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# Direct CP violation and determination of $\gamma$

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Technion & SLAC

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# outline

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- present status of  $\alpha$  and  $\gamma$  & motivation

methods and current data, HFAG, LP03:

- $B^0(t) \rightarrow \pi^+ \pi^-$
- $B \rightarrow K\pi$  , anomaly
- $B^+ \rightarrow \eta\pi^+$
- $B \rightarrow DK$
- $B \rightarrow VP$
- conclusion and prospects

# Acknowledgments

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## collaborators

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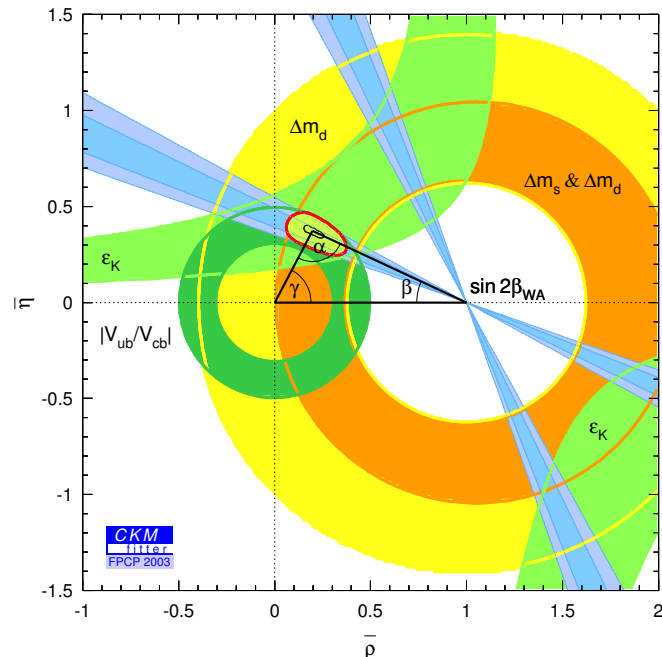
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# CKM matrix

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \quad \text{Arg}V_{ub} = -\gamma \quad \text{Arg}V_{td} = -\beta$$



# present bounds & motivation

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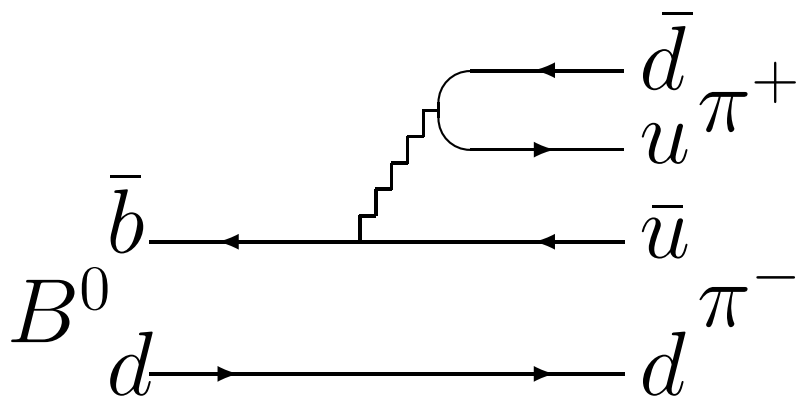
## CKM fitter (95% c.l. bounds):

- $20^\circ \leq \phi_1 \equiv \beta \leq 27^\circ$
- $78^\circ \leq \phi_2 \equiv \alpha \leq 122^\circ$
- $38 \leq \phi_3 \equiv \gamma \leq 80^\circ$

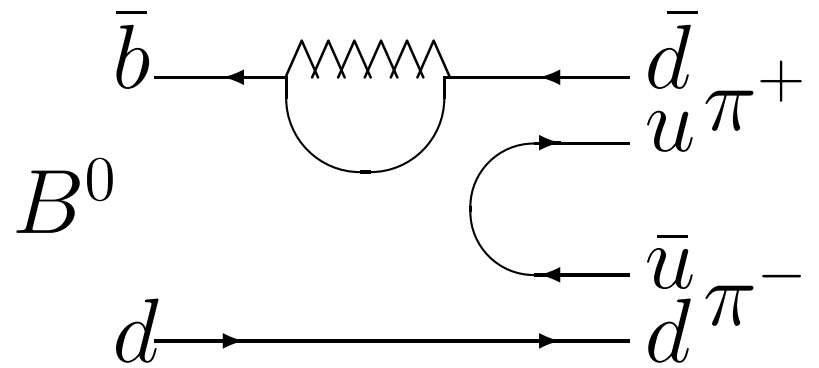
## motivation

- search for direct CP violation
- stronger constraints on  $\alpha$  and  $\gamma$
- values conflicting with CKM fits  $\Rightarrow$  new physics
- violation of rate relations (isospin)  $\Rightarrow$  new physics

$$B \longrightarrow \pi^+ \pi^-$$



$T$



$P$

$$B^0(t) \rightarrow \pi^+ \pi^-$$

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$$A(B^0 \rightarrow \pi^+ \pi^-) = |T|e^{i\gamma} + |P|e^{i\delta} \quad |P/T| \sim 0.3$$

$$\Gamma(B^0(t) \rightarrow \pi^+ \pi^-) \propto e^{-\Gamma t} [1 + C_{\pi\pi} \cos \Delta(mt) - S_{\pi\pi} \sin(\Delta mt)]$$

$$S_{\pi\pi} = \frac{2\text{Im}(\lambda_{\pi\pi})}{1 + |\lambda_{\pi\pi}|^2} = \sqrt{1 - C_{\pi\pi}^2} \sin \alpha_{\text{eff}} \neq \sin 2\alpha$$

$$-A_{\pi\pi} \equiv C_{\pi\pi} = \frac{1 - |\lambda_{\pi\pi}|^2}{1 + |\lambda_{\pi\pi}|^2} \neq 0$$

$$\lambda_{\pi\pi} \equiv e^{-2i\beta} \frac{A(\bar{B}^0 \rightarrow \pi^+ \pi^-)}{A(B^0 \rightarrow \pi^+ \pi^-)}$$

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# (1) isospin for $\alpha$

need to measure  $B^+ \rightarrow \pi^+ \pi^0$ ,  $B^0 \rightarrow \pi^0 \pi^0$  **MG, London**

$$\sqrt{2}A(\pi^+ \pi^0) - A(\pi^+ \pi^-) = \sqrt{2}A(\pi^0 \pi^0)$$

$$\mathcal{B}(10^{-6}) : \quad 5.27 \pm 0.79 \quad 4.55 \pm 0.44 \quad 1.97 \pm 0.47$$

isospin triangles for  $B$  and  $\bar{B}$  don't match

**mismatch angle  $2\Delta\alpha$  gives  $\alpha = \alpha_{\text{eff}} - \Delta\alpha$  (includes EWP)**

- $\mathcal{B}(\pi^0 \pi^0)$  not very small  $\Rightarrow |\Delta\alpha| \leq 49^\circ$  **90% c.l.** not useful

**Charles > Grossman, Quinn > MG, London, Sinha's**

- full isospin analysis requires  $B^0$  flavor tagging in  $B \rightarrow \pi^0 \pi^0$



## (2) flavor SU(3)

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$$A(B^0 \rightarrow \pi^+ \pi^-) = |T|e^{i\gamma} + |P|e^{i\delta}$$

can measure  $\alpha$  from  $C_{\pi\pi}$ ,  $S_{\pi\pi}$  IF  $|P|$  were known  
(or IF we use  $|P/T| \sim 0.3$ ) **Charles; MG, Rosner**

$$A(B^+ \rightarrow K^0 \pi^+) = |P'|e^{i\delta'} = |P|e^{i\delta'} \frac{f_K}{f_\pi \tan \theta_c}$$

### 2 approximations

- neglect tiny term with phase  $\gamma$  in  $B^+ \rightarrow K^0 \pi^+$
- factorization of  $P$  (will be checked in  $B^+ \rightarrow \bar{K}^0 K^+$ )

$|T/P|$ ,  $\delta$ ,  $\alpha$  from

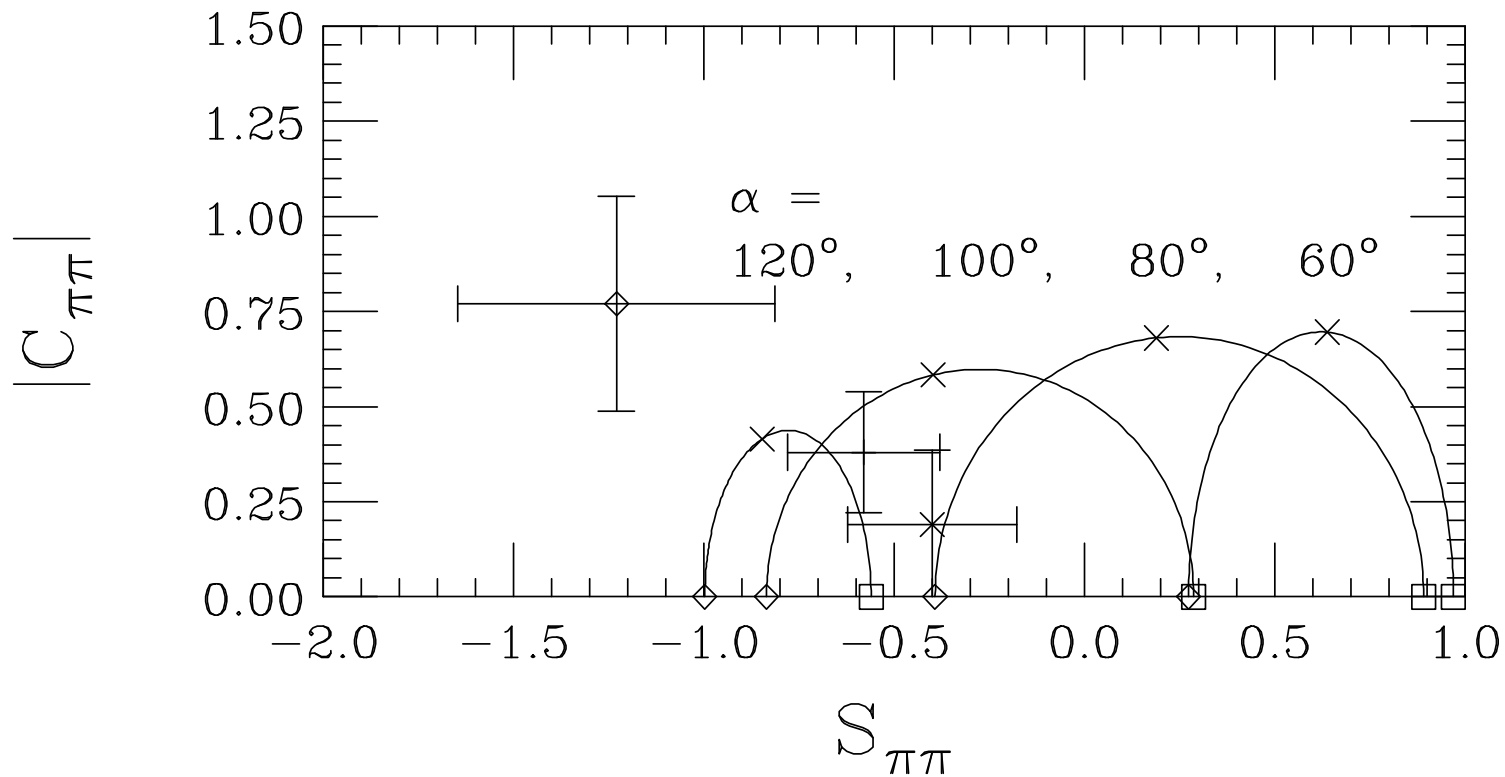
$S_{\pi\pi}$ ,  $C_{\pi\pi}$ ,  $\mathcal{B}(B^0 \rightarrow \pi^+ \pi^-) / \mathcal{B}(B^+ \rightarrow K^0 \pi^+)$

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# $C_{\pi\pi}, S_{\pi\pi}$ vs $\alpha$

insensitive to  $\mathcal{B}(B^0 \rightarrow \pi^+\pi^-)/\mathcal{B}(B^+ \rightarrow K^0\pi^+) = 0.23 \pm 0.03$



$\diamond : \delta = 0$        $\square : \delta = \pi$        $\times : \delta = \pi/2$

$S_{\pi\pi} = -0.58 \pm 0.20, C_{\pi\pi} = -0.38 \pm 0.16$  favors large  $\alpha$

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$$B \rightarrow K \pi$$

# $B \rightarrow K\pi$

- $B^0 \rightarrow K^+\pi^-$  vs  $B^+ \rightarrow K^0\pi^+$  MG, Rosner;  
Fleischer, Mannel

$$A(B^0 \rightarrow K^+\pi^-) = |P'|e^{i\delta_0} - |T'|e^{i\gamma} \quad \text{neglect EWPC}$$

$$A(B^+ \rightarrow K^0\pi^+) = |P'|e^{i\delta_0} \quad r \equiv |T'|/|P'|$$

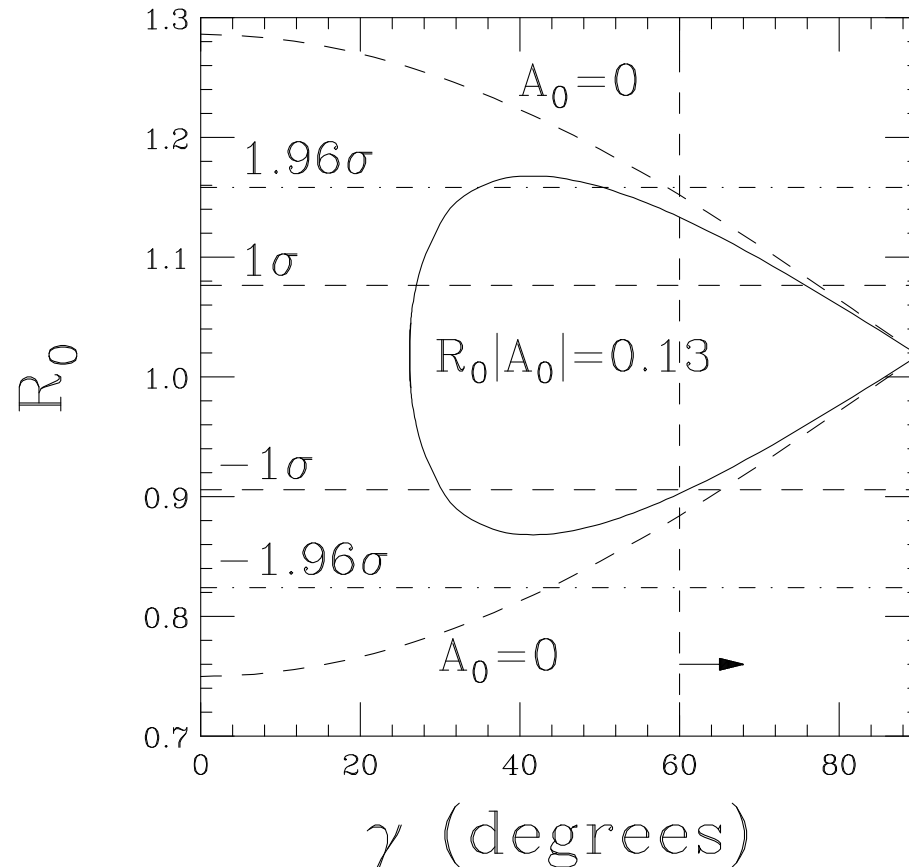
$$R_0 = \frac{\bar{\Gamma}(K^\pm\pi^\mp)}{\bar{\Gamma}(K^0\pi^\pm)} = 1 - 2r \cos \delta_0 \cos \gamma + r^2 \geq \sin^2 \gamma$$

$$A_0 = \frac{\Gamma(K^-\pi^+) - \Gamma(K^+\pi^-)}{\Gamma(K^-\pi^+) + \Gamma(K^+\pi^-)} = -2r \sin \delta_0 \sin \gamma / R_0$$

eliminate  $\delta_0$  and plot  $(R_0)_{\text{exp}} = 0.99 \pm 0.09$  vs  $\gamma$  for allowed  
range  $|A_0|_{\text{exp}} < 0.13$   $0.13 < r_{\text{th}} < 0.21$  ( $B \rightarrow \pi\pi/K\pi$ )  
most conservative bounds on  $\gamma$  at  $r = 0.13$

# $R_0$ vs $\gamma$ for $|A_0| < 0.13$ , $r = 0.13$

lower branch:  $\cos \delta_0 \cos \gamma > 0$



$\gamma \geq 60^\circ$  ( $1\sigma$ ): need smaller error in  $R_0$

# another $B \rightarrow K\pi$ ratio

- $B^+ \rightarrow K^+\pi^0 / K^0\pi^+$  MG, London, Rosner, Neubert

$$\sqrt{2}A(B^+ \rightarrow K^+\pi^0) = |P'|e^{i\delta_c} - |T' + C'|(e^{i\gamma} - \delta_{\text{EWP}})$$

$$A(B^+ \rightarrow K^0\pi^+) = |P'|e^{i\delta_c} \quad r_c \equiv |T' + C'|/|P'|$$

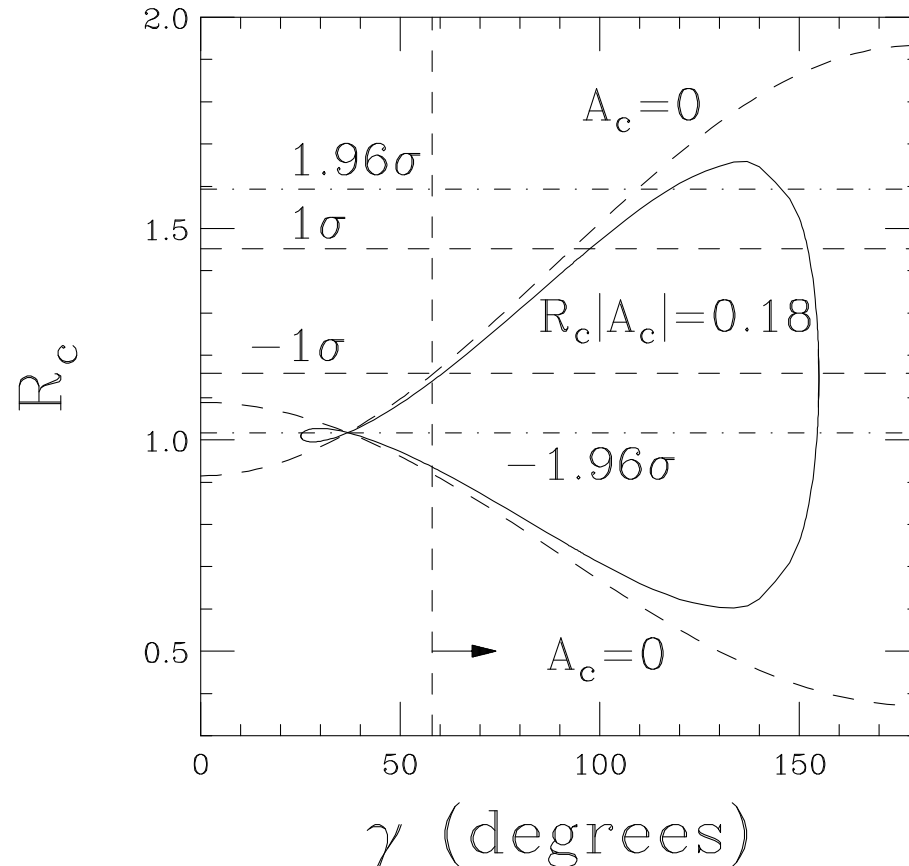
$$R_c = \frac{2\bar{\Gamma}(K^\pm\pi^0)}{\bar{\Gamma}(K^0\pi^\pm)} = 1 - 2r_c \cos \delta_c (\cos \gamma - \delta_{\text{EWP}}) + \mathcal{O}(r_c^2)$$

$$A_c = \frac{\Gamma(K^-\pi^0) - \Gamma(K^+\pi^0)}{\Gamma(K^-\pi^0) + \Gamma(K^+\pi^0)} = -2r_c \sin \delta_c \sin \gamma / R_c$$

eliminate  $\delta_c$  and plot  $(R_c)_{\text{exp}} = 1.31 \pm 0.15$  vs  $\gamma$  for allowed range  $|A_c|_{\text{exp}} < 0.11$   $0.18 < (r_c)_{\text{th}} < 0.22$  ( $B^+ \rightarrow \pi^+\pi^0 / \pi^+K^0$ )  
 $\delta_{\text{EWP}} = 0.65 \pm 0.15$ ; conservative bounds on  $\gamma$  at  $\delta_{\text{EWP}} = 0.80$

# $R_c$ vs $\gamma$ for $R_c|A_c| < 0.18$ , $r_c = 0.22$

lower branch:  $\cos \delta_c (\cos \gamma - \delta_{EW}) > 0$



$\gamma > 58^\circ$  ( $1\sigma$ ): need smaller error in  $R_c$

# The $K\pi$ anomaly

Isospin sum rule **MG, Rosner, hep-ph/0307095 (Lipkin)**

$$\frac{2[\Gamma(B^+ \rightarrow K^+\pi^0) + \Gamma(B^0 \rightarrow K^0\pi^0)]}{\Gamma(B^+ \rightarrow K^0\pi^+) + \Gamma(B^0 \rightarrow K^+\pi^-)}$$
$$= 1 + \frac{|P'_{EW}|^2}{|P'|^2} + \frac{\text{Re}(T'^* P'_{EW})}{|P'|^2} \quad \text{no linear } \Delta I = 1$$

$$\Delta I = 1 : < 4\%$$

**experiment:**  $24 \pm 10\%$  **new physics?**

$$R_n \equiv \bar{\Gamma}(B^0 \rightarrow K^+\pi^-) / 2\bar{\Gamma}(B^0 \rightarrow K^0\pi^0) = 0.81 \pm 0.10$$

$$R_c \equiv 2\bar{\Gamma}(B^+ \rightarrow K^+\pi^0) / \bar{\Gamma}(B^+ \rightarrow K^0\pi^+) = 1.31 \pm 0.15$$

$$R_c = R_n + \mathcal{O}(|P'_{EW}|^2/|P'|^2) \quad \text{underestimate } \pi^0 \text{ detec. effic.?}$$



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$$B^+ \rightarrow \eta(\eta')\pi^+$$

# $B^+ \rightarrow \eta\pi^+$

$$\eta = (s\bar{s} - u\bar{u} - d\bar{d})/\sqrt{3}$$

octet-singlet mixture,  $\sin\theta_{8,1} = -1/3$

Chiang, MG, Rosner  
hep-ph/0306021

$$\sqrt{3}A(B^+ \rightarrow \eta\pi^+) = |T + C|e^{i\gamma} + |2P + S|e^{i\delta}$$

$$\sqrt{2}A(B^+ \rightarrow \pi^+\pi^0) = |T + C|e^{i\gamma} \quad \uparrow \quad \uparrow = \text{small singlet}$$

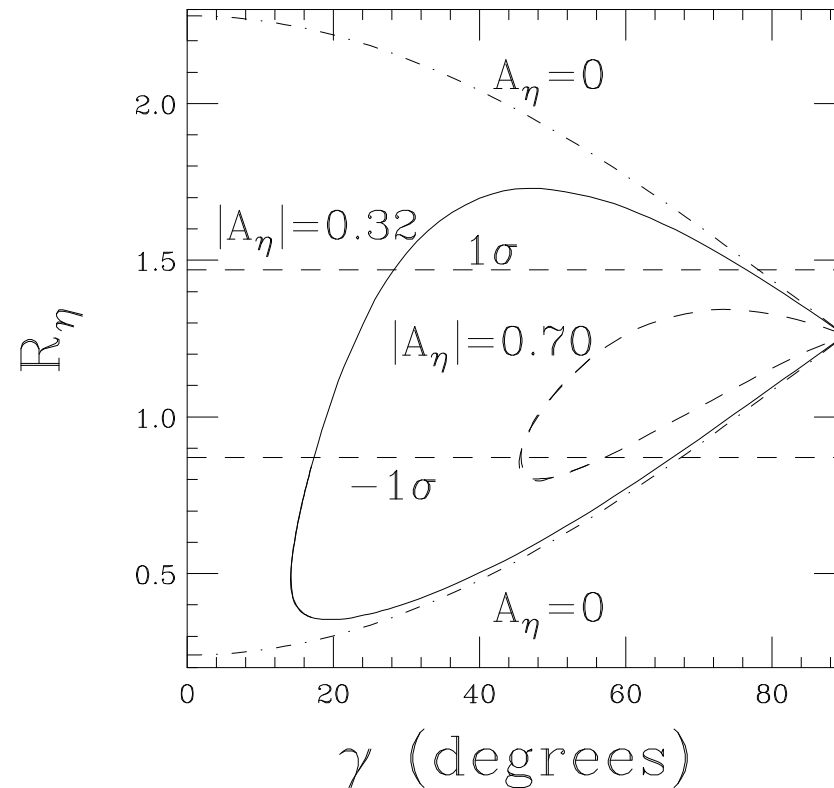
$$R_\eta = \frac{3\bar{\Gamma}(\eta\pi^\pm)}{2\bar{\Gamma}(\pi^\pm\pi^0)} = 1 + r_\eta^2 + 2r_\eta \cos\delta \cos\gamma = 1.17 \pm 0.30 \quad \begin{matrix} \text{BaBar} \\ \text{Belle} \end{matrix}$$

$$A_\eta = \frac{\Gamma(\eta\pi^-) - \Gamma(\eta\pi^+)}{\Gamma(\eta\pi^-) + \Gamma(\eta\pi^+)} = -\frac{2r_\eta \sin\delta \sin\gamma}{R_\eta} = -0.51 \pm 0.19 \quad \text{BaBar}$$

$$r_\eta \equiv \frac{|2P + S|}{|T + C|} \gtrsim \frac{2|P|}{|T + C|} = \frac{f_\pi \tan\theta_c}{f_K} \sqrt{\frac{2\mathcal{B}(K^0\pi^+)}{\mathcal{B}(\pi^+\pi^0)}} = 0.51 \pm 0.04$$

# $R_\eta$ vs $\gamma$ for a range in $A_\eta$

upper branch:  $\cos \delta \cos \gamma > 0$



large asymmetry is important

need more precise measurements of  $R_\eta$ ,  $A_\eta$

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$$B \rightarrow DK$$

# $\gamma$ from $B^\pm \rightarrow DK^\pm$ MG, London, Wyler, variants

interference between  $B^- \rightarrow D^0 K^-$  and  $B^- \rightarrow \bar{D}^0 K^-$

$$D_{\text{CP}\pm}^0 = \frac{1}{\sqrt{2}}(D^0 \pm \bar{D}^0), \quad D_{\text{CP}+}^0 \rightarrow K^+ K^-$$

$$A(B^- \rightarrow D_\pm^0 K^-) = \frac{1}{\sqrt{2}}[A(B^- \rightarrow D^0 K^-) \pm A(B^- \rightarrow \bar{D}^0 K^-)]$$

no penguin       $b \rightarrow c\bar{u}s$  phase=0       $b \rightarrow u\bar{c}s$  phase=- $\gamma$

ratio  $r \sim 0.2$

measured

difficult to measure

$$R_\pm = \frac{\Gamma(D_{\text{CP}\pm}^0 K^-) + \Gamma(D_{\text{CP}\pm}^0 K^+)}{\Gamma(D^0 K^-)} = 1 + r^2 \pm 2r \cos \delta \cos \gamma$$

$$A_\pm = \frac{\Gamma(D_{\text{CP}\pm}^0 K^-) - \Gamma(D_{\text{CP}\pm}^0 K^+)}{\Gamma(D_{\text{CP}\pm}^0 K^-) + \Gamma(D_{\text{CP}\pm}^0 K^+)} = \pm 2r \sin \delta \sin \gamma / R_\pm$$

$R_\pm, A_\pm$  determine  $\gamma$        $\sin^2 \gamma \leq R_\pm$ , both  $R_\pm \geq 1$  unlikely

# experimental situation

$$R(K/\pi) \equiv \frac{\bar{\mathcal{B}}(B^- \rightarrow D^0 K^-)}{\bar{\mathcal{B}}(B^- \rightarrow D^0 \pi^-)} \quad R(K/\pi)_\pm \equiv \frac{\bar{\mathcal{B}}(B^- \rightarrow D_{\text{CP}\pm}^0 K^-)}{\bar{\mathcal{B}}(B^- \rightarrow D_{\text{CP}\pm}^0 \pi^-)}$$

all 3 quantities measured  $\Rightarrow R_\pm = \frac{R(K/\pi)_\pm}{R(K/\pi)}$

do not require knowledge of  $B$  and  $D$  decay BR's

$$R_+ = 1.09 \pm 0.16 \quad A_+ = 0.07 \pm 0.13 \quad (\text{Belle, BaBar})$$

$$R_- = 1.30 \pm 0.25 \quad A_- = -0.19 \pm 0.18 \quad (\text{Belle})$$

$$A_{\text{av}} = 0.11 \pm 0.11$$

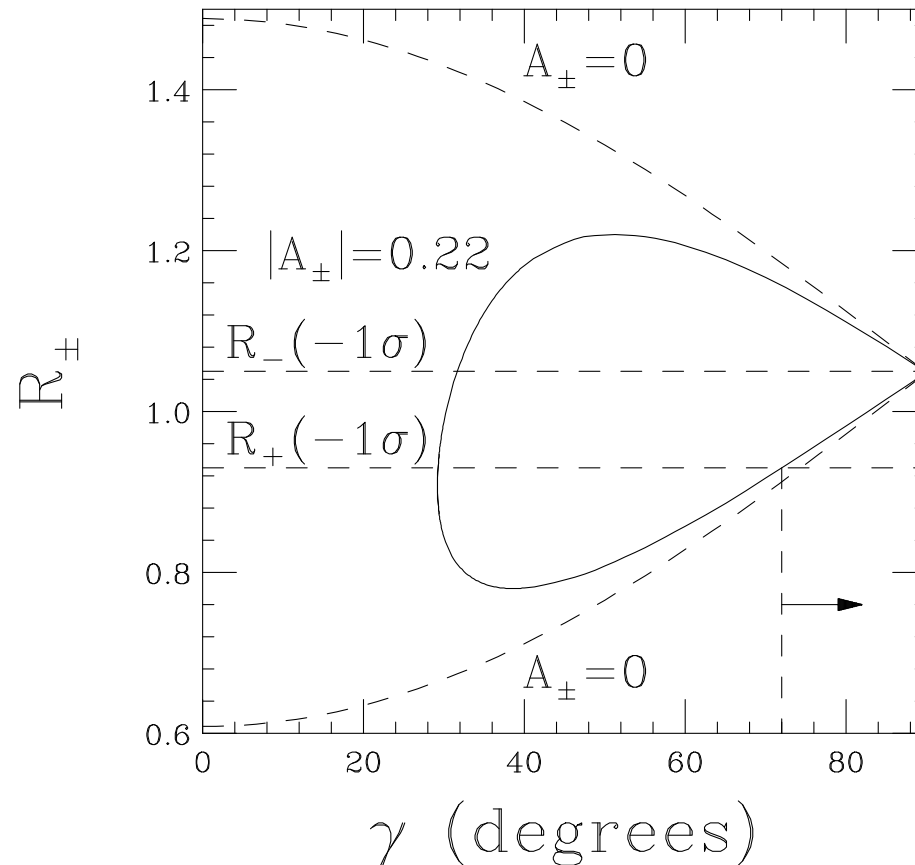
$$r = \sqrt{(R_+ + R_-)/2 - 1} = 0.44^{+0.14}_{-0.22} \quad B^- \rightarrow D^0 (\rightarrow K_S \pi^+ \pi^-) K^-$$

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$$r = 0.33 \pm 0.10 \quad (\text{Belle})$$

# $R_{\pm}$ vs $\gamma$ for $|A_{\pm}|^{1\sigma} < 0.22$ , $r_{\min}^{1\sigma} = 0.22$

lower (upper) branch of  $R_+$  ( $R_-$ ):  $\cos \delta \cos \gamma < 0$



$\gamma > 72^{\circ}$  ( $1\sigma$ ): need smaller error in  $R_{\pm}$

# non-CP, mixed-flavor D decay modes

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Dalitz plot for  $D \rightarrow K_S \pi^+ \pi^-$  in  $B^\pm \rightarrow D^0(\bar{D}^0)K^\pm$

Giri, Grossman, Soffer, Zupan

$$f(m_+^2, m_-^2) \equiv A(\bar{D}^0 \rightarrow K_S \pi^+ \pi^-)$$

$$A((K_S \pi^+ \pi^-)_D K^\pm) \propto f(m_+^2, m_-^2) + r e^{i(\delta+\gamma)} f(m_-^2, m_+^2)$$

Belle, hep-ex/0308043, 140 fb<sup>-1</sup>:

- model  $f$  by sum of resonances:  $K^{*\pm}, \rho^0, \omega, f_0, f_2, \sigma \dots$
- fit resonance amps & phases in tagged  $\bar{D}^0$  decays
- given  $f$ , determine  $r, \delta, \gamma$  from  $\Gamma((K_S \pi^+ \pi^-)_D K^\pm)$

90 % c.l.:  $0.15 < r < 0.50, 104^\circ < \delta < 214^\circ, 61^\circ < \gamma < 142^\circ$

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$$B \rightarrow VP$$

# $B \rightarrow VP$

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global fit to all  $B \rightarrow VP$  decays:

$\rho\pi, \omega\pi, \rho\eta, \rho\eta', K^*\pi, K^*\eta, K^*\eta', \rho K, \omega K, \phi K$

Chiang, MG, Luo, Rosner, Suprun, hep-ph/0307395

- flavor SU(3) including SU(3) breaking
  - 33 data points for rates and asymmetries; 12 parameters
  - good fit:  $\chi^2/\text{d.o.f.} \approx 1$
  - predictions for unobserved decays
  - tests SU(3) breaking = ratio of decay constants
  - small strong phases between tree and penguin
  - $51^\circ < \gamma < 74^\circ$  at 95% c.l.
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# conclusion and prospects

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- direct CP asymmetries and  $\gamma$  require interference
- $|P/T|_{\pi\pi} \sim 0.3$ ,  $|T/P|_{K\pi} \sim 0.2$ ,  $|C/T|_{DK} \sim 0.2$ ;  
 $|P/T|_{B^+ \rightarrow \eta(\eta')\pi^+} \sim 0.5 - 1.0 \Rightarrow$  potential large asym
- $\exists$  strict bounds on  $K\pi$  asymmetries  $\sim 10\%$
- watch the anomaly in  $K\pi$  rates: new physics ?
- ratios of  $K\pi$  rates, and of  $DK$  rates, are sensitive to  $\gamma$ ; current ratios in  $B \rightarrow K\pi$  &  $DK \Rightarrow 1\sigma$  bounds on  $\gamma$ ; bounds at 95% c.l. require reducing errors by  $< 2$
- $B \rightarrow D(K_S\pi^+\pi^-)K$  seems promising
- current bounds in  $B \rightarrow K\pi$  assume conservative SU(3) breaking, can be improved by experimental tests of SU(3) breaking

# further references

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- $B^0 \rightarrow \pi^+ \pi^-$ : Silva + Wolfenstein  
Fleischer + Matias  
Beneke *et al* (also  $B \rightarrow K\pi, VP$ )  
Keum + Li + Sanda (also  $B \rightarrow K\pi$ )
  - $B \rightarrow K\pi$ : Buras + Fleischer  
Deshpande    He *et al*    Hou *et al*  
Ciuchini *et al*    Ali *et al*
  - $B \rightarrow \eta/\eta' \pi^+$ : Barshay + Rein + Sehgal  
Ahmady + Kou
  - $B \rightarrow DK$ : Atwood + Dunietz + Soni  
Kayser + London + Sinhas  
Grossman *et al*    Fleischer
  - $B \rightarrow VP$ : Ali *et al*, Kramer *et al*
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