# Diquark-antidiquark Mesons : a new spectroscopy? *Report on work done with F. Piccinini, A. Polosa, V. Riquer SLAC, Feb. 25, 2005*

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### Tetraquark Mesons

An idea which got momentum in the 70s (R. Jaffe, H. Lipkin...); QCD encourages the speculation that such states are indeed possible; As we shall see, the light scalar mesons a(980), f(980) really look like  $[qq]_{col=\bar{3}}[\bar{q}\bar{q}]_{col=3}$ 

In alternative: a(980), f(980) could be K-Kbar "molecules", bound by one- $\pi$  exchange, i.e. in the configuration:

 $(q\bar{q})_{col=1}(q\bar{q})_{col=1}$ 

The existence of lighter partners,  $\sigma$  and  $\kappa$  is crucial;

Recent expts, at FNAL(E791), Frascati (KLOE) and BES, have seen again  $\sigma$  and  $\kappa$ : this would be against "molecules";

...and there are states with hidden/open charm that do not look like charmonium states: X(3872), X(3940), (Belle, Babar in B decays), X(2632) (SELEX).

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# σ(600) ad E791



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# *σ*(600)<sup>®</sup> BES II

• BES II:  $\sigma$  in  $J/\psi \rightarrow \omega \pi^+ \pi^-$ .



Partial wave analysis: pole position

 $(541 \pm 39) - i(252 \pm 42) MeV$ 





No k needed in Dalitz plot fit of  $D^0 \rightarrow K^- \pi^+ \pi^0 e D^0 \rightarrow K_S \pi^+ \pi^-$ (CLEO)

No k needed in Dalitz plot fit of  $D^0 \rightarrow K^0 K^-\pi^+ e D^0 \rightarrow K K^+\pi^-$ (BABAR)

 $\Gamma = 410 \pm 43 \pm 87 \text{ MeV}$ Non Res. Bkg. :90% (no k) $\rightarrow$ 13% (k)



# The present work (1)

Recent evidence for  $\sigma$  at low energy led us to reconsider the case of sub-GeV scalar mesons.

Many previous investigations (Joffe, Close&Tornqvist, Schecter and coll...).

We propose:

- all scalars below 1 GeV are diquark-antidiquark bound states (1 nonet),
- the q-qbar scalar nonet (L=1, S=1, J=0) has to be above.

Results:

• Low energy states show inverted mass spectrum, consistent with "perfect mixing";

• Strong decays are reasonably accounted for;

• Relations with ealier proposal by Rossi&Veneziano suggests connection to baryon-antibaryon, rather than meson-meson states (or molecule)

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### The present work (2)

- Heavy quark interactions are spin independent: new spin states?
  - We propose that X(3872) observed by Belle and by Babar *is a diquarkantidiquark bound state and estimate the spectrum of states of the spin multiplet with the same flavors:*
  - X(3872)=(J=1<sup>++</sup>)=  $(cq)_{col=\bar{3},S=1}(\bar{c}\bar{q})_{col=3,S=1}$
  - with the same parameters, we can accommodate the X(2632) observed by SELEX:
  - X(2632)=(J=2<sup>++</sup>) =  $(cq)_{col=\bar{3},S=1}(\bar{s}\bar{q})_{col=3,S=1}$
- we predict X(3872) is made by two states with  $\Delta m = (5-8) MeV \approx 2 (m_d m_u)$
- if one state only in the decay:  $B^+ \rightarrow K^+ X(3872)$ , the other must appear in  $B^0 \rightarrow K_S X(3872)$
- a charged partners must exist:  $X^+ = (CU)_{col=\bar{3},S=1} (\bar{s}d)_{col=3,S=1}$
- bounds to the production of  $X^+$  are close but not in contradiction with BaBar.

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# Summary

- Attractive and repulsive channels in QCD
- String structures: the "baryonium" model (Rossi & Veneziano, 1977)
- The light scalar mesons;
- Two-meson decays;
- Surprising charmonium states seen by Belle, Babar and Selex;
- S-wave Tetraquarks, the X(3872) and spectrum of related states;
- Selex particle, X(2632), and associated spectrum;
- Alignment to quark masses, isospin breaking;
- Conclusions

### Attractive & repulsive channels in QCD

Interaction of two colored objects:



With antisymmetry in color and spin and a common spatial configuration, Fermi statisti⊊s ⇒

Good diquarks:  $[qq]_{\mathbf{\bar{3}_c},\mathbf{1_s},\mathbf{\bar{3}_f}}$ Bad diquarks:  $(qq)_{\mathbf{\bar{3}_c},\mathbf{3_s},\mathbf{6_f}}$ 

Since spin interaction is a relativistic effect we might expect stronger for the lightest quarks....

Splitting:  $(ud) - [ud] > (us) - [us] > (uc) - [uc] \approx 0$ 

HQ Spin Symmetry

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### Quantum numbers and mass formula



### 4 parameters, 4 masses+1 mixing, one overall relation:

$$f_{\circ}(I = 0) = \frac{1}{\sqrt{2}} \left( [su][\bar{s}\bar{u}] + [sd][\bar{s}\bar{d}] \right)$$
  
$$\sigma_{\circ}(I = 0) = [ud][\bar{u}\bar{d}]$$

$$\begin{aligned} |f\rangle &= \cos \phi |f_{\circ}\rangle + \sin \phi |\sigma_{\circ}\rangle \\ |\sigma\rangle &= -\sin \phi |f_{\circ}\rangle + \cos \phi |\sigma_{\circ}\rangle. \end{aligned}$$



-Two solutions (see also Schecter et al.): First: almost "ideal mixing" Second: σ~u-ubar + d-dbar.

But: how to explain mass pattern in q-model? unfavoured by decays

- Linear mass formula gives very similar results
- With Linear m.f., parameters related to diquark masses:  $\alpha$ =480 MeV,  $\beta$  = 250 MeV
- Note:  $\alpha$ - $\beta$ =230 MeV vs m<sub>s</sub>=150 MeV.

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FIG. 1: The decay of a scalar meson S made up of a diquarkantidiquark pair in two mesons  $M_1M_2$  made up of standard  $(q\bar{q})$  pairs.

$$\Gamma(S \to i) = \frac{A^2}{8\pi} \frac{p}{M_s^2} x_{s \to i}, \qquad (13)$$

where p is the decay momentum, M the mass of the scalar meson and  $x_{s \to i}$  a factor which includes numerical coefficients in the individual amplitudes and isospin multiplicities.

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TABLE II: Fit with a single parameter A = 2.6 GeV. For  $g_{\pi}$  we have reported the upper limit to the decay rate obtained from the  $f - \sigma$  mixing considered previously, see text.

Maybe f  $\pi\pi$  comes from "one-loop":  $f \to K\bar{K} \to \pi\pi$ , or perhaps (!!)  $f \to B\bar{B} \to \pi\pi$  (Baryonium ?, see later)

All in all we get quite a consistent picture, reconciles the large  $\sigma$  width with narrow a and f widths and reinforces [qq][qbar qbar] assignement

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Observation of a narrow charmonium-like state in exclusive  $B^{\pm} \to K^{\pm} \pi^+ \pi^- J/\psi$  decays



### By the way...

□ Events selected within  $2\sigma$  (12 MeV/ $c^2$ ) of 3872 MeV/ $c^2$  show hints of a *B* signal.

- After cutting at  $m(\pi^+\pi^-\pi^0) > 750 \text{ MeV}/c^2$ , a cleaner signal is present over a low background. Fit yields  $10.0 \pm 3.6 \text{ events} (5.8 \sigma)$ 



## **A new peak in** $J/\psi$ **recoil** $e^+e^- \rightarrow J/\Psi + X$

X has Charge Conj. =+

At ICHEP '04 Belle presented an update with full statistics, extending the mass range again to the high part of the spectrum (3.8 - 4.5 GeV/c<sup>2</sup>)

□ No evidence for *X*(3872) on the recoil

New peak observed at higher mass:



### New status decaying to $J/\psi \omega$ ?





# Tetraquarks with open and hidden charm (Phys.Rev. **D70**, 054009 (2004); hep-ph/0412098)

- The spin-spin interaction between heavy quarks is O(1/M)
  - If S=0 diquarks are bound, S=1 diquarks do
  - − All states in the composition (S=0  $\oplus$  S=1) $\otimes$ (S=0  $\oplus$  S=1) must exist
  - not natural spin-parity only!
  - a large multiplet with composition:

$$2 (J^{PC}=0^{++})+(J=1^{++})+2 (J=1^{+-})+(J=2^{++}).$$

- Mass spectrum determined by:
  - constituent diquark massess
  - spin-spin interactions
  - the latter: from meson and baryon spectrum or from one gluon exchange

$$M = \sum_{i} m_i + \sum_{i < j} 2\kappa_{ij} (S_i \cdot S_j)$$

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TABLE III: Spin-spin couplings for quark-quark pairs in color  $\bar{\mathbf{3}}$  state from L = 0 baryons. One gluon exchange implies  $(\kappa_{ij})_{\bar{\mathbf{3}}} = 1/2(\kappa_{ij})_{\mathbf{0}}$ . The values in the second row, show the approximate scaling of the couplings with inverse masses (masses from the baryon spectrum).

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# Masses

- Two conflicting contributions to the mass of bound states:
  - Annihilation:  $d\bar{d} \rightarrow u\bar{u}$ -  $u\bar{u} \rightarrow d\bar{d}$

gives a matrix with all equal elements, which is diagonal in the isospin basis;

- **Quark Masses:** the eigenvectors are the states with quarks of definite flavor (e.g.  $\omega/\phi$  mixing)
- TOTAL:

- $\begin{pmatrix} 2m_u + \delta & \delta \\ \delta & 2m_d + \delta \end{pmatrix}$
- At charmonium scale, quark mass should dominate (Rossi -Veneziano; Maiani-Piccinini-Polosa-Riquer)
- and the approximate mass eigenstates should be
- $X_u = [cu][\bar{c}\bar{u}]$  $X_d = [cd][\bar{c}\bar{d}]$

rather then the I=1,0 states

• Belle sees both: X -> J+ $\rho$ , J+ $\omega$  with similar B.R.!!!! A new phenomenon !!!!

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# Isospin breaking

We consider in this section the finer structure of the X(3872). In particular, we consider the neutral states with the composition:

$$X_u = [cu][\bar{u}\bar{c}]; X_d = [cd][\bar{d}\bar{c}]$$
(32)

Physical states could be expected to fall in isospin multiplets with I = 1, 0:

$$a_{c\bar{c}} = (X_u + X_d)/\sqrt{2};$$
  
$$f_{c\bar{c}} = (X_u - X_d)/\sqrt{2}$$

$$X_{\text{low}} = \cos\theta X_u + \sin\theta X_d;$$
  
$$X_{\text{high}} = -\sin\theta X_u + \cos\theta X_d$$

we get:

$$M(X_d) - M(X_u) = \frac{2(m_{\text{down}} - m_{up})}{\cos(2\theta)} = \frac{(6-8) \text{ MeV}}{\cos(2\theta)}$$

$$\frac{\Gamma(3\pi)}{\Gamma(2\pi)} \chi_{l} = \frac{(\cos\theta + \sin\theta)^{2}}{(\cos\theta - \sin\theta)^{2}} \cdot \frac{\langle p_{\omega} \rangle}{\langle p_{\rho} \rangle}$$
$$\frac{\Gamma(3\pi)}{\Gamma(2\pi)} \chi_{h} = \frac{(\cos\theta - \sin\theta)^{2}}{(\cos\theta + \sin\theta)^{2}} \cdot \frac{\langle p_{\omega} \rangle}{\langle p_{\rho} \rangle}$$
(44)

(33) BELLE attributes all events with  $\pi^+\pi^-\pi^0$  mass above 750 MeV to  $\omega$  decay and divides by the total number of observed  $2\pi$  events. They find:

$$(\frac{\Gamma(3\pi)}{\Gamma(2\pi)})_{BELLE} = 0.8 \pm 0.3_{stat} \pm 0.1_{syst}$$
 (45)

The central value is compatible with eq.(44) for:

$$\theta \simeq \pm 20^0$$
 (46)

for  $X_l$  or  $X_h$ , respectively. Correspondingly, the mass difference of the two states is:

$$M(X_h) - M(X_l) \simeq 7 - 10 MeV$$
 (47)

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(34)

(35)

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### Interference !

$$\begin{aligned} \frac{d\Gamma(X \to \psi + e^+ e^-)}{ds} &= \\ &= \frac{|A|^2 B_{(\rho \to e^+ e^-)}}{8\pi M_X^2} \frac{M_\rho \Gamma_V}{\pi} \cdot p(s) \cdot \\ &\cdot \left| \frac{1}{(s - M_\rho^2) + i(M_\rho \Gamma_\rho)} \pm \frac{1/3}{(s - M_\omega^2) + i(M_\omega \Gamma_\omega)} \right|^2 \end{aligned}$$

we have assumed the quark-model ratio for the leptonic amplitudes of  $\rho$  and  $\omega$  and used the narrow width approximation. The sign  $\pm$  applies to  $X_u$  and  $X_d$ , respectively. Combining with eq.(43), with  $\theta = 0$ , we find:

$$B(X_u \to J/\Psi + e^+e^-) = 0.8 \cdot 10^{-4}$$
  

$$B(X_d \to J/\Psi + e^+e^-) = 0.3 \cdot 10^{-4}$$
(49)

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# Decay widths

- The baryonium picture implies that the two-meson decays go via intermediate baryon-antibaryon states of high mass. This implies basically narrow widths.
- We describe the decay by a single switch amplitude, associated to the process (subscripts indicate color configuration):  $[cu][\bar{c}\bar{u}] \rightarrow (c\bar{c})_{col=1}(u\bar{u})_{col=1}$

$$\begin{split} L_{X_u\Psi V} &= g_V \epsilon^{\mu\nu\rho\sigma} P_\mu X_\nu \psi_\rho V_\sigma = \\ &= g_V M_X (\mathbf{X} \wedge \psi) \cdot \mathbf{V} \end{split} \qquad g_V M_X = \frac{A}{\sqrt{2}} \\ \text{a bold guess: A=2.6 GeV} \qquad \Gamma(X_l \to J/\psi + \pi^+\pi^-) = \frac{2x_{l,\rho}|A|^2}{8\pi M_X^2} \langle p \rangle_\rho = \\ &= 2x_{l,\rho} \cdot 2.3 \text{ MeV}; \\ \Gamma(X_l \to J/\psi + \pi^+\pi^-\pi^0) = \frac{2x_{l,\omega}|A|^2}{8\pi M_X^2} \langle p \rangle_\omega = \\ &= 2x_{l,\omega} \cdot 0.4 \text{ MeV} \end{split}$$

• We anticipate small widths, comparable to the resolution of Belle and Babar

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# X particles in B decays

- Two amplitudes: the relative frequence of  $X_u$  vs.  $X_d$  is not determined
- Taking Belle data at face value, we conclude that only one of the two neutral states is produced appreciably in B<sup>+</sup> decay (too narrow to describe two resonances about 7MeV apart)
- The the other has to appear in B<sup>0</sup> decay:
  - The X particles in B<sup>+</sup> and B<sup>0</sup> decays are not the same, and have a mass difference of 7±2 MeV

 $D^+$ 

• Bounds to the production of X<sup>+</sup>:

$$R^{-} = \frac{\mathcal{B}(B^{+} \to K_{S}X^{+}) \cdot \mathcal{B}(X^{+} \to J/\Psi + \pi^{+}\pi^{0})}{\mathcal{B}(B^{+} \to K^{+}X_{l/h}) \cdot \mathcal{B}(X_{l/h} \to J/\Psi + \pi^{+}\pi^{-})} > 0.2$$

$$R^{0} = = \frac{\mathcal{B}(B^{0} \to K^{+}X^{-}) \cdot \mathcal{B}(X^{-} \to J/\Psi + \pi^{-}\pi^{0})}{\mathcal{B}(B^{0} \to K_{S}X_{h/l}) \cdot \mathcal{B}(X_{h/l} \to J/\Psi + \pi^{+}\pi^{-})} > 0.53$$

to be compared with the upper limit given by BaBar [27]:

$$R^{+} < 0.8$$

with large errors.

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# D-D\* molecule

- one state only: D<sup>0</sup>-D<sup>\*0</sup>
- ... and very extended:

$$R = \frac{1}{\sqrt{2M_D E_{bind}}} \sim 4 \, fm$$

- most of the time (70-80%), D and D\* are too far to exchange a c-quark and form a J/ $\Psi$ ;
- for a tight state: BR( $\Psi' \rightarrow \Psi \pi^+ \pi^-$ )  $\approx 0.3$ , maybe: BR( $X \rightarrow \Psi \pi^+ \pi^-$ )  $\approx 0.03$
- the measure of inclusive B(B<sup>+</sup>→ XK<sup>+</sup>) determines the X BR from the overall ratio:

• 
$$R = \frac{B(B^+ \to XK^+)B(X \to J/\Psi \pi^+ \pi^-)}{B(B \to \Psi'K^+)B(\Psi' \to J/\Psi \pi^+ \pi^-)} = 0.063 \pm 0.014$$

• and give an important clue (G. Wormser, yesterday talk).

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### The qq-qbar qbar shopping list for X(3872)

# Questions

- Do you see X in  $B^0 \rightarrow X + K_s$ ?
- can you see a mass difference between X ( $B^0$ ) and X ( $B^+$ )?
- can you look for the other partner?  $X^+ = (cu)(\bar{c}\bar{d})$
- •
- Other X-like states:
  - above thresh.:  $0_{high}^{++} \rightarrow D + \bar{D}$
  - below thresh.:  $0_{low}^{++} \rightarrow \eta_C + \dots$
  - X(3940): seen  $X(3940) \rightarrow J/\Psi + \omega$
  - what about ?  $X(3940) \rightarrow D + \overline{D}$  (??) (d-wave)
- SELEX-like particles in B decays ???
- how about  $D_{sJ}(2317)$ ,  $D_{sJ}(2460)$ ?

### Conclusions

- A convincing picture of light scalars as  $[qq][\bar{q}\bar{q}]$  states:
  - Masses
  - Ideal mixing
  - Decays reasonably described (exact SU3!) but for OZI violating (??)
  - Note:  $\Delta m(f-a) \sim 10 \text{MeV}$ ,  $\Delta m(\text{up-down}) \sim 5 \text{MeV}$ : are f(980) and a(980) pure I-spin eigenstates?
- New phenomena
  - States  $[cq][\bar{c}\bar{q}]$  and  $[cq][\bar{c}\bar{s}]$  should exist, with both natural and unnatural spin parity;
  - I-spin breaking expected maximal in certain decay: was the SELEX particle just the first case?
  - X(3872) a good candidate, X(3940) predicted

### WERE ARE THE EXOTIC STATES??? !

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