)$$

$$\nu_R \quad (1, 1, 0) \leftarrow$$

no gauge int. at all!

need $\mathcal{L} \ni \lambda_e \bar{L}_L e_R H \Rightarrow m_e = \lambda_e v$

can understand why $m_e < v \ll M_{Pl}$

can write $\mathcal{L} \ni M \nu_R \nu_R$

M does not have to be small

why not $M \sim M_{Pl}$?

Seesaw mechanism

ν_R can be heavy

$M \gg \nu$

not allowed due to gauge inv.

$$\mathcal{L} \ni (\bar{\nu}_L \ \nu_R) \begin{pmatrix} 0 & m_D \\ m_D & M \end{pmatrix} \begin{pmatrix} \bar{\nu}_L \\ \nu_R \end{pmatrix}$$

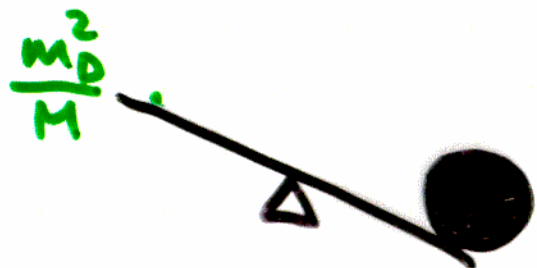
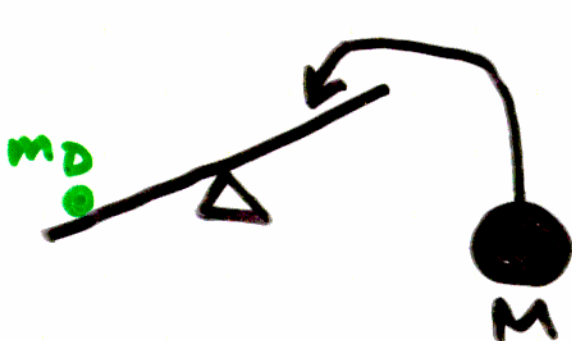
expect $m_D \sim m_t$ for 3rd gen.

two eigenvalues:

$$M, \quad -\frac{m_D^2}{M}$$

if $M \gg \nu$

\Rightarrow naturally explains why neutrinos light



Yanagida
Gell-Mann, Ramond,
Slansky

three generations:

$$-\frac{m_D^2}{M} \Rightarrow - (m_D) (M)^{-1} (m_D)^T$$

m_D, M 3×3 matrices

SO(10) GUT

$$\underline{16} = \begin{pmatrix} u_L & u_L & u_L & \nu_L \\ d_L & d_L & d_L & e_L \\ u_R & u_R & u_R & \nu_R \\ d_R & d_R & d_R & e_R \end{pmatrix}$$

all fermions in a single multiplet

SO(10): the smallest anomaly-free gauge group with chiral fermions

$$SO(10) \rightarrow SU(3) \times SU(2) \times U(1) \quad \langle \phi \rangle = M_{GUT}$$

$$\mathcal{L} \ni \phi \nu_R \nu_R \Rightarrow M \sim M_{GUT}$$

$$\text{cf. if } m_{\nu_3} = (\Delta m_{\oplus}^2)^{1/2} \simeq 0.05 \text{ eV}$$

$$\simeq \frac{m_t^2}{M}$$

$$\Rightarrow M \simeq 10^{15} \text{ GeV}$$

Possible reasons why $h\nu < 10^{-12}$

However, "naive $SO(10)$ " dead

$$\mathcal{L} \ni 16 \ 16 \ H$$

$$\underline{\lambda_u \sim \lambda_d \sim \lambda_q \sim \lambda_\nu}$$

all hierarchical
small mixing

$$M \sim M_{GUT} \begin{pmatrix} 1 & \\ & \dots \end{pmatrix}$$

$$(m_\nu) = (\lambda_\nu v) M^{-1} (\lambda_\nu^T v)$$

$$\sim \frac{v^2}{M_{GUT}}$$

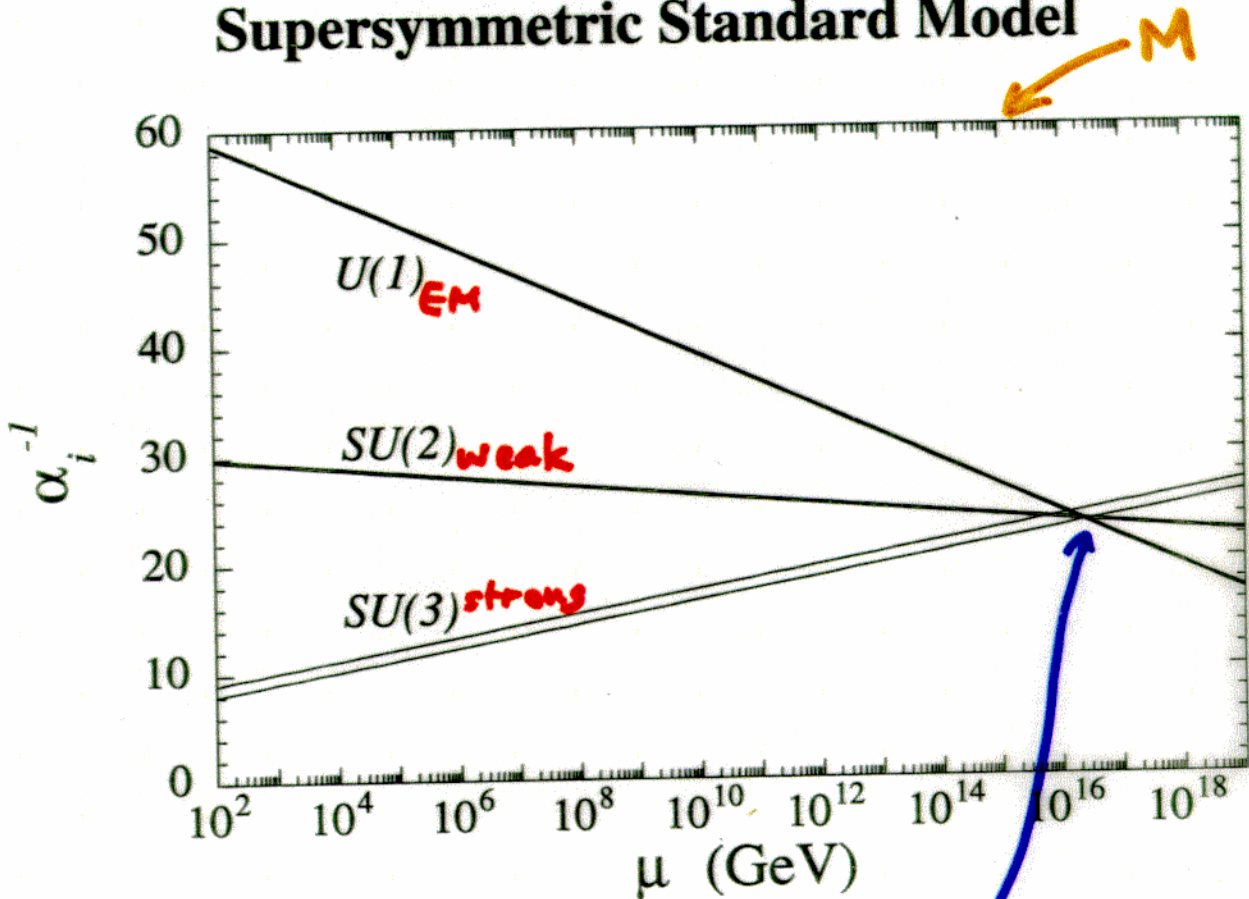
$$\underline{\lambda_\nu \lambda_\nu^T}$$

also hierarchical
small mixing

Super K killed it!

⇒ "not-so-naive $SO(10)$ "
alternative ideas

Supersymmetric Standard Model

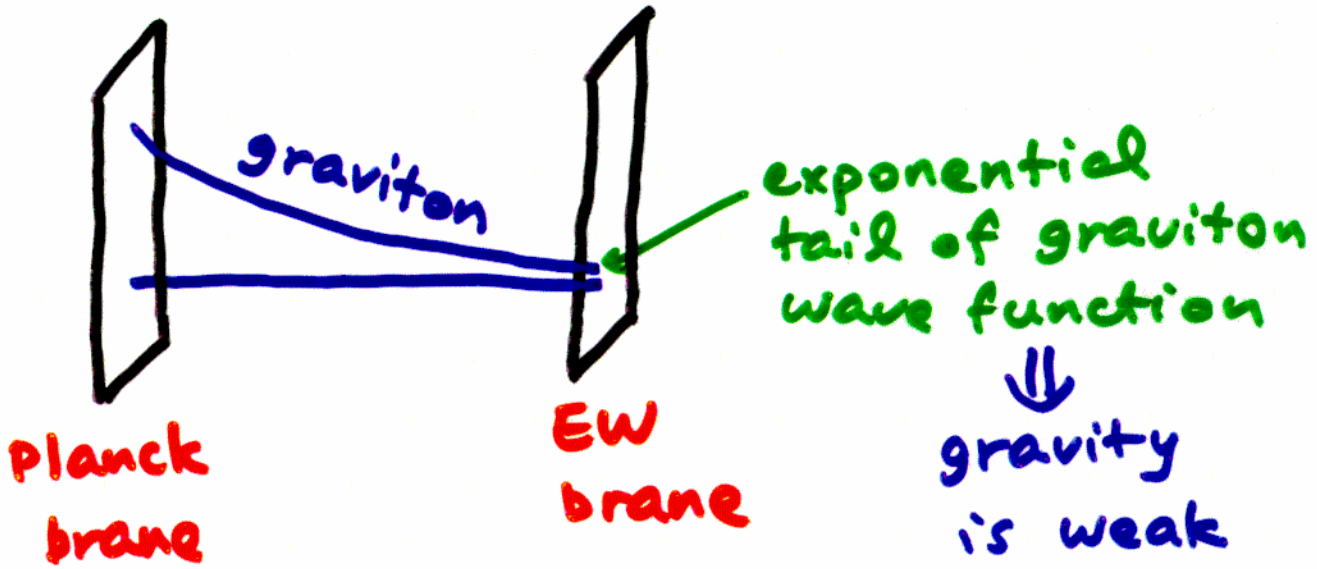


Grand Unification?

Dimopoulos
Raby
Wilczek

Dine
Fischler

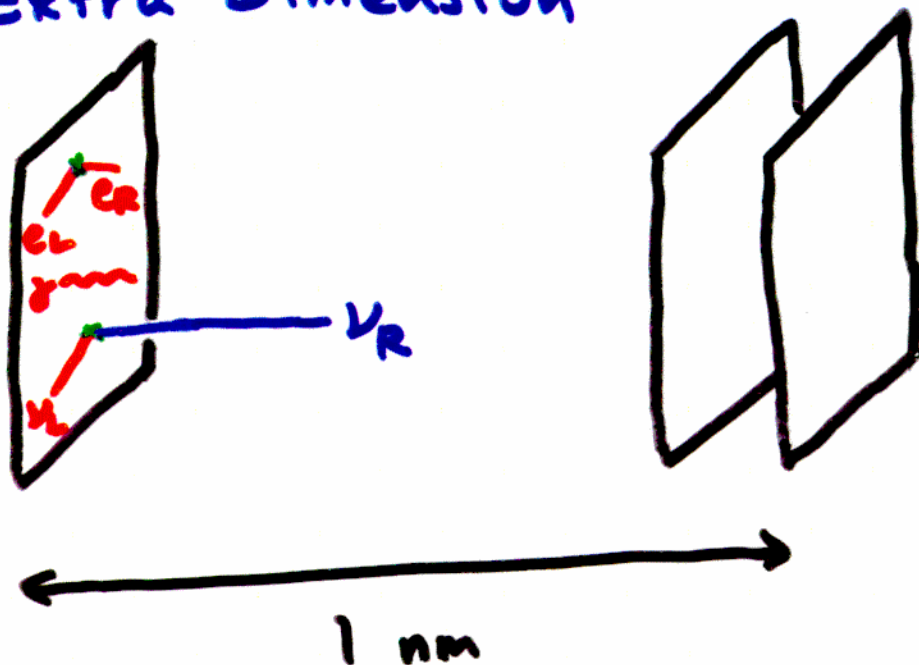
Warped Extra Dimension



V_R Yukawa
is weak

Grossman, Neubert

Large Extra Dimension



even if $h_\nu \sim h_t \sim O(1)$

V_R is spread out and doesn't
come on top of our brane so often

all particles with gauge interaction
confined on the brane

but V_R is gauge singlet

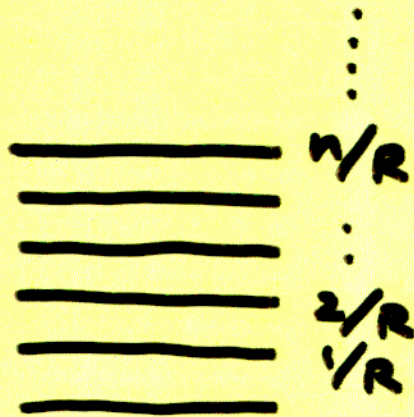
is allowed to escape from
the brane

Dienes,
Dudas,
Gherghetta

Arkani-Hamed, Dimopoulos,
Dvali, March-Russell

not only

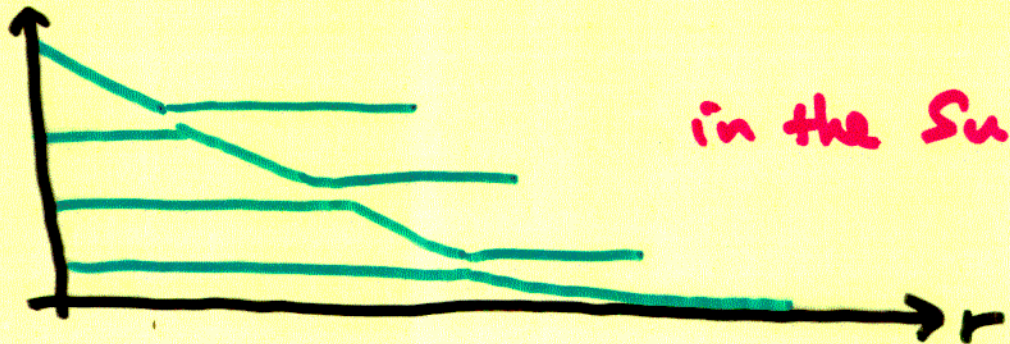
$\exists \nu_R$ in addition to ν_L



energy levels
= mass

infinite tower of
light sterile neutrinos

Dvali, Smirnov



MSW multiple resonances

Protected by new symmetries

e.g. new $U(1)$ charge + SUSY

$$U(1)_L \times U(1)_N \rightarrow U(1)_L$$

$$L (1, 0) \rightarrow 1$$

$$N (0, -1) \rightarrow -1$$

$$\chi (1, -1) \rightarrow 0 \quad \langle \chi \rangle \neq 0$$

$$\int d^4\theta \frac{\chi^\dagger}{M_{Pl}^2} L N H_u$$

$$\Rightarrow h\nu \sim \frac{m_{SUSY}}{M_{Pl}}$$

\tilde{N} : right-handed sneutrinos ξT_{el}
may even be dark matter

Arkani-Hamed,
Hall,
HM,
Smith,
Weiner

if L further violated

e.g. $U(1)_{B-L}$ gauged

broken $\sim \text{TeV}$

$\langle \phi \rangle \neq 0$

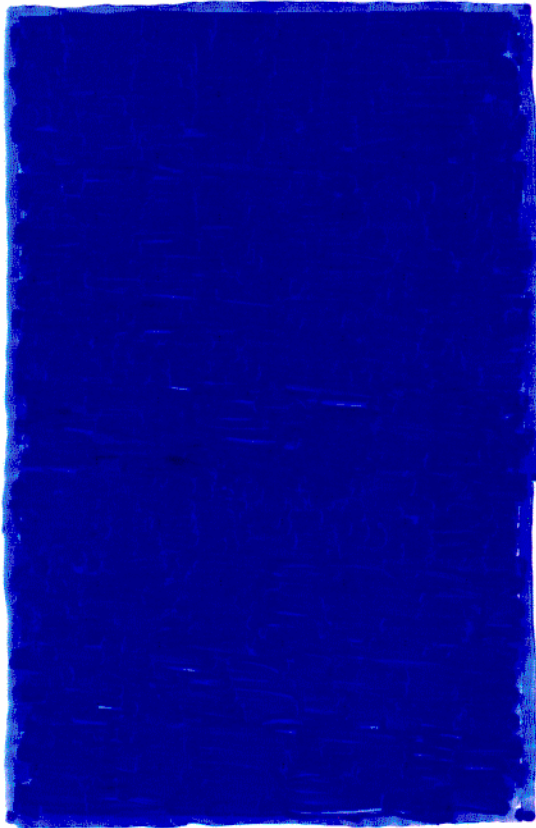
$B-L = 1$

$$\mathcal{L} \ni \frac{\phi\phi}{M_{\text{pl}}} NN$$

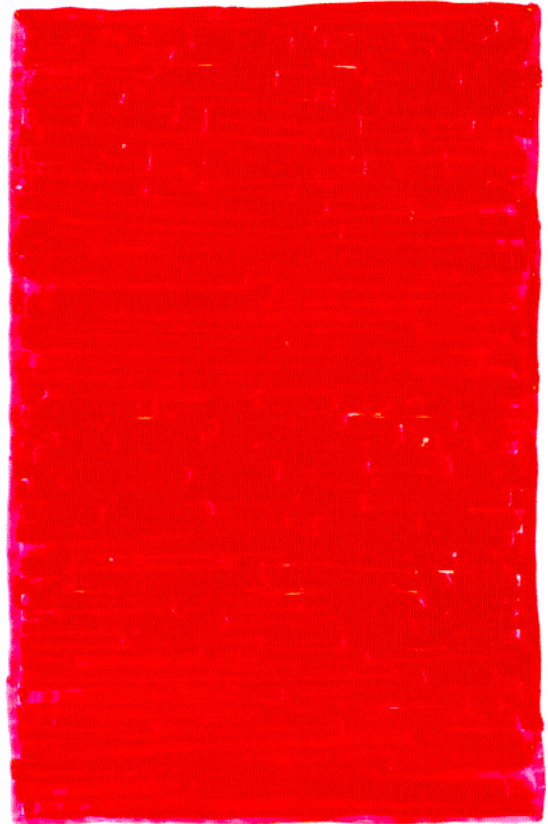
$\left. \begin{array}{l} 3 \text{ } N\text{'s} \\ 3 \text{ } \nu_L\text{'s} \end{array} \right\} \text{all mix}$

\Rightarrow $\begin{array}{l} 3 \text{ active} \\ 3 \text{ sterile} \end{array}$ neutrinos

g
10,000,000,00



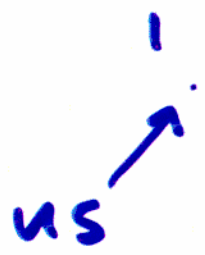
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Early Universe

$T \gtrsim 1 \text{ GeV}$

cosmic baryon asymmetry

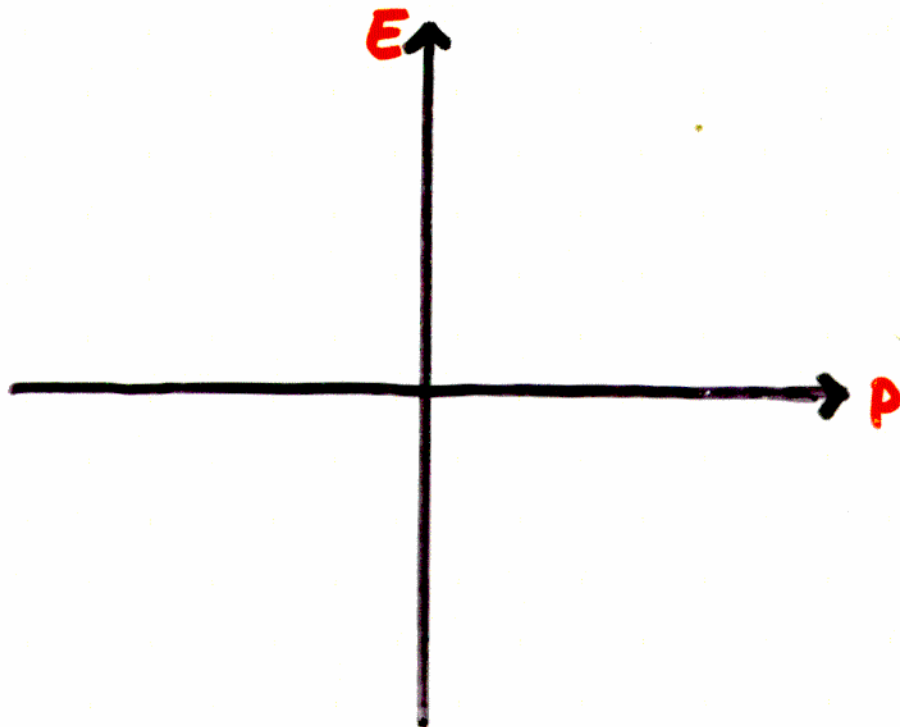


now

lepton-number violation

\Rightarrow SM baryon-number violation

$$i \gamma^\mu (\partial_\mu - ie W_\mu) \psi = 0 \quad \text{Dirac eq.}$$



$T > 200 \text{ GeV}$

W massless \sim EM field

"W-plasma" W always

ends up w/ a gauge equivalent config.

creates $\Delta L_L = \Delta B_L = \Delta Q_L = \Delta S_L = 1$

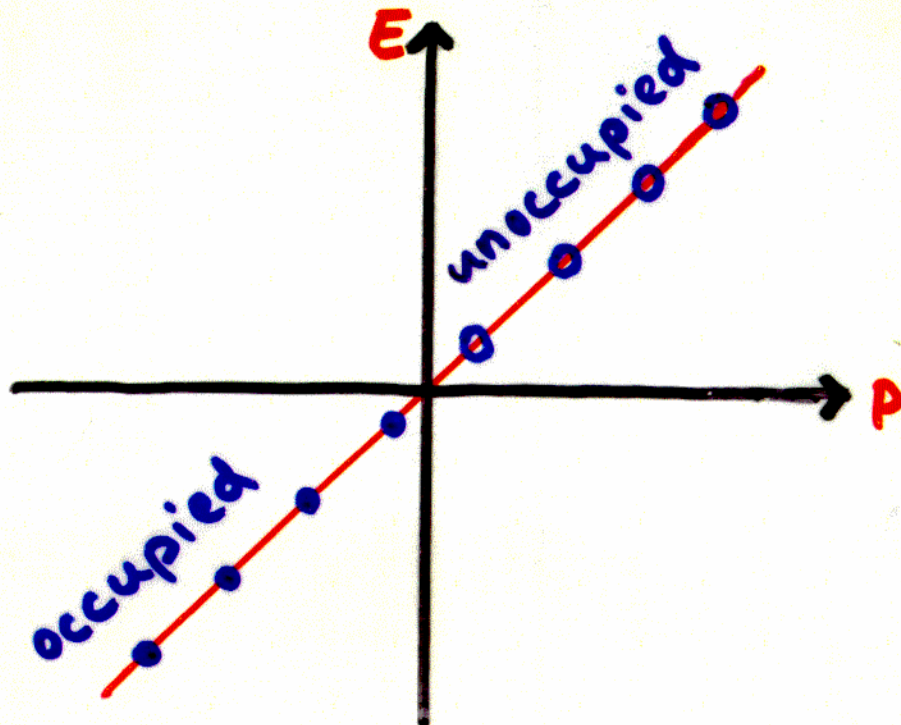
violates $B+L$, preserves $B-L$

+ Majorana ν : \Downarrow violates $B-L$
 "anomaly"

lepton-number violation

\Rightarrow SM baryon-number violation

$$i \gamma^\mu (\partial_\mu - ie W_\mu) \psi = 0 \quad \text{Dirac eq.}$$



$T > 200 \text{ GeV}$

W massless \sim EM field

"W-plasma" W always fluctuate

ends up w/ a gauge equivalent config.

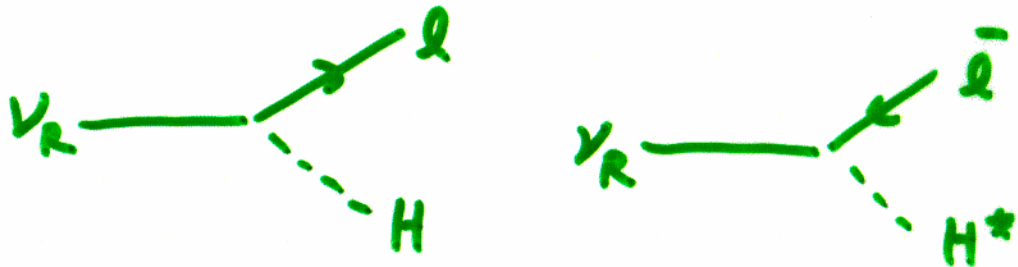
creates $\Delta L_L = \Delta \bar{L}_L = \Delta \bar{L}_R = \Delta L_R = 1$

violates $B+L$, preserves $B-L$

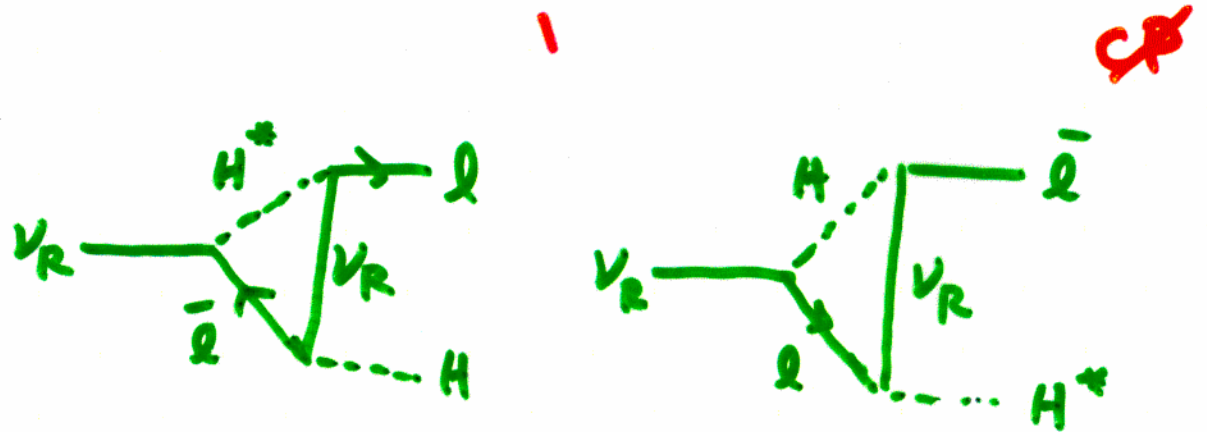
+ Majorana ν : \Downarrow violates $B-L$
 "anomaly"

Leptogenesis

Fukugita, Yanagida

 ν_R 's in thermal equilibrium⊙ $T > M$ once $T < M$, ν_R 's no longer produced

$$\Gamma(\nu_R \rightarrow l H) = \Gamma(\nu_R \rightarrow \bar{l} H^*)$$



decay of ν_R produces net $L \neq 0$

lepton number created

⇓ SM anomaly

chemical equilibrium between $B \neq L$

$$B \approx 0.35 (B-L)$$

$$L \approx -0.75 (B-L)$$

baryon asymmetry created

CP in ν sector may explain
cosmic baryon asymmetry

caveat there are three CP phases
relevant to this issue, but
only one of them can affect
 ν oscillation.

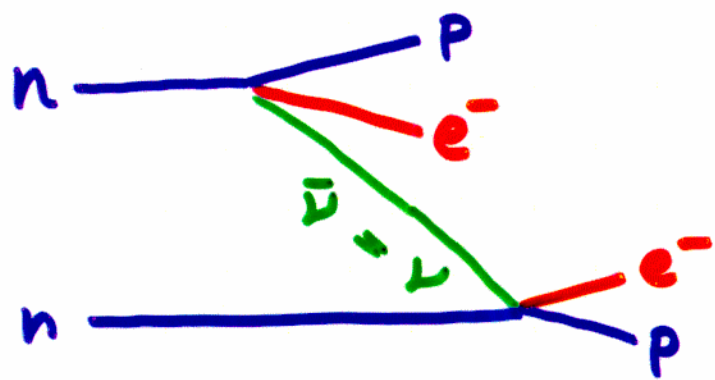
MODELS

seesaw mechanism

⇒ Majorana neutrinos

⇒ lepton number violation

$0\nu\beta\beta$ (neutrinoless double beta) decay?



$$(A, Z) \longrightarrow (A, Z+2) + e^- + e^- + 0\nu$$

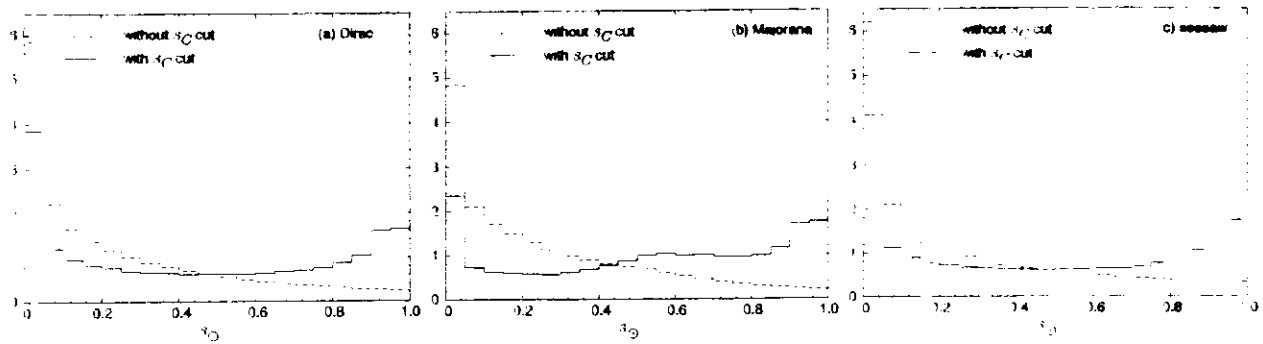


FIG. 3. Plots of the normalized, binned distributions of s_0 for Dirac (a), Majorana (b), and seesaw (c) cases. The distribution after imposing the s_0 cut (solid) shows a greater preference for large s_0 compared with the original distribution (dashed).

symmetry models, there is no reason to expect M_3 is particularly small, and long baseline experiments which probe Δm_{ν}^2 , such as K2K and MINOS, will likely see large signals in $\bar{\nu}_e$ appearance. If Δm_{ν}^2 is at the lower edge of the current Superkamiokande limit, this could be seen at a future extreme long baseline experiment with a muon source. Furthermore, in this scheme Δm_{ν}^2 is large enough to be probed at KamLAND, which will measure large ν_e disappearance.

ACKNOWLEDGMENTS

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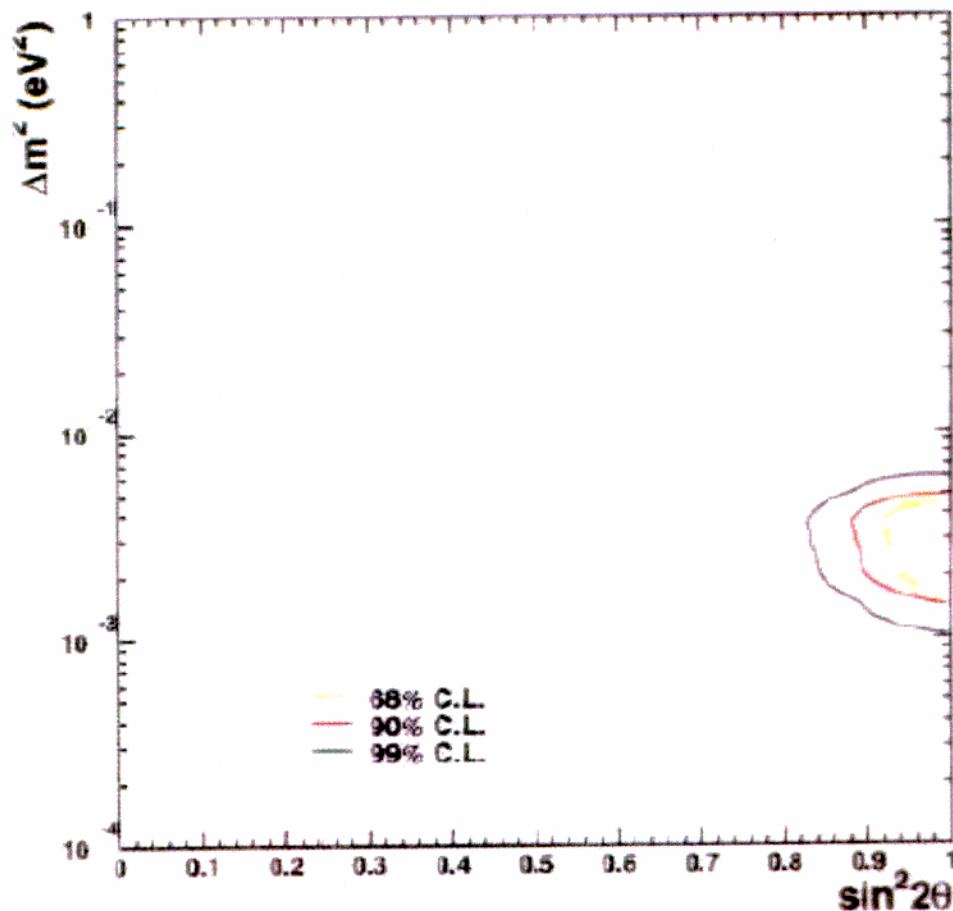
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FC, PC, UpMu

$$\nu_{\mu} = \nu_{\tau}$$



Result of Oscillation Analysis (FC + PC + Upmu)

- Assuming $\nu_{\mu} \leftrightarrow \nu_{\tau}$ oscillation

Best fit :

$$\chi^2_{\min} = 135.3 / 152 \text{ d.o.f}$$

$$\text{at } (\sin^2 2\theta, \Delta m^2) = (1.01, 3.2 \times 10^{-3} \text{ eV}^2)$$

(Including unphysical region)

$$\chi^2_{\min} = 135.4 / 152 \text{ d.o.f}$$

$$\text{at } (\sin^2 2\theta, \Delta m^2) = (1.00, 3.2 \times 10^{-3} \text{ eV}^2)$$

(Physical region)

- Assuming null oscillation

strikingly maximal mixing

⇒ must be special structures

permutation symmetry S_3

Fukugita, Tanimoto, Yanagida

$$(\bar{L}_1 \bar{L}_2 \bar{L}_3) \begin{pmatrix} | & | & | \\ | & | & | \\ | & | & | \end{pmatrix} \begin{pmatrix} E_1 \\ E_2 \\ E_3 \end{pmatrix} H$$

$(S_3)_L \times (S_3)_E \Rightarrow$ democracy

\Rightarrow hierarchy $m_\tau \neq 0$

$m_e, m_\mu \ll m_\tau$

large rotation of L 's

$$(L_1 L_2 L_3) \begin{pmatrix} & & \\ & & \\ & & \end{pmatrix} \begin{pmatrix} L_1 \\ L_2 \\ L_3 \end{pmatrix} \frac{H^2}{M}$$

two possible matrices

$$\begin{pmatrix} | & | & | \\ | & | & | \\ | & | & | \end{pmatrix}, \begin{pmatrix} | & & \\ | & & \\ | & & \end{pmatrix}$$

\leftarrow choose only this

\Rightarrow no rotation of neutrinos
big rotation of leptons

$$\Rightarrow \sin^2 2\theta_{23} = 1, \sin^2 2\theta_{12} = \frac{4}{9}, \sin^2 \theta_{13} = 0$$

maximal mixing

$$m_\nu = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \rightarrow 45^\circ$$

but

$$\rightarrow \begin{pmatrix} -1 & 1 \\ 1 & 1 \end{pmatrix} \quad \Delta m^2 = 0$$

add $\begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix}$

$$m_\nu = \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix} \rightarrow \begin{pmatrix} 0 & 2 \end{pmatrix}$$

3 generations

$$m_\nu = \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} \rightarrow \begin{pmatrix} 0 & 0 \\ 0 & 3 \end{pmatrix}$$

democracy

hierarchy

how do we justify it?

Minimal Higgs sector of $SO(10)$

Albright, Barr

$$\lambda_u = \begin{pmatrix} \eta & 0 & 0 \\ 0 & 0 & \frac{1}{3}\epsilon \\ 0 & -\frac{1}{3}\epsilon & 1 \end{pmatrix}$$

$$\lambda_d = \begin{pmatrix} 0 & \delta & \delta' \\ \delta & 0 & \sigma + \frac{1}{3}\epsilon \\ \delta' & -\frac{1}{3}\epsilon & 1 \end{pmatrix}$$

$$\lambda_\nu = \begin{pmatrix} \eta & 0 & 0 \\ 0 & 0 & -\epsilon \\ 0 & \epsilon & 1 \end{pmatrix}$$

$$\lambda_e = \begin{pmatrix} 0 & \delta & \delta' \\ \delta & 0 & -\epsilon \\ \delta' & \sigma + \epsilon & 1 \end{pmatrix}$$

$$M = \begin{pmatrix} 0 & A\epsilon^2 & 0 \\ A\epsilon^2 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\sigma \simeq 1.8$$

$$\epsilon \simeq 0.14$$

$$\delta \simeq |\delta'| \simeq 0.008$$

$$\eta \simeq 6 \times 10^{-6}$$

$$A \simeq 0.05$$

$$\Rightarrow \text{VAC}$$

$$\sin^2 2\theta_{13} = 0.00$$

TABLE II. Matter superfields in the proposed model.

$\mathbf{16}_1(-\frac{1}{2} - 2p)^{+-}$	$\mathbf{16}_2(-\frac{1}{2} + p)^{++}$	$\mathbf{16}_3(-\frac{1}{2})^{++}$
$\mathbf{16}(-\frac{1}{2} - p)^{-+}$	$\mathbf{16}'(-\frac{1}{2})^{-+}$	
$\overline{\mathbf{16}}(\frac{1}{2})^{+-}$	$\overline{\mathbf{16}}'(-\frac{3}{2} + 2p)^{+-}$	
$\mathbf{10}_1(-1 - p)^{-+}$	$\mathbf{10}_2(-1 + p)^{++}$	
$\mathbf{1}_1(2 + 2p)^{+-}$	$\mathbf{1}_2(2 - p)^{++}$	$\mathbf{1}_3(2)^{++}$
$\mathbf{1}_1^c(-2 - 2p)^{+-}$	$\mathbf{1}_2^c(-2)^{+-}$	$\mathbf{1}_3^c(-2 - p)^{++}$

In terms of these fermion fields and the Higgs fields previously introduced, one can then spell out all the terms in the Yukawa superpotential which follow from their $\text{SO}(10)$ and $\text{U}(1) \times \text{Z}_2 \times \text{Z}_2$ assignments:

$$\begin{aligned}
W_{\text{Yukawa}} = & \mathbf{16}_3 \cdot \mathbf{16}_3 \cdot T_1 + \mathbf{16}_2 \cdot \mathbf{16} \cdot T_1 \\
& + \mathbf{16}' \cdot \mathbf{16}' \cdot T_1 + \mathbf{16}_3 \cdot \mathbf{16}_1 \cdot T_0' \\
& + \mathbf{16}_2 \cdot \mathbf{16}_1 \cdot T_0 + \mathbf{16}_3 \cdot \overline{\mathbf{16}} \cdot A \\
& + \mathbf{16}_1 \cdot \overline{\mathbf{16}}' \cdot Y' + \mathbf{16} \cdot \overline{\mathbf{16}} \cdot P \\
& + \mathbf{16}' \cdot \overline{\mathbf{16}}' \cdot S + \mathbf{16}_3 \cdot \mathbf{10}_2 \cdot C' \\
& + \mathbf{16}_2 \cdot \mathbf{10}_1 \cdot C + \mathbf{10}_1 \cdot \mathbf{10}_2 \cdot Y \\
& + \mathbf{16}_3 \cdot \mathbf{1}_3 \cdot \overline{C} + \mathbf{16}_2 \cdot \mathbf{1}_2 \cdot \overline{C} \\
& + \mathbf{16}_1 \cdot \mathbf{1}_1 \cdot \overline{C} + \mathbf{1}_3 \cdot \mathbf{1}_3^c \cdot Z \\
& + \mathbf{1}_2 \cdot \mathbf{1}_2^c \cdot P + \mathbf{1}_1 \cdot \mathbf{1}_1^c \cdot X \\
& + \mathbf{1}_3^c \cdot \mathbf{1}_3^c \cdot V_M + \mathbf{1}_1^c \cdot \mathbf{1}_2^c \cdot V_M, \quad (2)
\end{aligned}$$

where the coupling parameters have been suppressed. The

following values are obtained compared with experiment [12] in parentheses:

$$\begin{aligned}
 m_c(m_c) &= 1.23 \text{ GeV}, & (1.27 \pm 0.1 \text{ GeV}), \\
 m_b(m_b) &= 4.25 \text{ GeV}, & (4.26 \pm 0.11 \text{ GeV}), \\
 m_s(1 \text{ GeV}) &= 148 \text{ MeV}, & (175 \pm 50 \text{ MeV}), \\
 m_d(1 \text{ GeV}) &= 7.9 \text{ MeV}, & (8.9 \pm 2.6 \text{ MeV}), \\
 |V_{ub}/V_{cb}| &= 0.080, & (0.090 \pm 0.008),
 \end{aligned} \tag{15}$$

where finite SUSY loop corrections for m_b and m_s have been scaled to give $m_b(m_b) \simeq 4.25 \text{ GeV}$ for $\tan\beta = 5$.

The effective light neutrino mass matrix of Eq. (10) leads to bimaximal mixing with a large angle solution for atmospheric neutrino oscillations [13] and the “just-so” vacuum solution [14] involving two pseudo-Dirac neutrinos, if we set $\Lambda_R = 2.4 \times 10^{14} \text{ GeV}$ and $A = 0.05$. We then find

$$\begin{aligned}
 m_3 &= 54.3 \text{ MeV}, & m_2 &= 59.6 \mu\text{eV}, & m_1 &= 56.5 \mu\text{eV}, \\
 U_{e2} &= 0.733, & U_{e3} &= 0.047, & U_{\mu 3} &= -0.818, \\
 & & \delta'_{CP} &= -0.2^\circ, \\
 \Delta m_{23}^2 &= 3.0 \times 10^{-3} \text{ eV}^2, & \sin^2 2\theta_{\text{atm}} &= 0.89, \\
 \Delta m_{12}^2 &= 3.6 \times 10^{-10} \text{ eV}^2, & \sin^2 2\theta_{\text{solar}} &= 0.99, \\
 \Delta m_{13}^2 &= 3.0 \times 10^{-3} \text{ eV}^2, & \sin^2 2\theta_{\text{reac}} &= 0.009.
 \end{aligned} \tag{16}$$

The effective scale of the right-handed Majorana mass contribution turns 2 orders of magnitude lower than the

TABLE I. Higgs superfields in the proposed model.

Higgs fields needed to solve the 2-3 problem:	
45_{B-L} :	$A(0)^{+-}$
16 :	$C(\frac{3}{2})^{-+}, C'(\frac{3}{2} - p)^{++}$
$\overline{16}$:	$\overline{C}(-\frac{3}{2})^{++}, \overline{C}'(-\frac{3}{2} - p)^{-+}$
10 :	$T_1(1)^{++}, T_2(-1)^{+-}$
1 :	$X(0)^{++}, P(p)^{+-}, Z_1(p)^{++}, Z_2(p)^{++}$
Additional Higgs fields for the mass matrices:	
10 :	$T_0(1 + p)^{+-}, T'_0(1 + 2p)^{+-},$ $\overline{T}_0(-3 + p)^{-+}, \overline{T}'_0(-1 - 3p)^{-+}$
1 :	$Y(2)^{-+}, Y'(2)^{++}, S(2 - 2p)^{--}, S'(2 - 3p)^{--},$ $V_M(4 + 2p)^{++}$

$$W_{\text{Higgs}} = W_A + W_{CA} + W_{2/3} + W_{H_D} + W_R,$$

$$W_A = \text{tr}A^4/M + M_A \text{tr}A^2,$$

$$W_{CA} = X(\overline{C}C)^2/M_C^2 + F(X) + \overline{C}'(PA/M_1 + Z_1)C \\ + \overline{C}(PA/M_2 + Z_2)C',$$

$$W_{2/3} = T_1AT_2 + Y'T_2^2,$$

$$W_{H_D} = T_1\overline{C}CY'/M + \overline{T}_0CC' + \overline{T}_0(T_0S + T'_0S'),$$

$$W_R = \overline{T}_0\overline{T}_0V_M. \quad (1)$$

Do we really need such a rigid structure

do nothing \Rightarrow "anarchy"

Hall,
HM,
Weiner

if there is no particular structure
in a mass matrix

each element would appear random

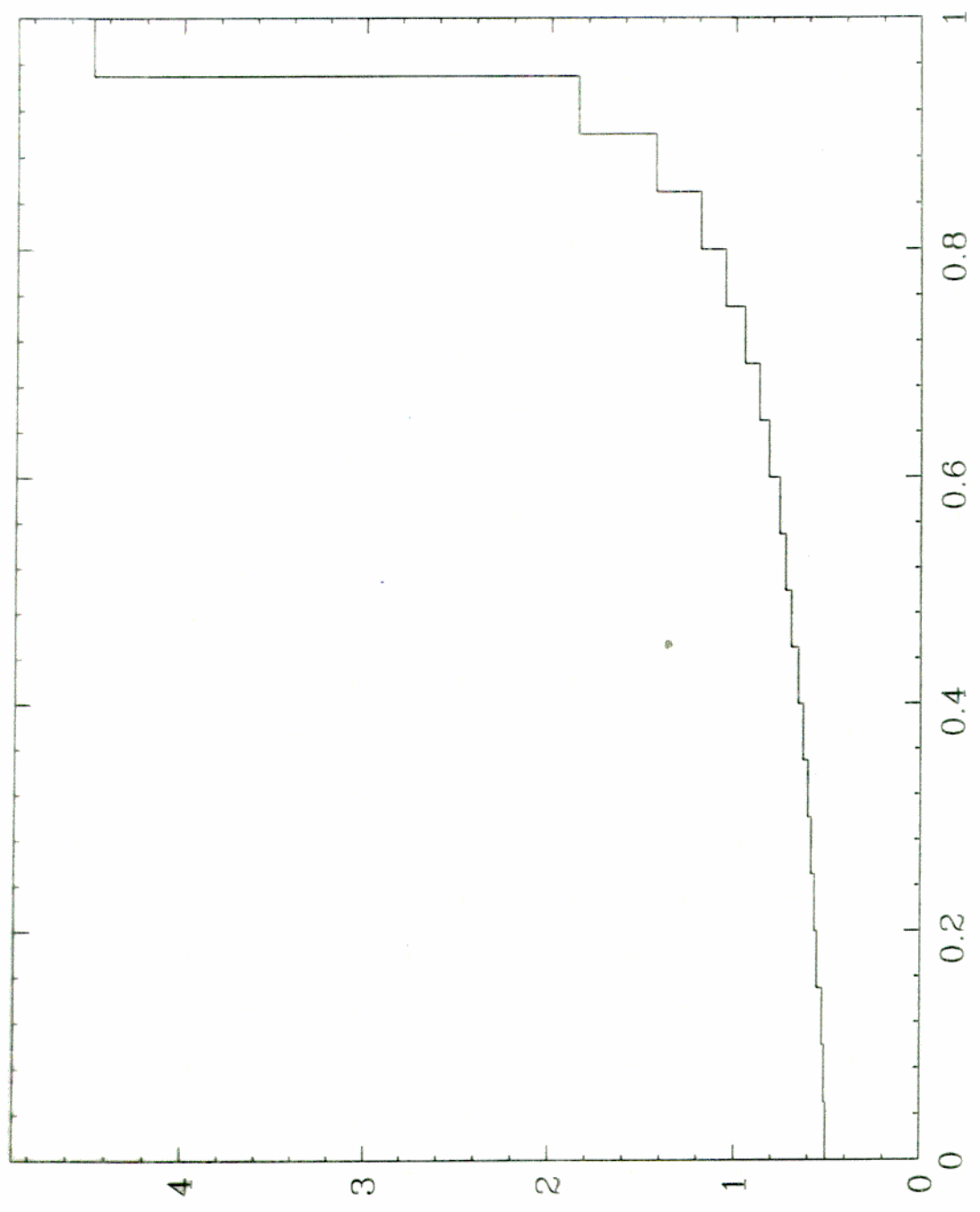
throw dice

\Rightarrow see if near-maximal mixing
is really so special

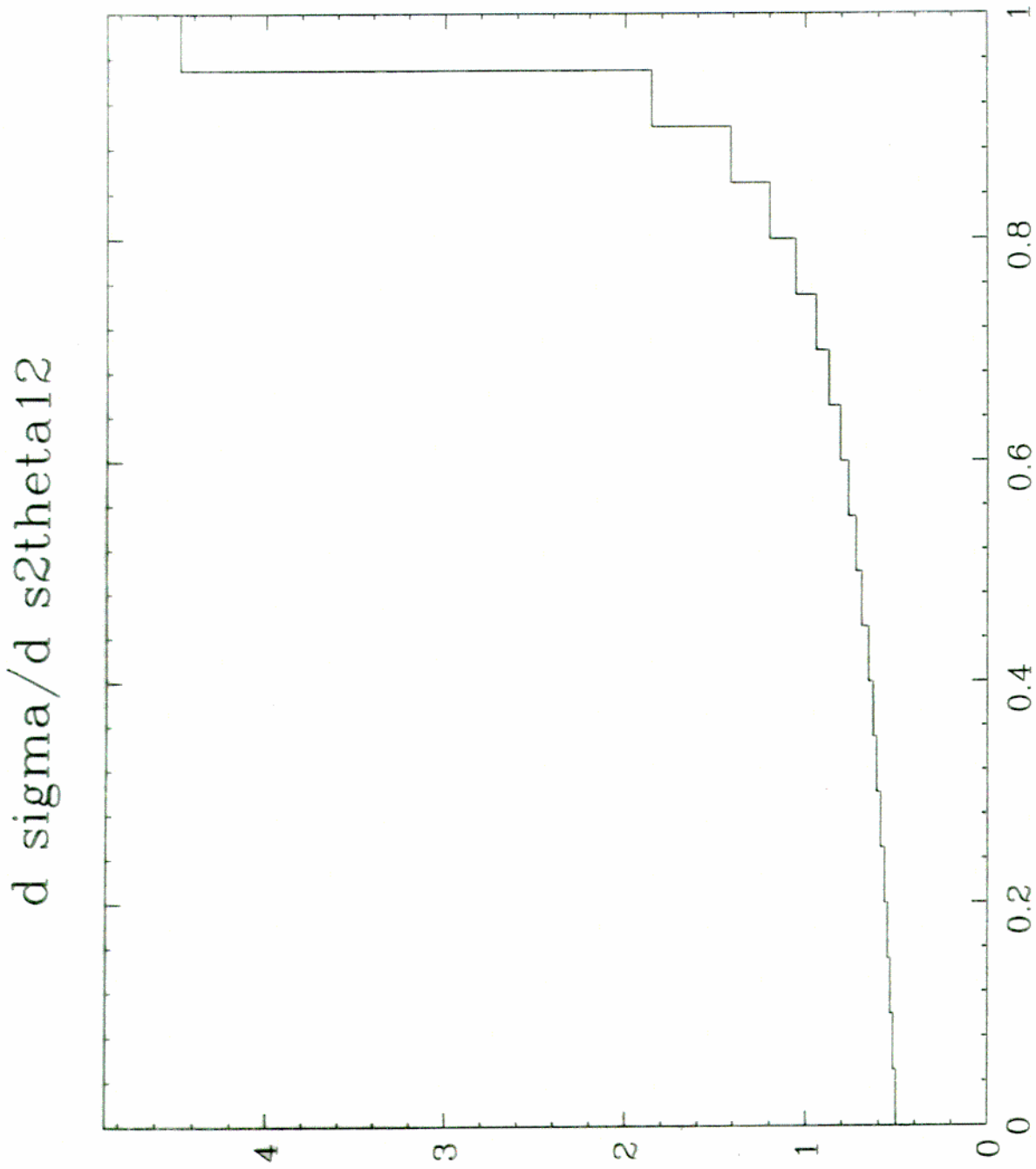
$$M_\nu = (m_D) (M)^{-1} (m_D)^T$$

m_D, M random 3×3

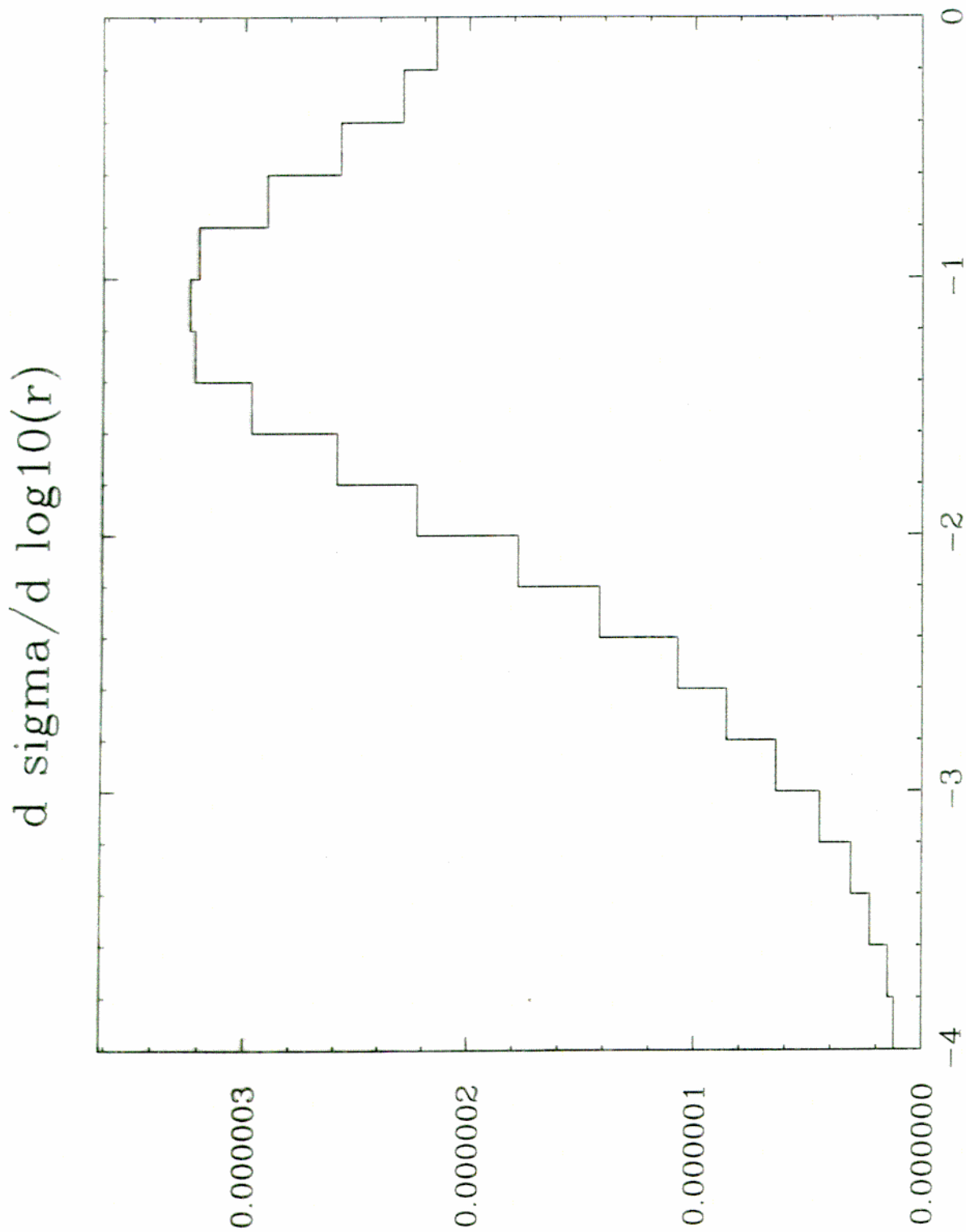
$d \sigma / d s_{2\theta_{23}}$



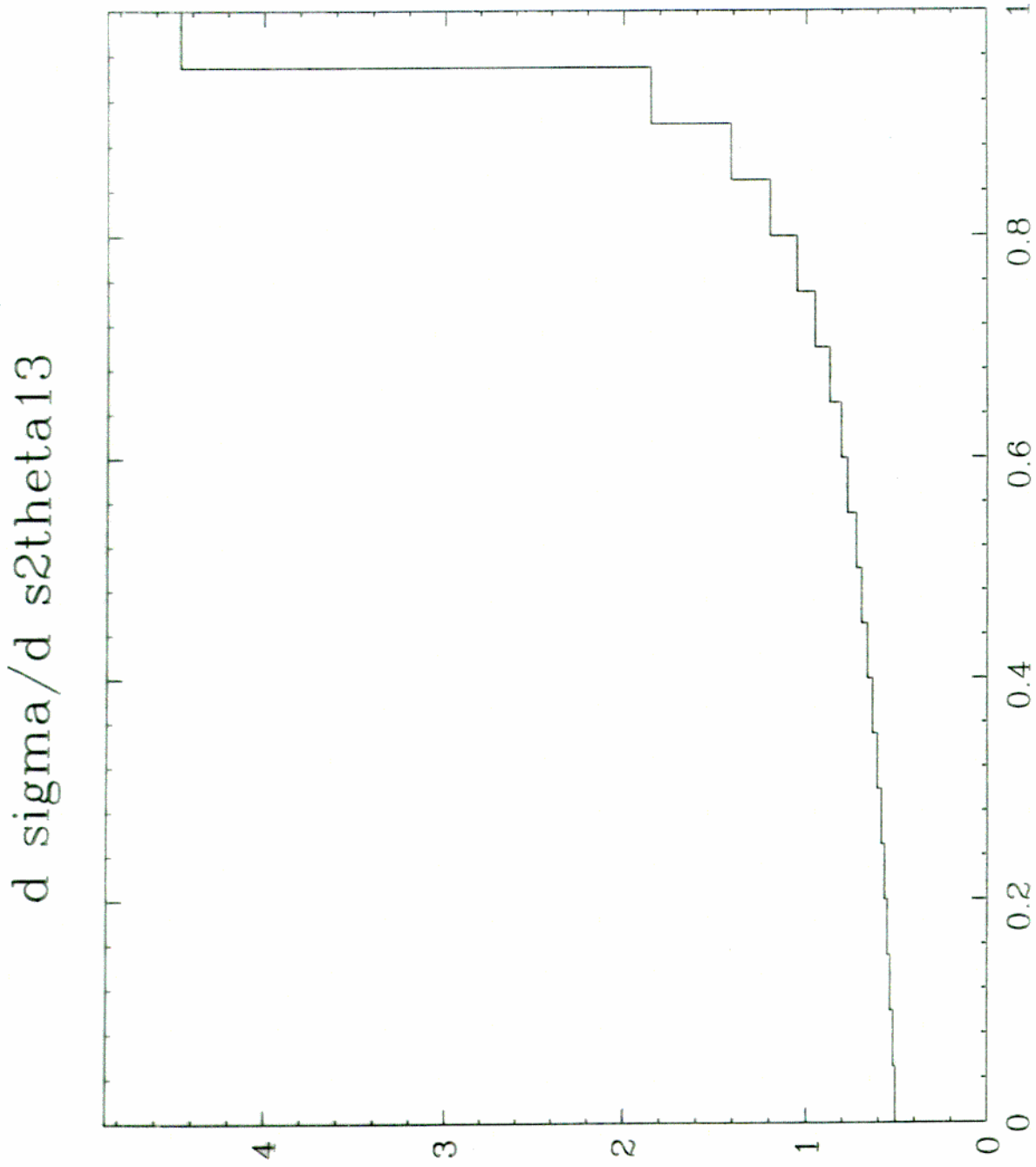
$\sin^2 2\theta_{23}$



$\sin^2 2\theta_{12}$



$\log_{10}(\Delta m^2 / \Delta m^2_{\oplus})$



$\sin^2 2\theta_{13}$

do nothing

⇒ all angles tend to be
near maximal

$$\Rightarrow \Delta m_{01}^2 / \Delta m_{23}^2 \sim \frac{1}{20}$$

perfect for LMA

price:

only 10% chance to satisfy

Chooz limit $\sin^2 2\theta_{13} \leq 0.2$

does not appear

particularly damaging

we don't seem to need any
particular (i.e. artificial, engineered)
structure in ν mass + mixing

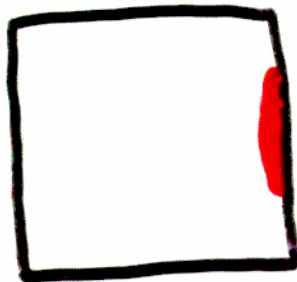
distributions in angles:

consequence of basis independence

⇒ group Haar measure

flat in $\sin^2 \theta_{12}$, $\sin^2 \theta_{23}$, $\cos^4 \theta_{13}$

Haar, HM



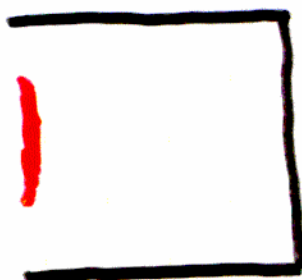
$\sin^2 2\theta_{23}$

$$\sin^2 2\theta_{23} > 0.88$$

(90% CL)

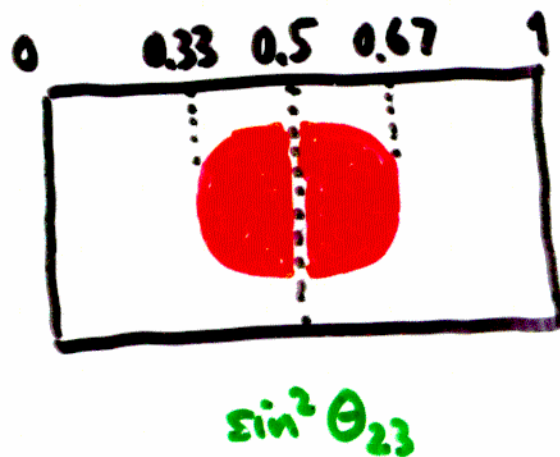
special, large

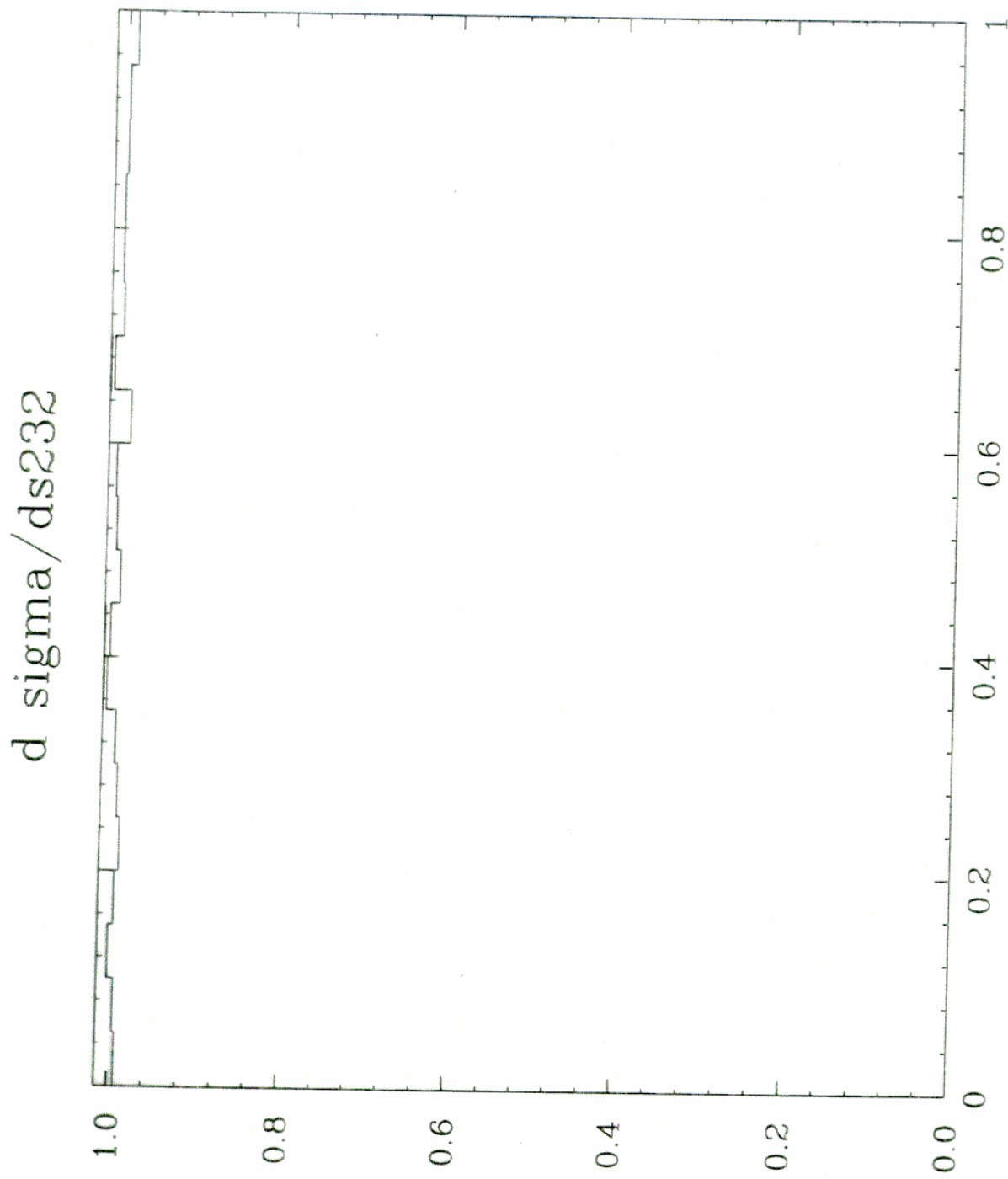
at the boundary of physical region



center

— moderate



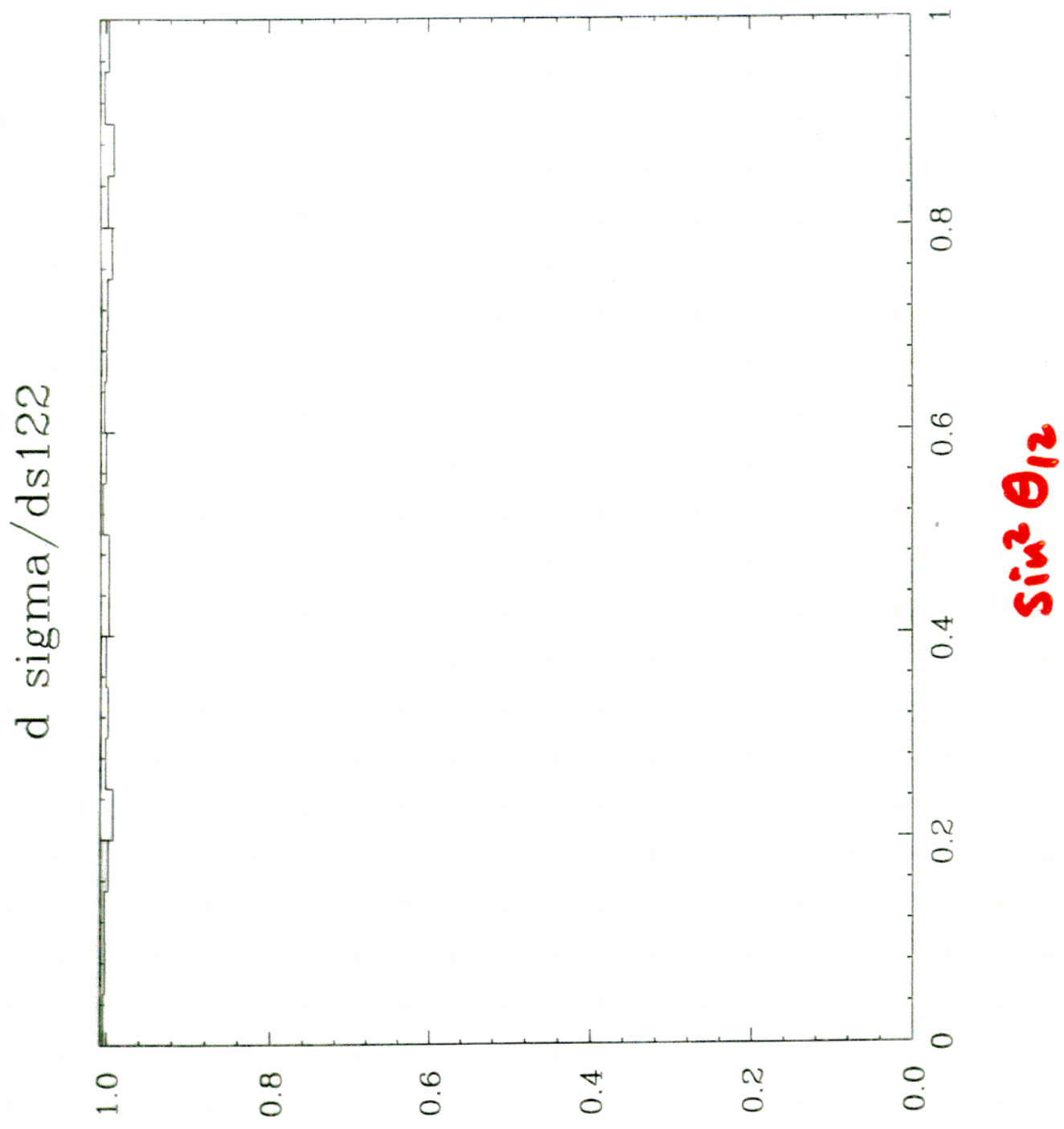


$\sin^2 \theta_{23}$

147

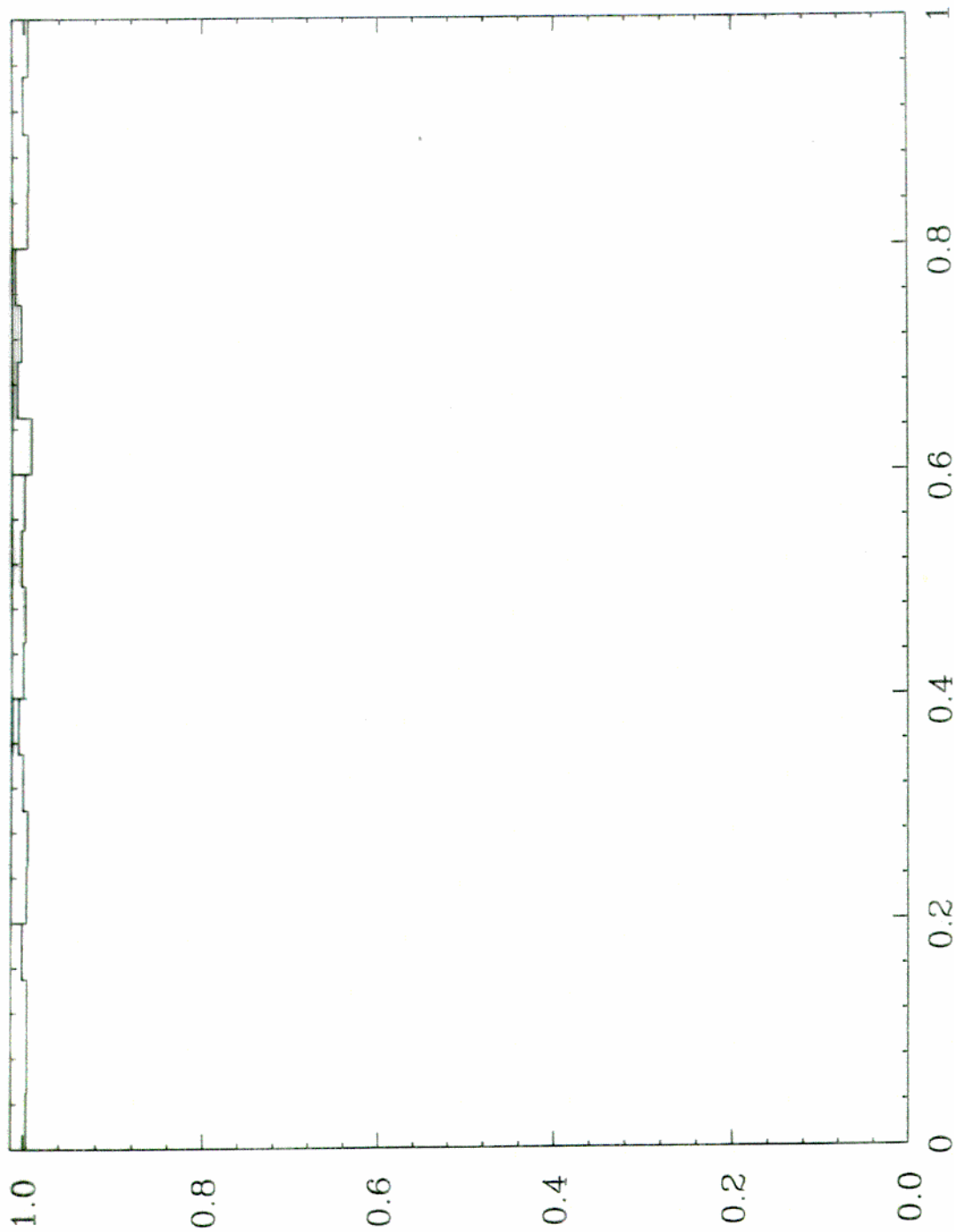
147

851



5/11

d sigma/dc134



$\cos^4 \theta_{13}$

§ signature of anarchy

• LMA

⇒ testable by KamLAND

• ν_{e3}

probably not too small

⇒ MINOS, ICANOE

$$\nu_{\mu} \rightarrow \nu_e$$

$$\Delta m^2 = \Delta m_{\text{atm}}^2 + \Delta m_{\odot}^2$$

$$\simeq \Delta m_{\text{atm}}^2$$

• $0\nu\beta\beta$

set the scale s.t. $\Delta m_{\text{atm}}^2 = 3 \times 10^{-3} \text{ eV}^2$

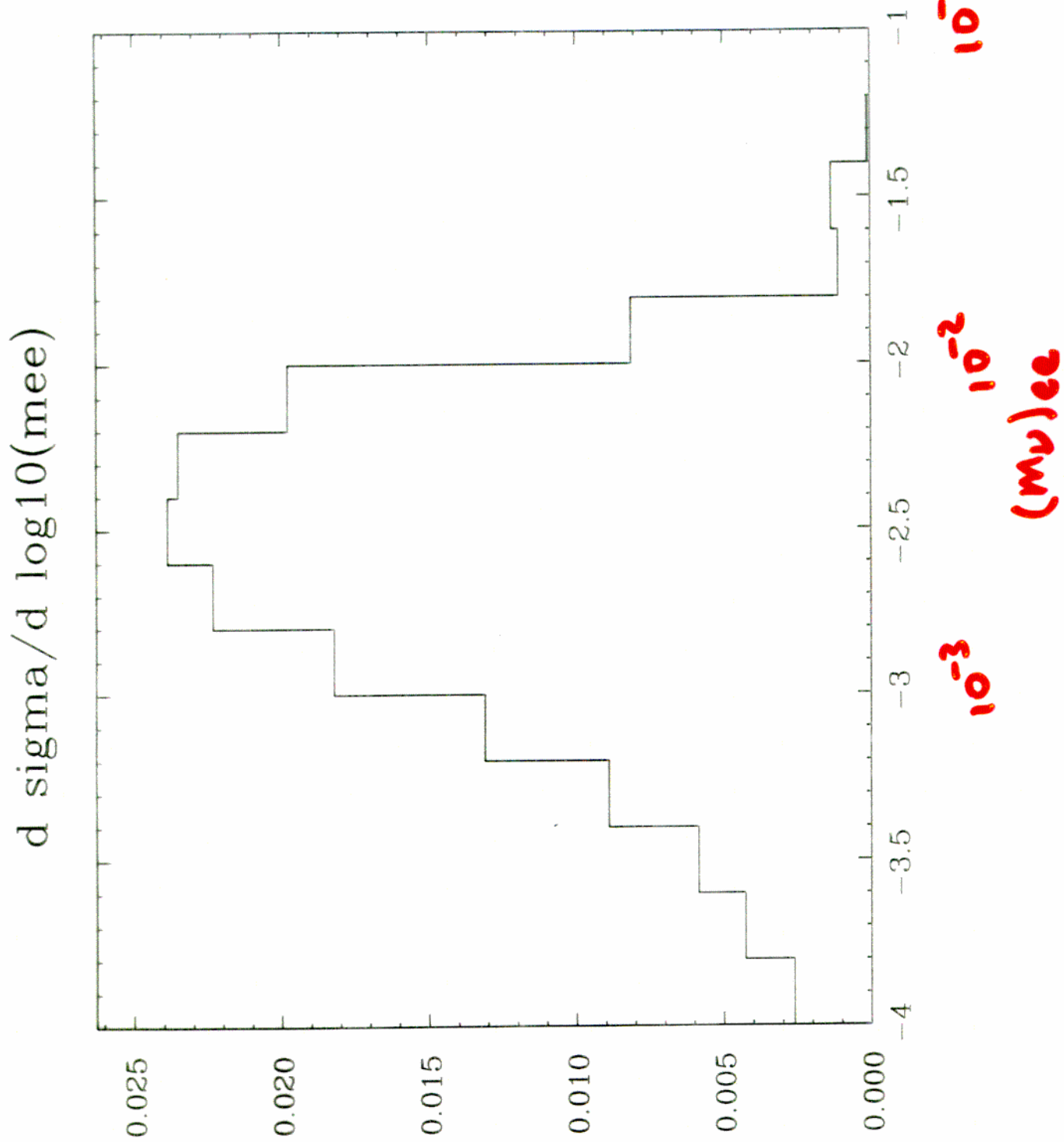
(SuperK best fit FC)

$$\Rightarrow (m_m)_{ee}$$

usually considered sizable only
for degenerate neutrinos

practically zero for SMA, Low, VAC

• CP in ν oscillation



FUTURE

IS BRIGHT