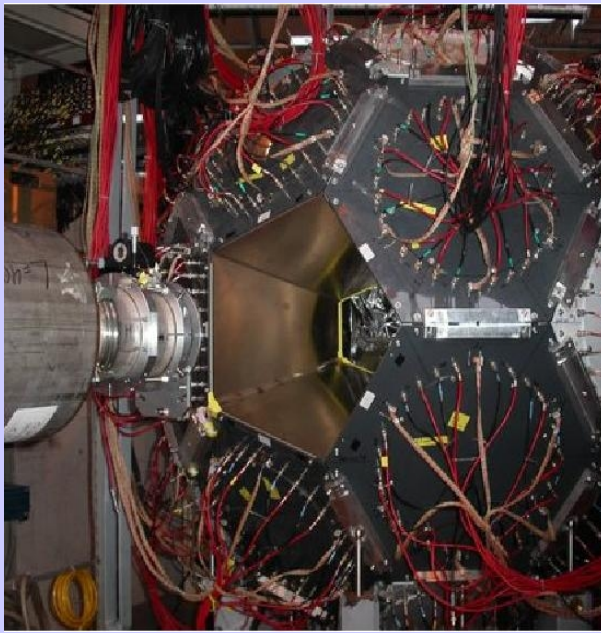


Precision measurements of μ^+ , μ^-H , and μ^-D lifetimes.

**Tim Gorringer, Univ. of Kentucky,
for the MuLan, MuCap, MuSun Collaborations**

SLAC experimental seminars, May 10, 2011.

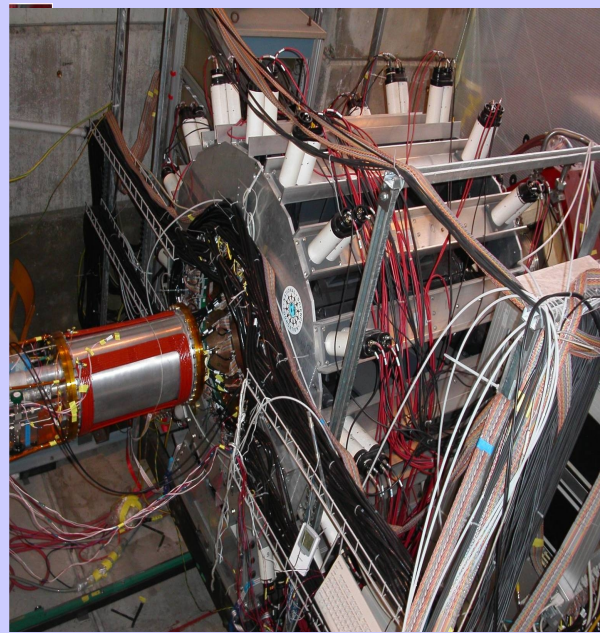


MuLan

pure leptonic weak interactions...

From the Fermi Constant...

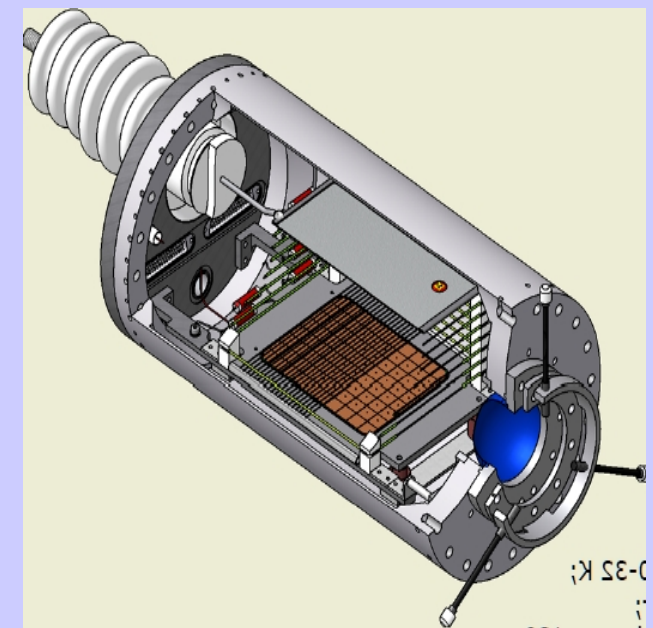
by part-per-million measurements of μ^+ , μ^-H , and μ^-D lifetimes



MuCap

to nucleonic weak interaction...

to the proton's weak interaction...



MuSun

and weak nuclear interaction

and solar hydrogen burning

Outline

intense, pulsed μ 's at PSI

scientific goals

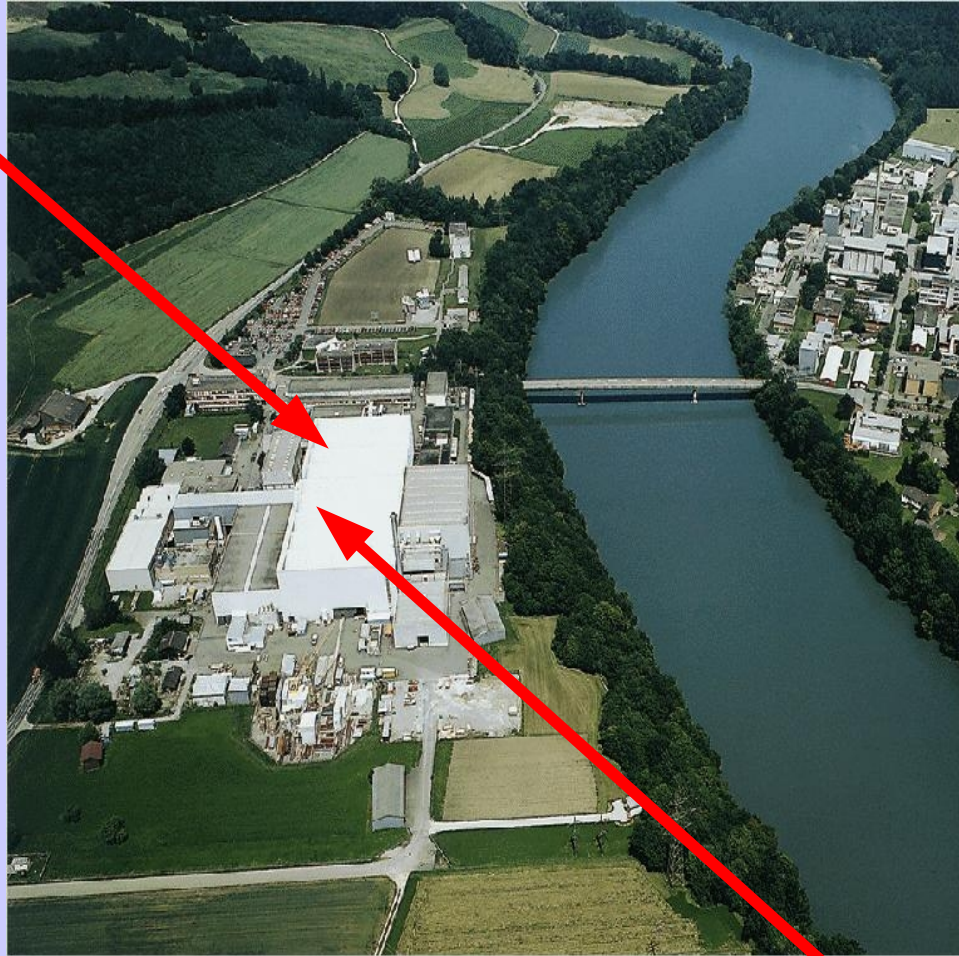
setups and challenges

results and status

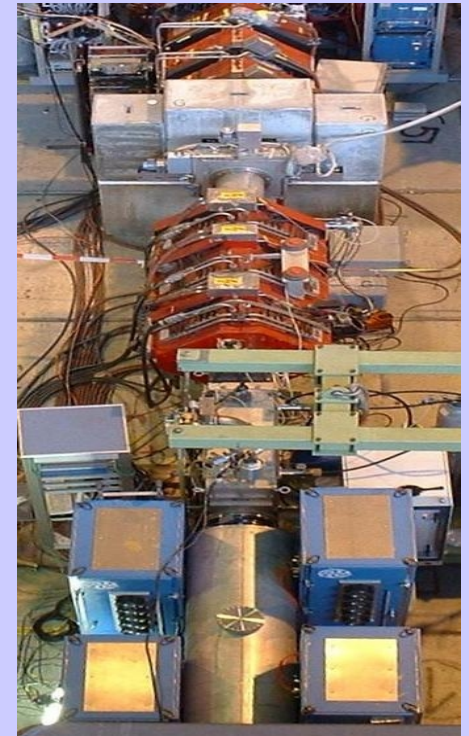
Paul Scherrer Institute.



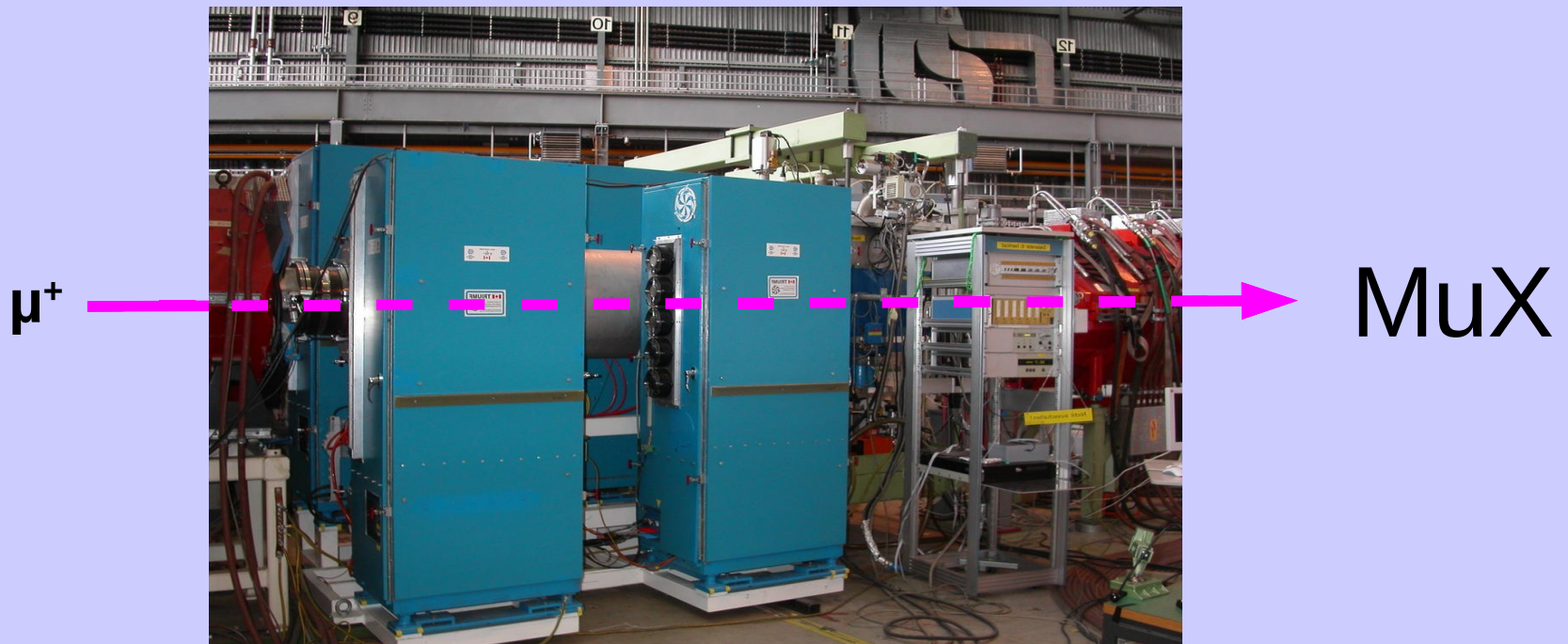
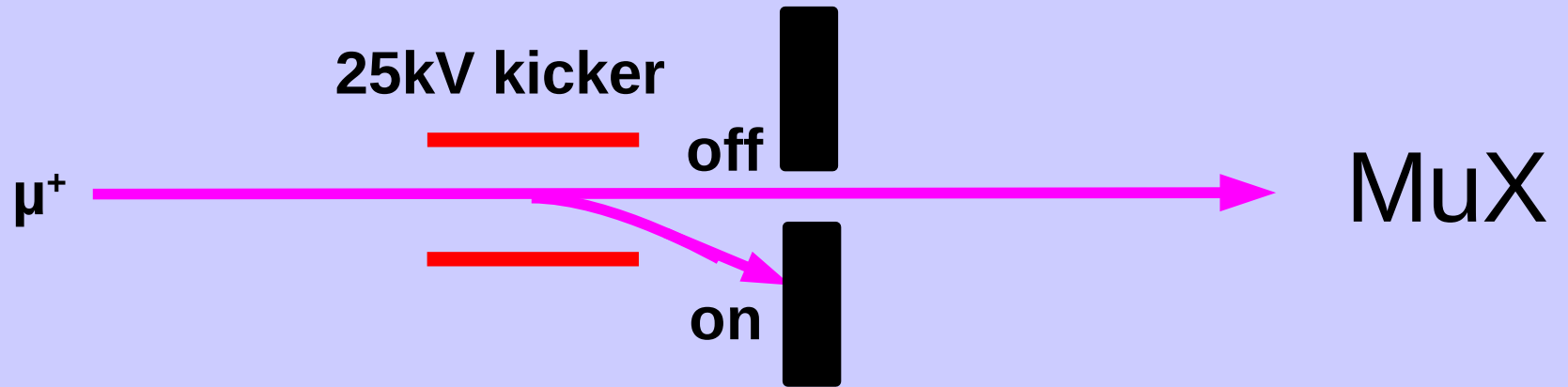
2.0 mA, 590 MeV,
1 MWatt, proton
cyclotron

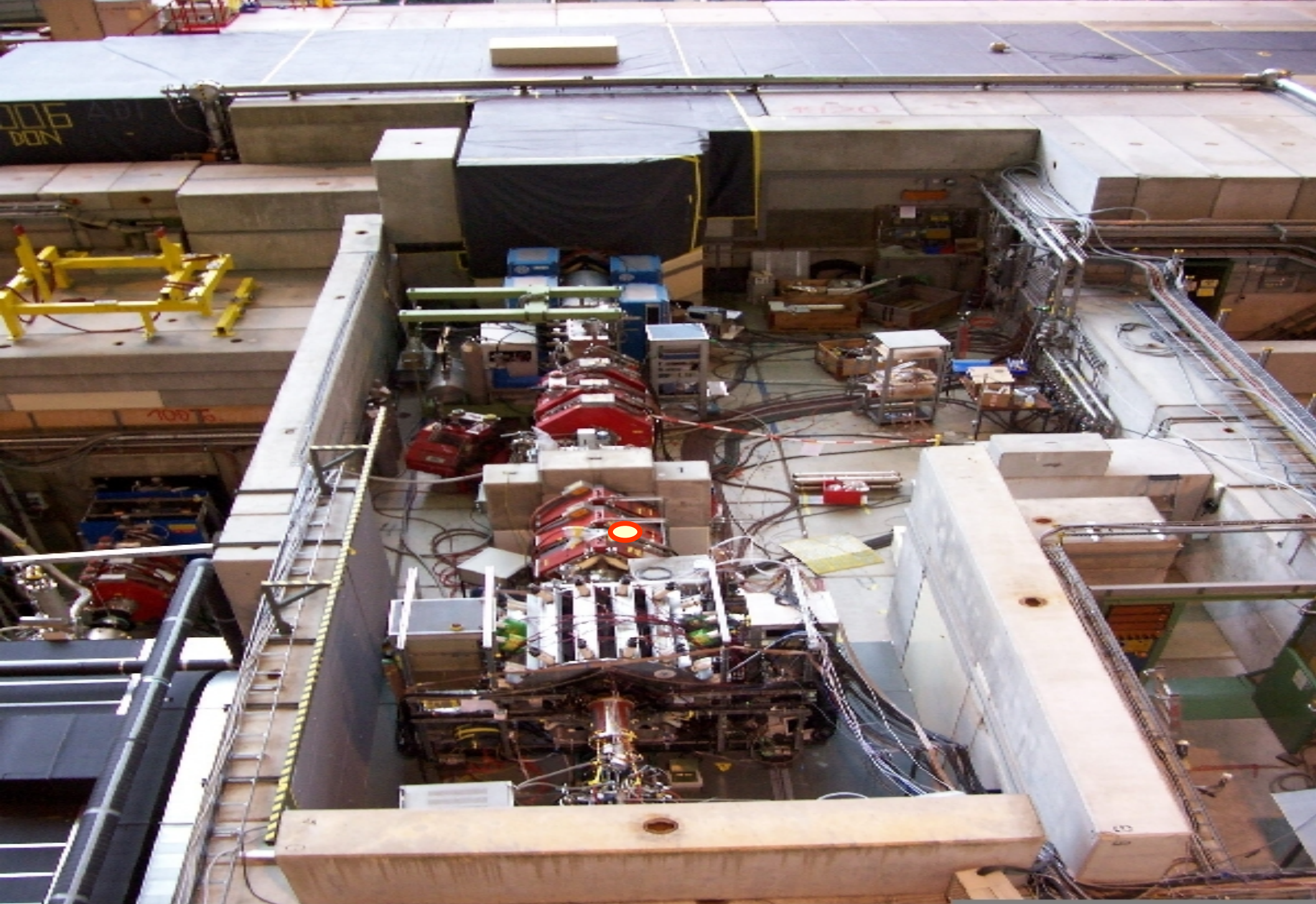


time-structured,
5 MeV, 30 MeV/c
 μ^\pm beams



Pulsed Muons and Muon On Request.





$\pi E3$ beamline

$$-\frac{\hbar}{i} \frac{\partial}{\partial t} = \frac{p^2}{2m} - \frac{Ze^2}{r}$$

$$\alpha = \frac{\hbar^2}{ec}$$

Mulan — the muon lifetime and Fermi constant.



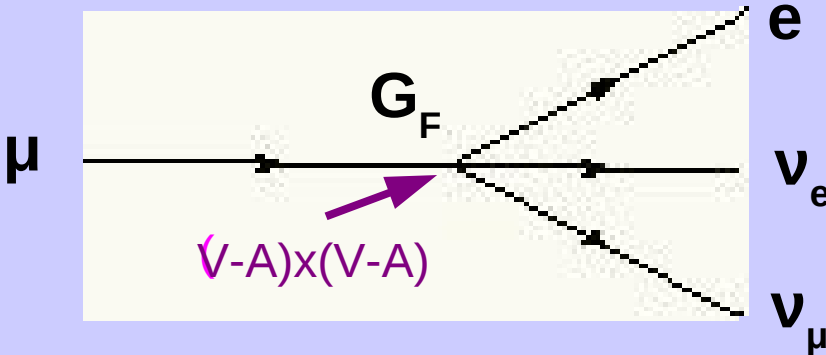
Why we measure τ_{μ^+} ?

knowledge of muon lifetime τ_{μ^+} allows precision measurements of weak nuclear interactions in muonic hydrogen, deuterium atoms.

twenty-fold improvement in knowledge of fundamental constant G_F of electroweak sector of standard model [presently α (± 0.7 ppb), G_F (± 10 ppm) M_Z (± 23 ppm)].

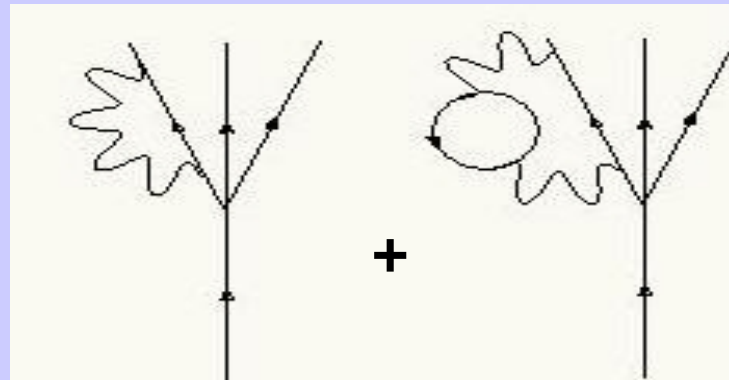
knowledge of α , M_Z , G_F allows precision tests of standard model via measurements of Weinberg angle Θ_W , M_W , ...

Relation between muon lifetime and Fermi constant.
 (muon decay is pure leptonic weak decay with lifetime that's straightforward to measure)



$$\frac{1}{\tau_{\mu}} = \frac{G_F^2 m_{\mu}^5}{192 \pi^2} (1 + \Delta q)$$

Δq contains electron mass and QED, QCD radiative corrections



1999, von Rittbergen and Stuart, 2-loop QED corrections

2008, Pak and Czarnecki, higher-order electron mass corrections

Relation between muon lifetime and Fermi Constant.

$$\frac{\Delta G_F}{G_F} = \frac{1}{2} \sqrt{\left(\frac{\Delta \tau}{\tau}\right)^2 + 5\left(\frac{\Delta m_\mu}{m_\mu}\right)^2 + \left(\frac{\Delta theory}{theory}\right)^2}$$

Last generation experiments

17 ppm

18 ppm

0.1 ppm

30 ppm

New generation experiments

0.6 ppm

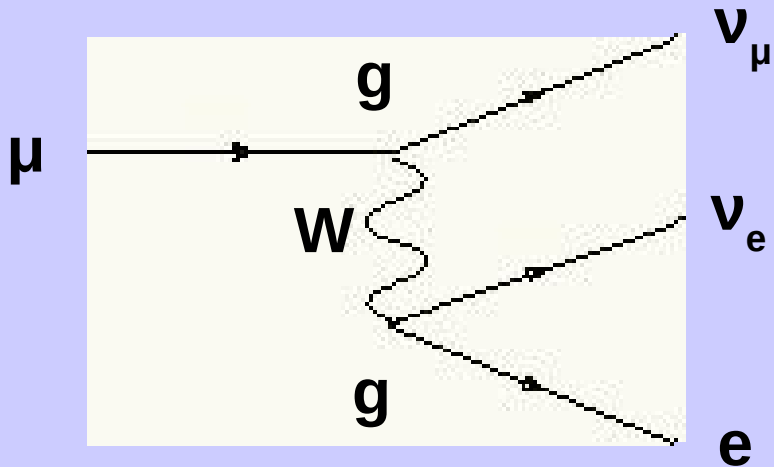
1.0 ppm

0.1 ppm

0.3 ppm

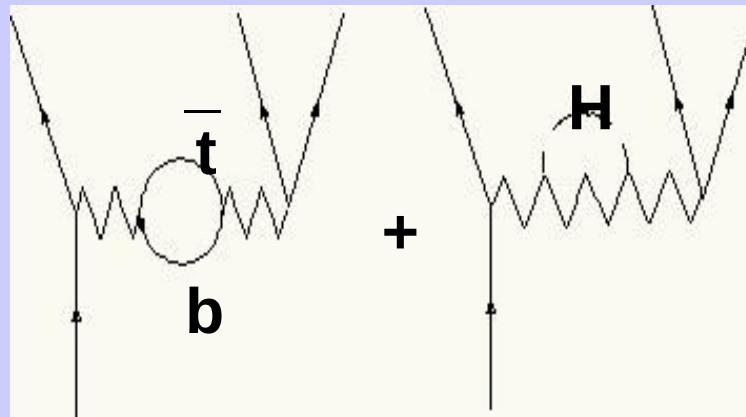
(negligible effect from finite ν -mass)

Interpretation of Fermi constant in Standard Model



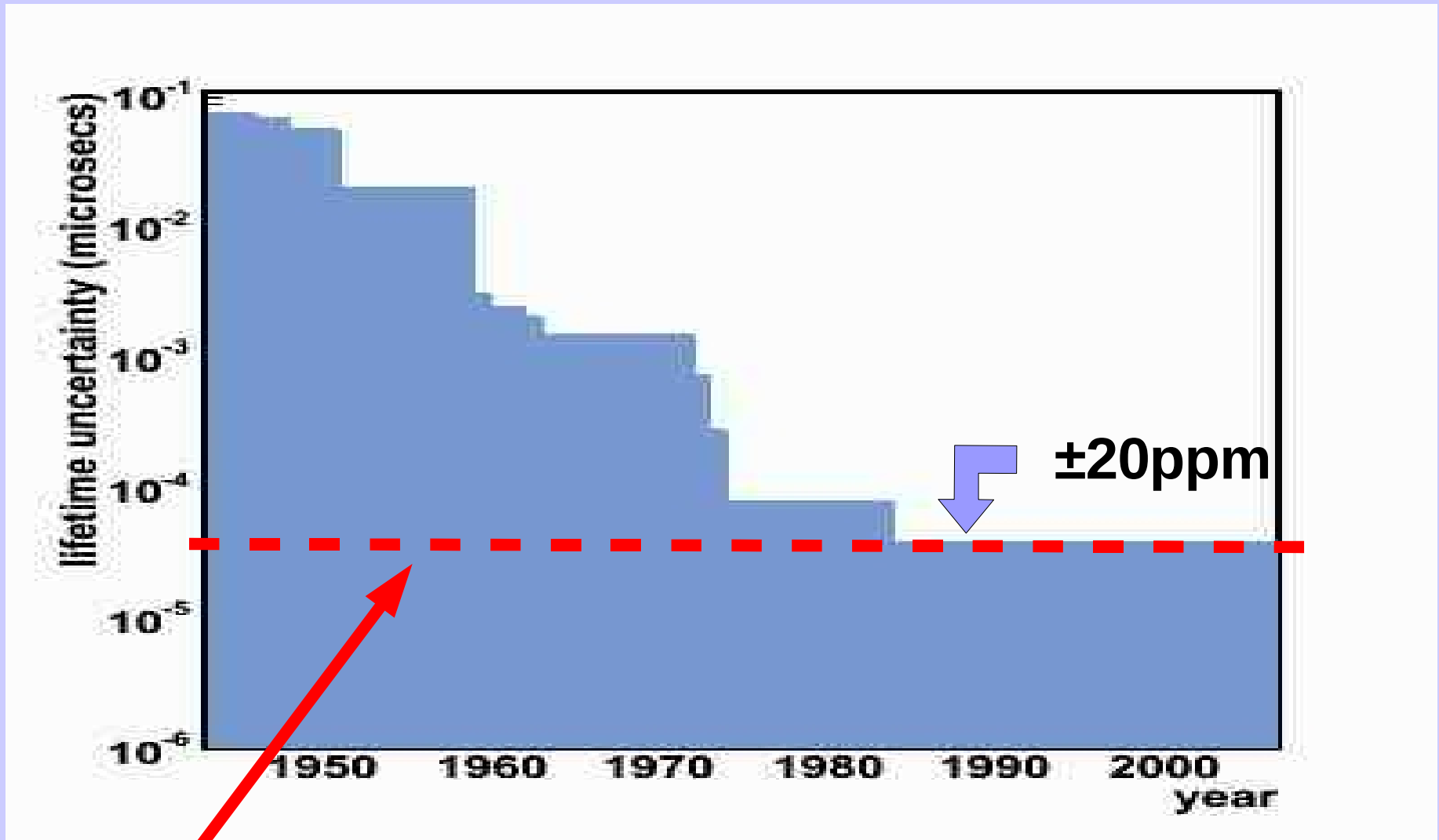
$$\frac{G_F}{\sqrt{2}} = \frac{g^2}{8 M_W^2} (1 + \Delta r)$$

Δr contains electroweak radiative corrections



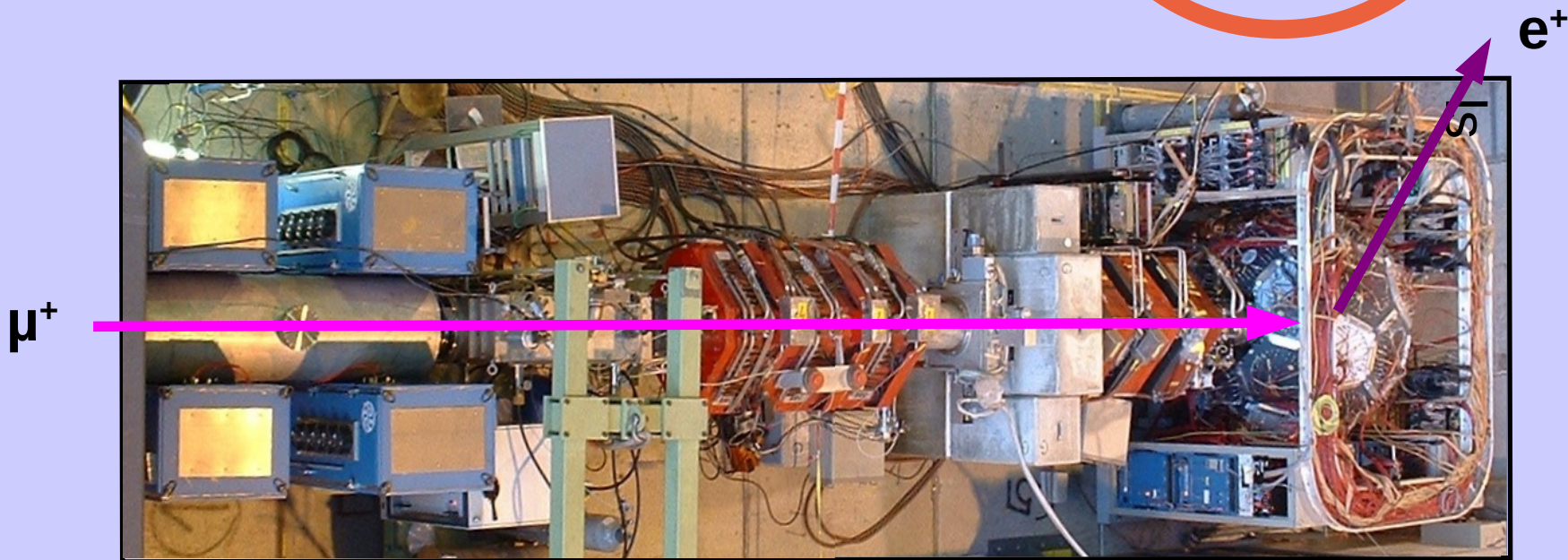
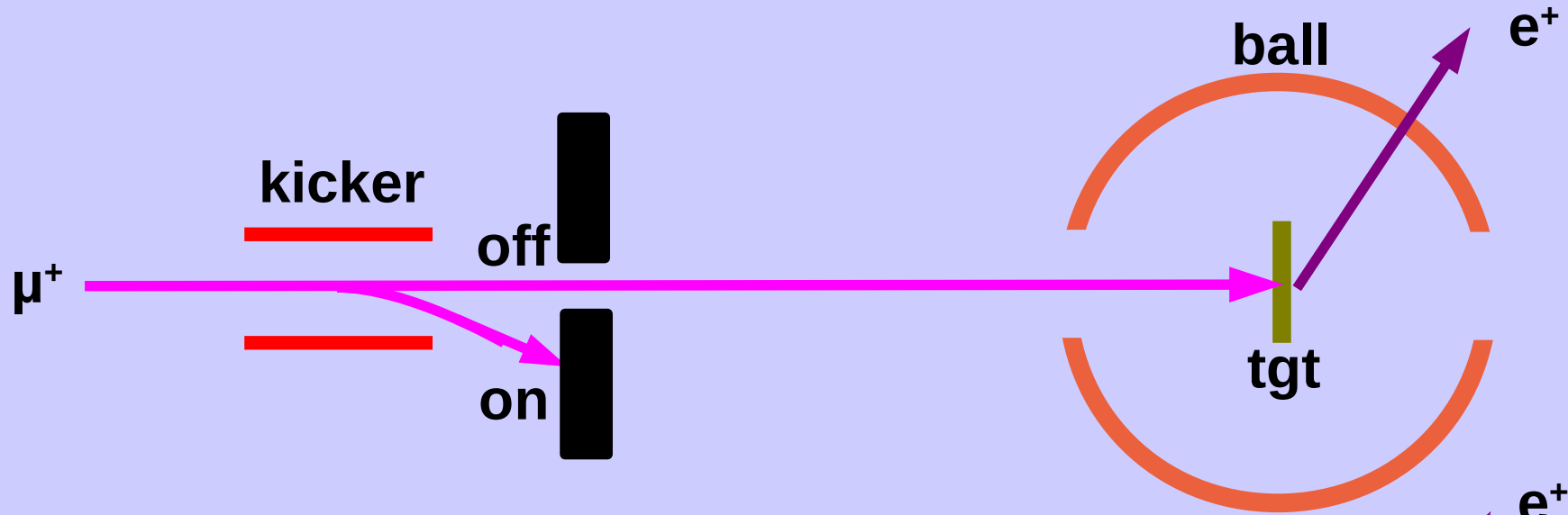
e.g. Contributions from top quark, Higg's particle

muon lifetime history, $\tau_\mu = 2.19703(4) \mu\text{s}$



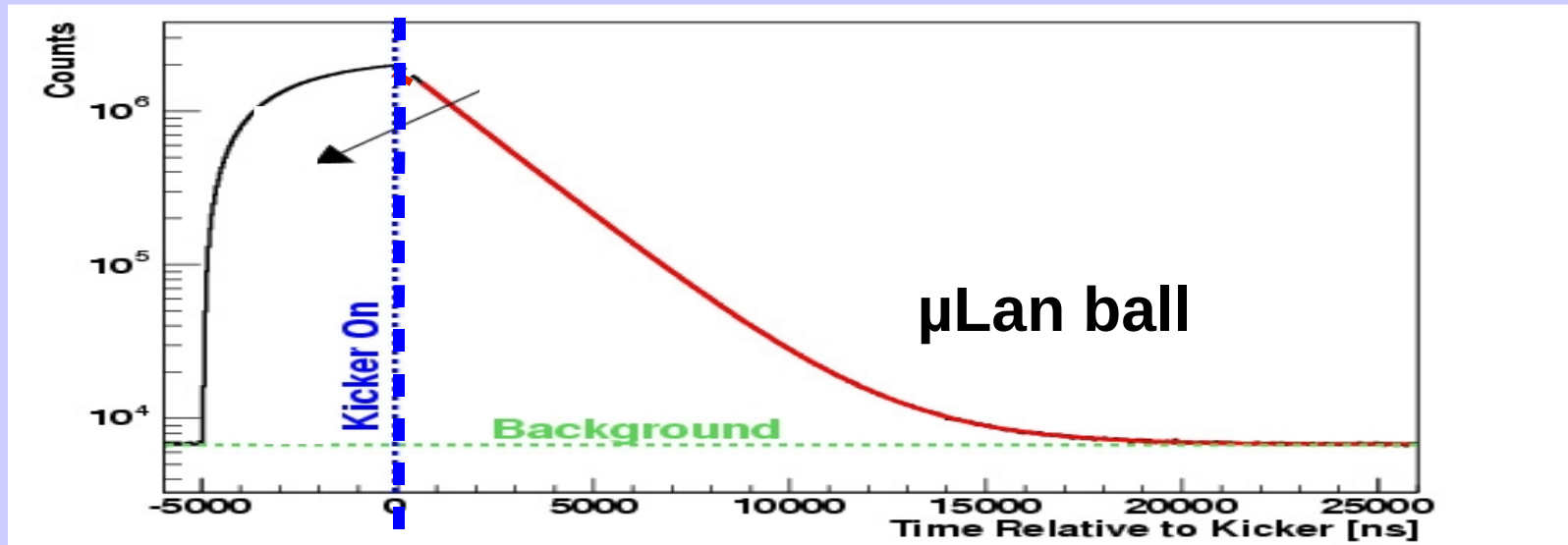
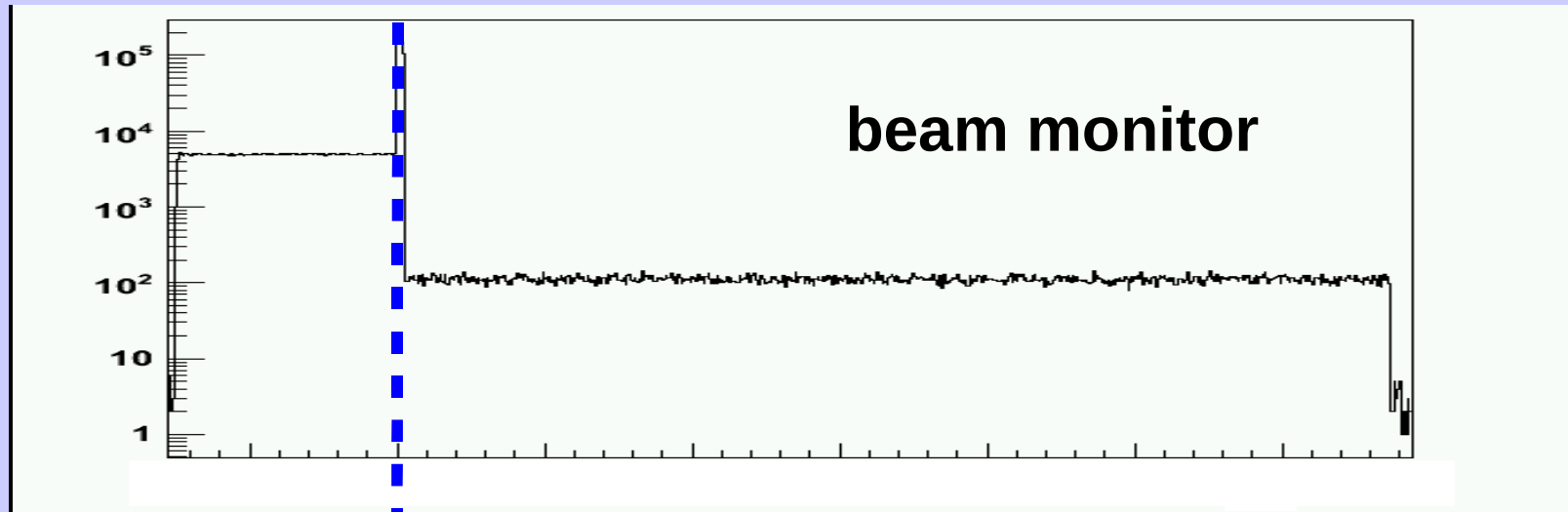
one-by-one exptl limit and one-loop QED limit

accumulating μ^+ 's and measuring e^+ 's



roughly 30 μ stops, 20 e detected per cycle

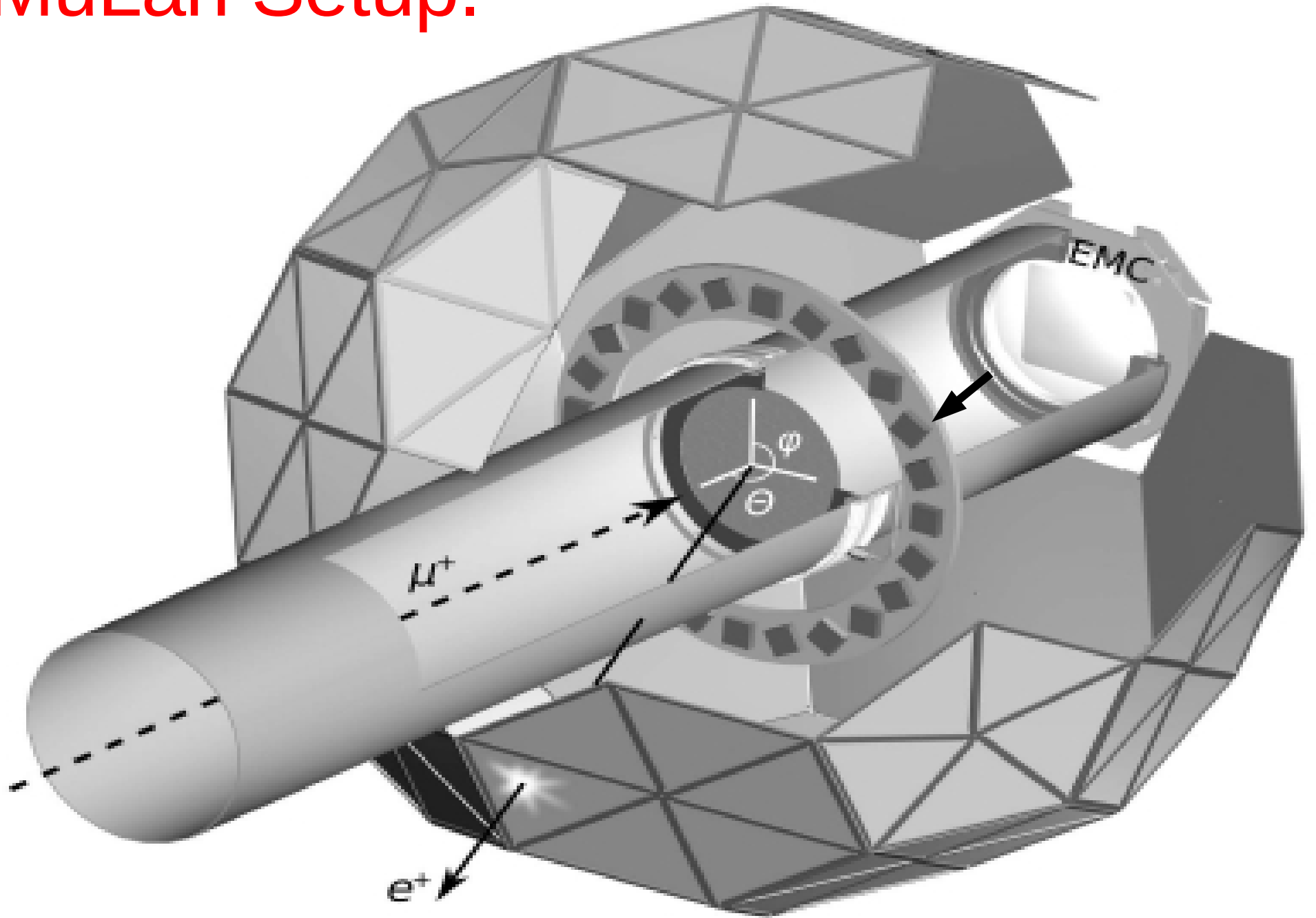
accumulating μ^+ 's and measuring e^+ 's



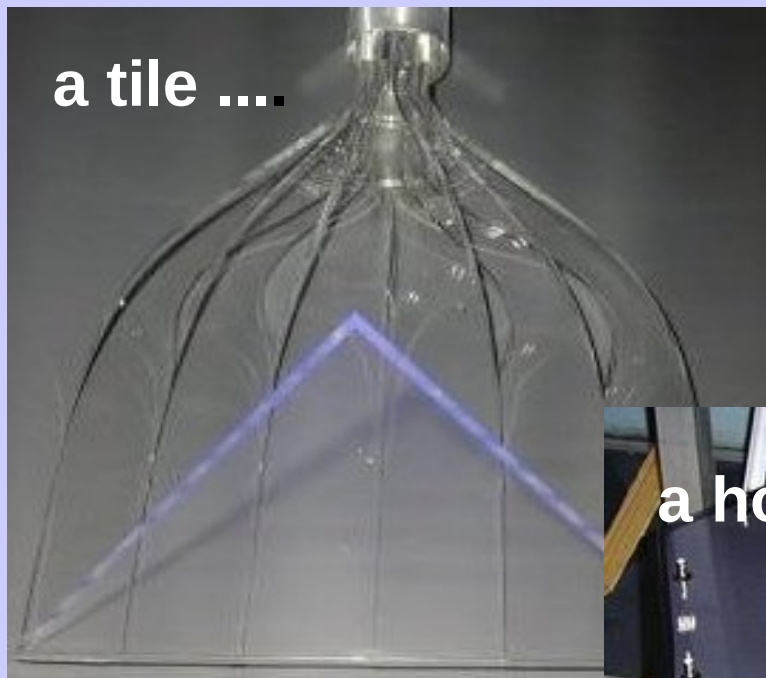
beam on

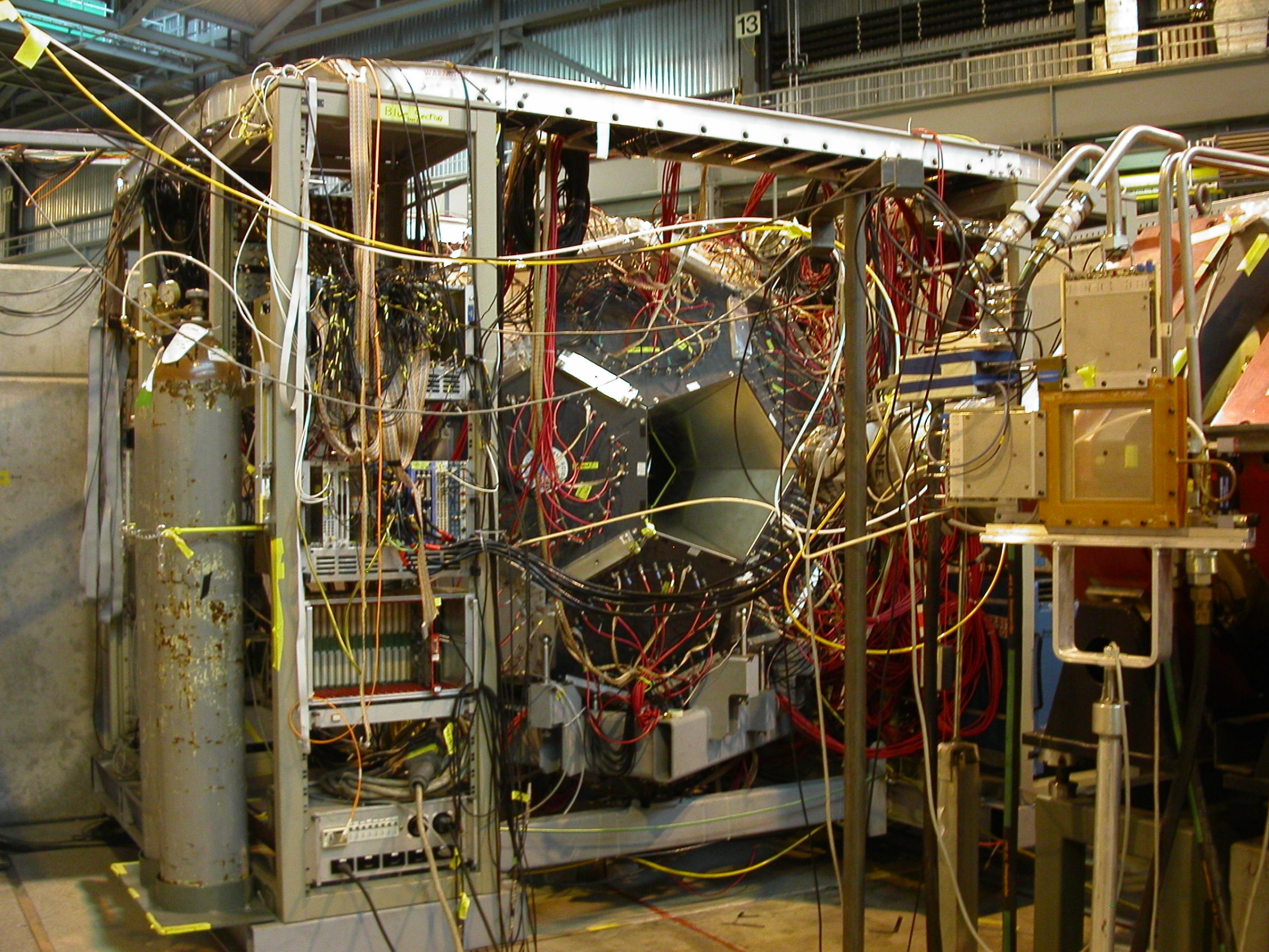
beam off

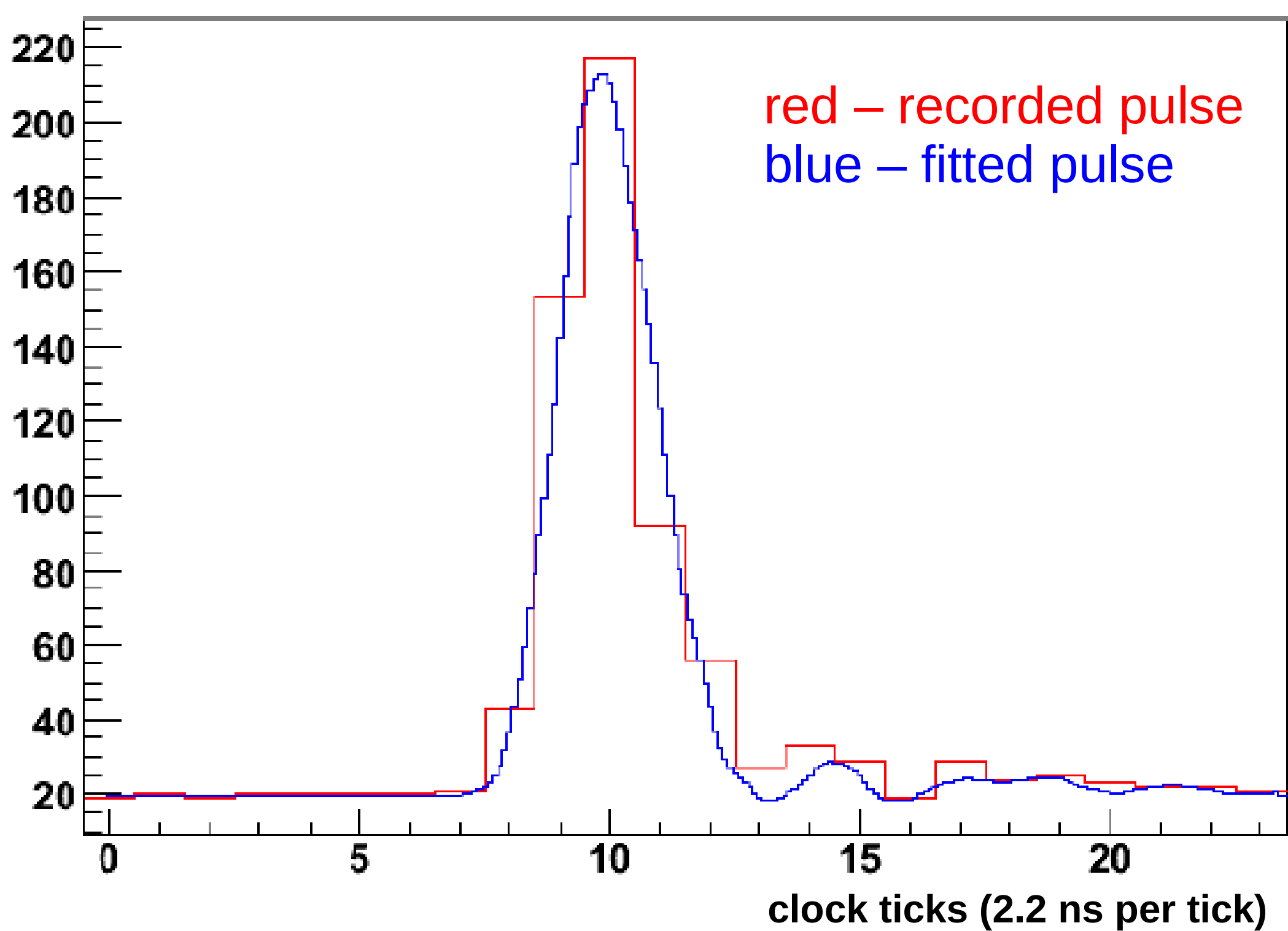
MuLan Setup.

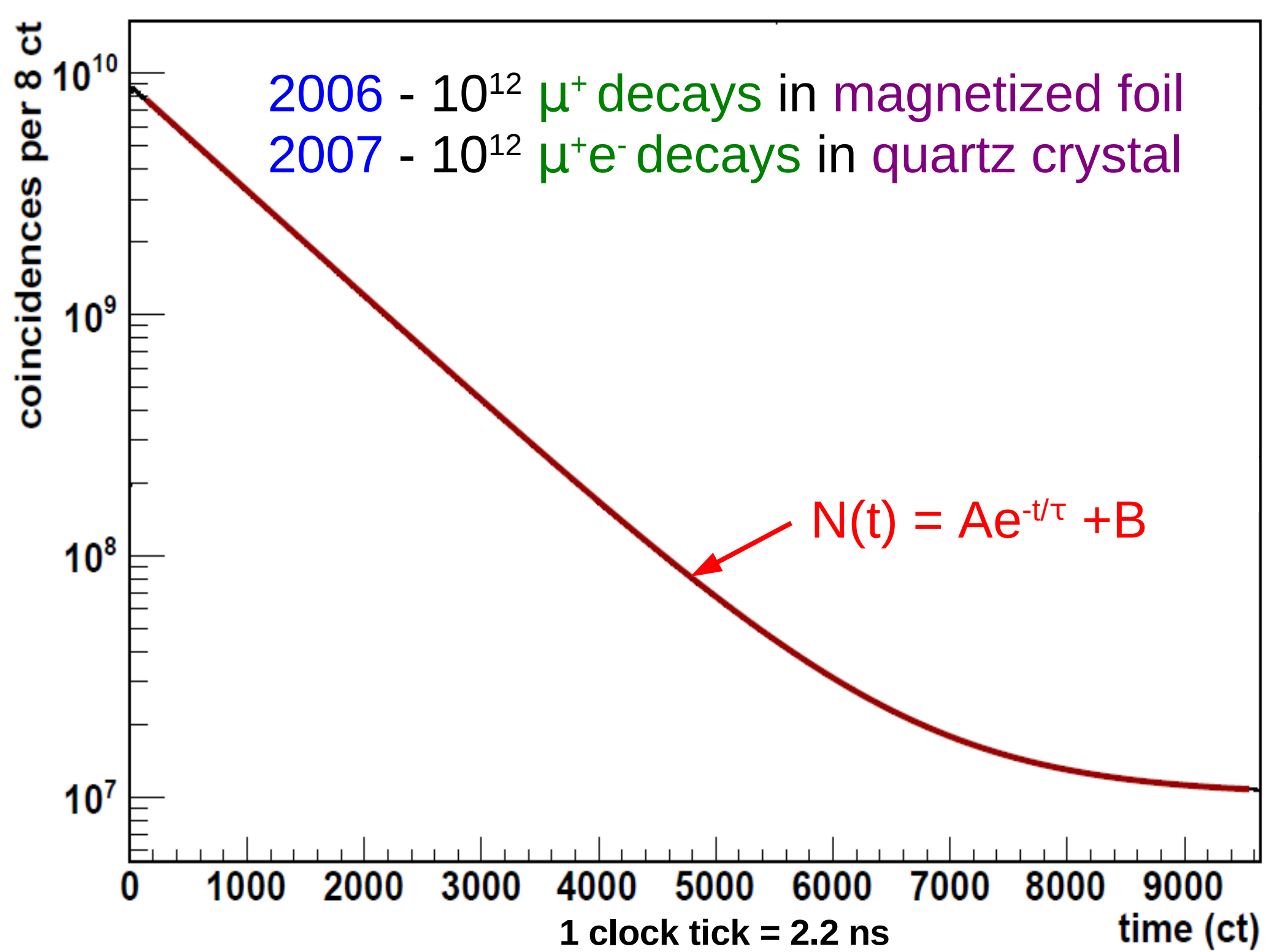


MuLan

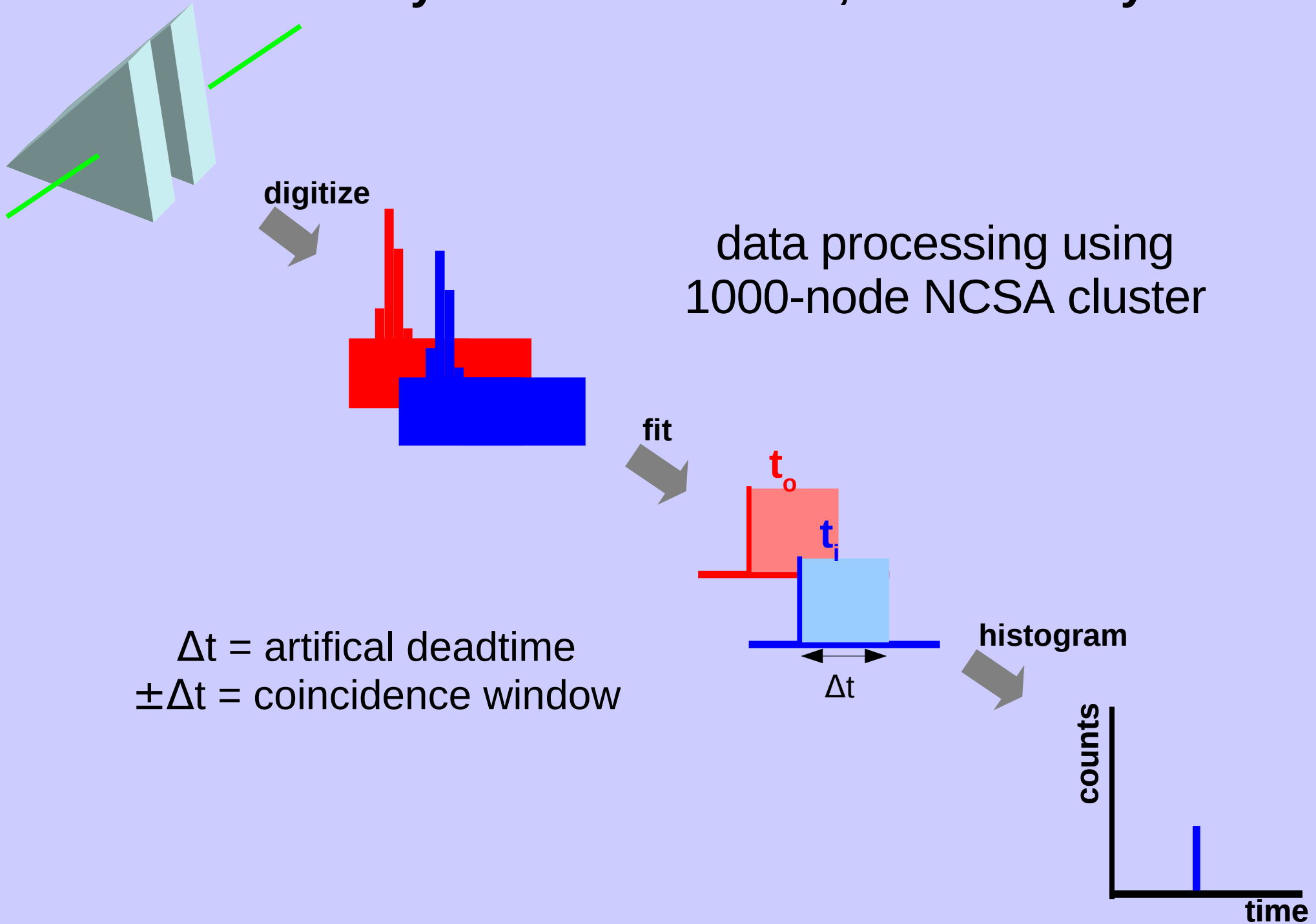




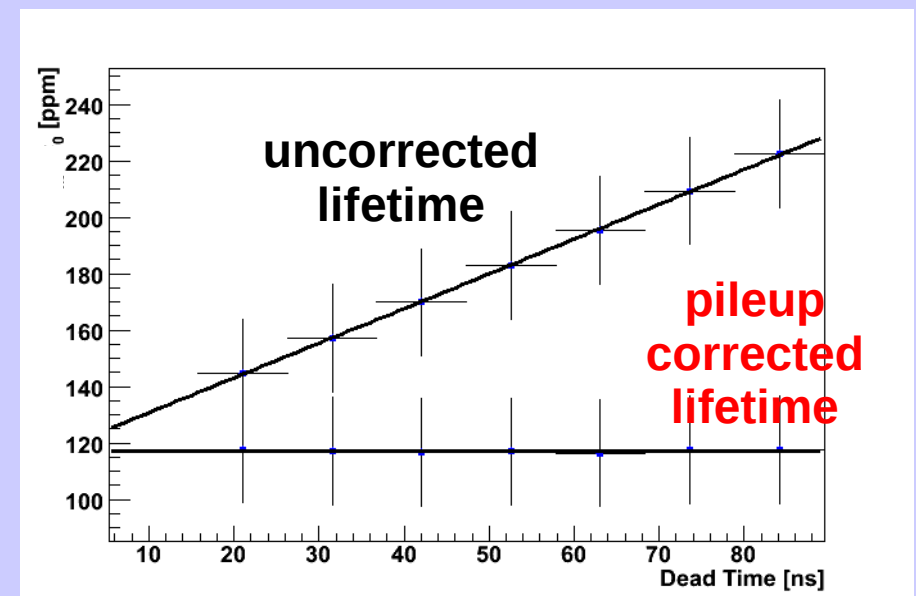
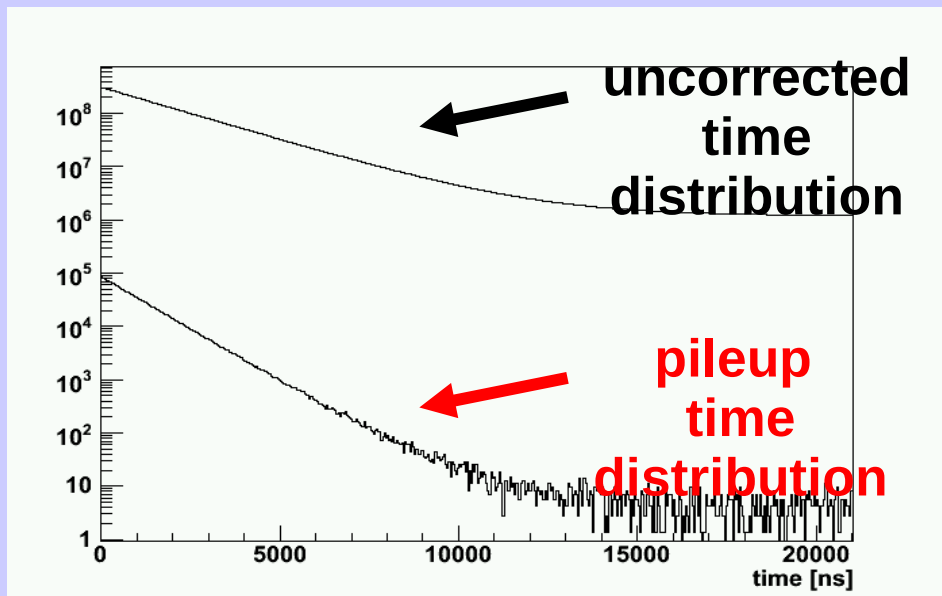
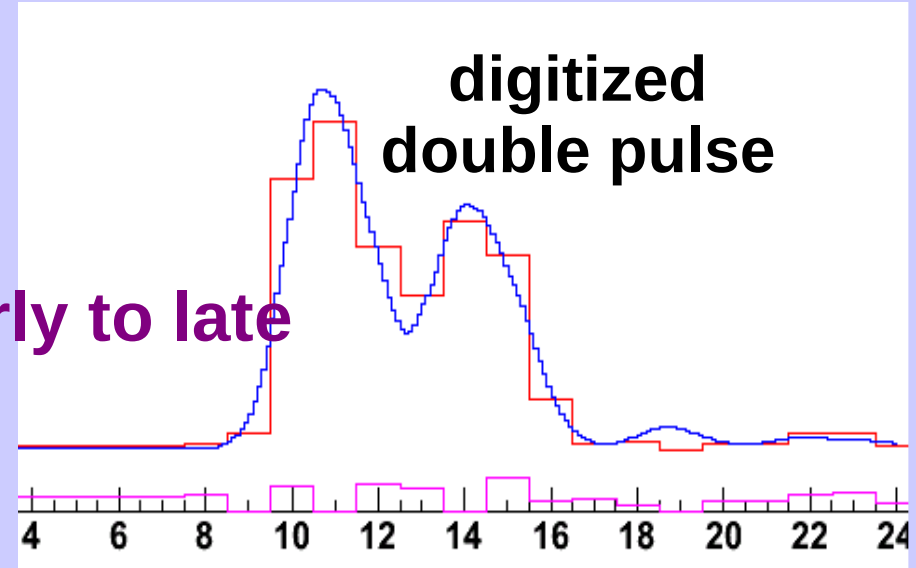
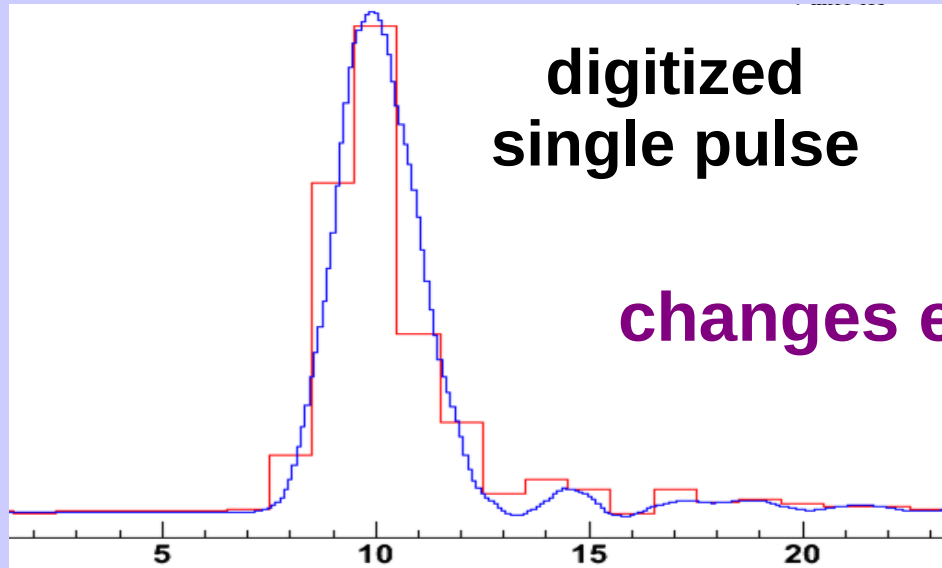




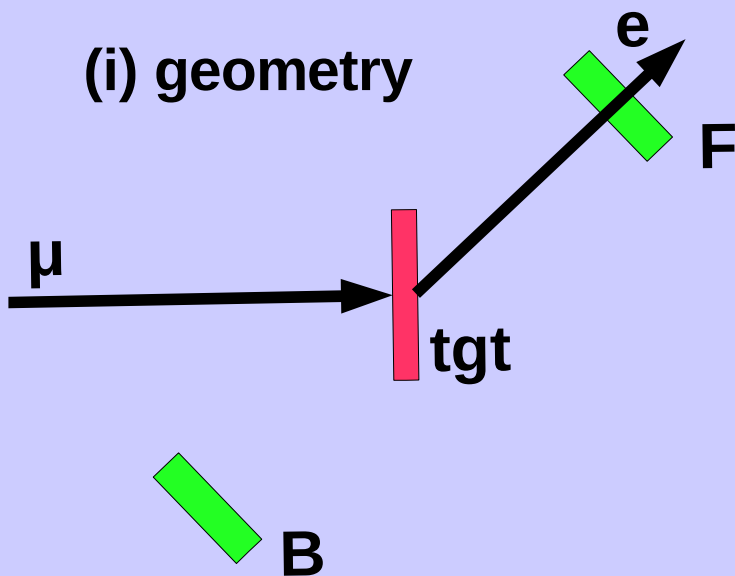
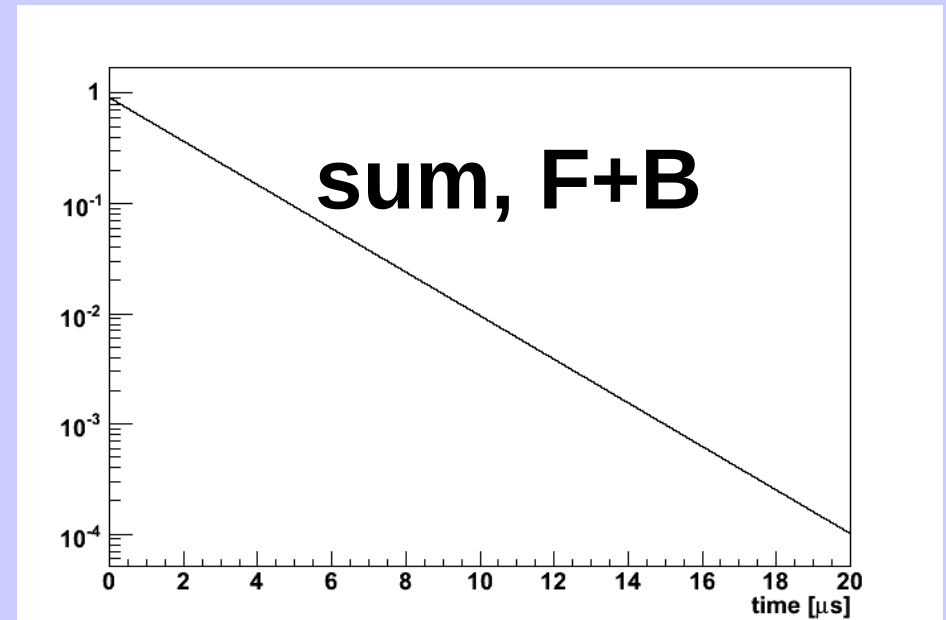
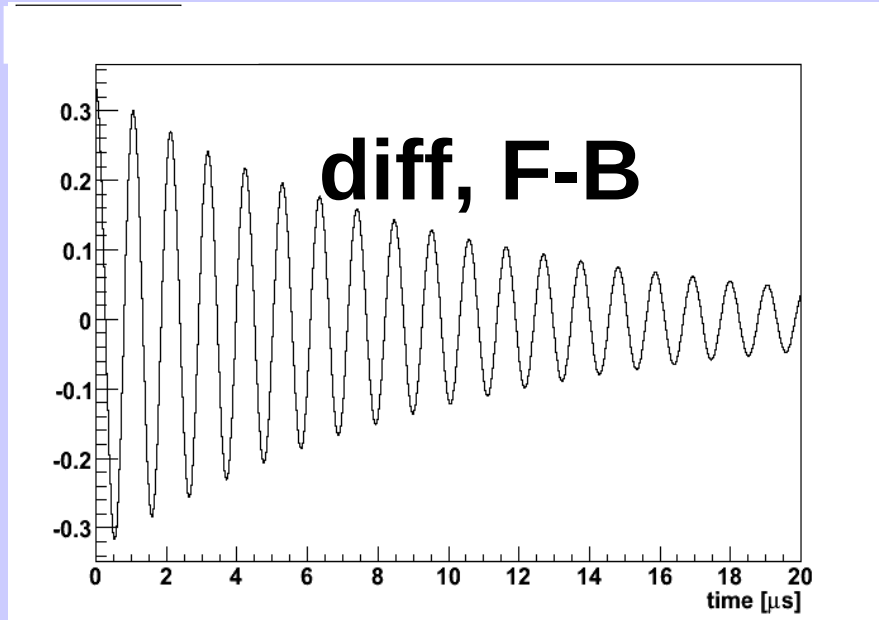
blind analyses of 130TB data, 2×10^{12} decays



- most worrisome systematics (1) - positron pulse pile-up



- most worrisome systematics (2) - muon spin rotation

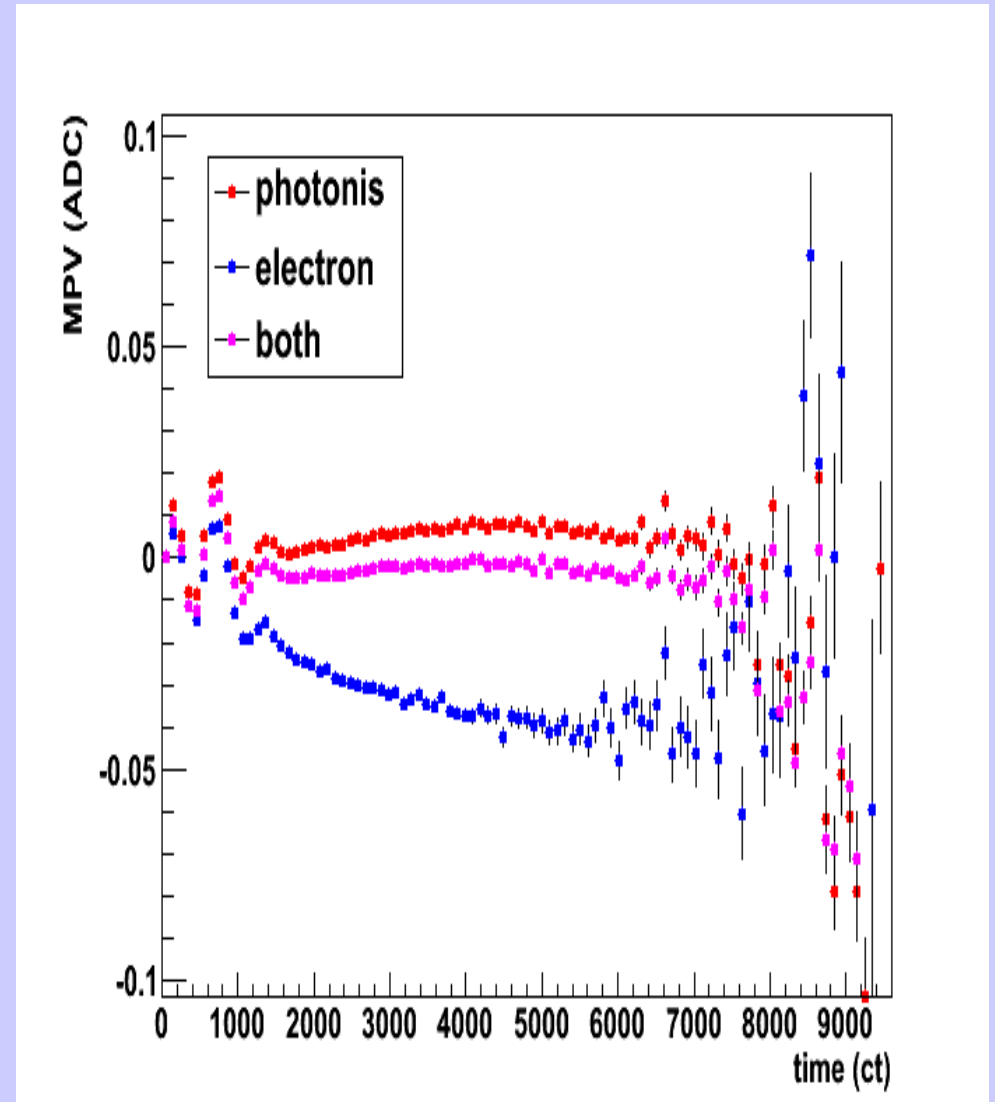
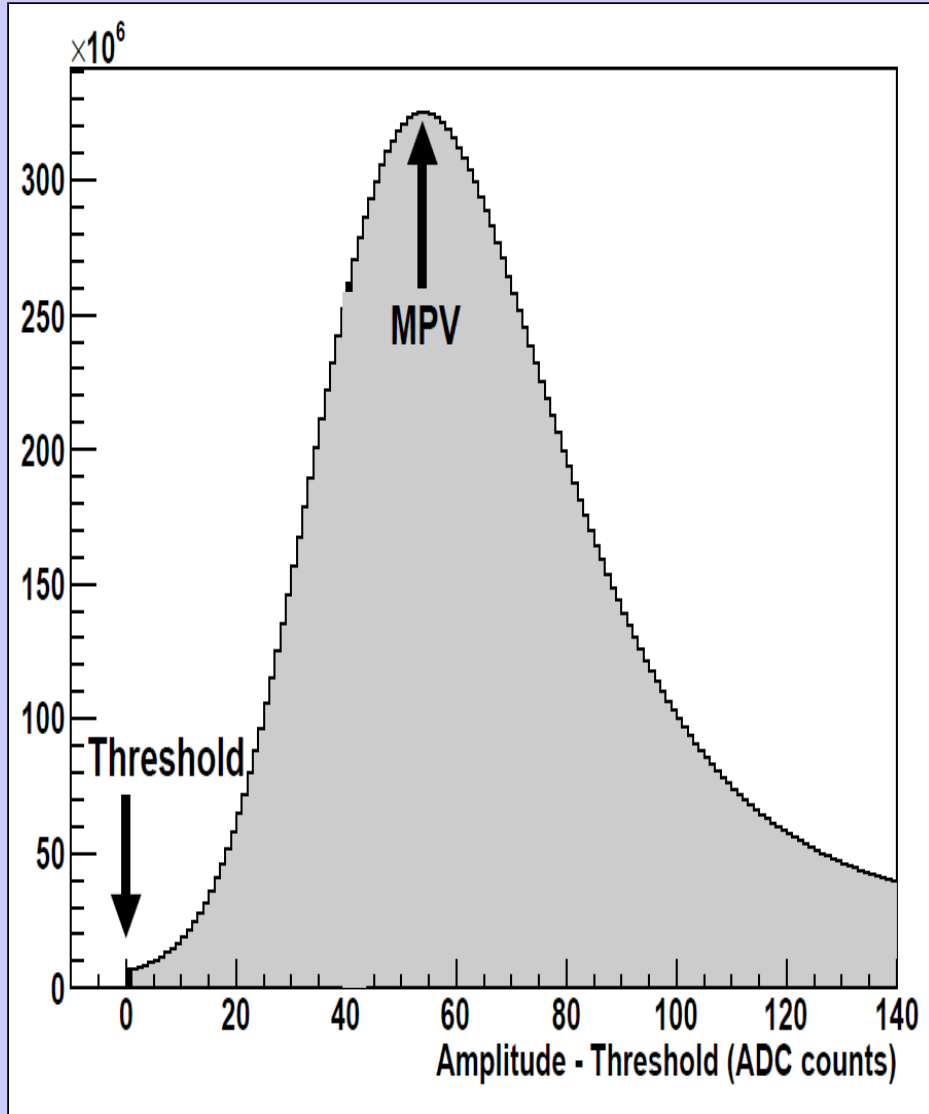


(ii) dephasing

magnetized ferromagnetic foil
(high internal B-field, fast μ^+ precession)

single quartz crystal
(moderate external B-field, fast μ^+e^- precession)

- most worrisome systematics (3) - gain variations



MuLan Results

$$2006: \tau_{\mu} = 2196979.9 \pm 2.5(\text{stat}) \pm 0.9(\text{sys}) \text{ ps}$$

$$2007: \tau_{\mu} = 2196981.2 \pm 3.7(\text{stat}) \pm 0.9(\text{sys}) \text{ ps}$$

$$G_F = 1.166\,378\,8(7) \times 10^{-5} \text{ GeV}^{-2} \quad (0.6 \text{ ppm})$$

Recent Muon Lifetime Measurements

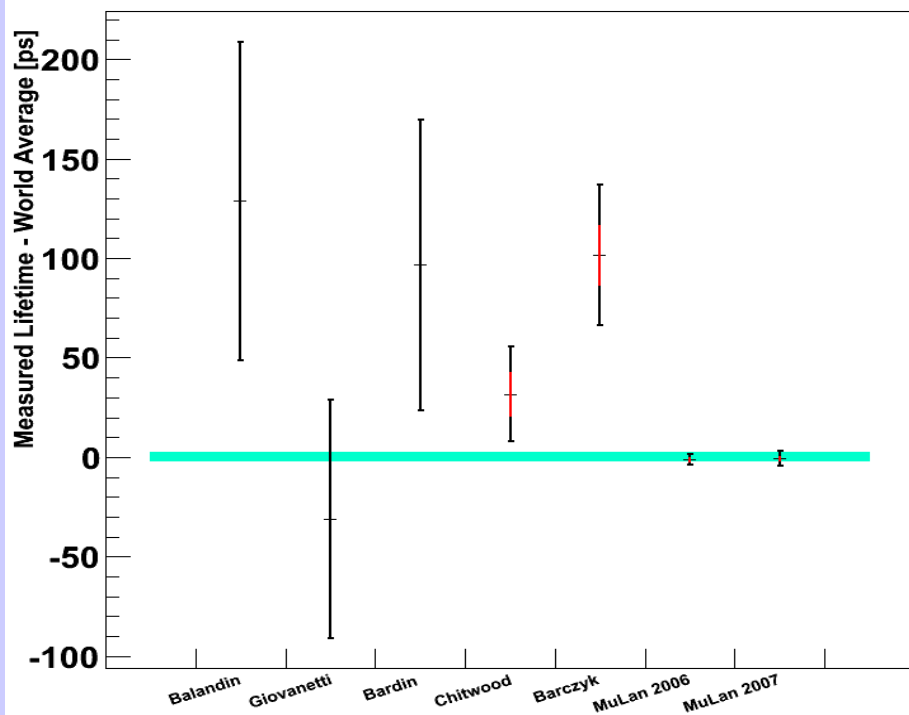
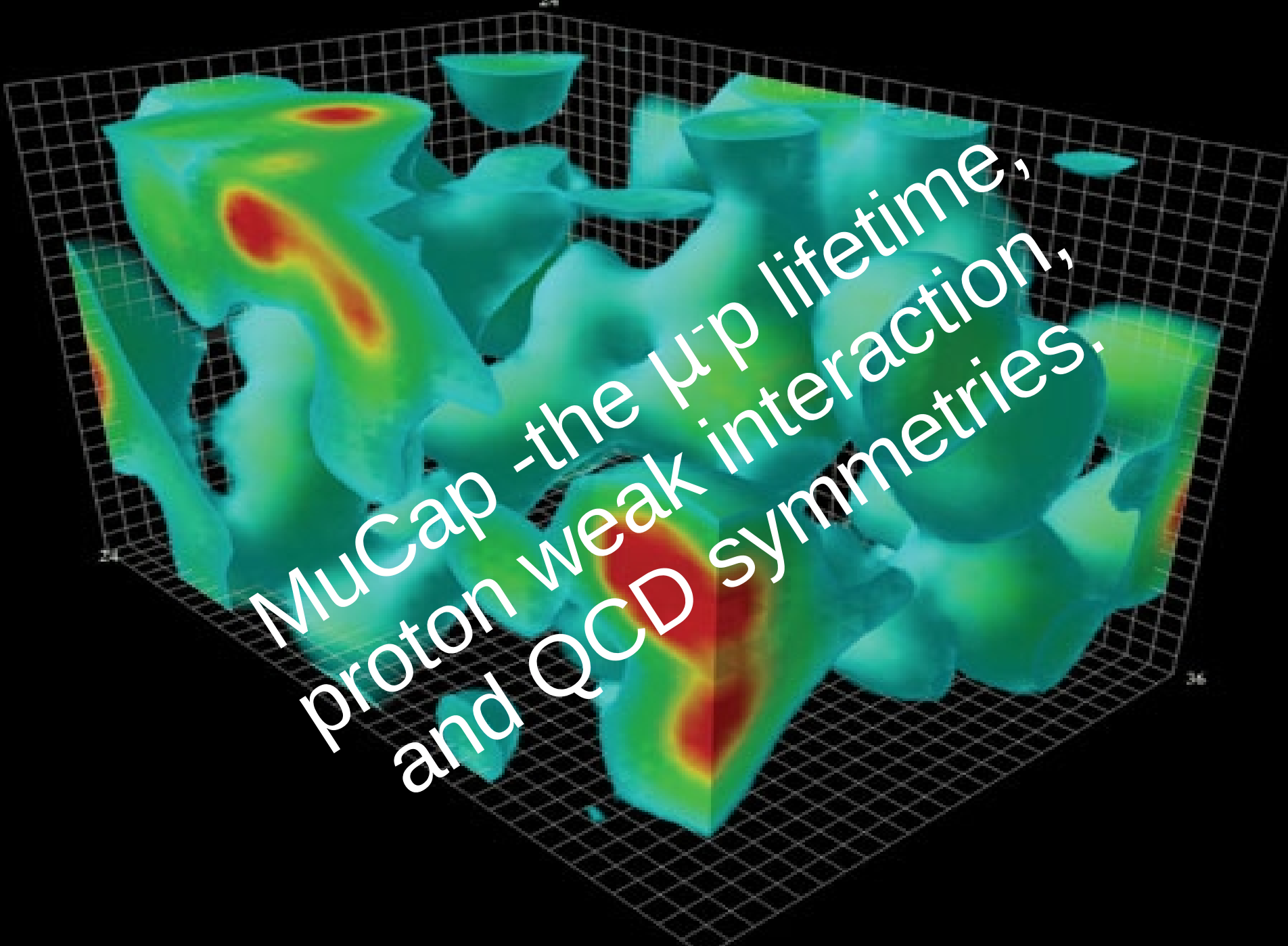


TABLE I: Systematic and statistical uncertainties in ppm. Common uncertainties are represented by single number and dataset-dependent uncertainties are given with one number for each period.

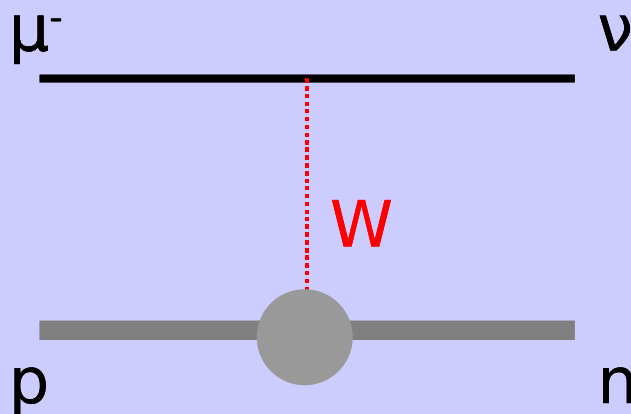
Effect uncertainty in ppm	R06	R07
Kicker stability	0.20	0.07
Spin precession / relaxation	0.10	0.20
Pileup	0.20	
Gain stability	0.25	
Upstream muon stops	0.10	
Timing stability	0.12	
Clock calibration	0.03	
Total systematic	0.42	0.42
Statistical uncertainty	1.14	1.68



MuCap - the μ -p lifetime,
proton weak interaction,
and QCD symmetries.

Why we measure $\tau_{\mu p}$?

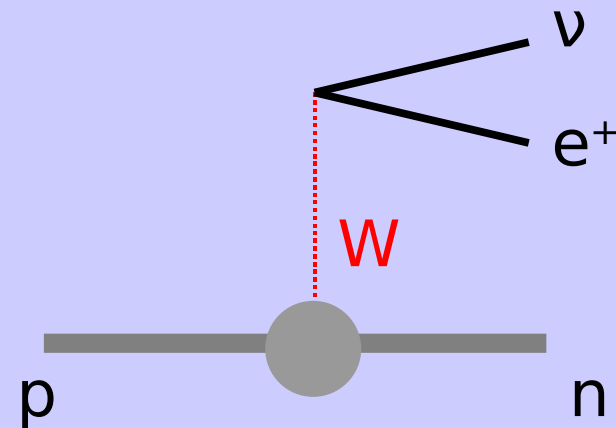
muon capture,
 $\mu^- p \rightarrow \nu n$



proton's weak couplings

g_v, g_a, g_m, g_p

beta decay,
 $p \rightarrow n e^+ \nu$



proton's weak couplings

g_v, g_a

knowing g_v, g_a, g_m determine g_p ,
the poorly known **proton induced pseudoscalar coupling**

Why we determine g_p ?

fundamental quantity describing the proton's weak interaction

the approximate conservation of axial current enforces a rigorous relation between the weak couplings g_p , g_a

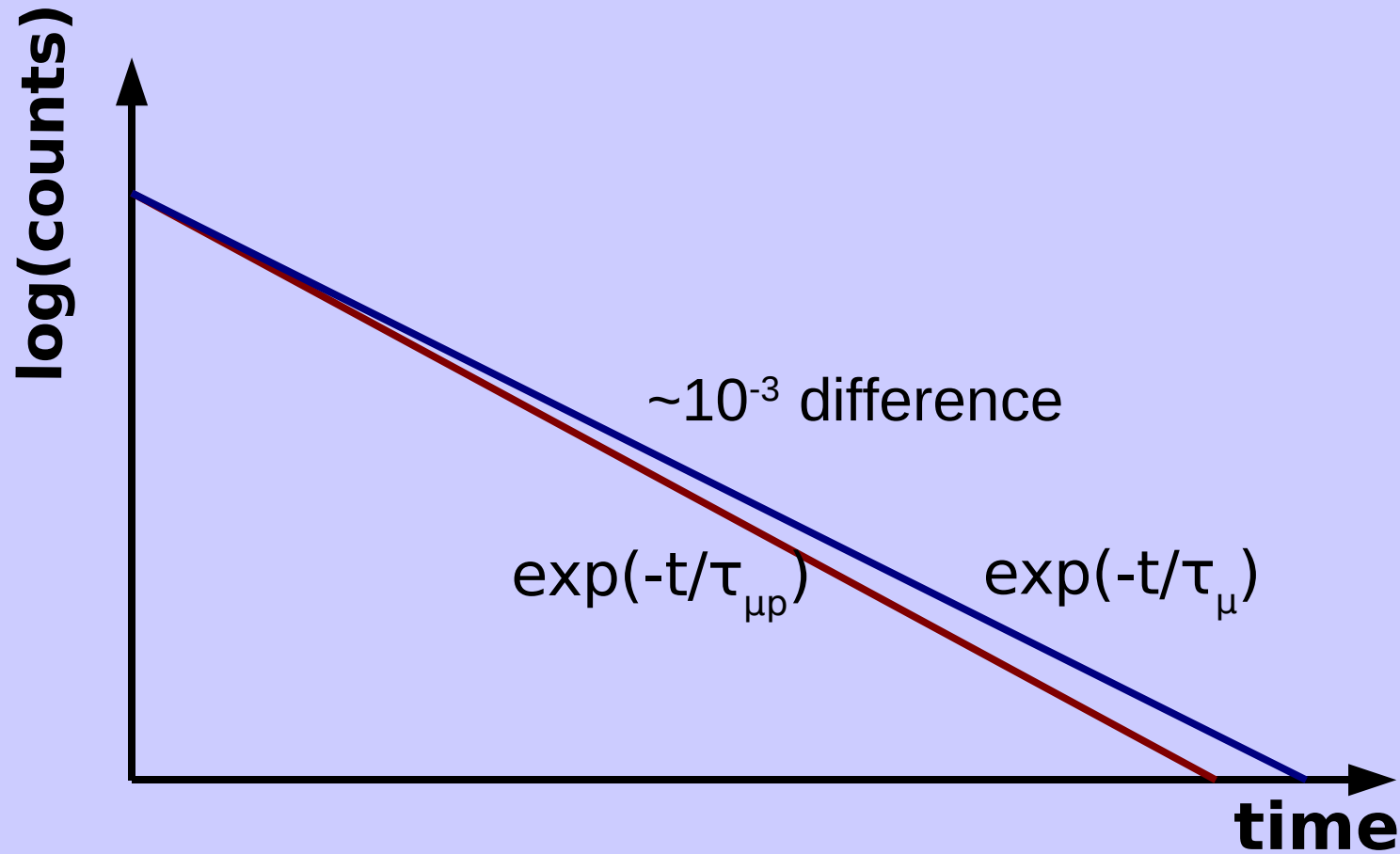
$$g_p(q^2 = -0.88m_\mu^2) = (6.47 \pm 0.18) g_a(0) = 8.26 \pm 0.23$$

Its verification represents an important test of QCD symmetries and spontaneous, explicit symmetry breaking.

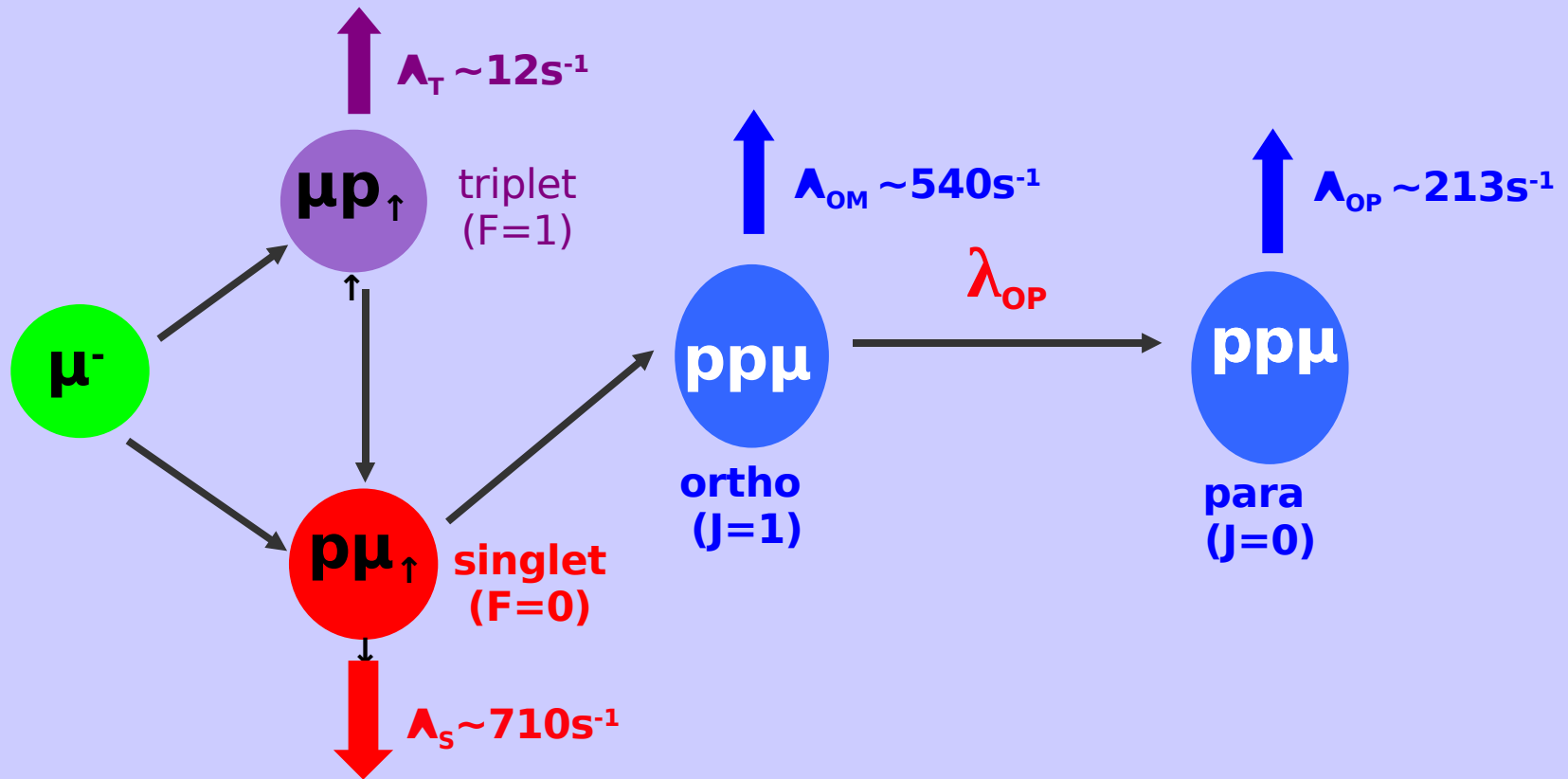
knowledge of g_p (and g_v , g_a , g_m) allows precision studies of weak nuclear interactions through nuclear muon capture (for example our μ -D experiment)

How we determine g_p ?

$$\Lambda_s \cong 1/\tau_{\mu-p} - 1/\tau_{\mu+}$$



μ chemistry, a complication

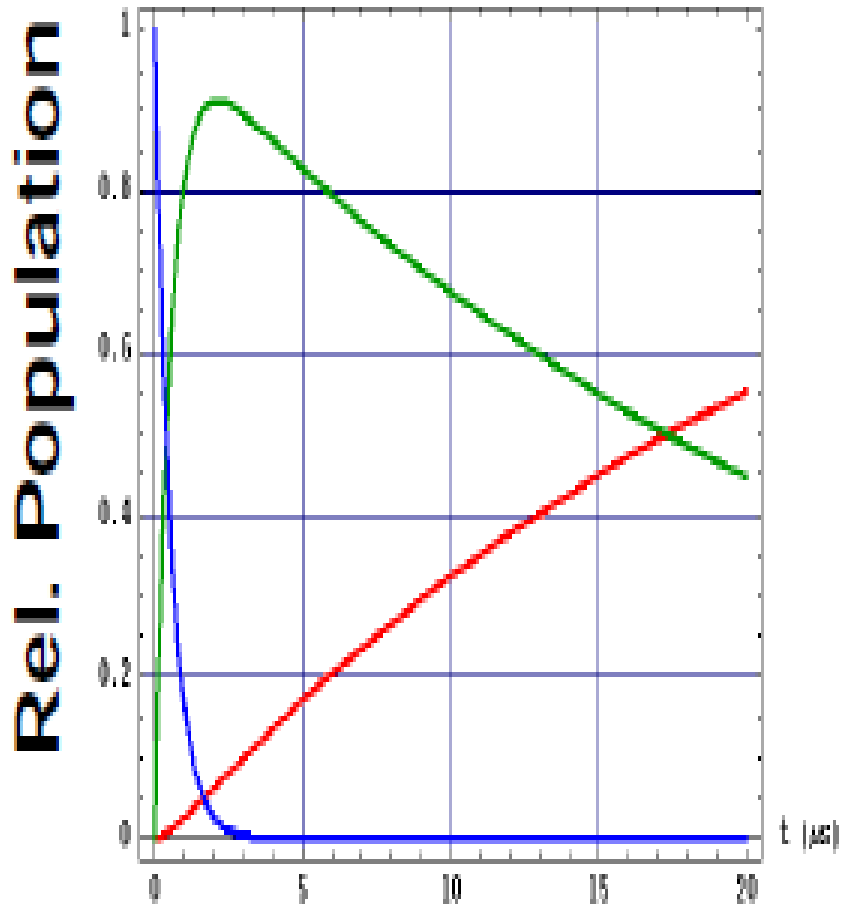


use ultra-pure (chemically, isotopically)
10 bar H_2 (1% liquid hydrogen density)

→ 96% singlet capture

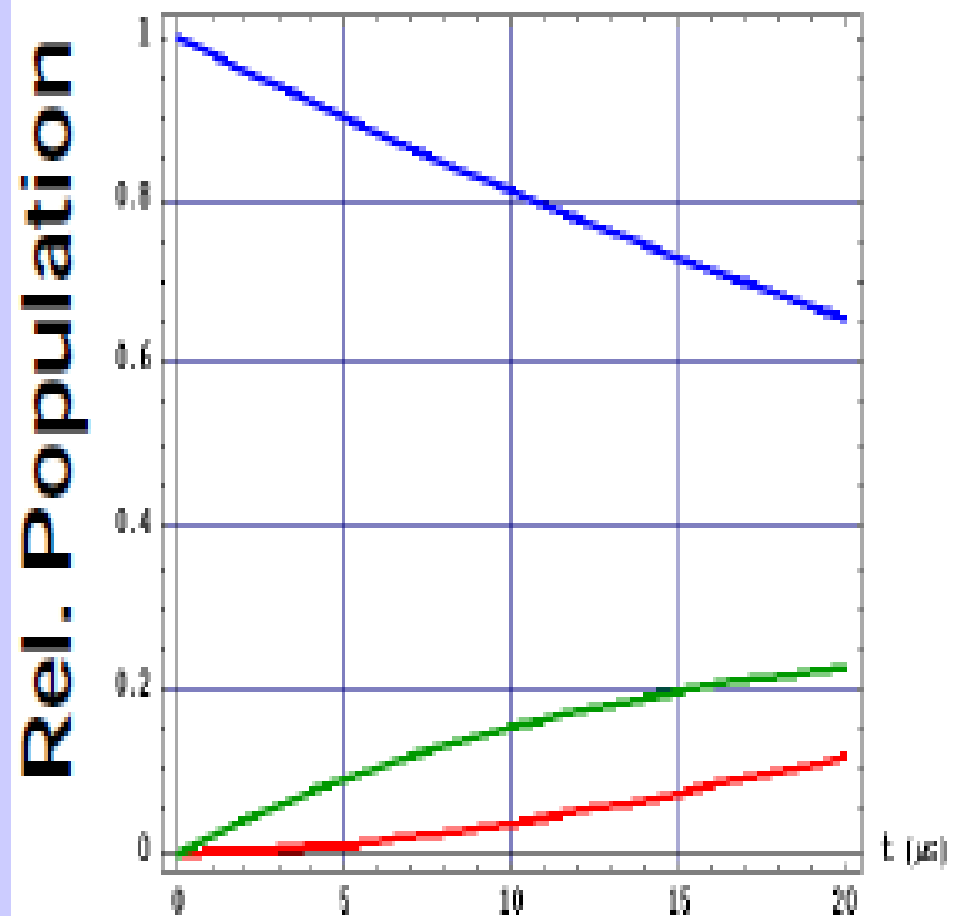
Relative populations of
singlet atoms, ortho molecules, para molecules
in liquid and gas

$\phi = 1$ (Liquid)



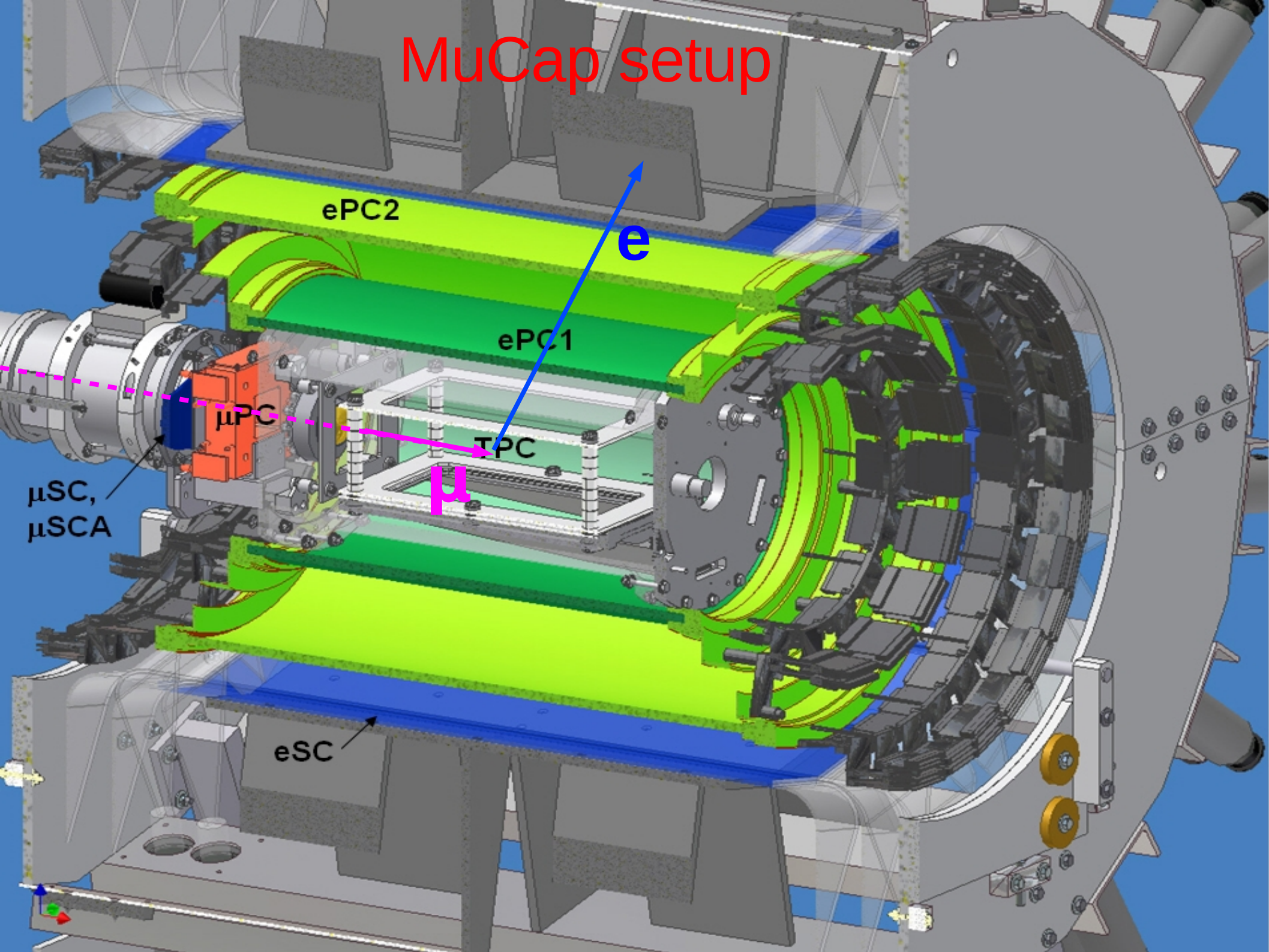
Time after μp Formation

$\phi = 0.01$ (~10 bar gas)

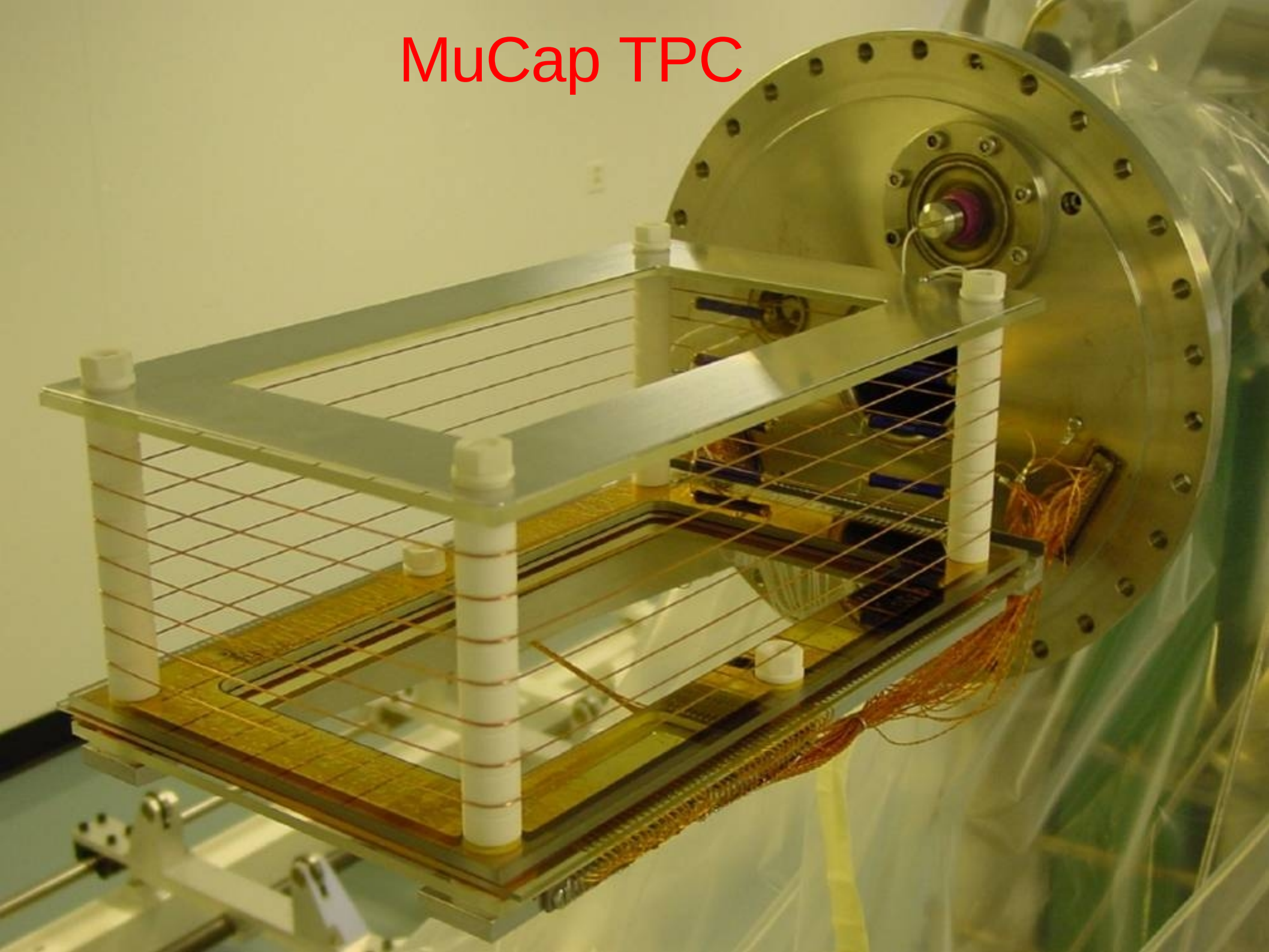


Time after μp Formation

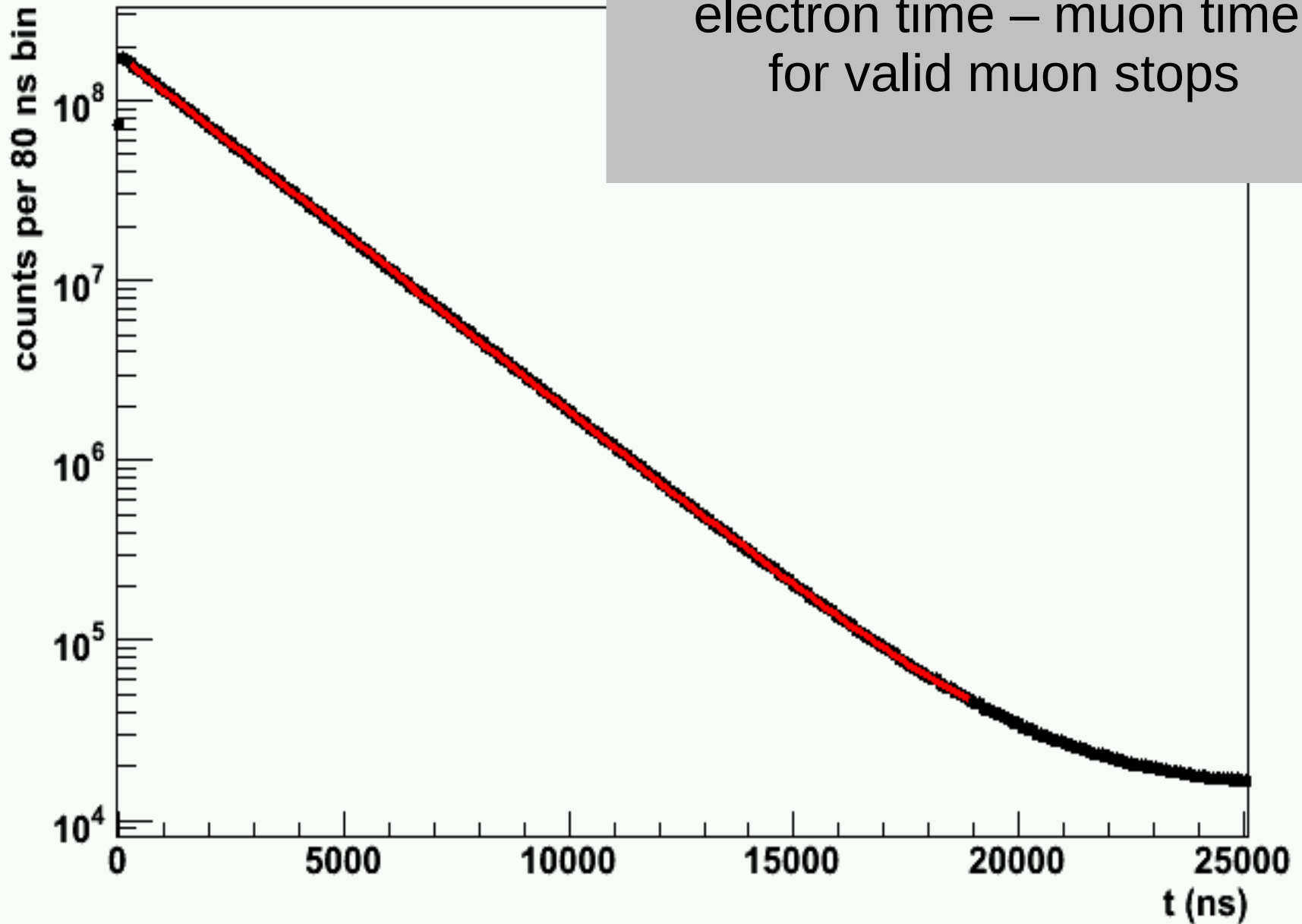
MuCap setup



MuCap TPC

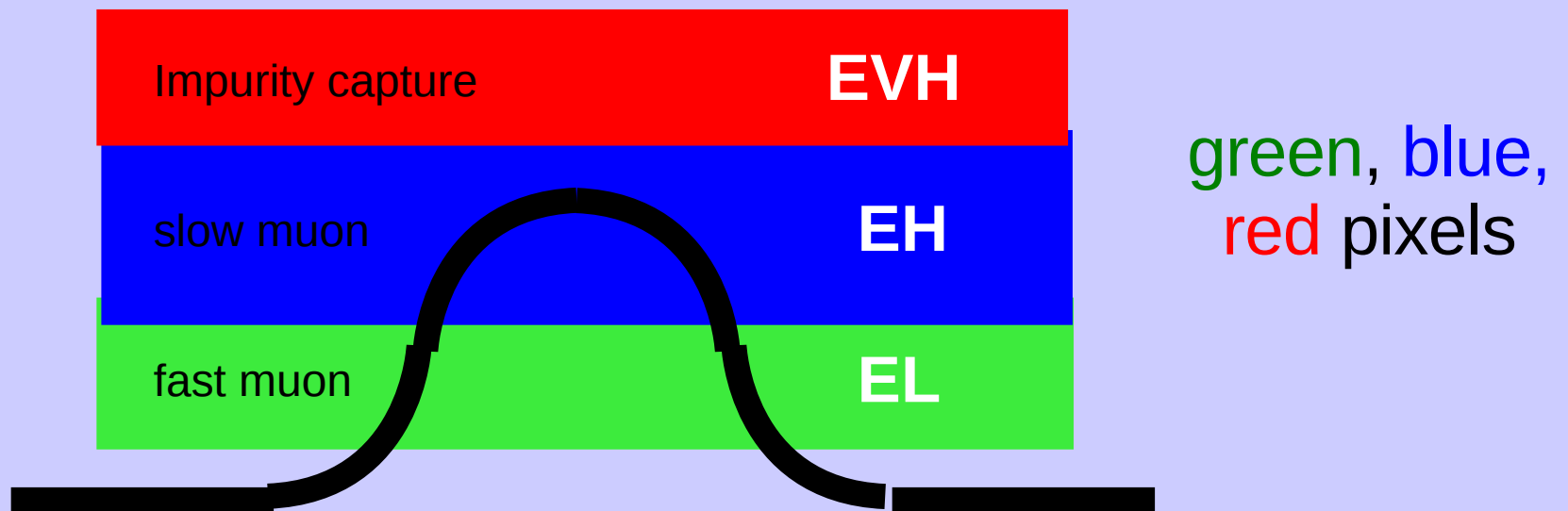
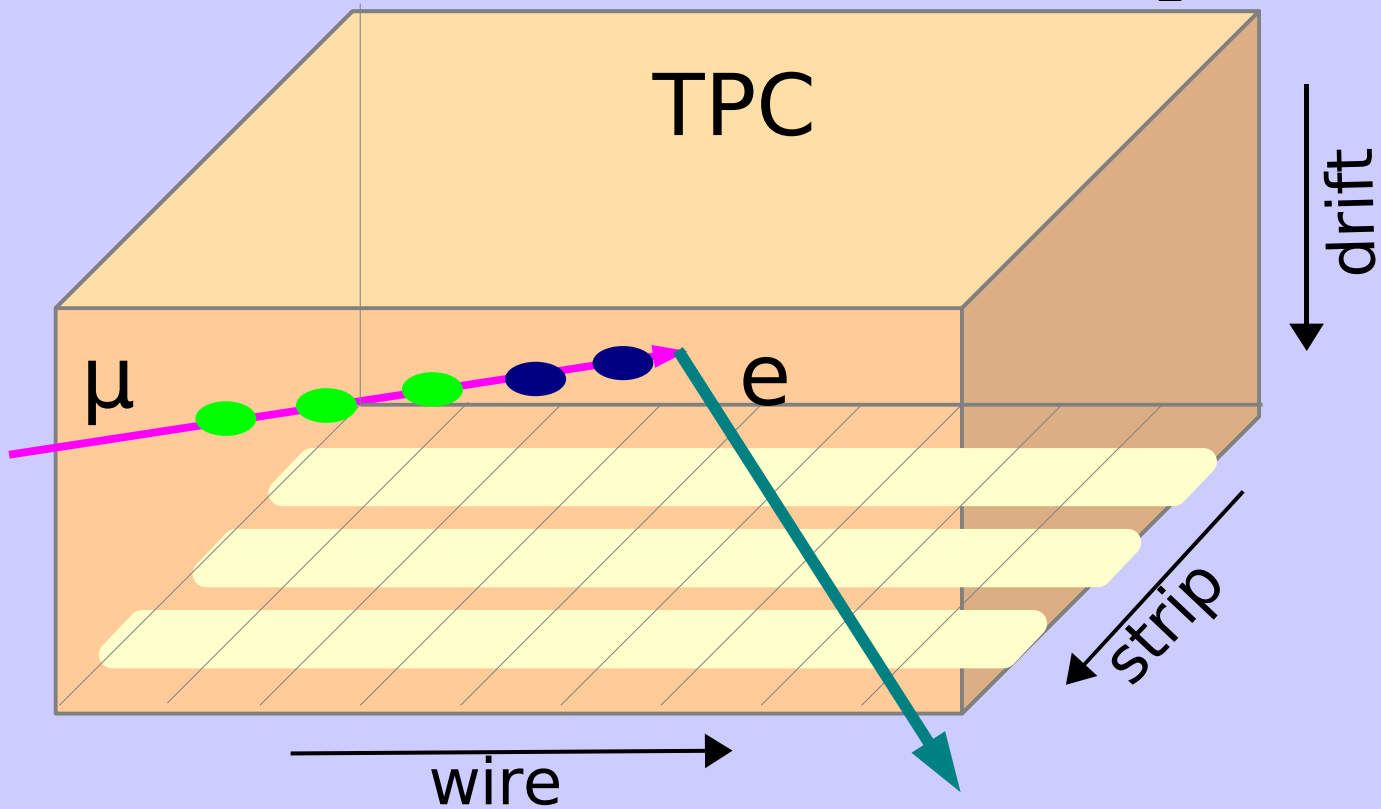


Lifetime histogram



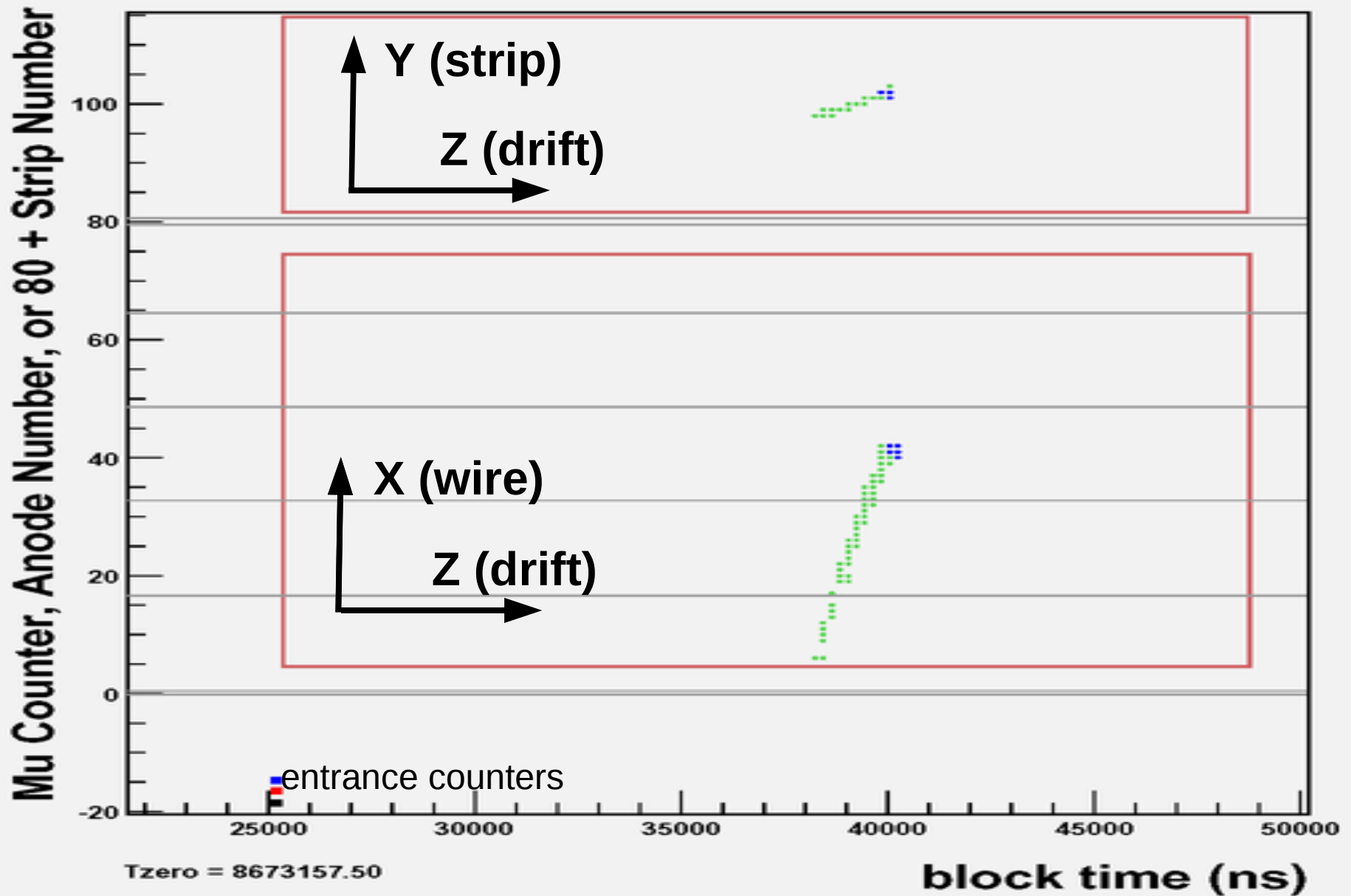
electron time – muon time
for valid muon stops

Validation of μ stops in H_2 gas

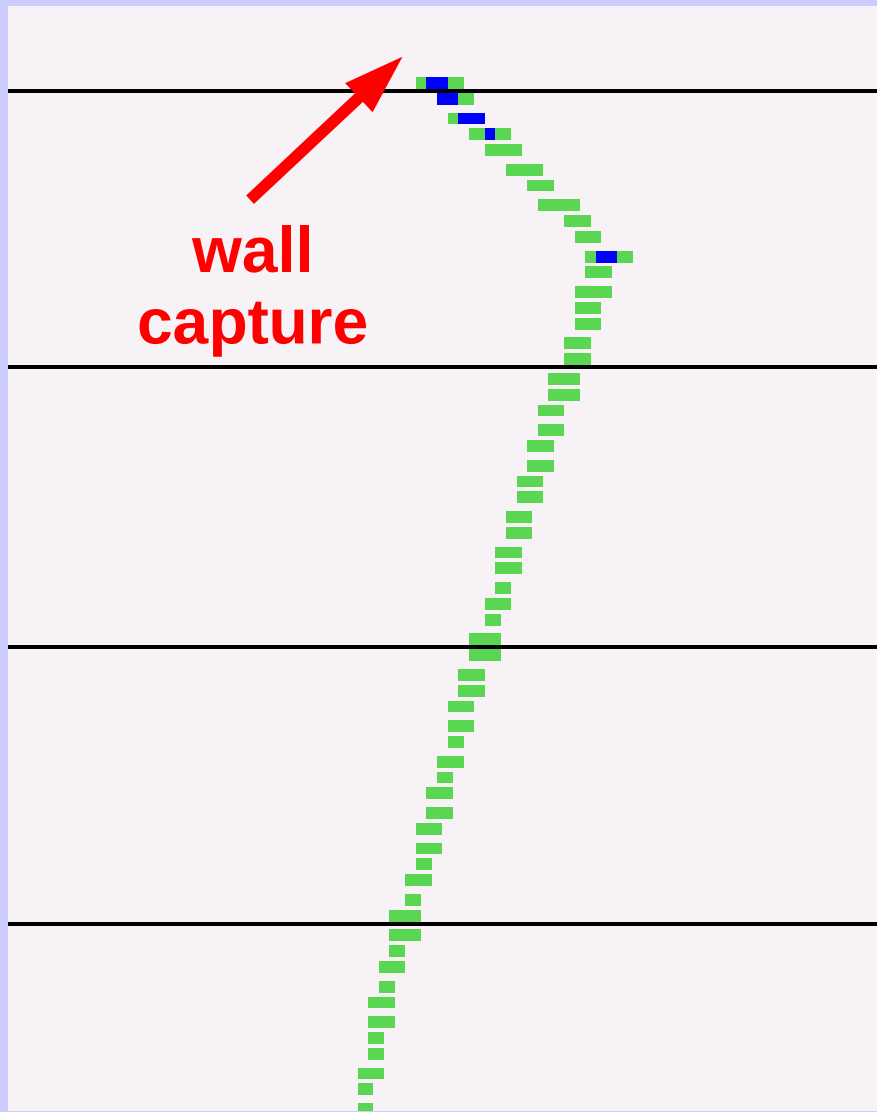


Validation of μ stops in H_2 gas

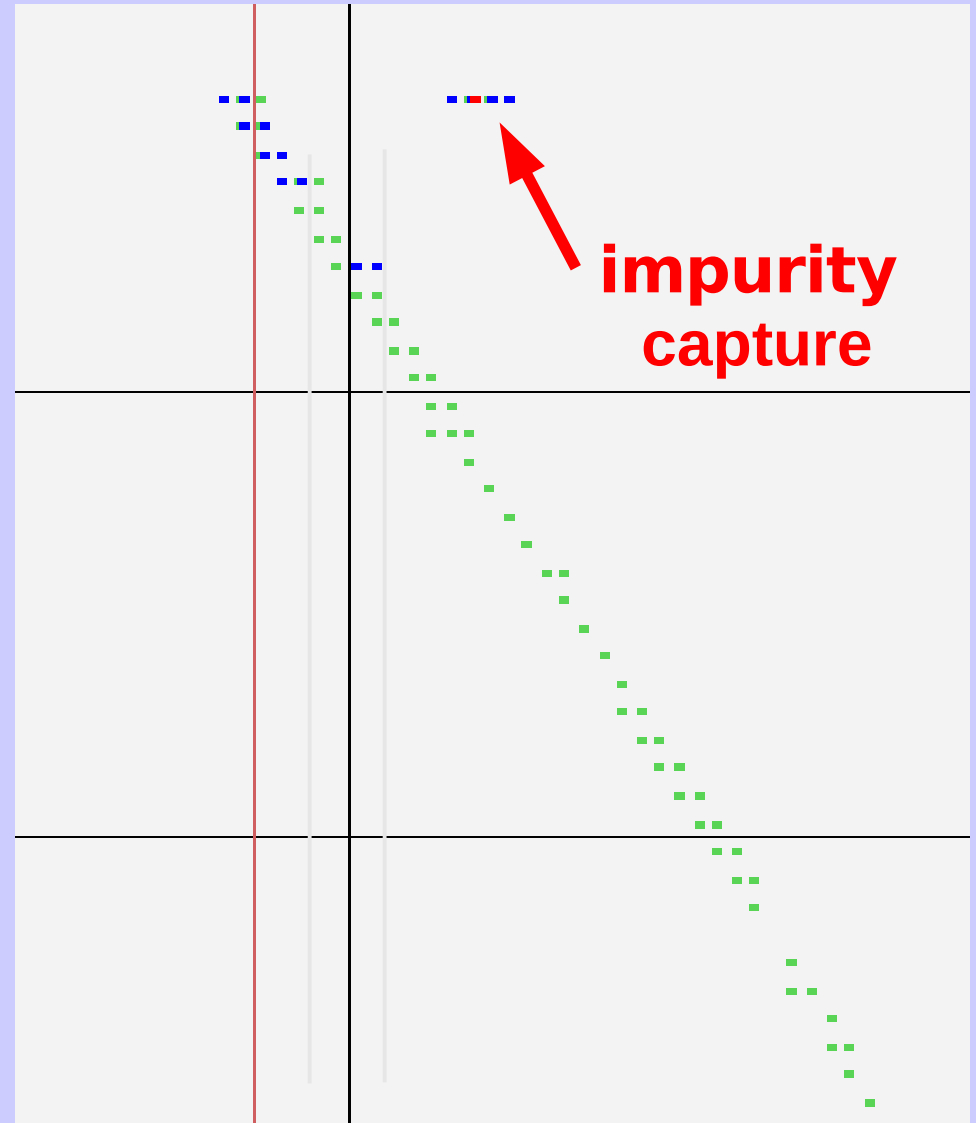
TPC Display



- worrisome systematics -
muon capture on $Z > 1$ materials
e.g. walls and impurities



μ scatter event



μ transfer event

MuCap Results

$$2005: \Lambda_s = 725.0 \pm 13.7(\text{stat}) \pm 10.7(\text{syst}) \text{ s}^{-1}$$

$$g_p(q^2 = -0.88 \text{ m}^2_{\mu}) = 7.8 \pm 1.1$$

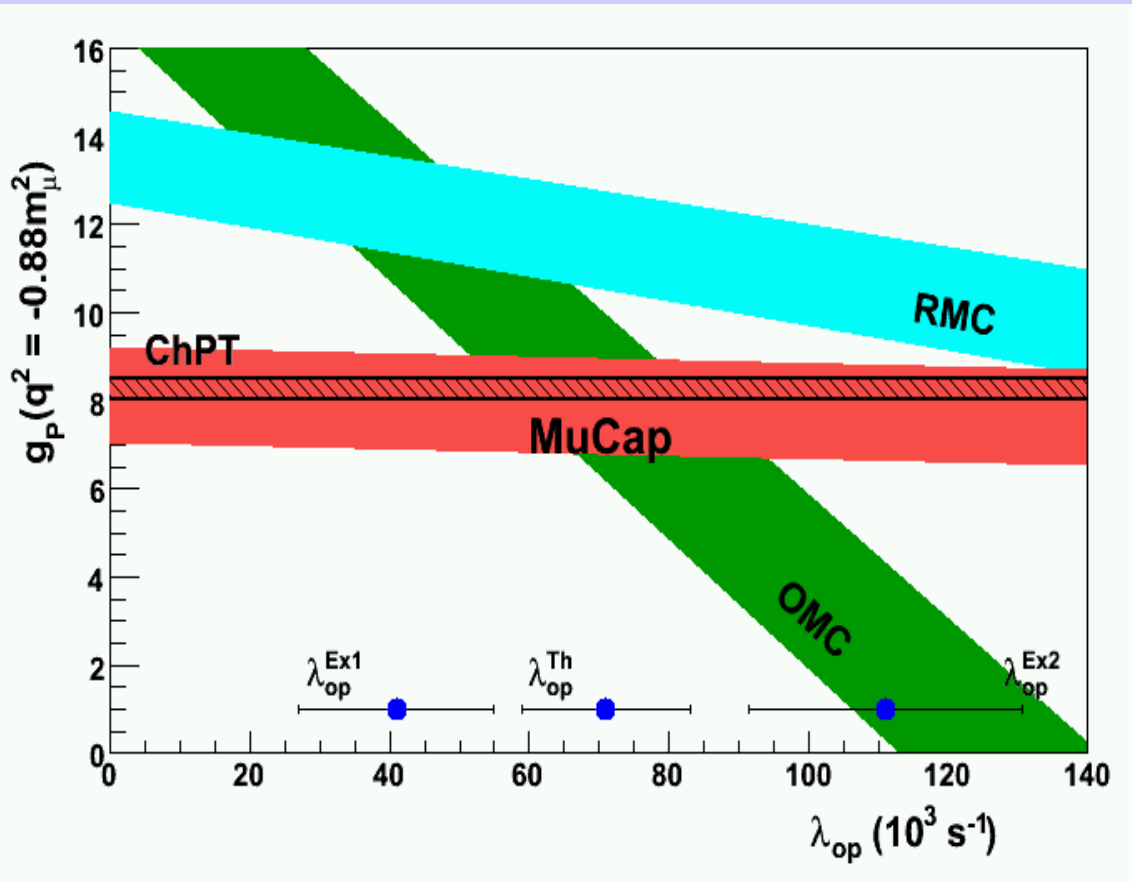



TABLE I. Systematic corrections and uncertainties applied to the observed μ^- disappearance rate λ .

Source	Correction (s^{-1})	Uncertainty (s^{-1})
$Z > 1$ impurities	-19.2	5.0
μd diffusion	-10.2	1.6
μp diffusion	-2.7	0.5
$\mu + p$ scattering		3
μ pileup veto efficiency		3
Total	-32.1	8.5

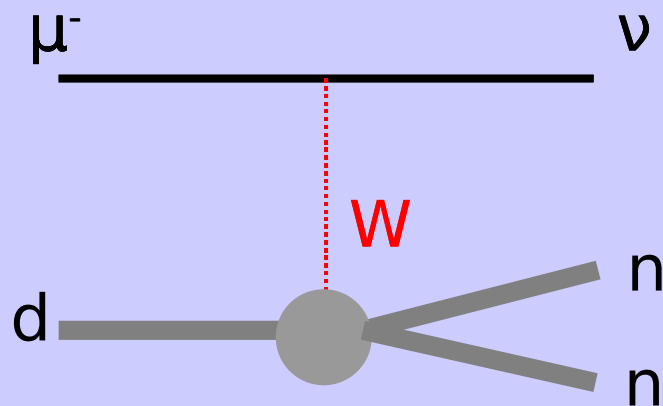
goal for 2006/2007 datasets is Λ_s to $\pm 5 \text{ s}^{-1}$



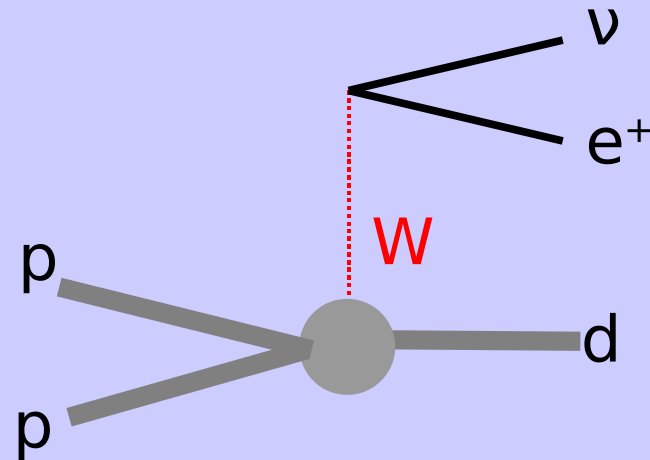
MuSun -the μ -d lifetime,
elementary weak nuclear interaction,
and solar hydrogen burning.

Why we measure $\tau_{\mu d}$?

muon capture,
 $\mu^- d \rightarrow \nu n n$



proton-proton fusion,
 $pp \rightarrow de^+\nu$



knowing g_v , g_a , g_m and g_p ,
the **deuteron wavefunction** and **NN interaction**,
measure the poorly known $\mu^- d$ capture rate and
determine the poorly known **two-body weak axial current** (L_{1A})

Why we determine Λ_d , L_{1A} ?

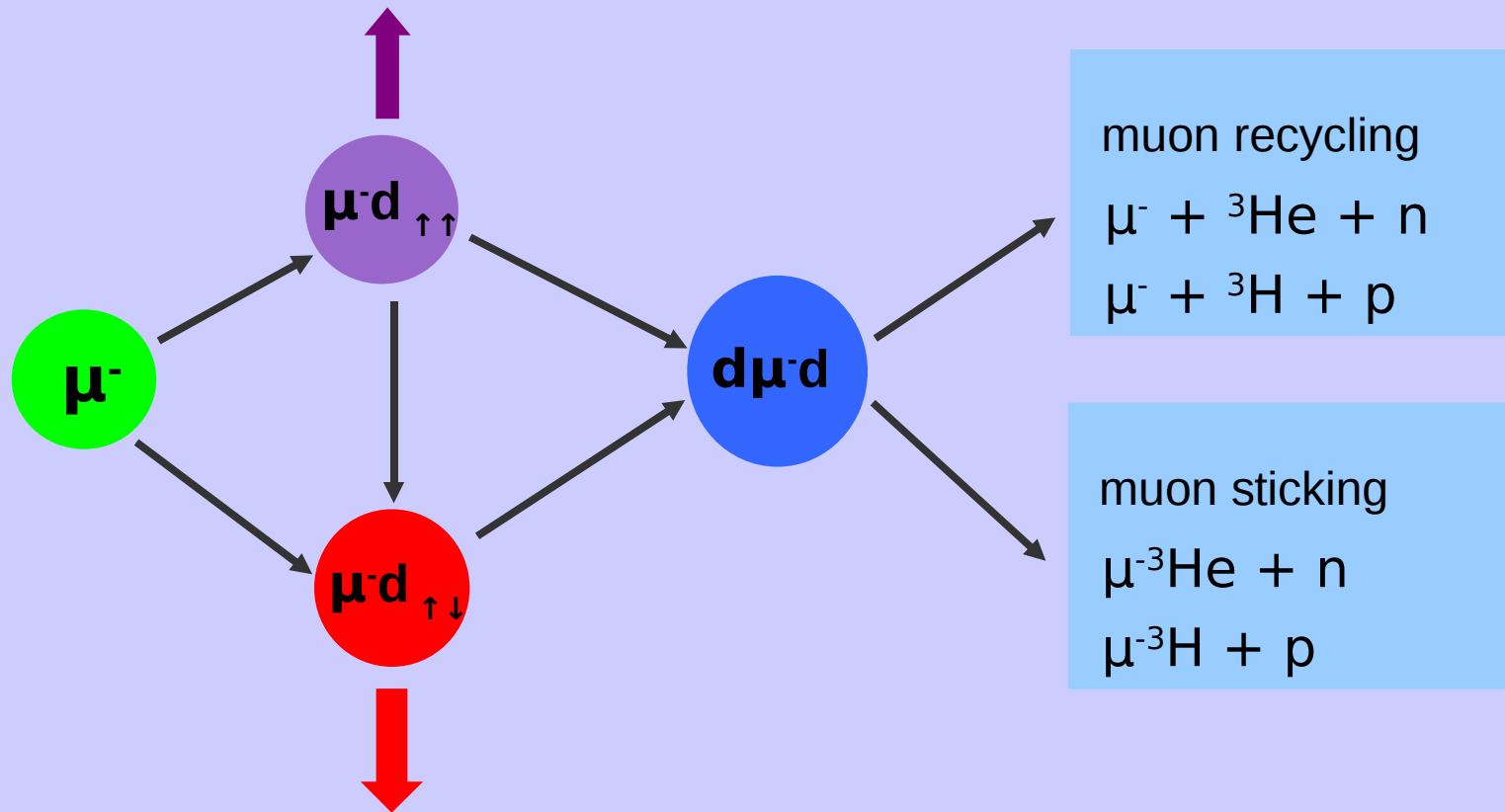
elementary weak nuclear interaction where precision measurement and precision calculation are possible.

$\mu^-d \rightarrow \nu nn$ reaction related to weak processes of intense interest in solar physics (pp fusion) and neutrino physics (νd interactions).

Involve effects of poorly known two-body weak currents

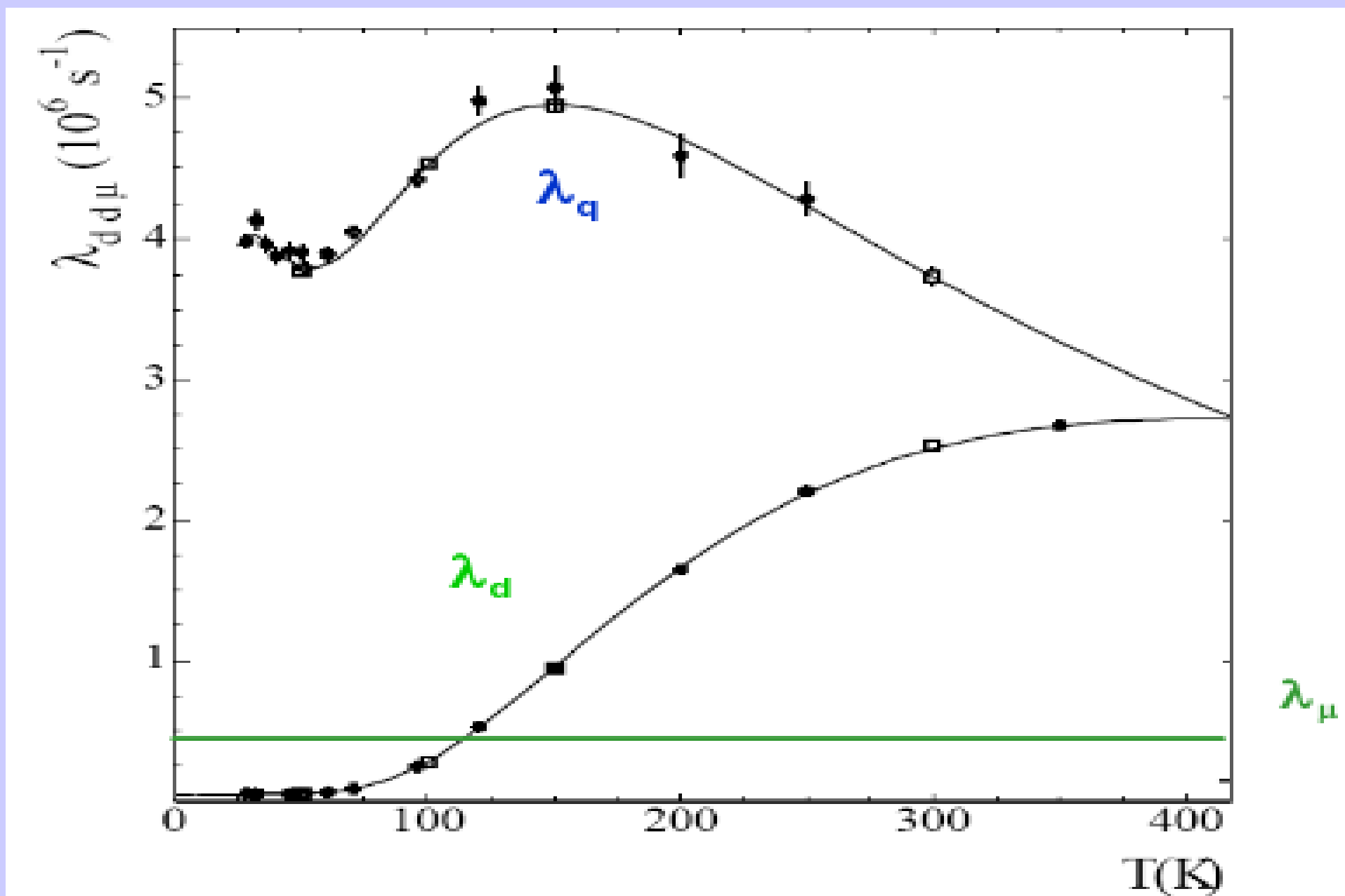
goal of $\pm 1.5\%$ measurement of capture rate Λ_d is five-fold improvement over existing measurements of $470 \pm 29 \text{ s}^{-1}$ (Bardin et al.) and $409 \pm 40 \text{ s}^{-1}$ (Cargnelli et al.)

μ chemistry, a complication

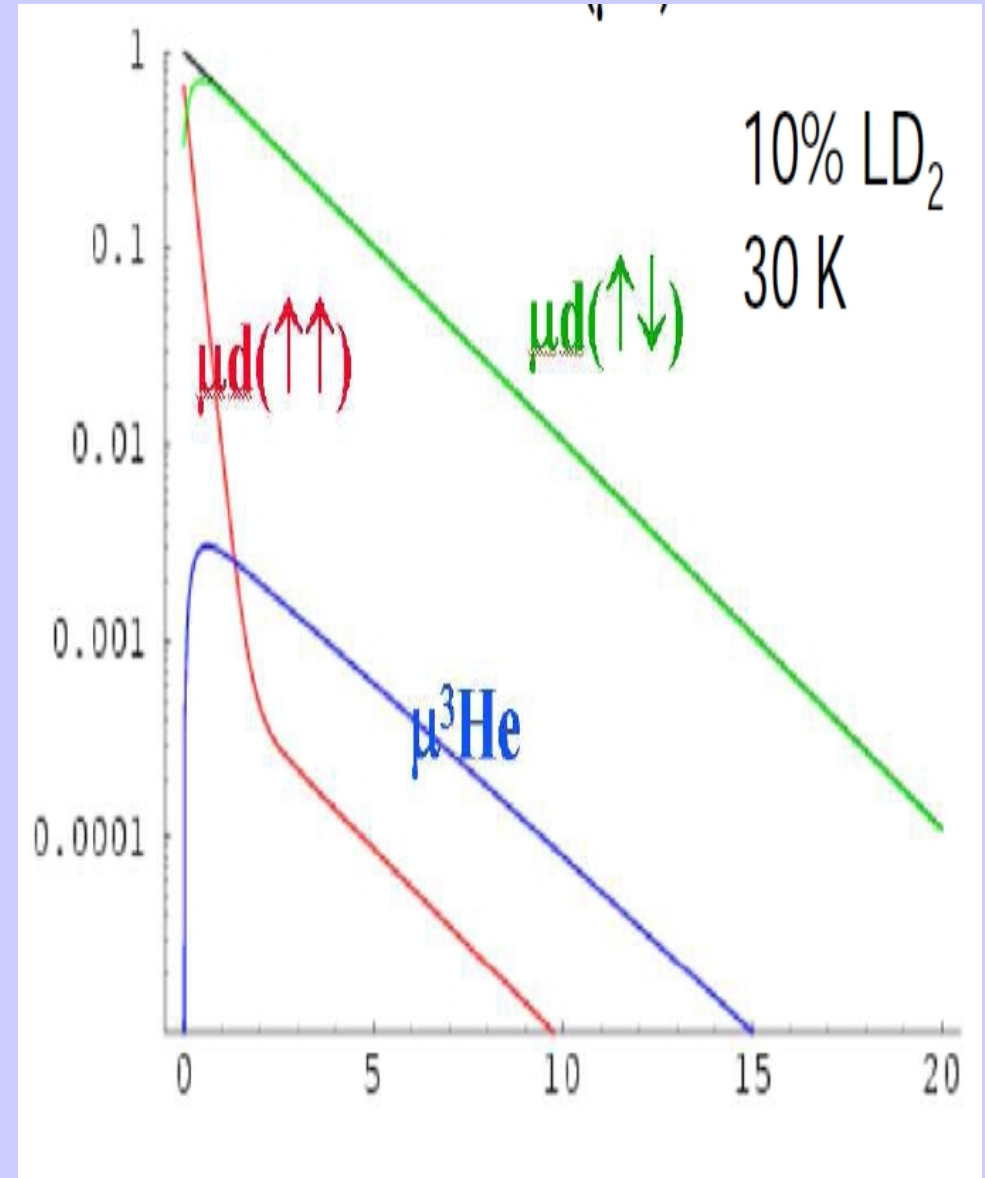
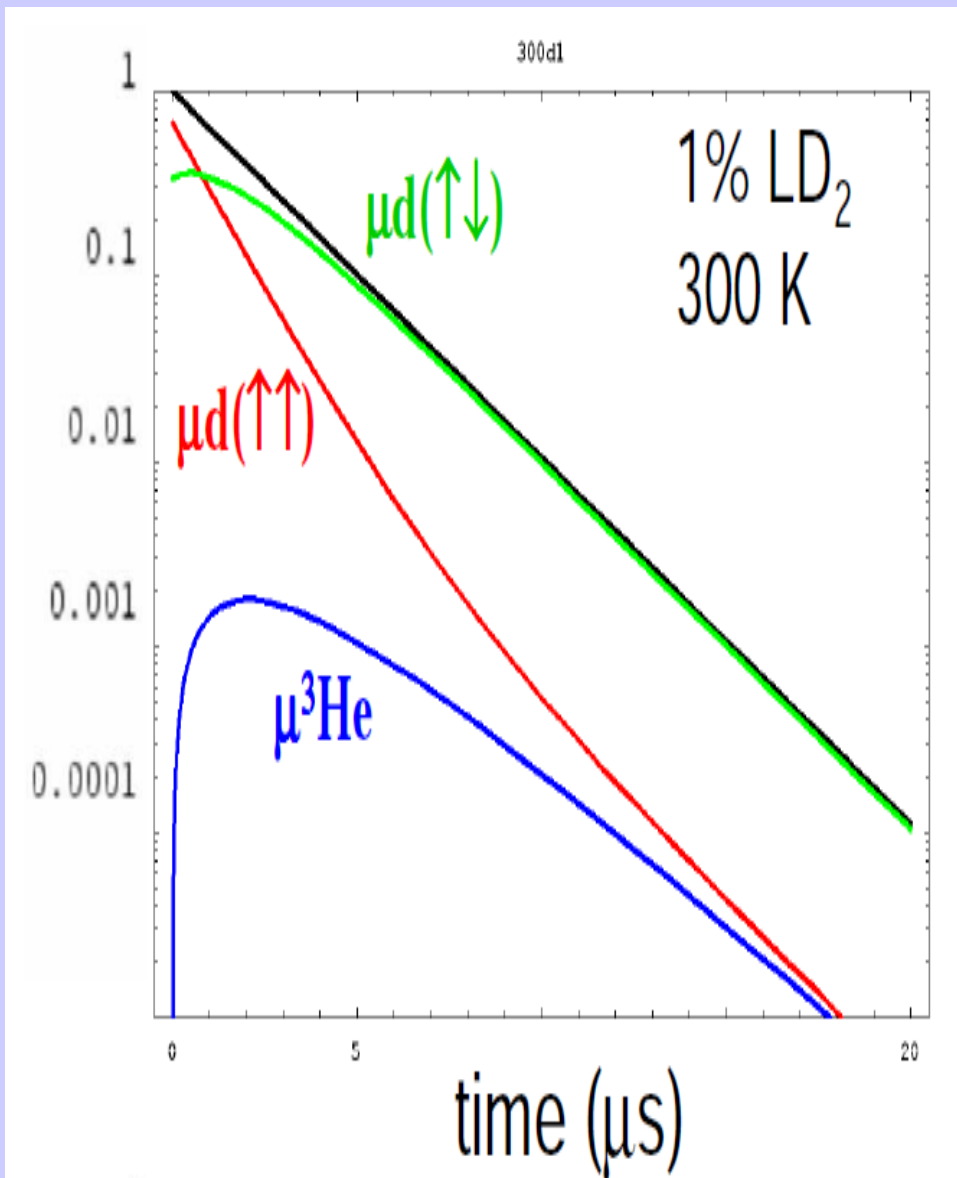


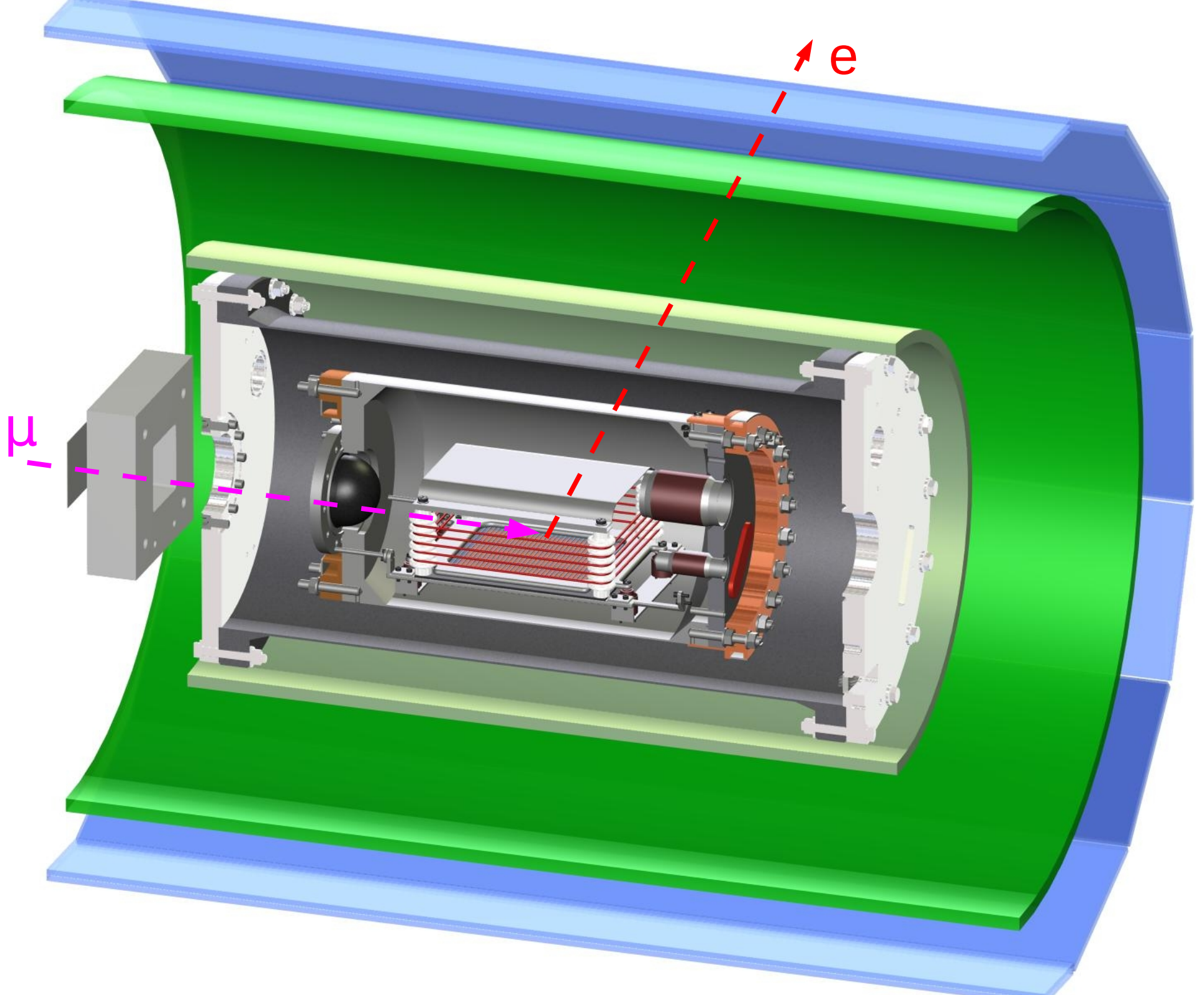
**use ultra-pure (chemically, isotopically)
30 Kelvin, 5% liquid density D_2 gas**

temperature dependence of $d\mu d$ formation.

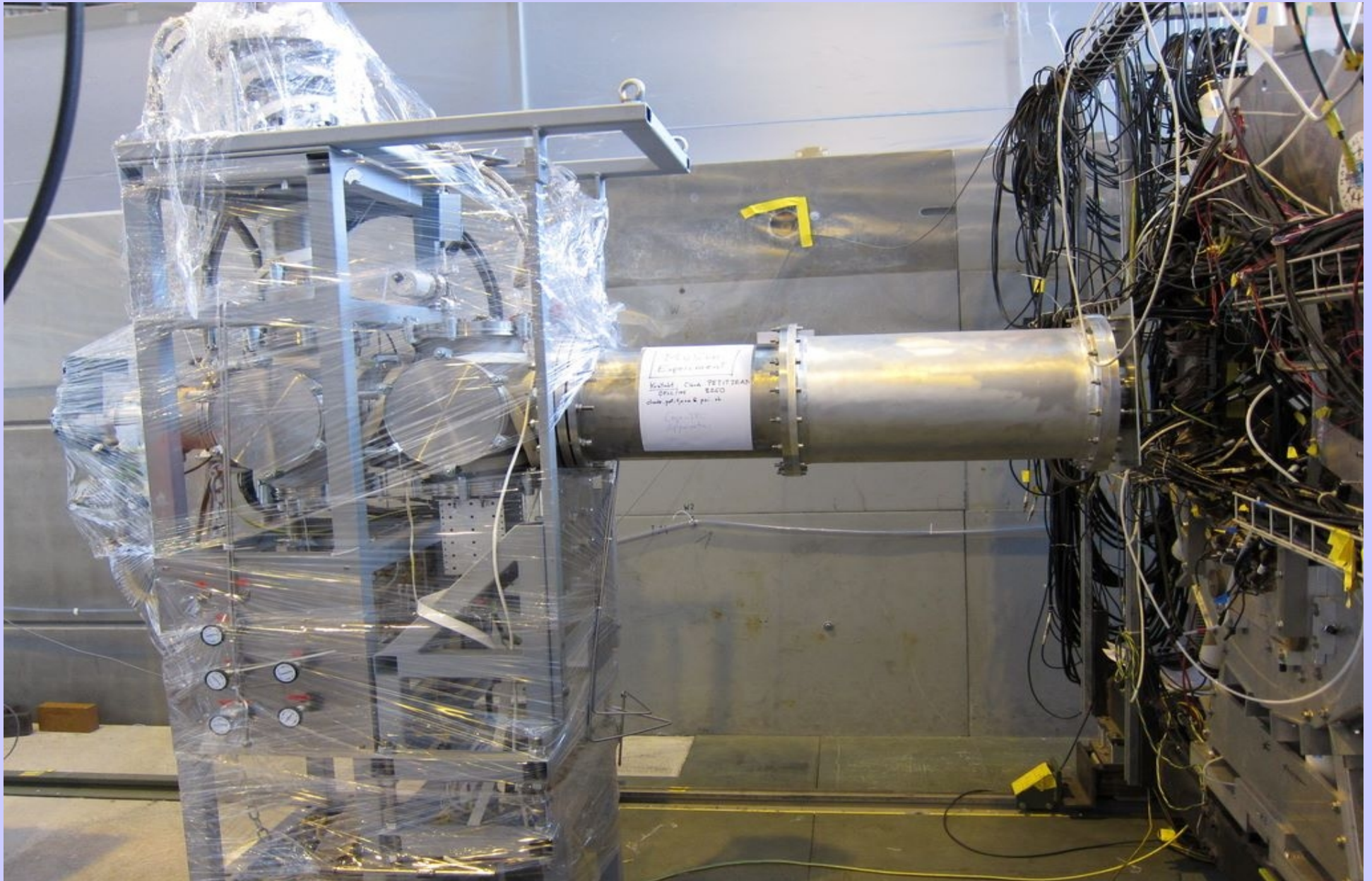


Relative populations of doublet atoms, quadruplet atoms, $\mu^3\text{He}$ atoms in warm/cold gas

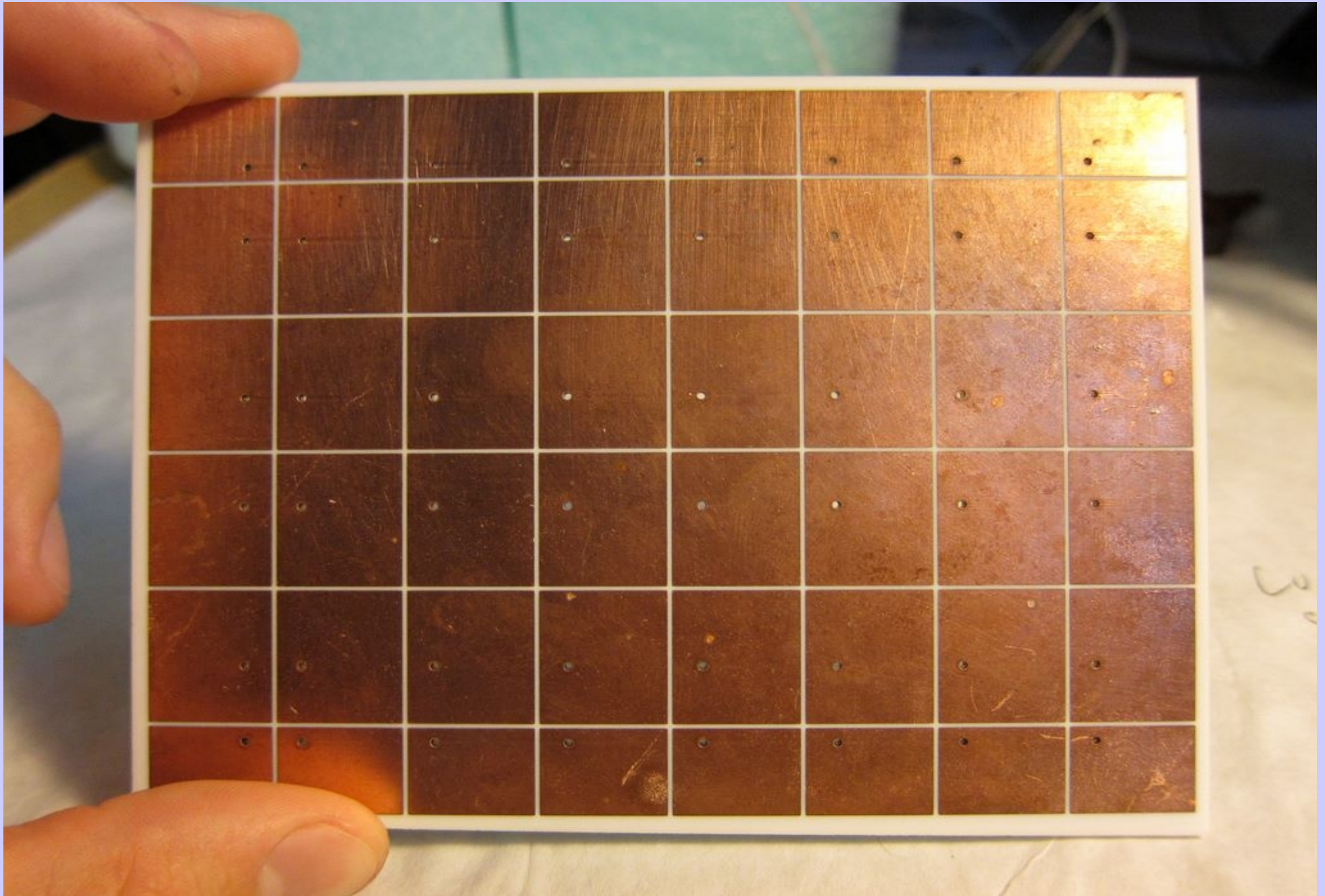




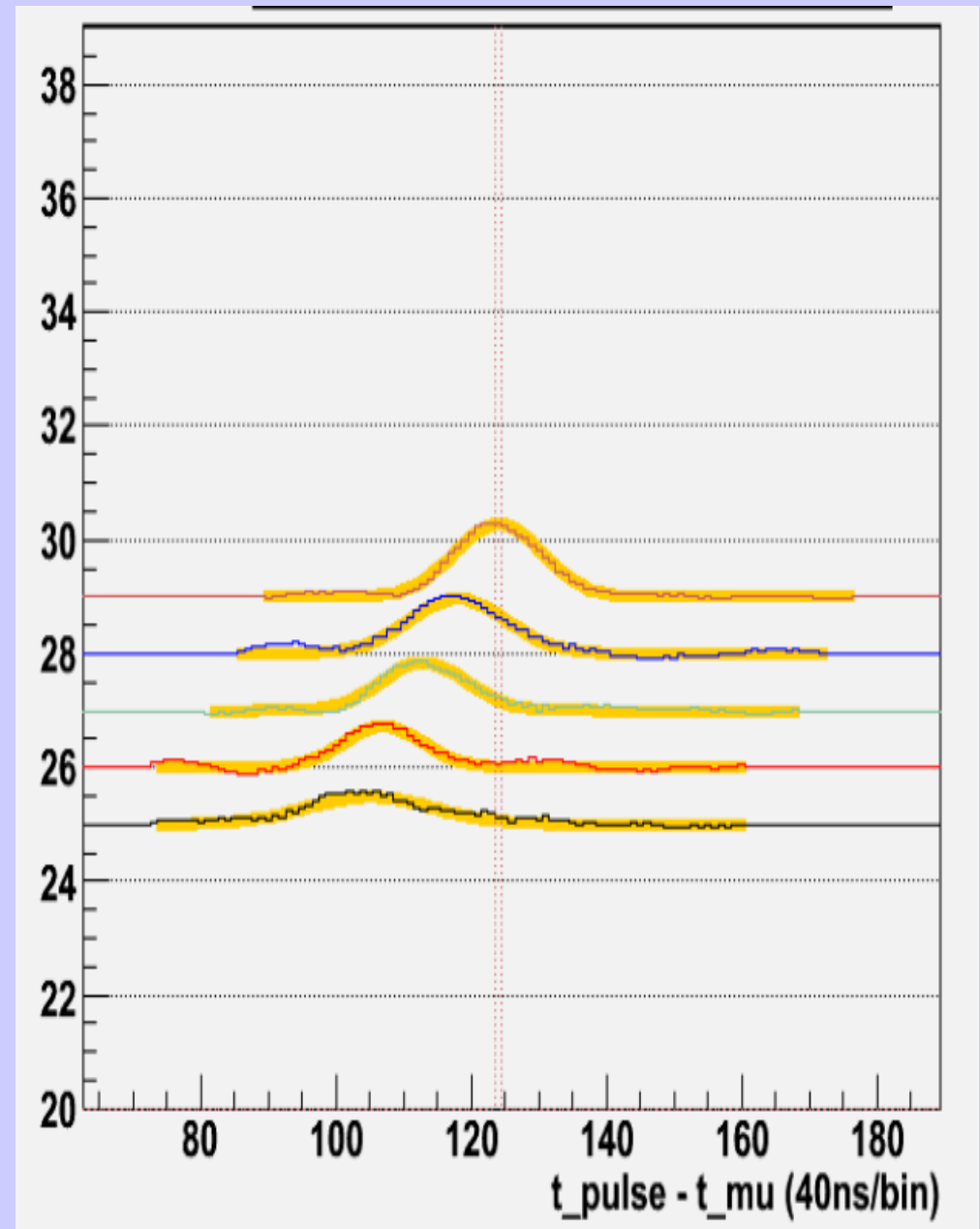
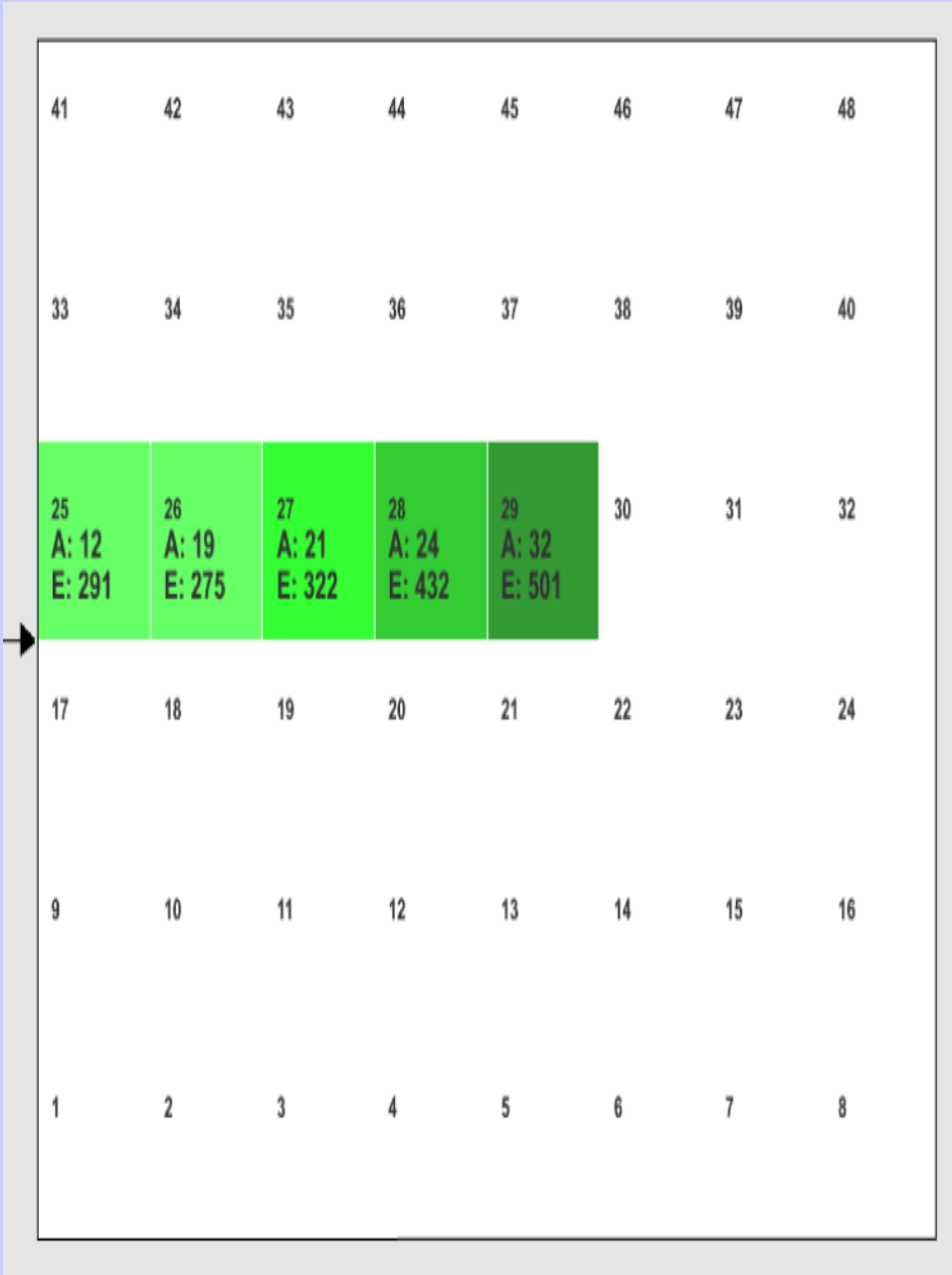
Cryogenic TPC assembly



Cryogenic TPC design



Cryogenic TPC event



Conclusions

MuX experiments - precision measurements of positive muon, muonic hydrogen, muonic deuterium lifetimes addressing fundamental leptonic, nucleonic and nuclear weak interactions.

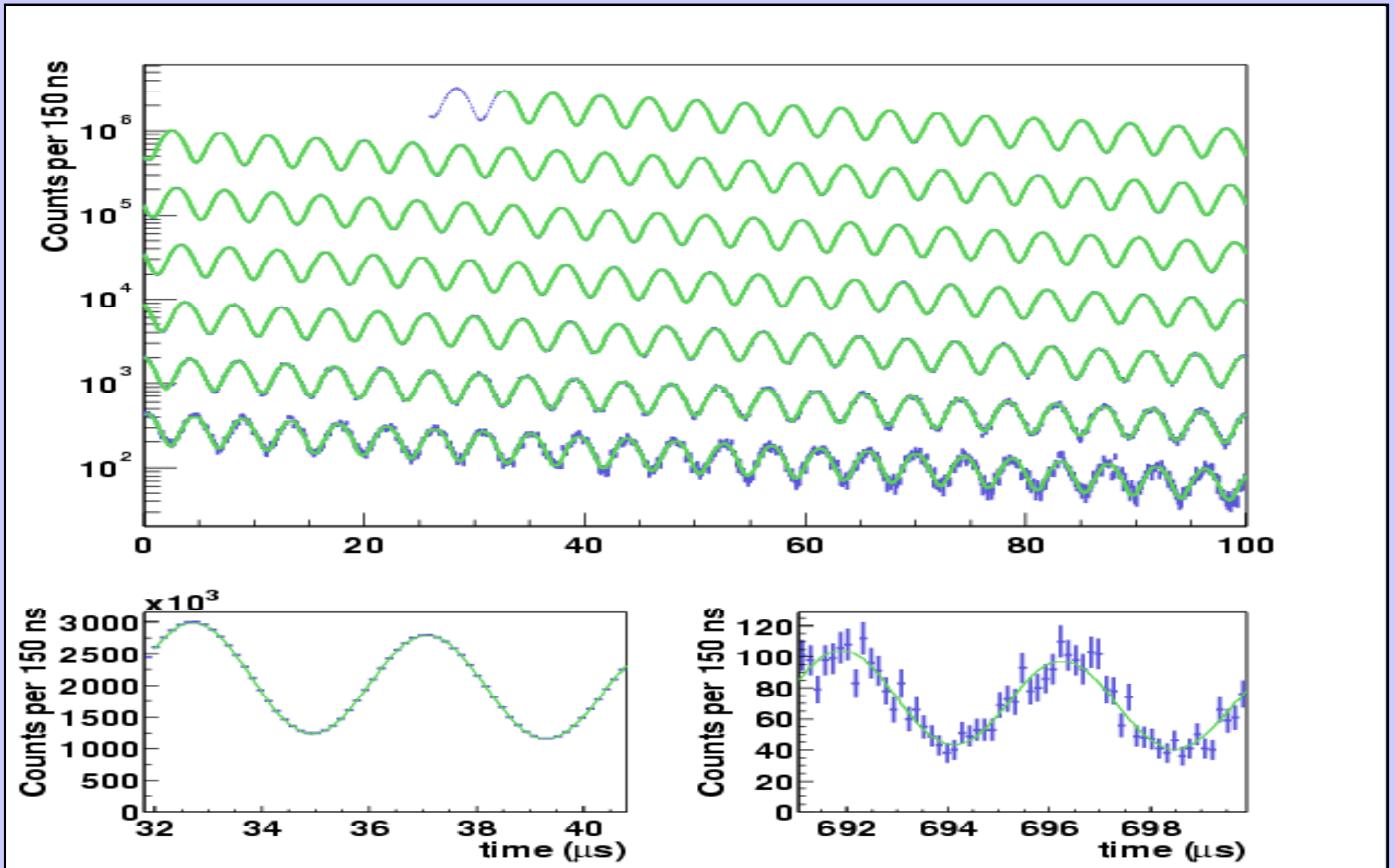
MuLan experiment - $\tau_\mu = 2196979.9 \pm 2.5(\text{stat}) \pm 0.9(\text{sys})$ ps [2006], $\tau_\mu = 2196981.2 \pm 3.7(\text{stat}) \pm 0.9(\text{sys})$ ps [2007], $G_F = 1.166\,3788(7) \times 10^{-5} \text{ GeV}^{-2}$
- a thirty-fold improvement over earlier experiments.

MuCap experiment - $\Lambda_s = 725.0 \pm 13.7(\text{stat}) \pm 10.7(\text{syst}) \text{ s}^{-1}$,
 $g_p(q^2 = -0.88\text{m}_\mu^2) = 7.3 \pm 1.1$ – with goal of improvement to $\pm 5\text{s}^{-1}$.

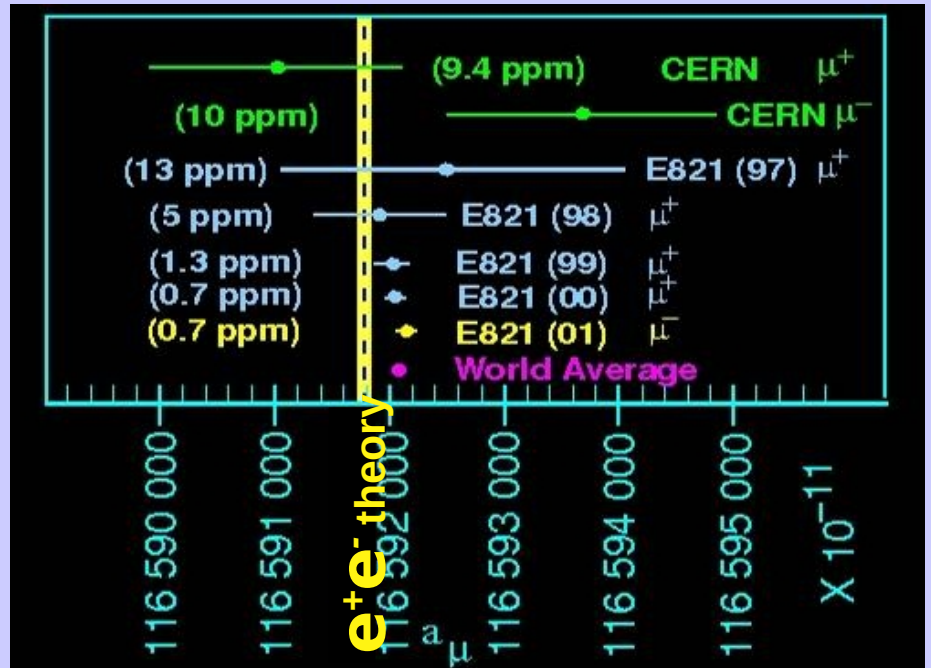
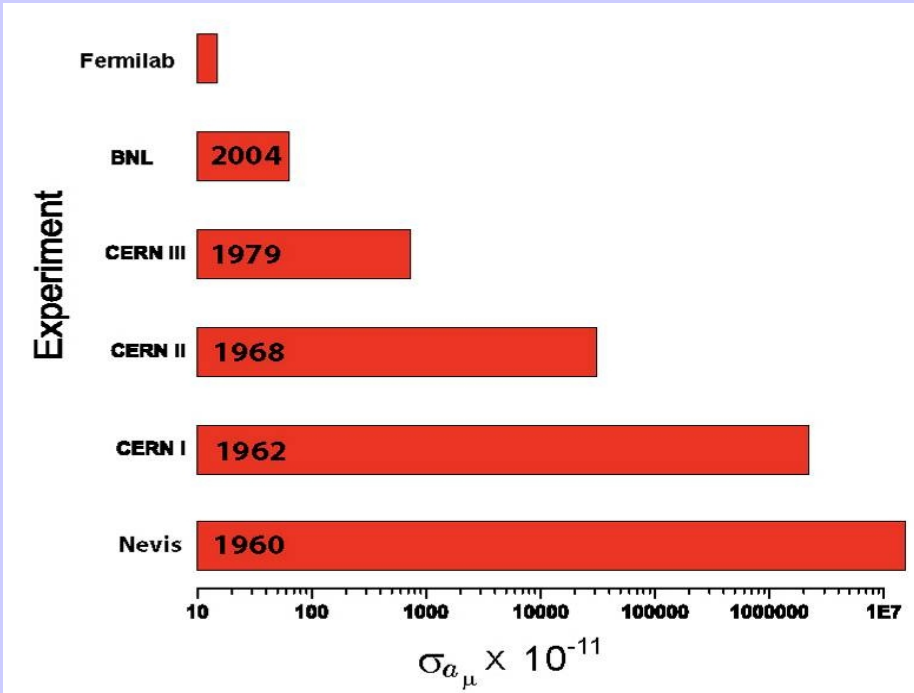
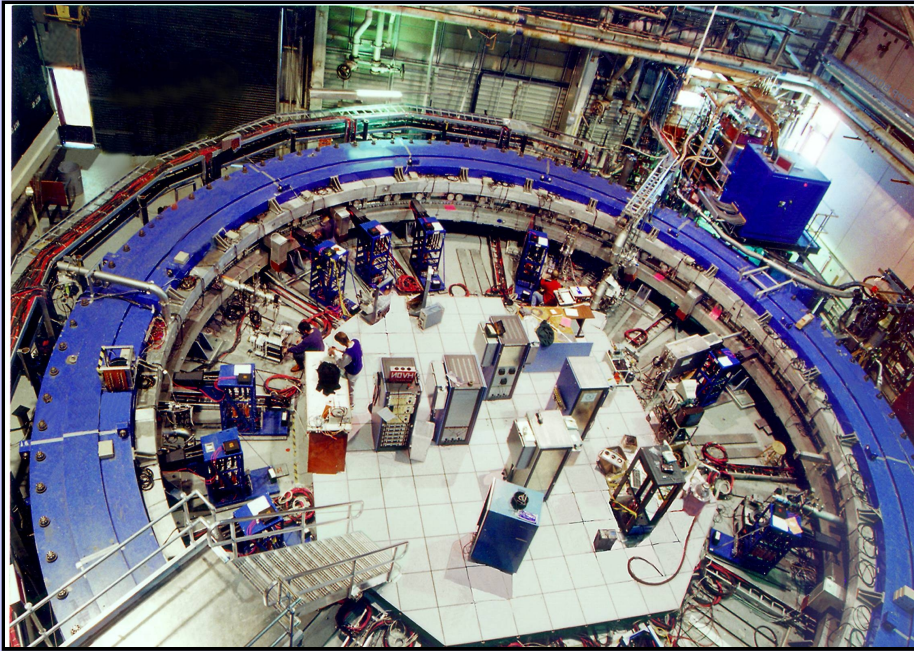
MuSun experiment – **goal of Λ_s to $\pm 1.5\%$** - precision measurement of two-nucleon weak interaction of great interest to solar physics, neutrino physics and two-body weak currents.

Advertisement

new g-2 expt on muon campus at Fermilab



g-2 @ FNAL



g-2 @ FNAL



muon storage ring from BNL to FNAL by barge and helicopter

Extras

Relation to Standard Model

$$\sqrt{4\pi\alpha} = gg' / \sqrt{g^2 + g'^2}$$

$$G_F = \sqrt{2}/v^2$$

$$M_Z = \sqrt{g^2 + g'^2} v$$

→ exacting tests of standard model
by precision measurements of θ_w , M_w , ...

Cryogenic TPC design

