

# Investigation of the Dalitz decay of the $\eta$ meson and the determination of the $\eta$ transition formfactor

Henning Berghäuser  
Volker Metag  
II. Physikalisches Institut

JUSTUS-LIEBIG-



- motivation
- experimental setup
- identification of the  $\eta \rightarrow e^+e^-\gamma$  decay; background suppression
- experimental results
- comparison to other experiments and calculations
- summary and outlook



HADRON 2011  
Munich, June 13-17, 2011



# Electromagnetic transition formfactor

---

hadrons = composite (non-point-like) particles of quarks and gluons  
with internal structure

access to internal structure: measurement of formfactors  $F(q^2)$

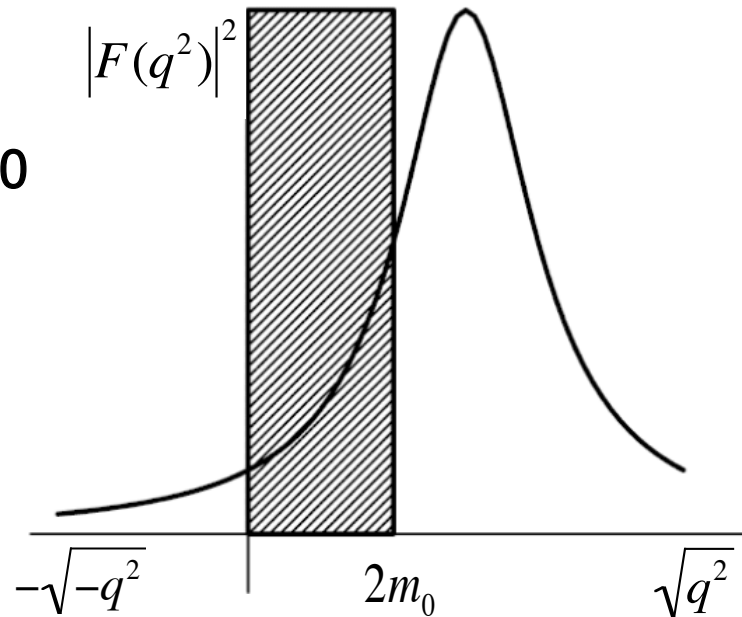
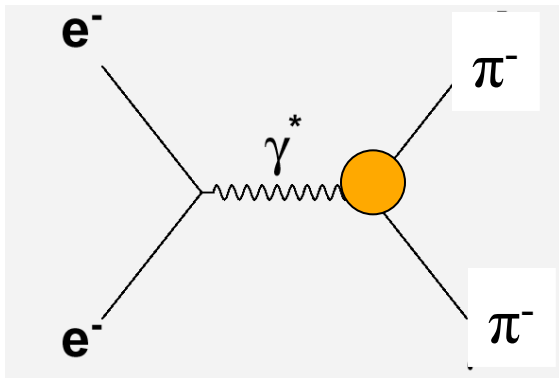
# Electromagnetic transition formfactor

hadrons = composite (non-point-like) particles of quarks and gluons with internal structure

access to internal structure: measurement of formfactors  $F(q^2)$

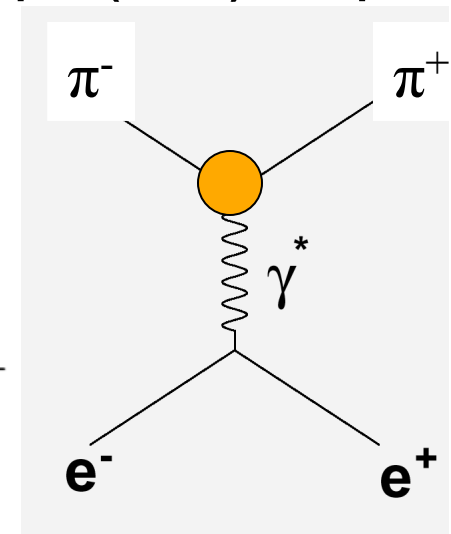
**elastic scattering**  
**space like:**

$$q^2 = (\Delta E/c)^2 - \Delta p^2 < 0$$



**annihilation**  
**time-like**

$$q^2 = (\Delta E/c)^2 - \Delta p^2 > 0$$



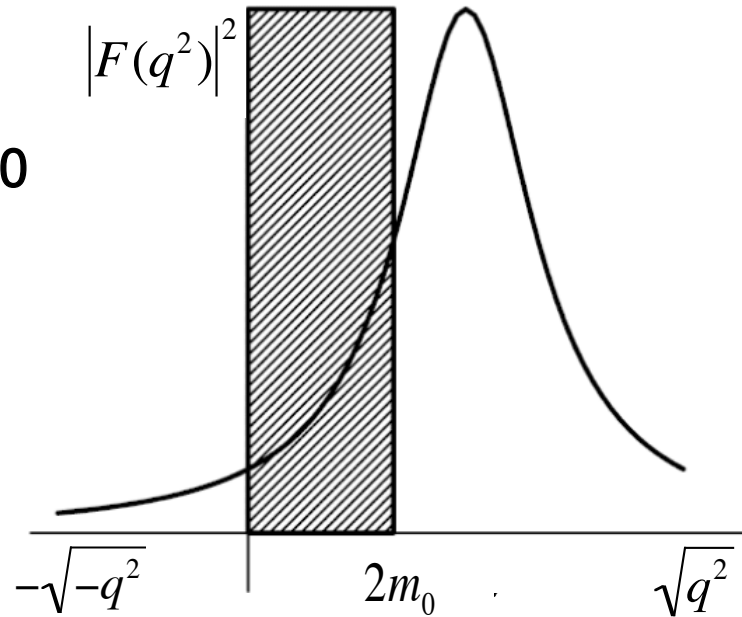
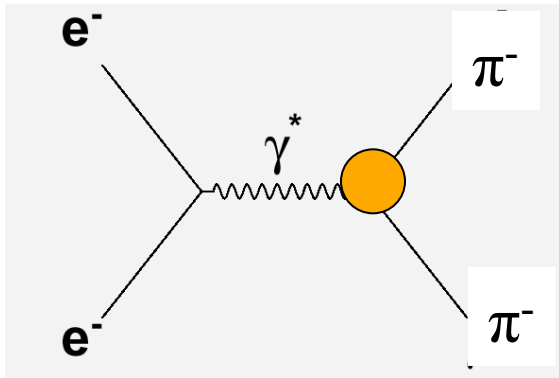
# Electromagnetic transition formfactor

hadrons = composite (non-point-like) particles of quarks and gluons with internal structure

access to internal structure: measurement of formfactors  $F(q^2)$

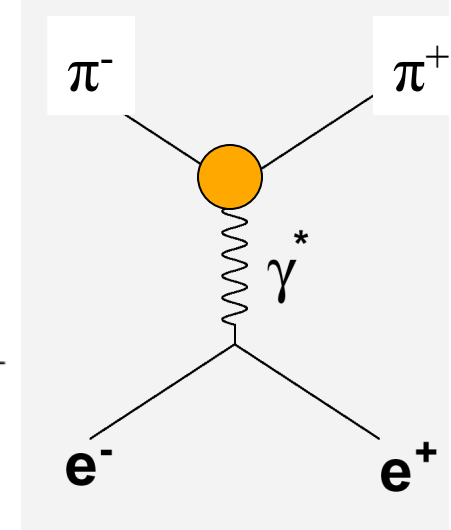
**elastic scattering**  
**space like:**

$$q^2 = (\Delta E/c)^2 - \Delta p^2 < 0$$

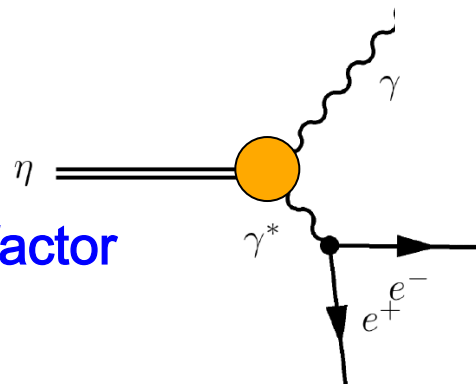


**annihilation**  
**time-like**

$$q^2 = (\Delta E/c)^2 - \Delta p^2 > 0$$



**transition form factor**



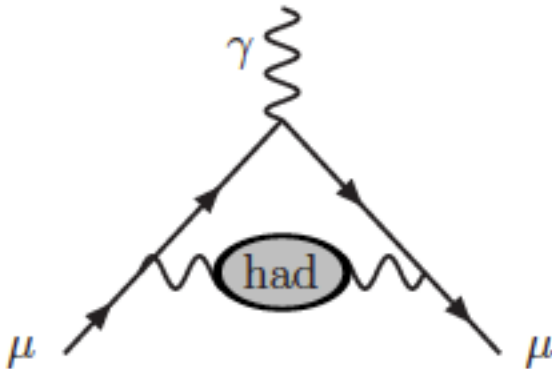
only access for  $0 < \sqrt{q^2} < 2m_0$

# Search for new physics

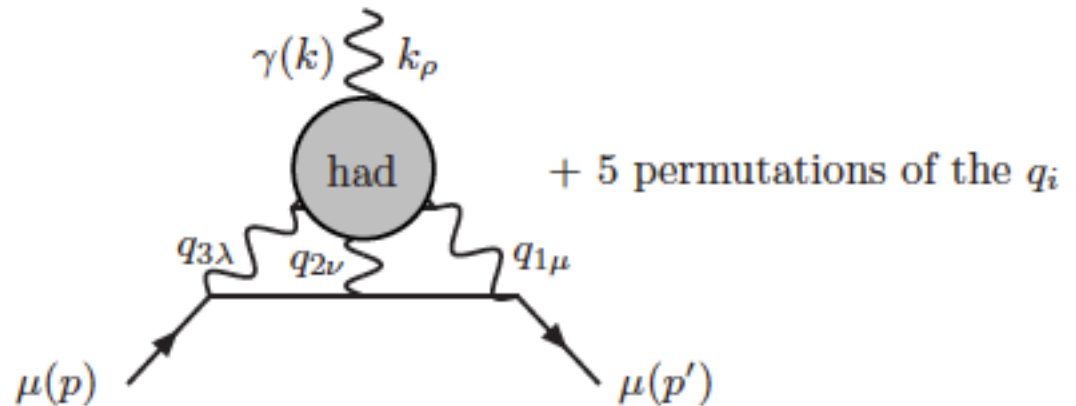
knowledge of lepton-hadron coupling also important in the search for new physics: precision measurement and interpretation of  $g-2$  of the muon.

## hadronic corrections:

### vacuum polarization



### light-by-light scattering



# transition formfactors

$$\eta \rightarrow \gamma e^+ e^-$$

formfactors in particle decays:

$$\frac{d\Gamma}{dq^2} = \left( \frac{d\Gamma}{dq^2} \right)_{\text{pointlike}} \cdot |F(q^2)|^2$$

# transition formfactors

$$\eta \rightarrow \gamma e^+e^-$$

formfactors in particle decays:

$$\frac{d\Gamma}{dq^2} = \left( \frac{d\Gamma}{dq^2} \right)_{\text{pointlike}} \cdot |F(q^2)|^2$$

G. Landsberg, Phys.Rep. 128 (1985) 30

$$\frac{d\Gamma(P \rightarrow e^+e^-\gamma)}{dm \Gamma(P \rightarrow \gamma\gamma)} = \frac{4\alpha}{3\pi m} \sqrt{1 - \frac{4m_e^2}{m^2}} \left( 1 + \frac{2m_e^2}{m^2} \right) \left[ 1 - \frac{m^2}{m_P^2} \right]^3 |F(q^2)|^2;$$

measure  $\eta \rightarrow \gamma e^+e^-$  relative to  $\eta \rightarrow \gamma \gamma$  !!!

# transition formfactors

$$\eta \rightarrow \gamma e^+ e^-$$

formfactors in particle decays:

$$\frac{d\Gamma}{dq^2} = \left( \frac{d\Gamma}{dq^2} \right)_{\text{pointlike}} \cdot |F(q^2)|^2$$

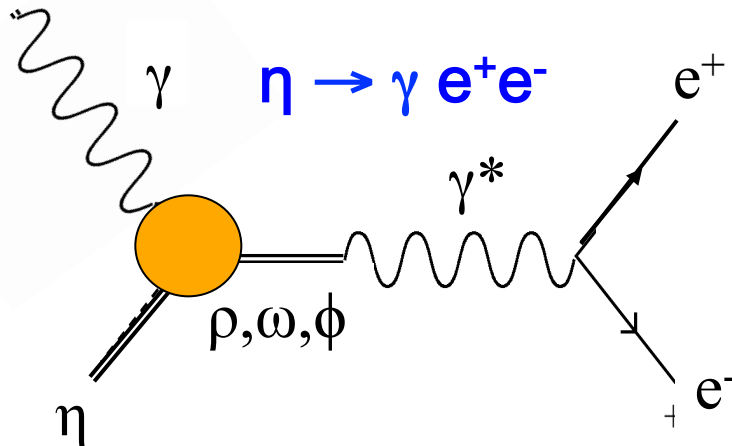
G. Landsberg, Phys.Rep. 128 (1985) 30

$$\frac{d\Gamma(P \rightarrow e^+ e^- \gamma)}{dm \Gamma(P \rightarrow \gamma \gamma)} = \frac{4\alpha}{3\pi m} \sqrt{1 - \frac{4m_e^2}{m^2}} \left( 1 + \frac{2m_e^2}{m^2} \right) \left[ 1 - \frac{m^2}{m_P^2} \right]^3 |F(q^2)|^2;$$

measure  $\eta \rightarrow \gamma e^+ e^-$  relative to  $\eta \rightarrow \gamma \gamma$  !!!

**Vector meson dominance (VDM) model:**

dileptons couple to hadrons via vector mesons



pole parametrization

$$F(q^2) = \frac{1}{1 - \frac{q^2}{\Lambda^2}}$$

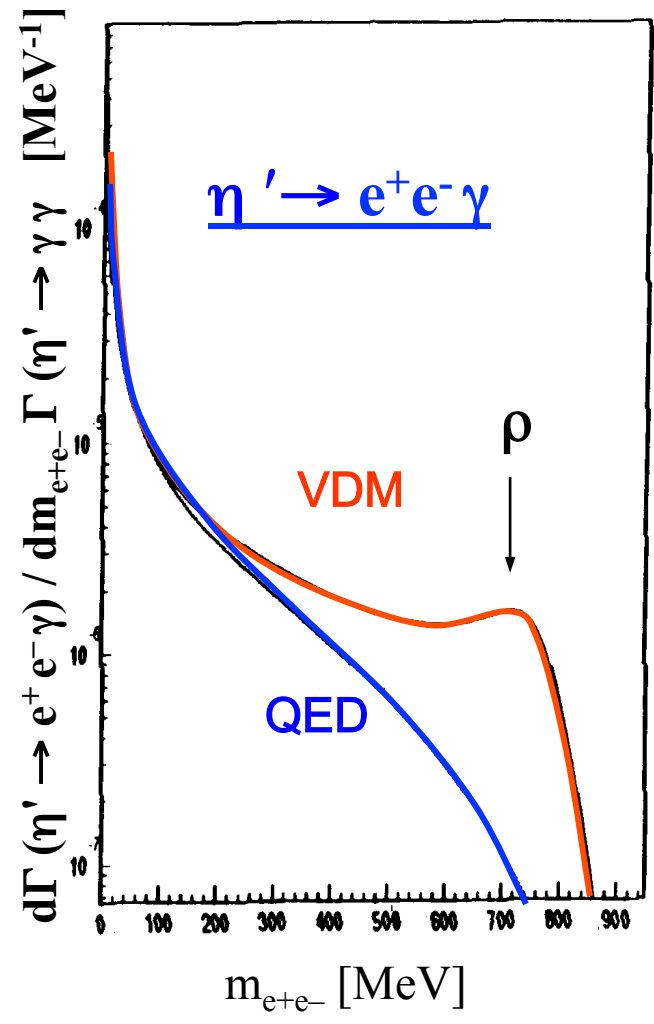
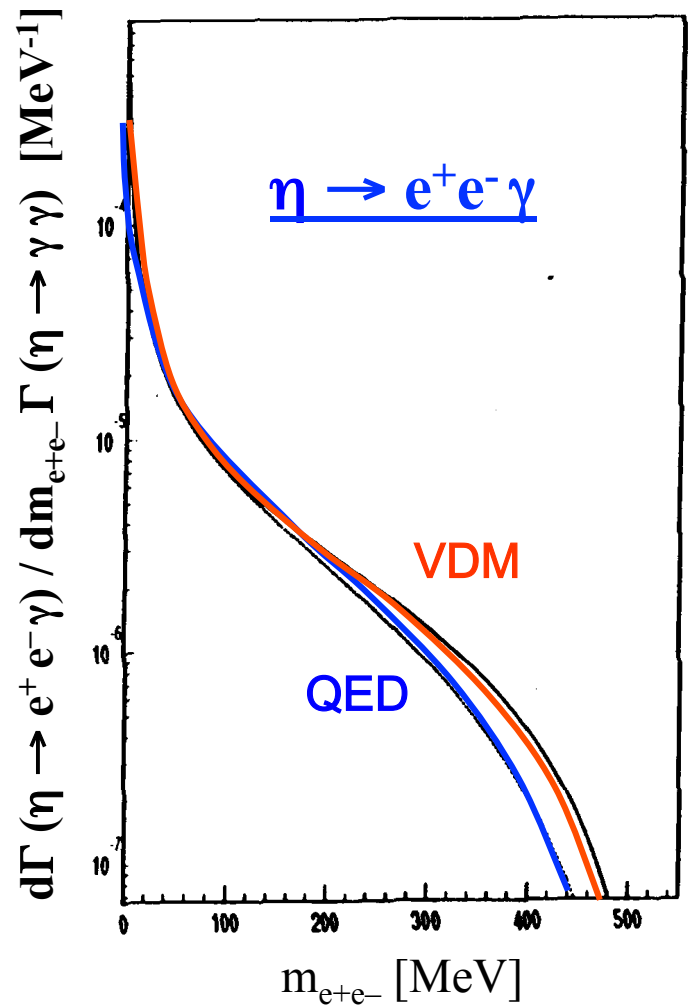
Virtual photon and neutral vector mesons have the same quantum numbers  $J^\pi=1^-$



# electromagnetic transition form factors: comparison QED / VDM

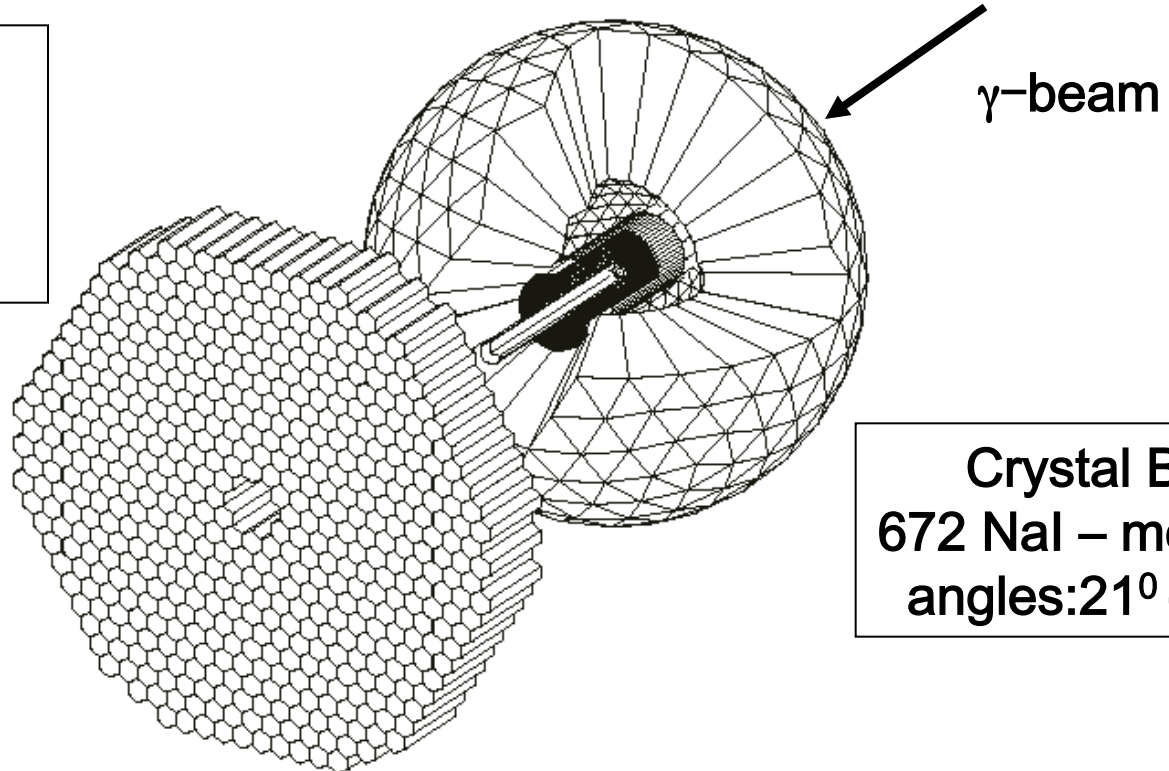
$$\frac{d\Gamma}{dq^2} = \left( \frac{d\Gamma}{dq^2} \right)_{\text{pointlike}} \cdot |F(q^2)|^2$$

pole parametrization:  $F(q^2) = \frac{1}{1 - \frac{q^2}{\Lambda^2}}$



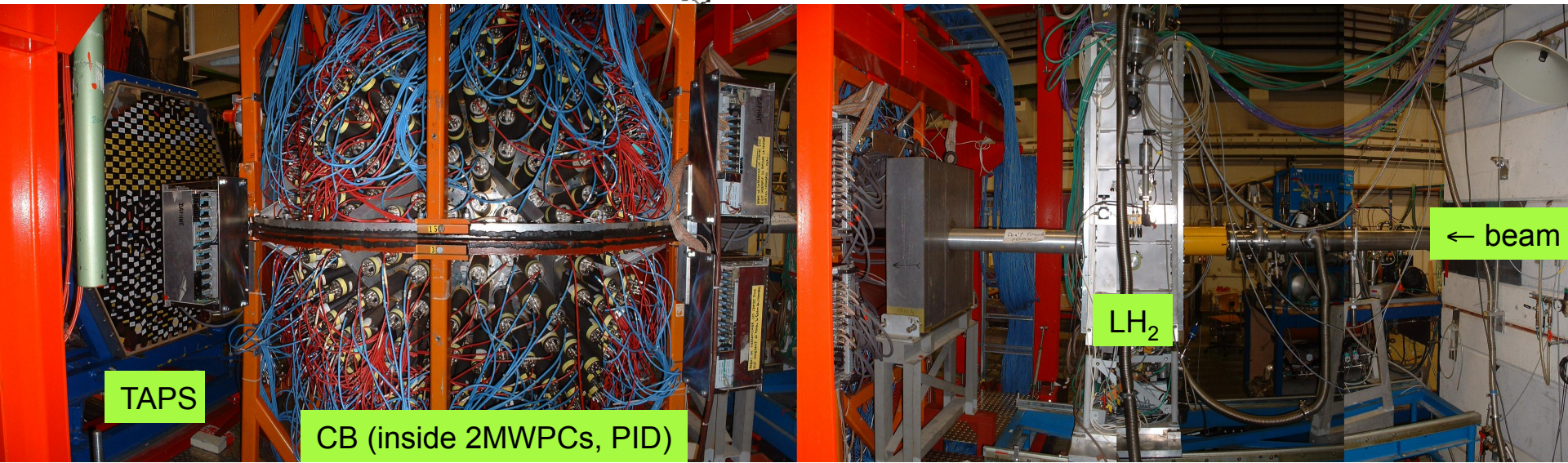
# CB/TAPS@MAMI

TAPS forward wall  
384 BaF<sub>2</sub> modules  
distance: 150 cm  
angles: 1.1° – 20.0°



Crystal Ball  
672 NaI – modules  
angles: 21° - 155°

no magnetic field !!



TAPS

CB (inside 2MWPCs, PID)

LH<sub>2</sub>

← beam

# Liquid hydrogen target and beamline



Kapton cell for liquid hydrogen target

## material around the target:

125  $\mu\text{m}$  Kapton

8 layers superisolation foil  
(8  $\mu\text{m}$  Mylar, 2  $\mu\text{m}$  Alu)

1 mm CFK vacuum tube

## material budget:

altogether: 0.8% of  $X_0$

low material budget important  
for **suppressing conversion** of  
real photons:  $\eta \rightarrow \gamma\gamma \rightarrow \gamma e^+e^-$



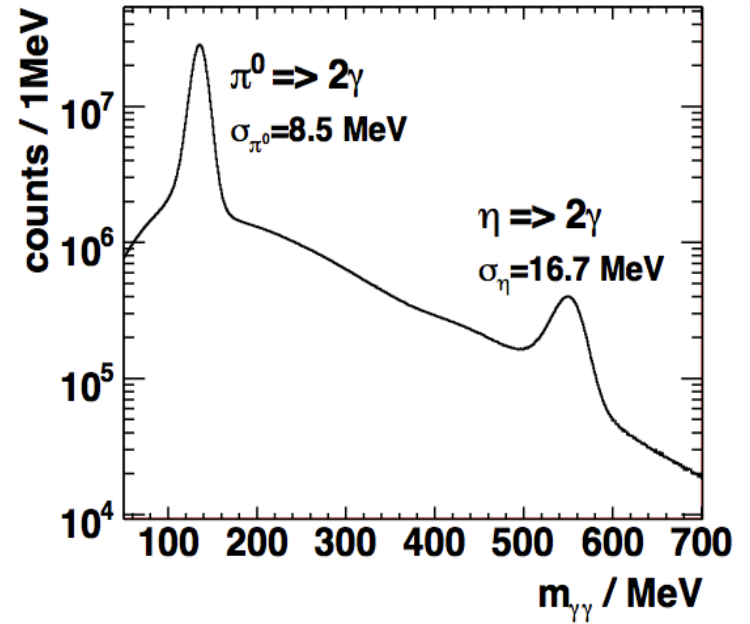
Carbon fiber vacuum tube

# particle identification

$$\underline{\eta \rightarrow e^+e^-\gamma}$$

neutral particles:

$$\underline{\pi^0, \eta \rightarrow \gamma\gamma}$$



# particle identification

$$\underline{\eta \rightarrow e^+e^-\gamma}$$

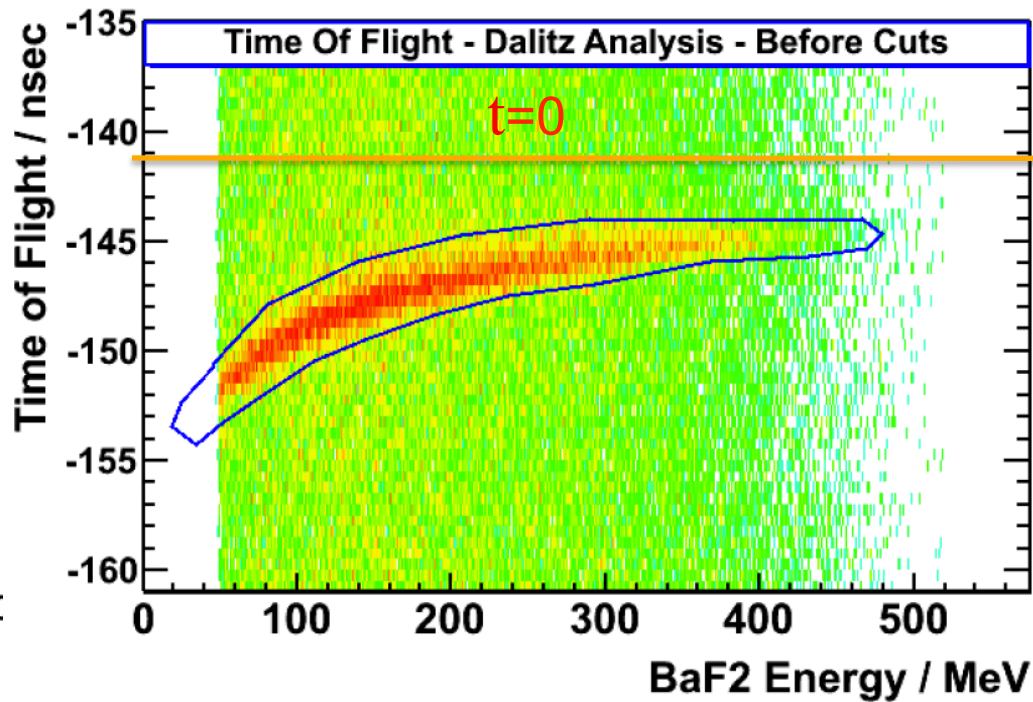
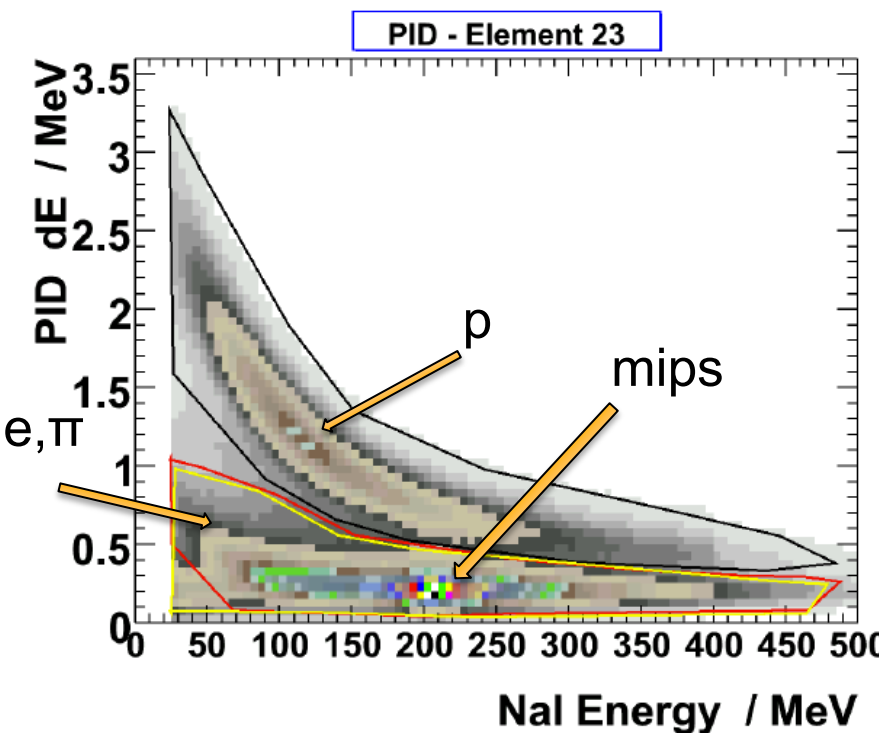
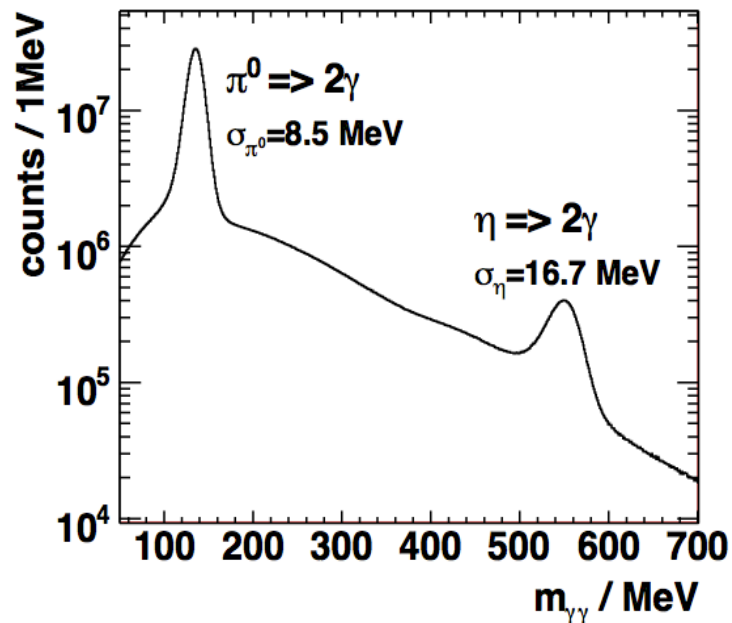
neutral particles:

$$\underline{\pi^0, \eta \rightarrow \gamma\gamma}$$

charged particles:

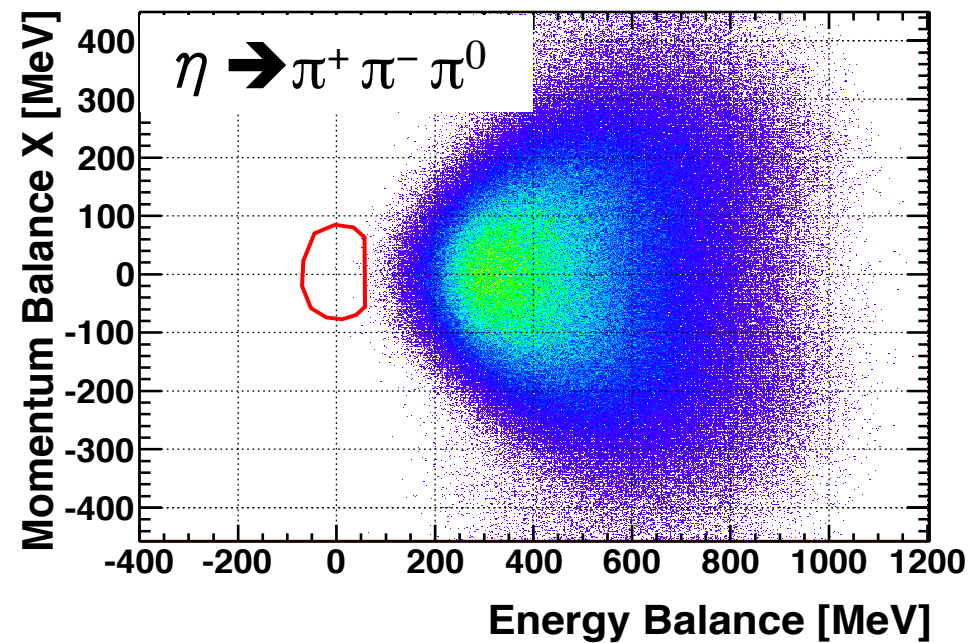
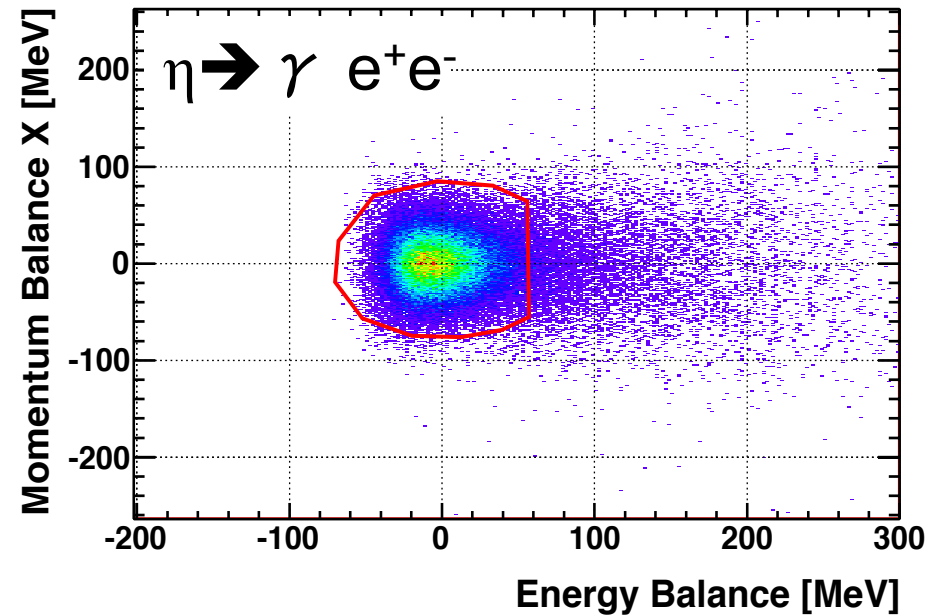
24 plastic scintillators (2 mm thick) in cylindrical arrangement around target + veto detectors in front of TAPS

$\Delta E$  vs.  $E$ ;  $E$  vs.  $t$  (TAPS)



# electron / pion misidentification

Simulation: exploiting energy- and momentum- balance for e /  $\pi$  separation



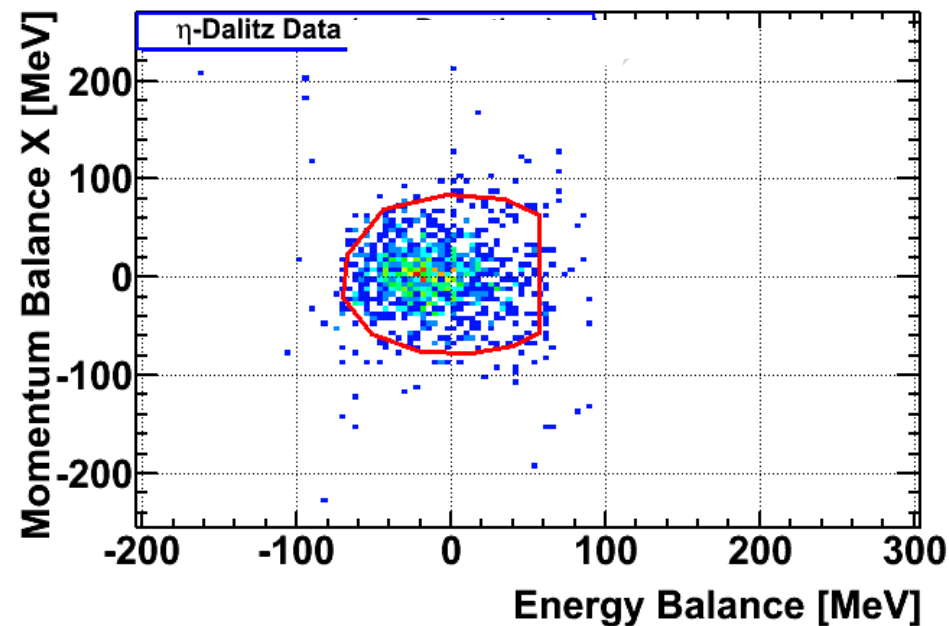
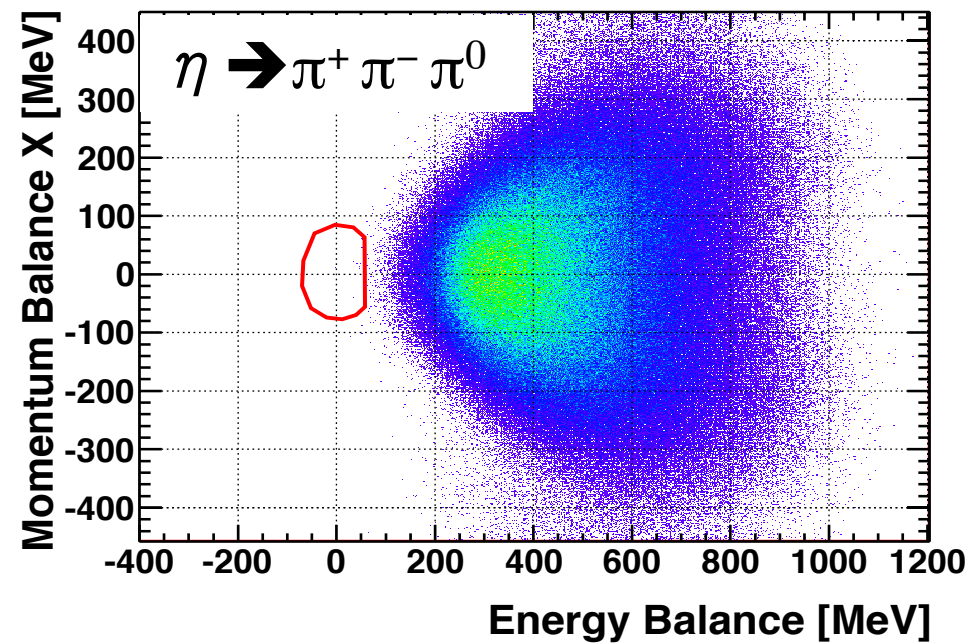
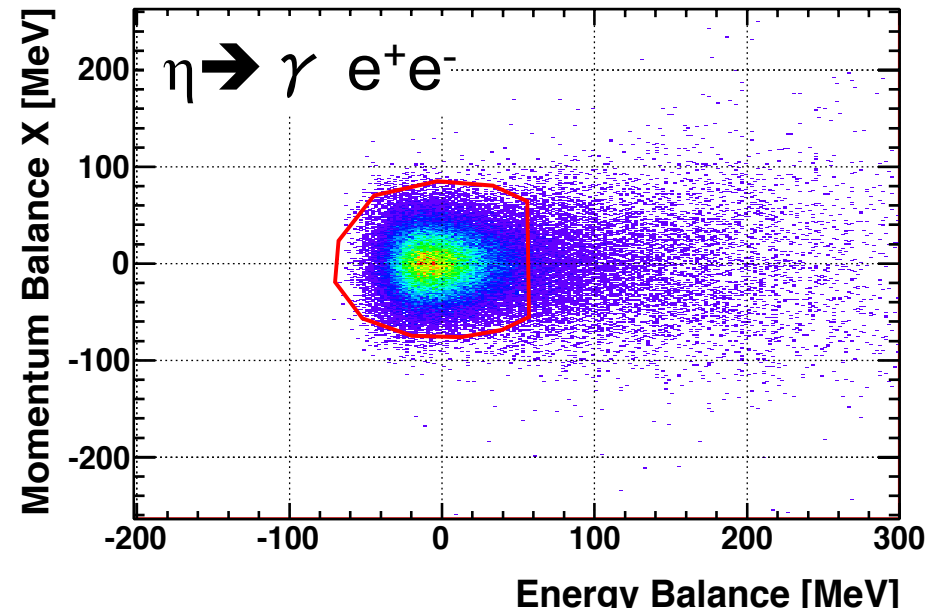
Pions misidentified as electrons

8 counts out of  $9.2 \cdot 10^6$  events  
in cut range

→ upper limit for  $e^+e^-/\pi^+\pi^-$   
misidentification:  $1 \cdot 10^{-6}$

# electron / pion misidentification

Simulation: exploiting energy- and momentum- balance for e /  $\pi$  separation



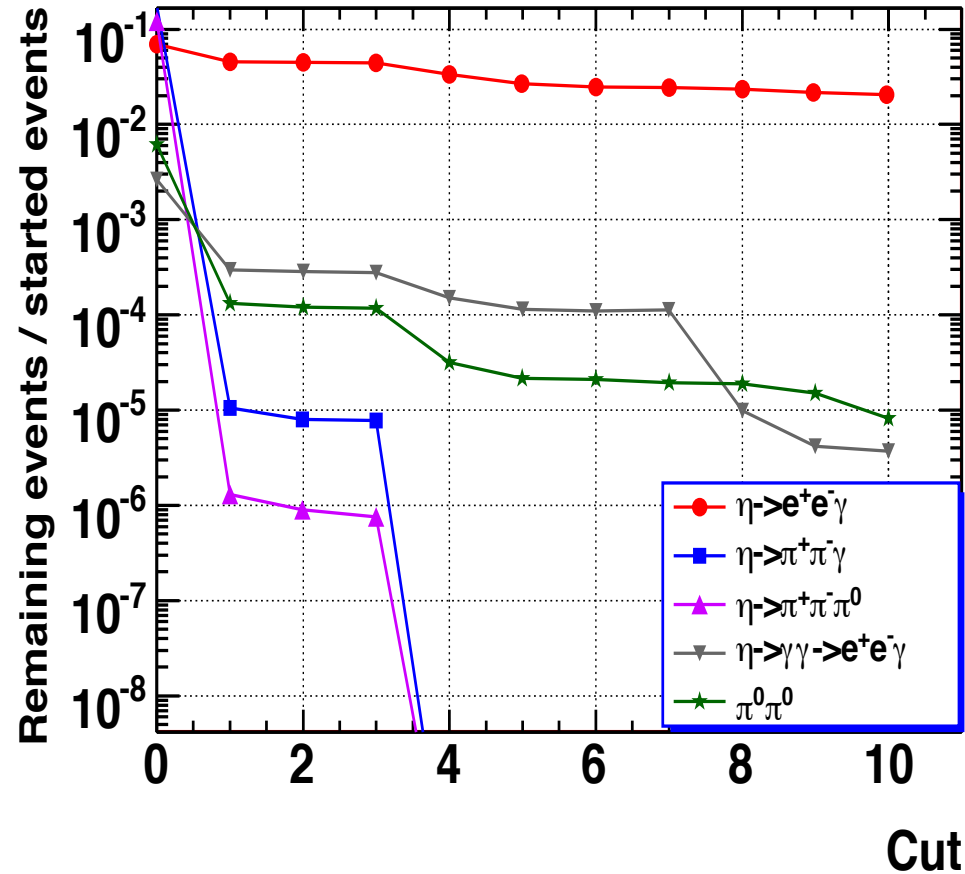
Pions misidentified as electrons

8 counts out of  $9.2 \cdot 10^6$  events  
in cut range

→ upper limit for  $e^+ e^- / \pi^+ \pi^-$   
misidentification:  $1 \cdot 10^{-6}$

# cuts to select reaction of interest: $\gamma p \rightarrow p \eta \rightarrow p \gamma e^+ e^-$

Cut-Nr	Name [Unit]	Limits
1	Momentum Balance X vs. Energy Balance	2D-Cut see Fig. 3
2	Momentum Balance Y vs. Energy Balance	2D-Cut
3	Momentum Balance Z [MeV]	-100.0 to 105.0
4	Missing Mass [MeV]	900 to 960
5	Beam Energy [MeV]	750 to 1210
6	Coplanarity [°]	167 to 193
7	$\Theta_{proton}$ [°]	0 to 50
8	opening angle $e^+ e^-$ [°]	10 to 140
9	$e^\pm$ Cluster Size	4 to 14
10	Angle $e^\pm \gamma$ [°]	50 to 175

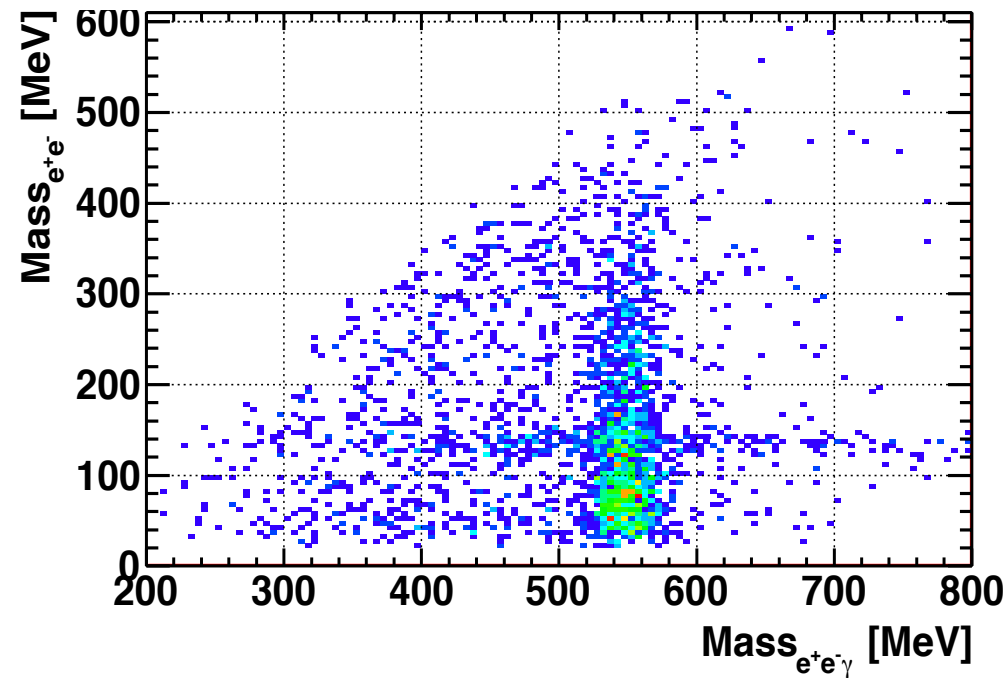


acceptance ( $\gamma p \rightarrow p \eta \rightarrow p \gamma e^+ e^-$ ) =  $(2.0 \pm 0.1)\%$

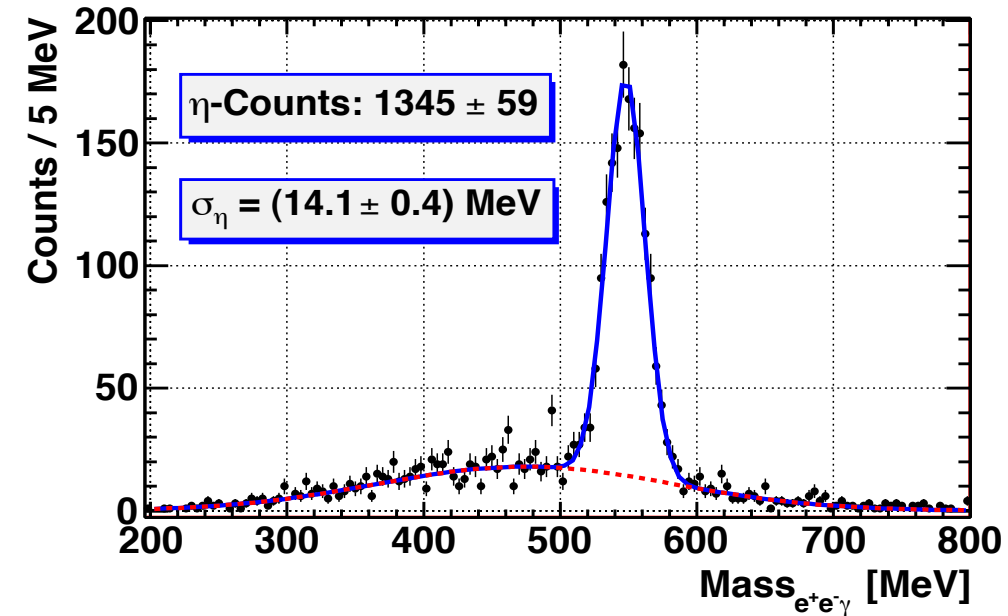
all other channels suppressed by more than 3 orders of magnitude



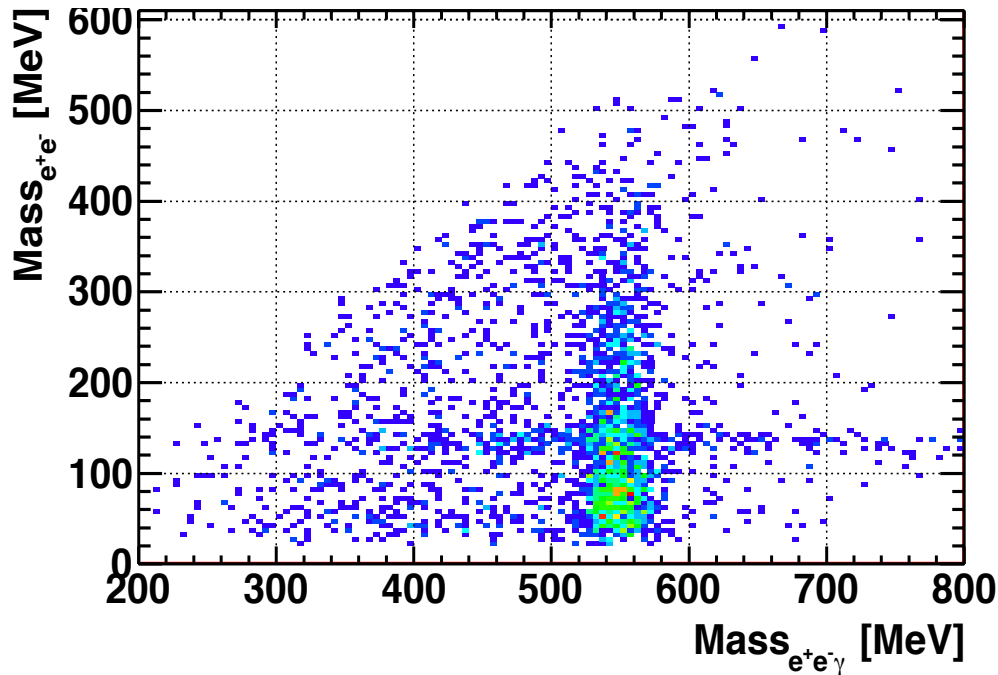
# Analysis of $\eta$ Dalitz decay: $\eta \rightarrow e^+e^- \gamma$



← e/ $\gamma$  mis-identification



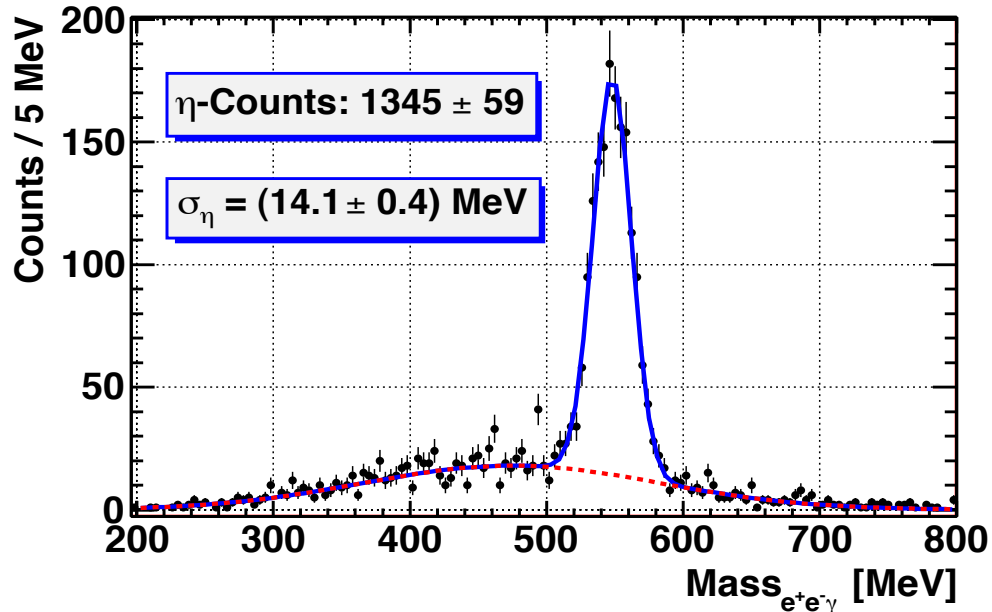
# Analysis of $\eta$ Dalitz decay: $\eta \rightarrow e^+e^- \gamma$



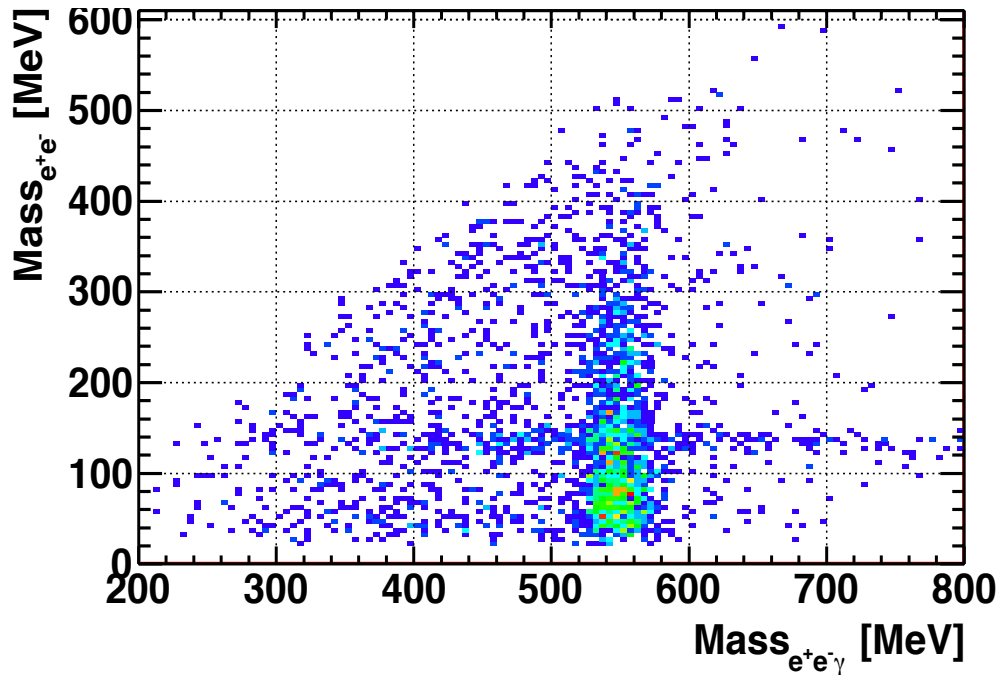
observed:  $N(\eta \rightarrow e^+e^- \gamma) = 1345 \pm 49$   
 $\varepsilon(\gamma p \rightarrow p \eta \rightarrow p e^+e^- \gamma) = (2.0 \pm 0.1)\%$   
total  $N(\eta \rightarrow e^+e^- \gamma) = (6.72 \pm 0.42) \cdot 10^4$

observed:  
 $N(\eta \rightarrow \gamma \gamma) = (4.81 \pm 0.24) \cdot 10^5$   
 $\varepsilon(\gamma p \rightarrow p \eta \rightarrow p \gamma \gamma) = 12.1\%$   
 $N(\eta \rightarrow \gamma \gamma) = (4.01 \pm 0.18) \cdot 10^6$

total number of  $\eta$  produced:  
 $(10.2 \pm 0.45) \cdot 10^6$



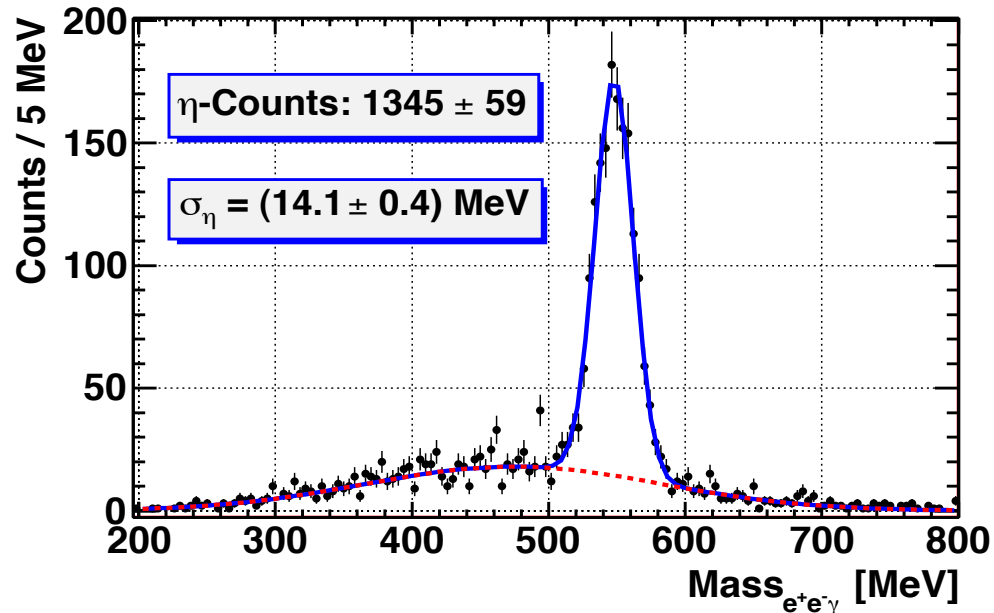
# Analysis of $\eta$ Dalitz decay: $\eta \rightarrow e^+e^- \gamma$



observed:  $N(\eta \rightarrow e^+e^- \gamma) = 1345 \pm 49$   
 $\varepsilon(\gamma p \rightarrow p \eta \rightarrow p e^+e^- \gamma) = (2.0 \pm 0.1)\%$   
 total  $N(\eta \rightarrow e^+e^- \gamma) = (6.72 \pm 0.42) \cdot 10^4$

observed:  
 $N(\eta \rightarrow \gamma \gamma) = (4.81 \pm 0.24) \cdot 10^5$   
 $\varepsilon(\gamma p \rightarrow p \eta \rightarrow p \gamma \gamma) = 12.1\%$   
 $N(\eta \rightarrow \gamma \gamma) = (4.01 \pm 0.18) \cdot 10^6$

total number of  $\eta$  produced:  
 $(10.2 \pm 0.45) \cdot 10^6$



relative branching ratio:

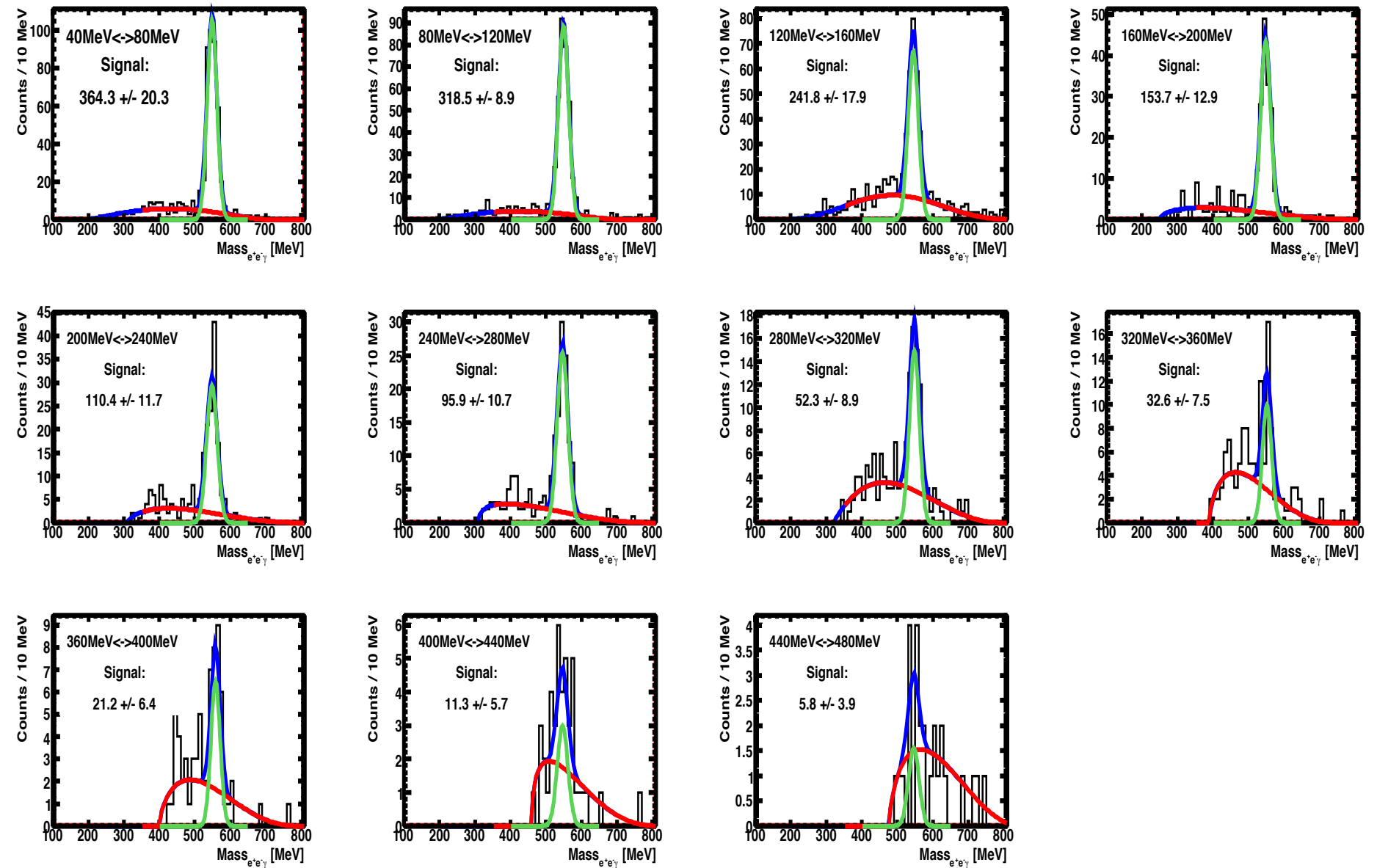
$$\frac{\Gamma_{\eta \rightarrow \gamma e^+e^-}}{\Gamma_{\eta \rightarrow \gamma \gamma}} = \frac{N_{\eta \rightarrow \gamma e^+e^-}}{N_{\eta \rightarrow \gamma \gamma}} \cdot \frac{\varepsilon_{\eta \rightarrow \gamma \gamma}}{\varepsilon_{\eta \rightarrow \gamma e^+e^-}}$$

$$= (1.68 \pm 0.10) \cdot 10^{-2}$$

$$\text{Br}(\eta \rightarrow \gamma e^+e^-) = (6.6 \pm 0.4 \pm 0.4) \cdot 10^{-3}$$

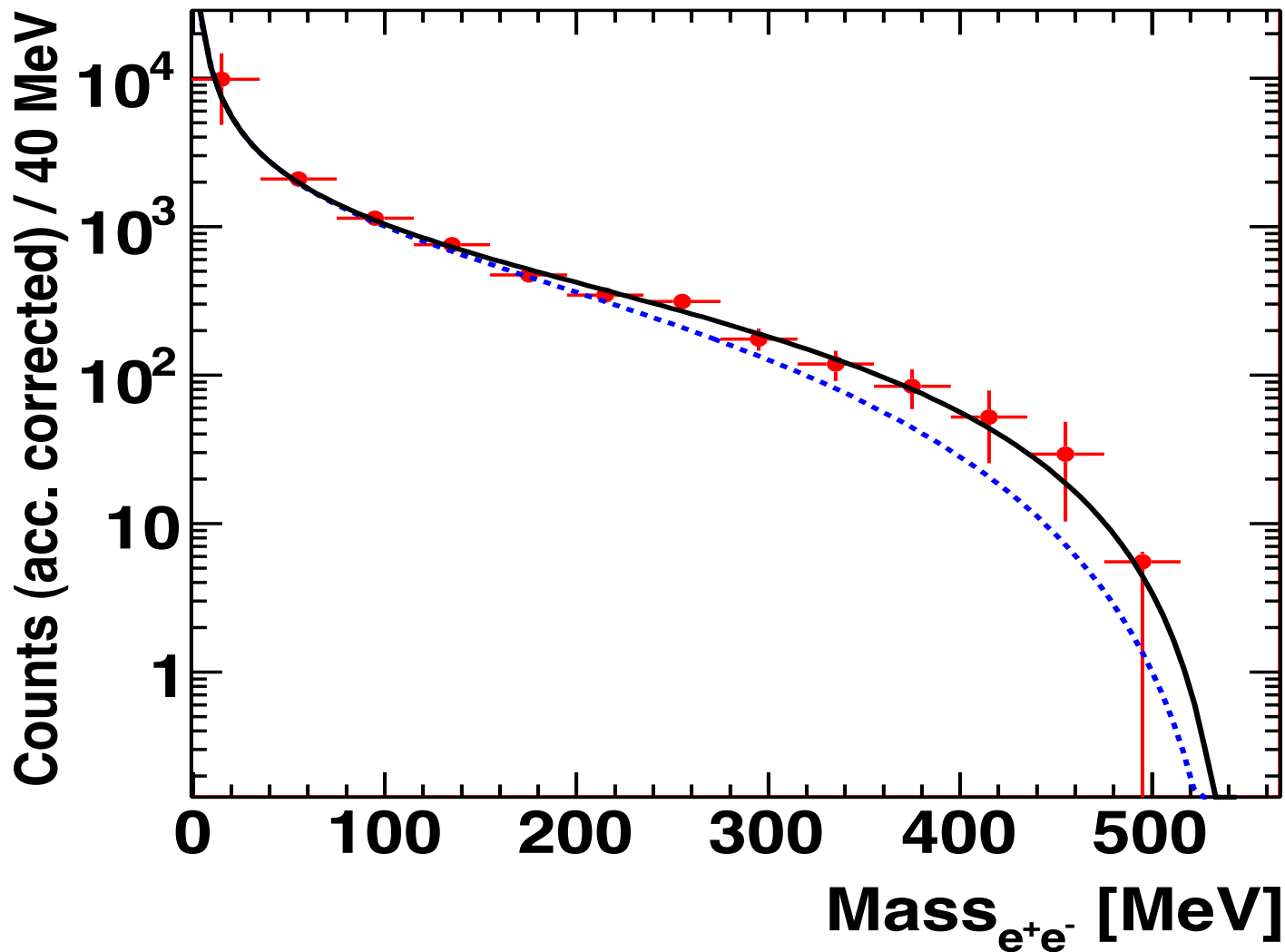
$$\text{PDG: Br}(\eta \rightarrow \gamma e^+e^-) = (7.0 \pm 0.7) \cdot 10^{-3}$$

# $\eta \rightarrow \gamma e^+e^-$ signal for different bins in $m_{e^+e^-}$



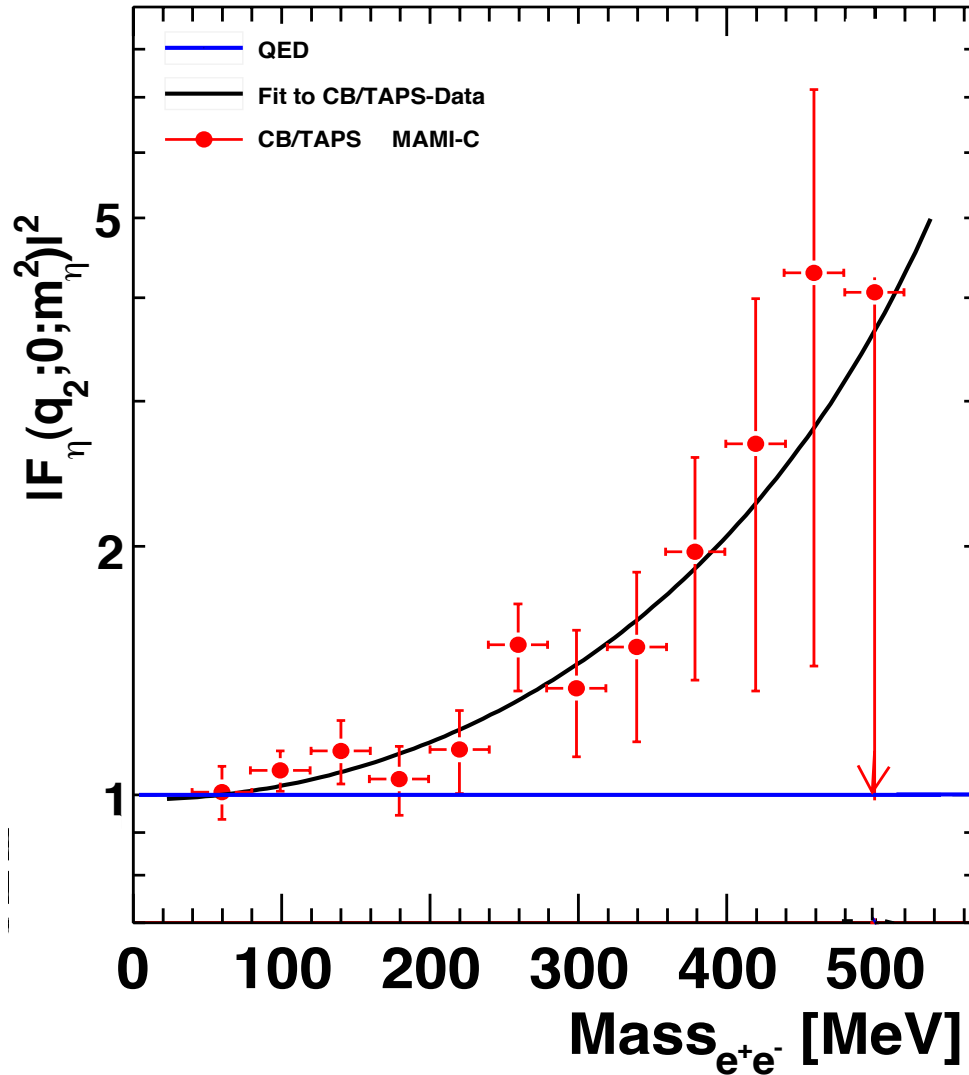
# $e^+e^-$ invariant mass distribution for $\eta \rightarrow \gamma e^+e^-$ events

after acceptance correction



deviation of experimental data from QED prediction  $\rightarrow$  form-factor

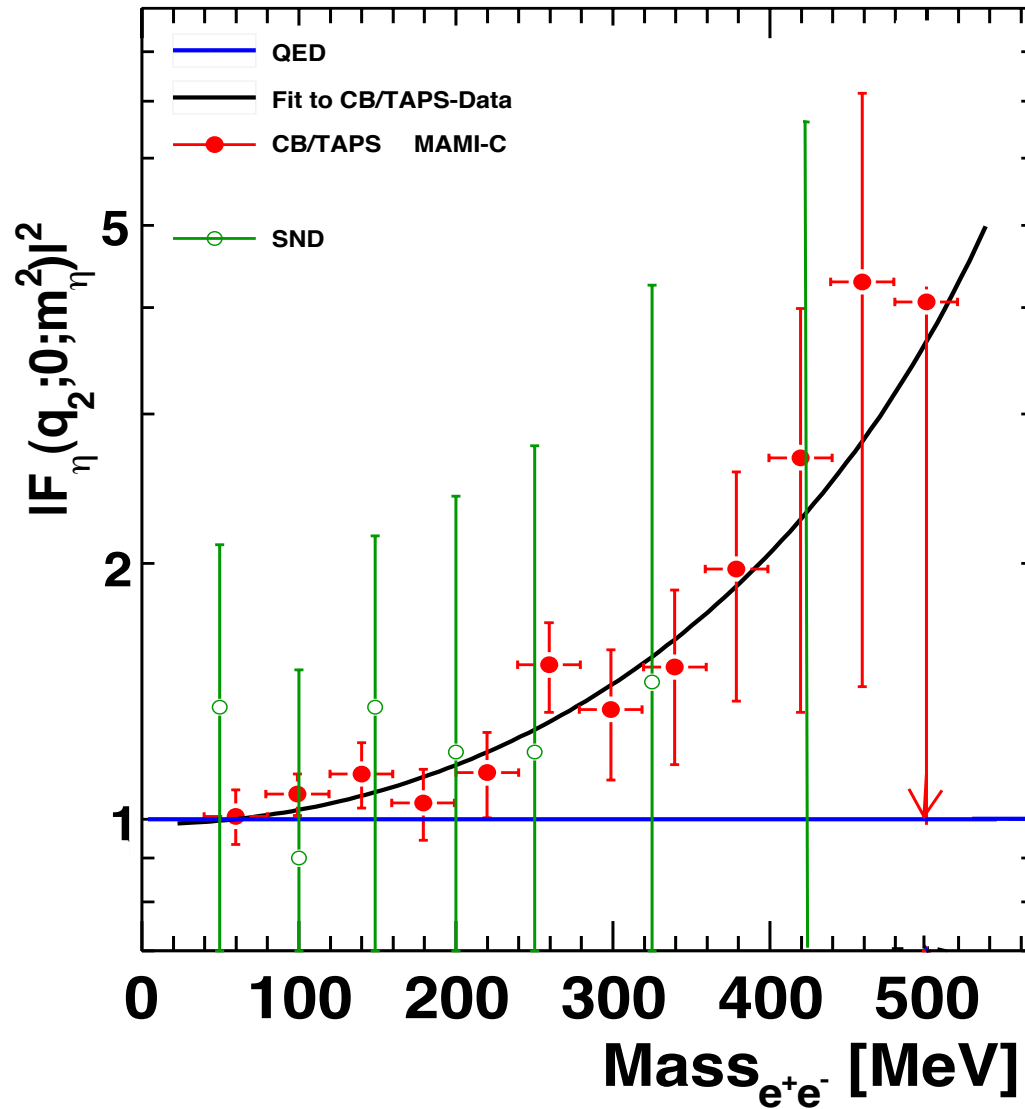
# electromagnetic transition form-factor of the $\eta$ meson



$$F(q^2) = (1 - q^2/\Lambda^2)^{-1}$$

$\eta \rightarrow \gamma e^+e^-$ ; this work:  $b_\eta = \Lambda^{-2} = (1.92 \pm 0.35(\text{stat}) \pm 0.13(\text{syst})) \text{ GeV}^{-2}$   
 $\Lambda = (720 \pm 60(\text{stat}) \pm 50(\text{syst})) \text{ MeV}$

# comparison to SND data



$$F(q^2) = (1 - q^2/\Lambda^2)^{-1}$$

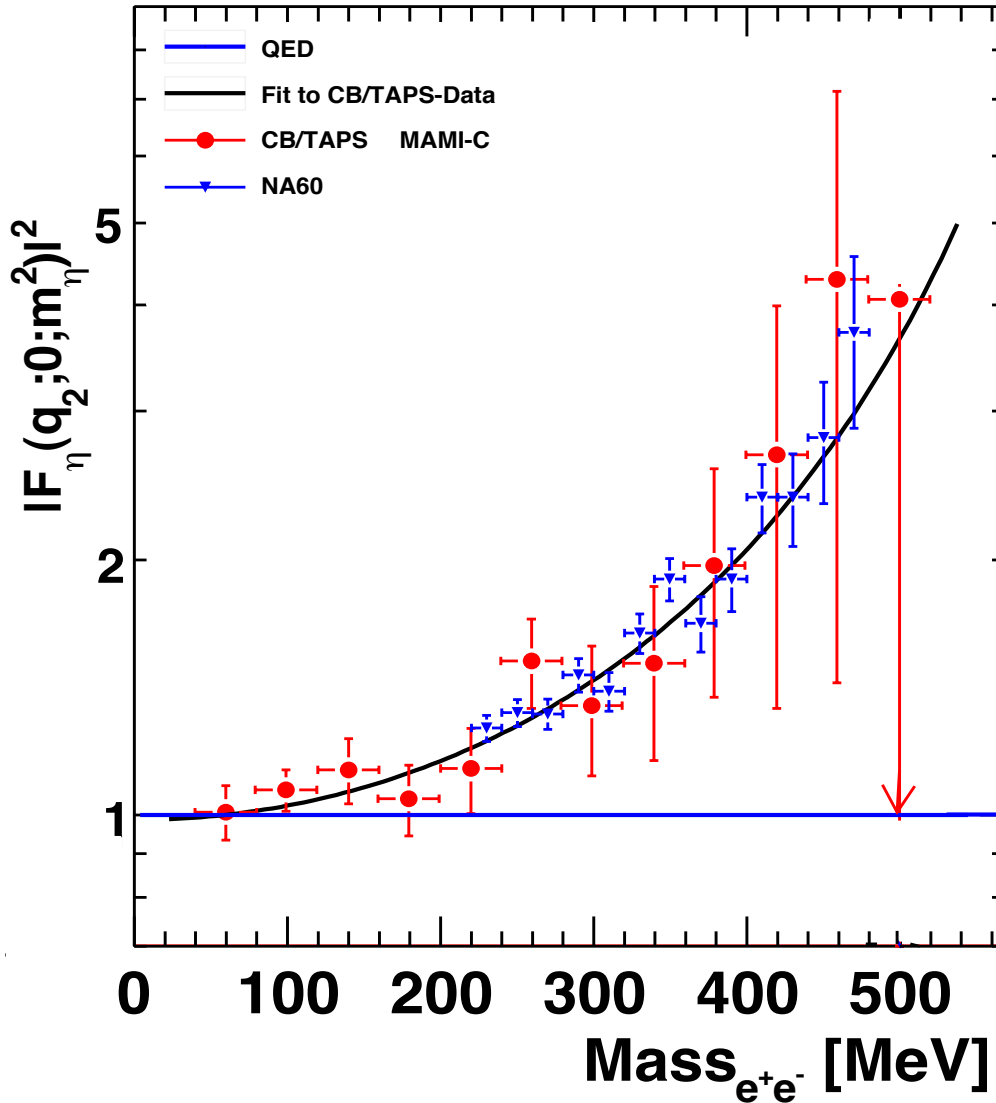
**SND:**

M.N. Achasov et al.,  
PLB 504 (2001) 275

$\eta \rightarrow \gamma e^+e^-$ ; **this work:**  $b_\eta = \Lambda^{-2} = (1.92 \pm 0.35(\text{stat}) \pm 0.13(\text{syst})) \text{ GeV}^{-2}$

$\eta \rightarrow \gamma e^+e^-$ ; **SND:**  $b_\eta = \Lambda^{-2} = (1.6 \pm 2.0) \text{ GeV}^{-2}$

# Comparison to NA60 data



$$F(q^2) = (1 - q^2/\Lambda^2)^{-1}$$

## NA60:

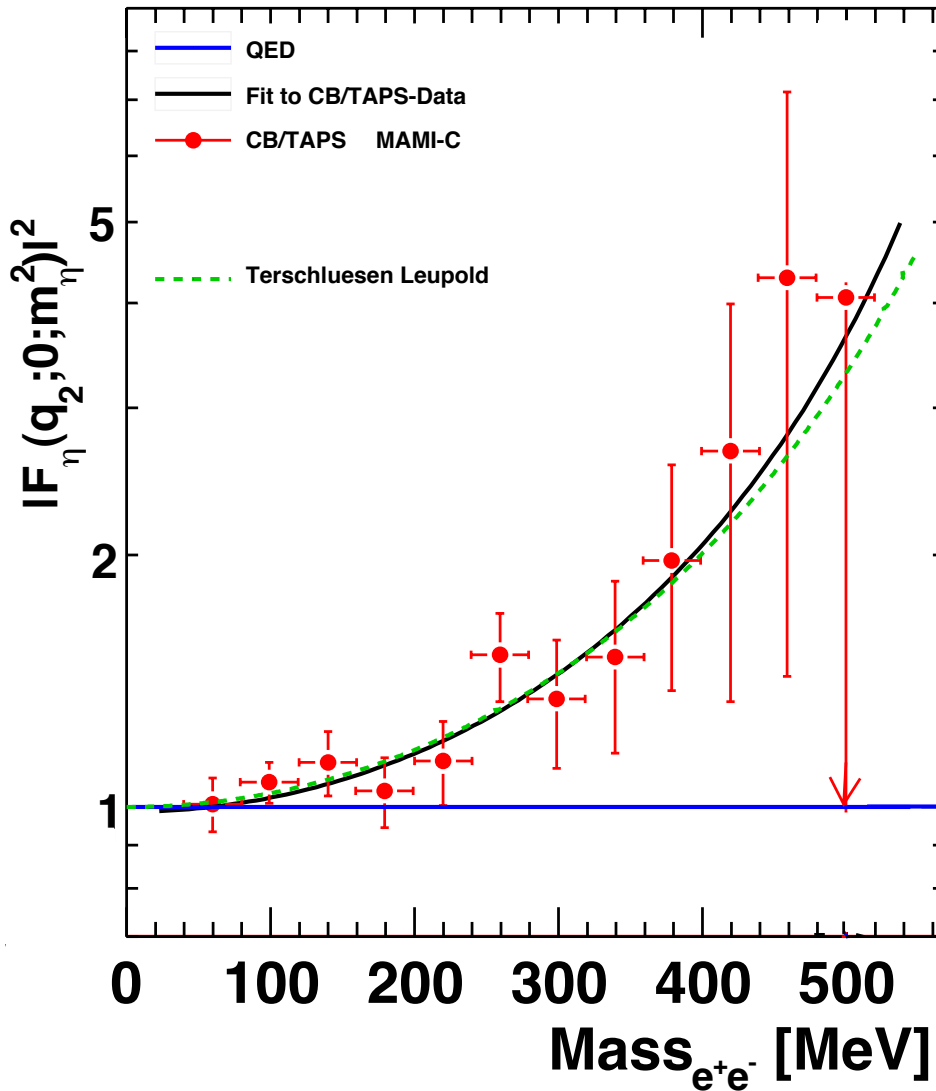
no photon detection,  
 → no reconstruction of  $\eta$  meson;  
 formfactor deduced from  
 unfolding  $\mu^+\mu^-$  mass spectrum,  
 starting at  $m_{\mu^+\mu^-} \geq 220$  MeV

$\eta \rightarrow \gamma e^+e^-$ ; **this work:**  $b_\eta = \Lambda^{-2} = (1.92 \pm 0.35(\text{stat}) \pm 0.13(\text{syst})) \text{ GeV}^{-2}$

$\eta \rightarrow (\gamma) \mu^+\mu^-$ ; **NA60:**  $b_\eta = \Lambda^{-2} = (1.95 \pm 0.17(\text{stat}) \pm 0.05(\text{syst})) \text{ GeV}^{-2}$



# Comparison to calculations



$$F(q^2) = (1 - q^2/\Lambda^2)^{-1}$$

C. Terschluesen and S. Leupold,  
PLB 691 (2010) 191

C. Terschluesen;  
Diploma thesis, Univ. Giessen  
(2010)

$\eta \rightarrow \gamma e^+e^-$ ; **this work:**  $b_\eta = \Lambda^{-2} = (1.92 \pm 0.35(\text{stat}) \pm 0.13(\text{syst})) \text{ GeV}^{-2}$

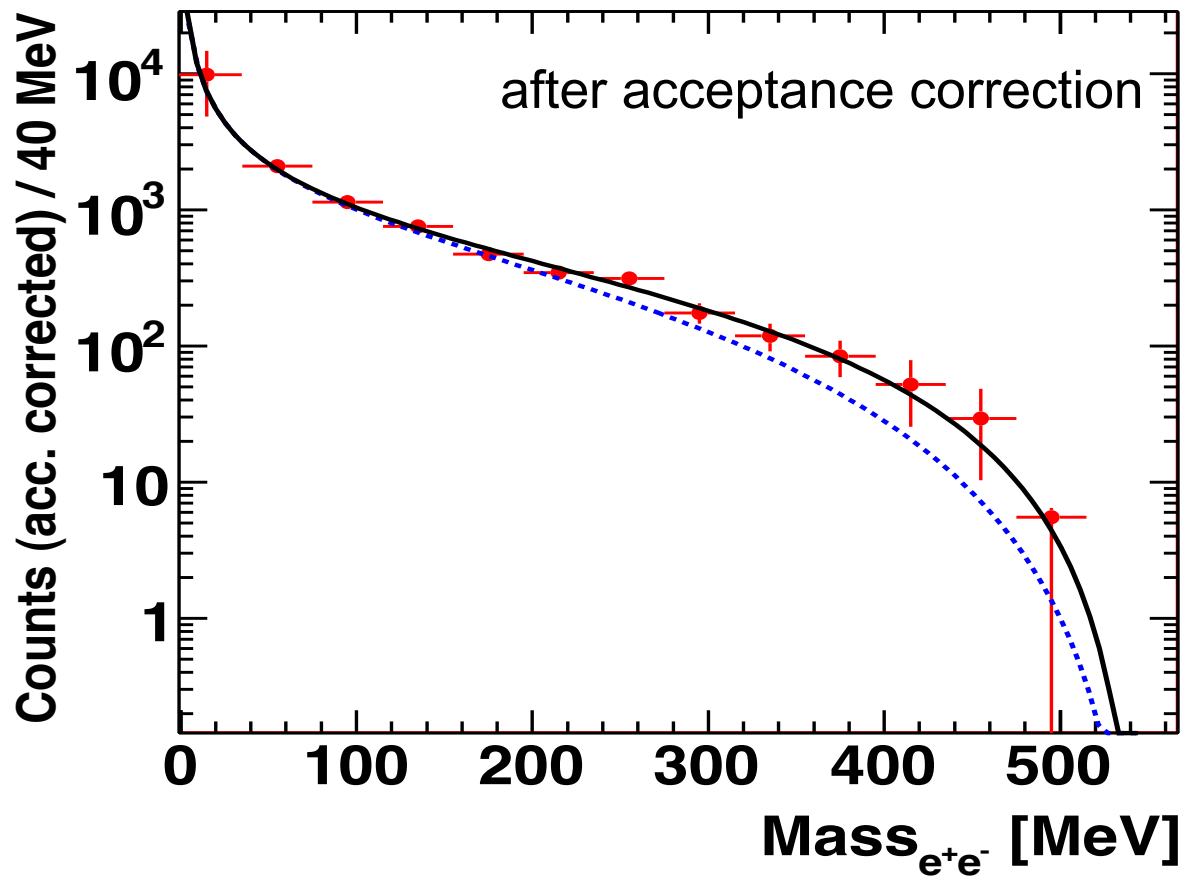
$\eta \rightarrow \gamma e^+e^-$ ; **theory:**  $b_\eta = \Lambda^{-2} = 1.79 \text{ GeV}^{-2}$ ; **VMD:**  $b_\eta = \Lambda^{-2} = 1.78 \text{ GeV}^{-2}$

## summary

- $10.2 \cdot 10^6$   $\eta$  mesons produced in photo nuclear reaction on  $\text{LH}_2$  target
- $\eta \rightarrow e^+e^-\gamma$  Dalitz decay identified in **exclusive reaction**  $\gamma p \rightarrow p \eta$  exploiting the full kinematic information: momentum-, energy balance, missing mass, etc.
- improvement in statistics compared to most recent measurement in the  $e^+e^-\gamma$  channel by an order of magnitude.
- resulting slope parameter of the form factor:  
 $b_\eta = \Lambda^{-2} = (1.92 \pm 0.35(\text{stat}) \pm 0.13(\text{syst})) \text{ GeV}^{-2}$   
in good agreement with NA60 measurement in  $\mu^+\mu^- (\gamma)$  channel
- resulting slope parameter of the form factor in good agreement with calculations by Terschlüsen, Leupold, Lutz within field theoretical approach and with the VMD prediction
- branching ratio for Dalitz decay:  
 $\text{Br}(\eta \rightarrow e^+e^-\gamma) = (6.6 \pm 0.4(\text{stat}) \pm 0.4(\text{syst})) \cdot 10^{-3}$   
PDG:  $(7.0 \pm 0.7) \cdot 10^{-3}$

See also poster 13 by Michael Kunkel (CLAS-collaboration) !!

# $e^+e^-$ invariant mass distribution for $\eta \rightarrow \gamma e^+e^-$ events



deviation of experimental data from QED prediction  
→ form-factor

