

Bottomonium results at Belle

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BINP

For Belle Collaboration

Hadron 2011, June 14, 2011

Puzzles of $\Upsilon(5S)$ decays

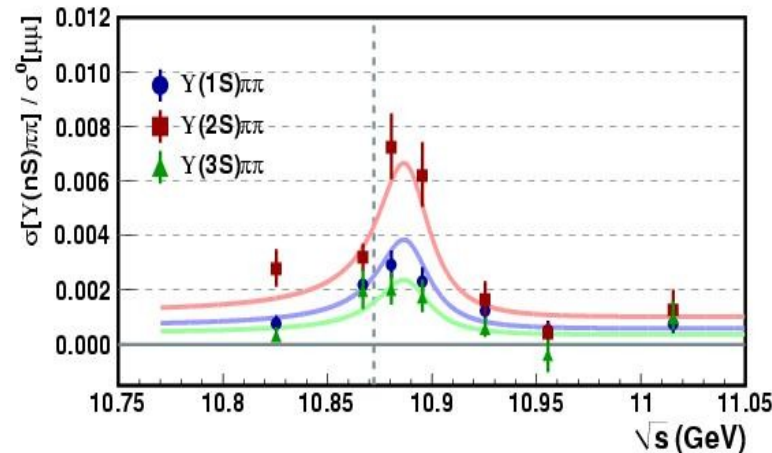
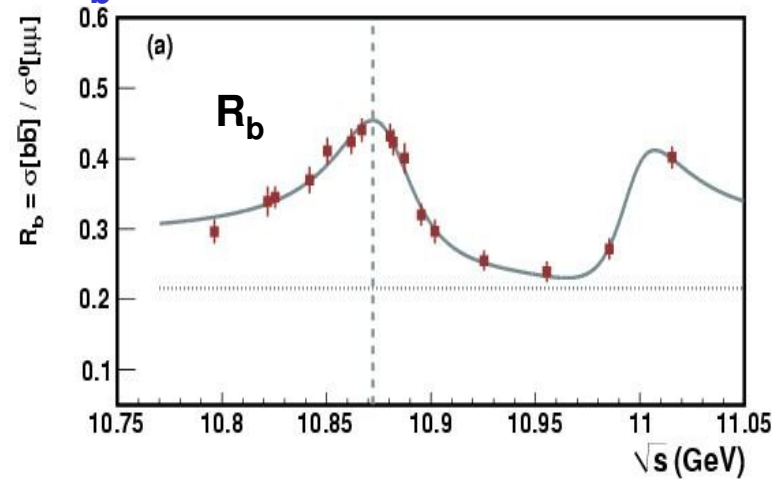
At 21.7 fb^{-1} $\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+ \pi^-$ two orders of magnitude larger than in $\Upsilon(4S)$ decay

$\Gamma(\text{MeV})$

PRD82,091106R(2010)

$\Upsilon(5S) \rightarrow \Upsilon(1S) \pi^+ \pi^-$	$0.59 \pm 0.04 \pm 0.09$
$\Upsilon(5S) \rightarrow \Upsilon(2S) \pi^+ \pi^-$	$0.85 \pm 0.07 \pm 0.16$
$\Upsilon(5S) \rightarrow \Upsilon(3S) \pi^+ \pi^-$	$0.52^{+0.20}_{-0.17} \pm 0.10$
$\Upsilon(2S) \rightarrow \Upsilon(1S) \pi^+ \pi^-$	0.0060
$\Upsilon(3S) \rightarrow \Upsilon(1S) \pi^+ \pi^-$	0.0009
$\Upsilon(4S) \rightarrow \Upsilon(1S) \pi^+ \pi^-$	0.0019

Dedicated energy scan \Rightarrow
 shapes of R_b and $\sigma(\Upsilon\pi\pi)$ different (2σ)



-Rescattering $\Upsilon(5S) \rightarrow BB\pi\pi \rightarrow \Upsilon(nS)\pi\pi$

Simonov JETP Lett 87,147(2008)

-Exotic resonance Y_b near $\Upsilon(5S)$

$\Upsilon(5S)$ is very interesting and not yet understood

Finally Belle recorded 121.4 fb^{-1} at $\Upsilon(5S)$

arXiv:1104.2025

Observation of $e^+e^- \rightarrow \pi^+\pi^- h_c$ by CLEO

\Rightarrow Belle search for h_b in $\Upsilon(5S)$ data

Introduction to $h_b(nP)$

$(\bar{b}b) : S=0 \ L=1 \ J^{PC}=1^{+-}$

Expected mass (CoG of χ_{bJ})

$$\approx (M\chi_{b0} + 3 M\chi_{b1} + 5 M\chi_{b2}) / 9$$

$\Delta M_{\text{HF}} \Rightarrow$ test of hyperfine interaction

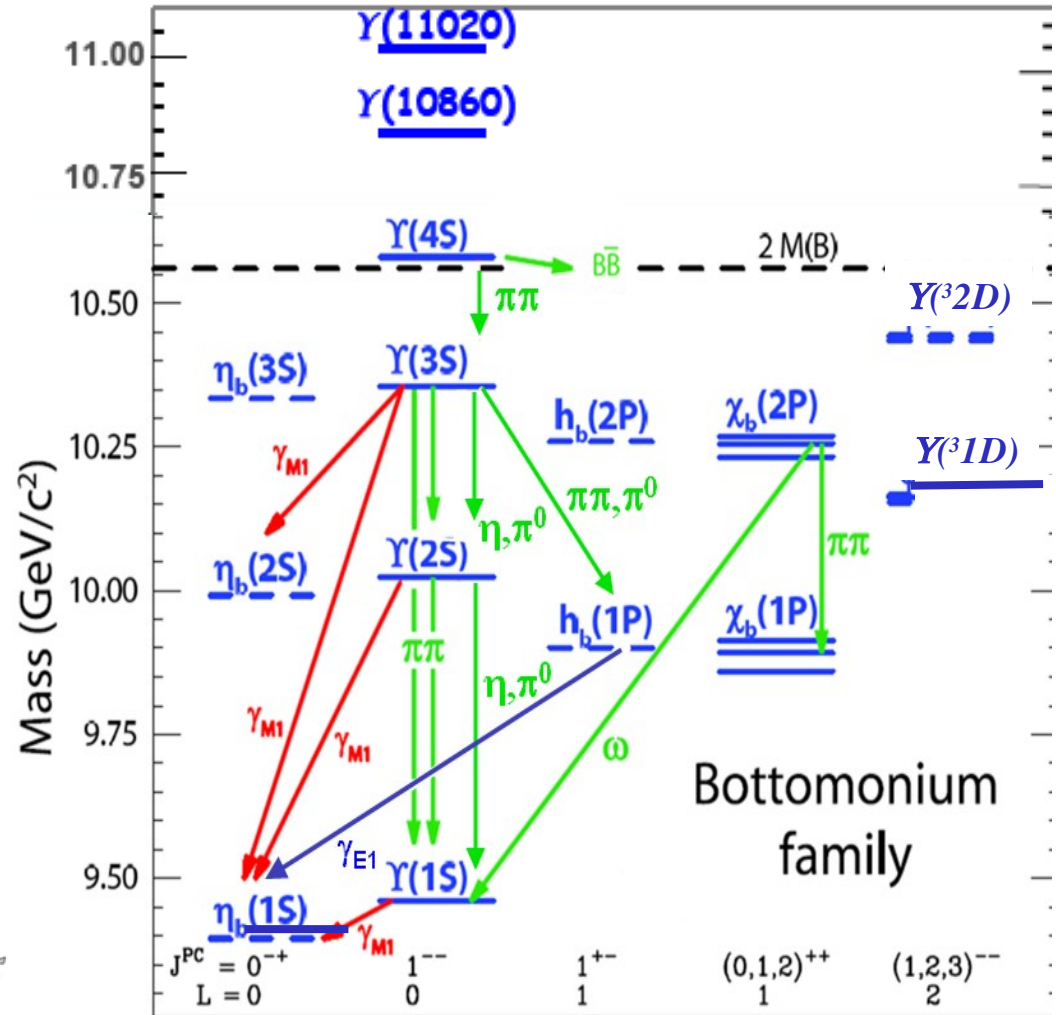
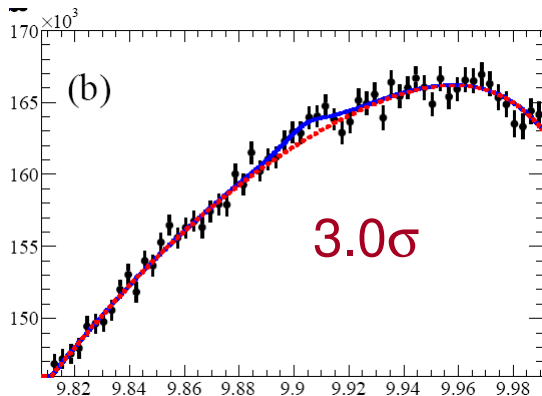
For h_c $\Delta M_{\text{HF}} = -0.12 \pm 0.30$,

expect smaller deviation for $h_b(nP)$.

arXiv:1102.4565

Evidence from BaBar

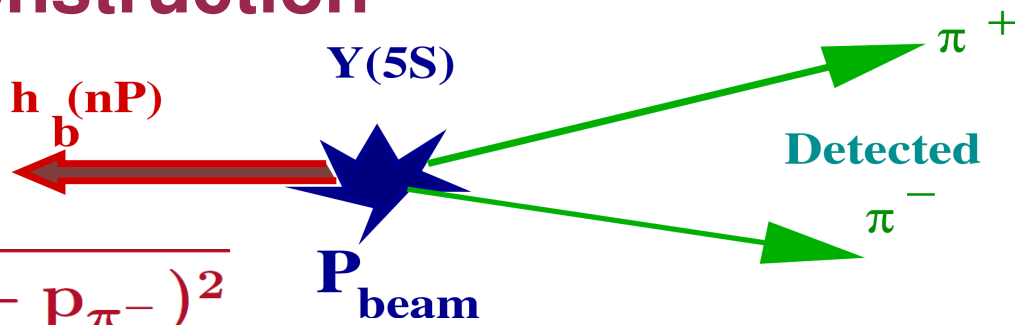
$\Upsilon(3S) \rightarrow \pi^0 h_b(1P) \rightarrow \pi^0 \gamma \eta_b(1S)$



$$B(\Upsilon(3S) \rightarrow \pi^0 h_b) \times B(h_b \rightarrow \gamma \eta_b) = (3.7 \pm 1.1 \pm 0.7) \times 10^{-4}$$

h_b reconstruction

Missing mass to $\pi\pi$ system



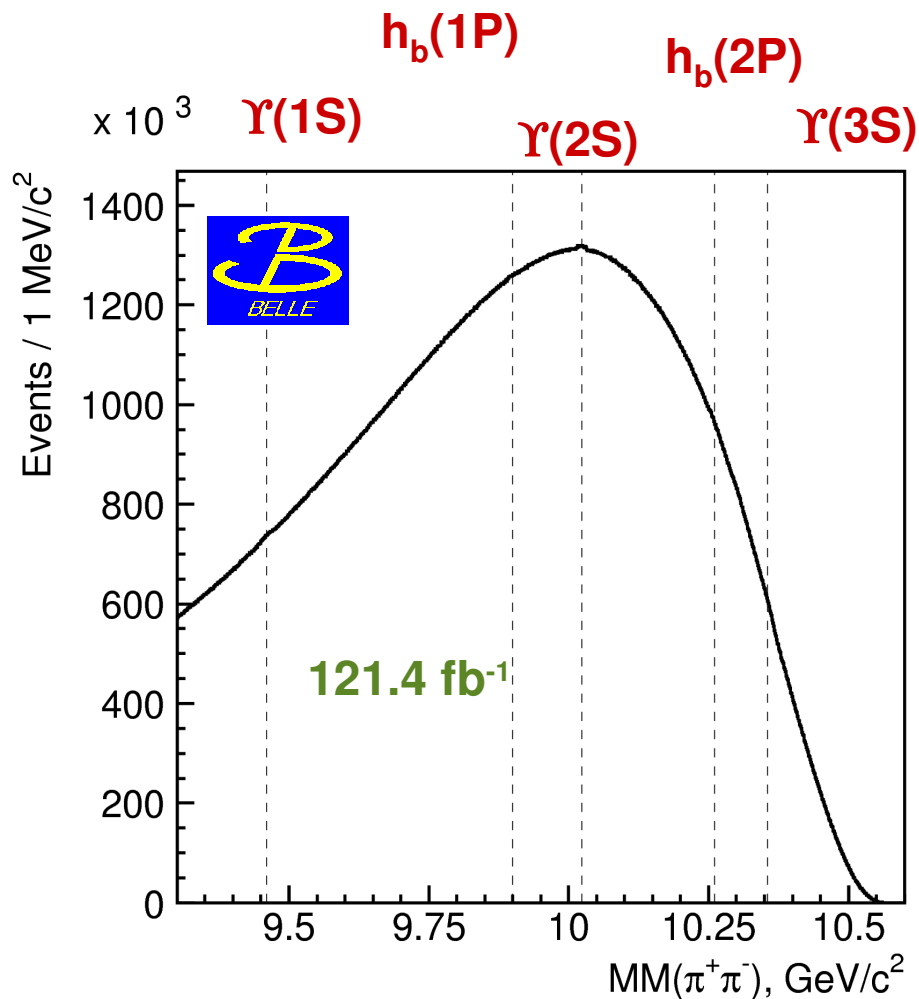
$$M_{\text{miss}} = \sqrt{P_{\text{beam}}^2 - (p_{\pi^+} + p_{\pi^-})^2}$$

Simple selection :

$\pi^+\pi^-$: good quality, positively identified

Suppression of continuum events
FW R2 < 0.3

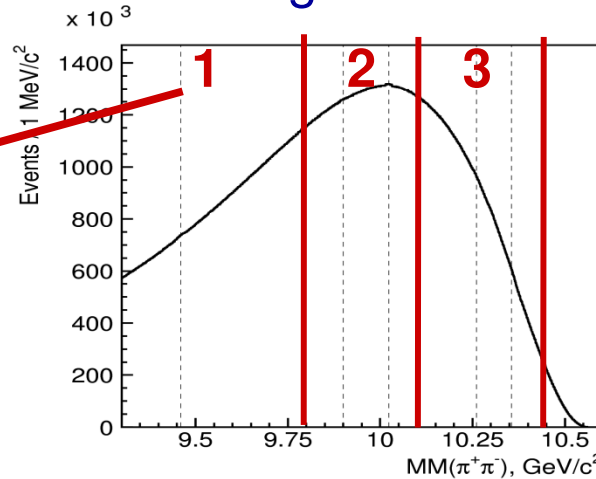
\Rightarrow Search for $h_b(nP)$ peaks
in $MM(\pi^+\pi^-)$ spectrum



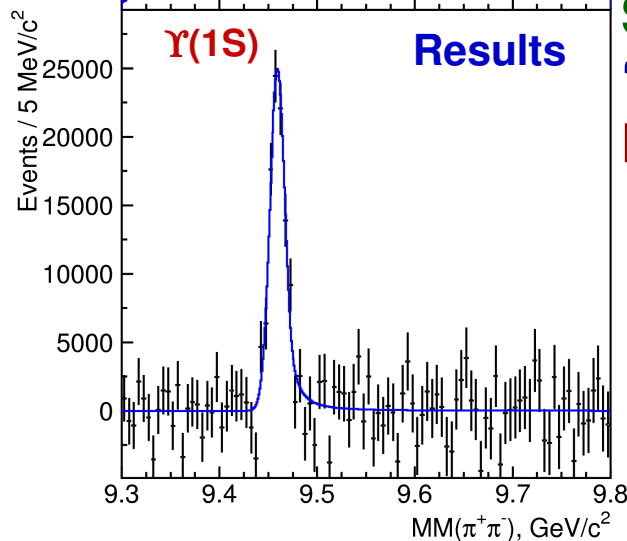
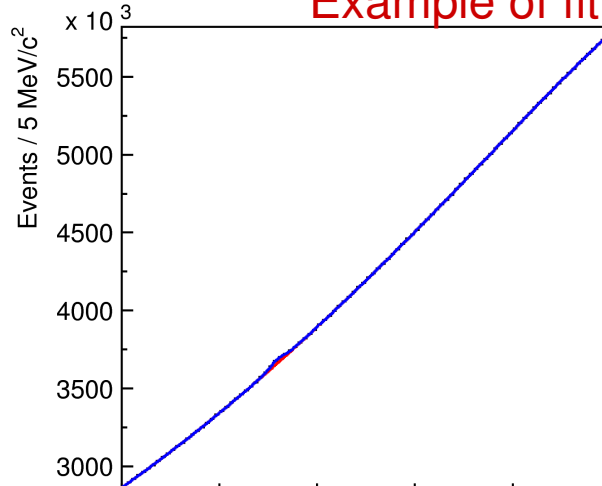
Description of fit to $MM(\pi^+\pi^-)$



Three fit regions



Example of fit

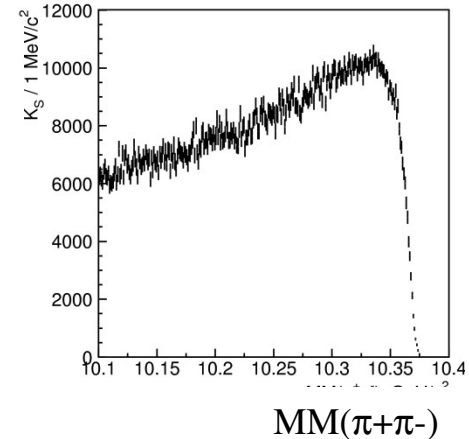
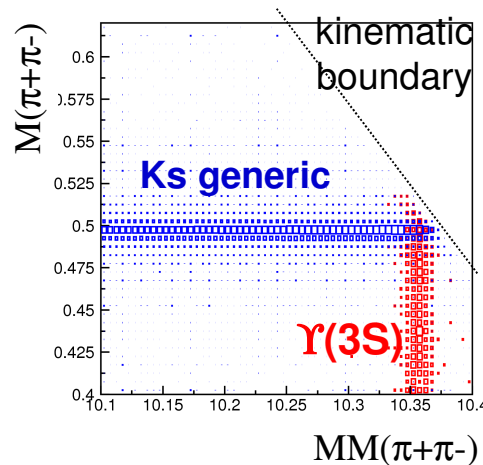


BG: Chebyshev polynomial 6th-7th order

Signal: shape is fixed from $\mu^+\mu^-\pi^+\pi^-$ data

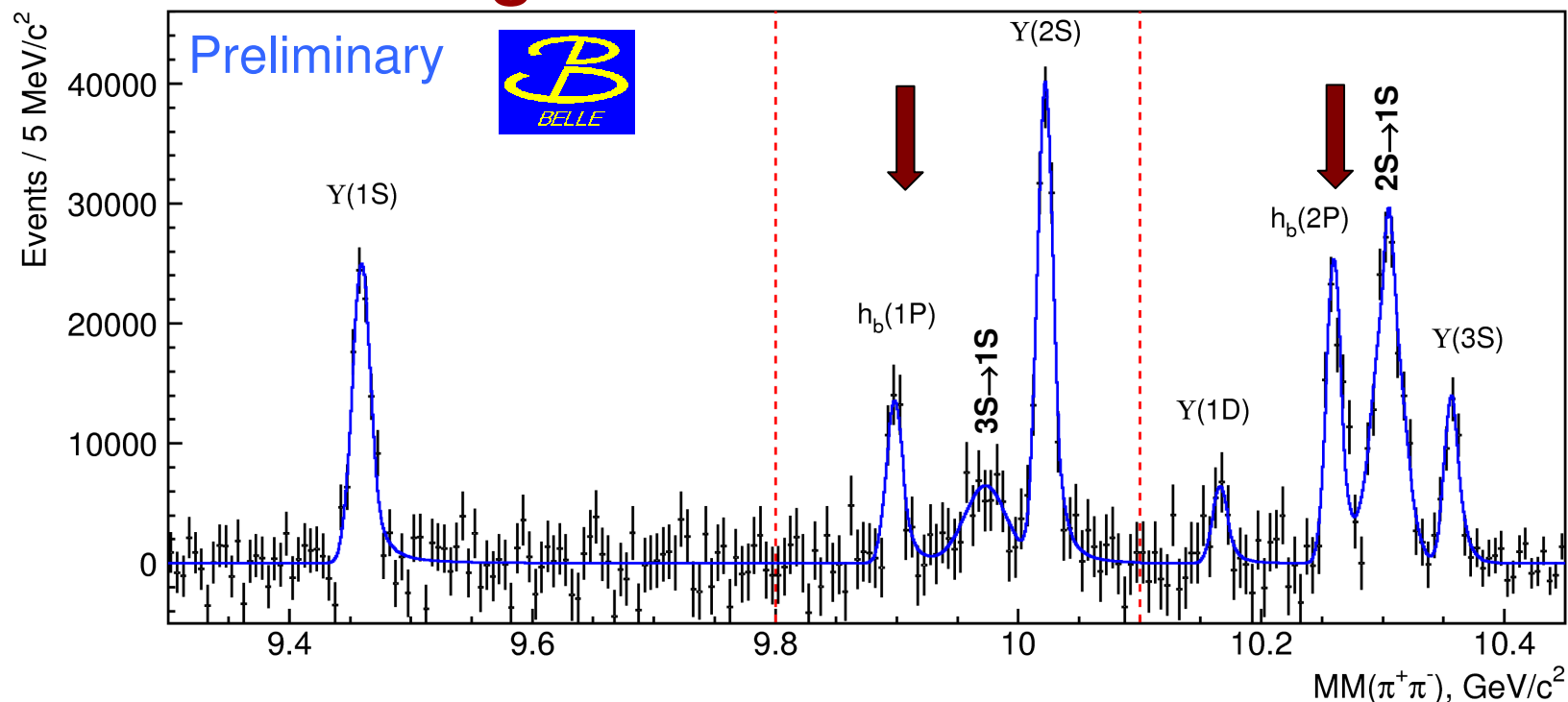
“Results” – subtract polynomial from data points

K_S contribution: subtract bin-by-bin in region #3



Background Subtracted Results

121.4 fb⁻¹



	Yield, 10 ³	Mass, MeV/c ²	Signif.
$\Upsilon(1S)$	$105.2 \pm 5.8 \pm 3.0$	$9459.42 \pm 0.53 \pm 1.02$	18.2σ
$h_b(1P)$	$50.4 \pm 7.8^{+4.5}_{-9.1}$	$9898.25 \pm 1.06^{+1.03}_{-1.07}$	6.2σ
$3S \rightarrow 1S$	55 ± 19	9973.01	2.9σ
$\Upsilon(2S)$	$143.4 \pm 8.7 \pm 6.8$	$10022.25 \pm 0.41 \pm 1.01$	16.6σ
$\Upsilon(1D)$	22.1 ± 7.8	10166.2 ± 2.4	2.4σ
$h_b(2P)$	$84.4 \pm 6.8^{+23.}_{-10.}$	$10259.76 \pm 0.64^{+1.43}_{-1.03}$	12.4σ
$2S \rightarrow 1S$	$151.6 \pm 9.7^{+9.0}_{-20.}$	$10304.57 \pm 0.61 \pm 1.03$	15.7σ
$\Upsilon(3S)$	$44.9 \pm 5.1 \pm 5.1$	$10356.56 \pm 0.87 \pm 1.06$	8.5σ

arXiv:1103.3419

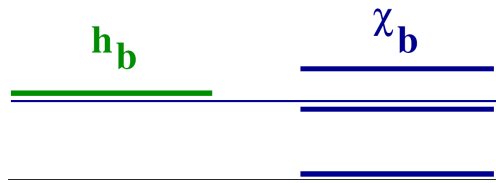
Significance
w/systematics

$h_b(1P)$ 5.5σ

$h_b(2P)$ 11.2σ

h_b results

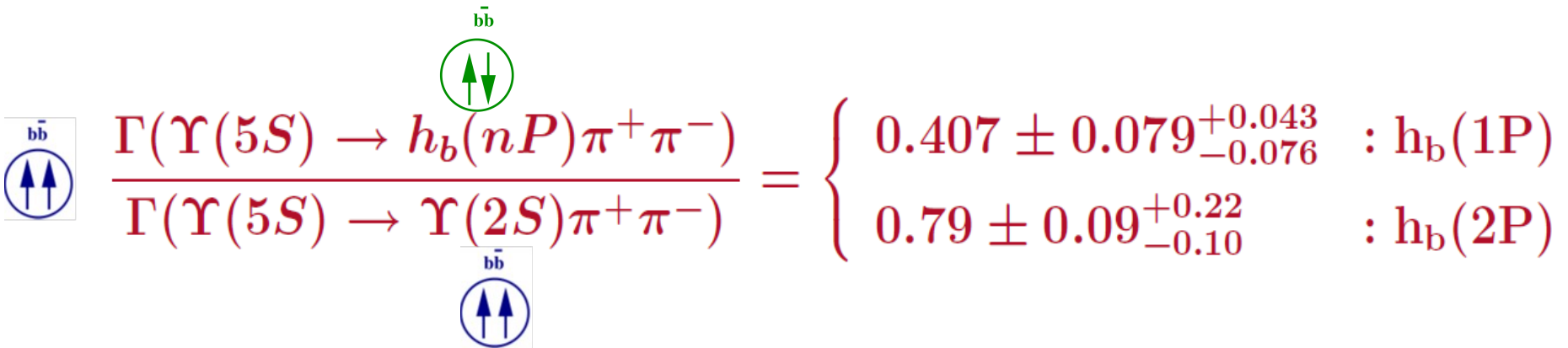
Deviations from CoG of χ_{bJ} masses consistent with zero.



$$\Delta M = 1.62 \pm 1.57 \text{ MeV}/c^2 : h_b(1P)$$

$$\Delta M = 0.48^{+1.57}_{-1.22} \text{ MeV}/c^2 : h_b(2P)$$

Ratio of production rates



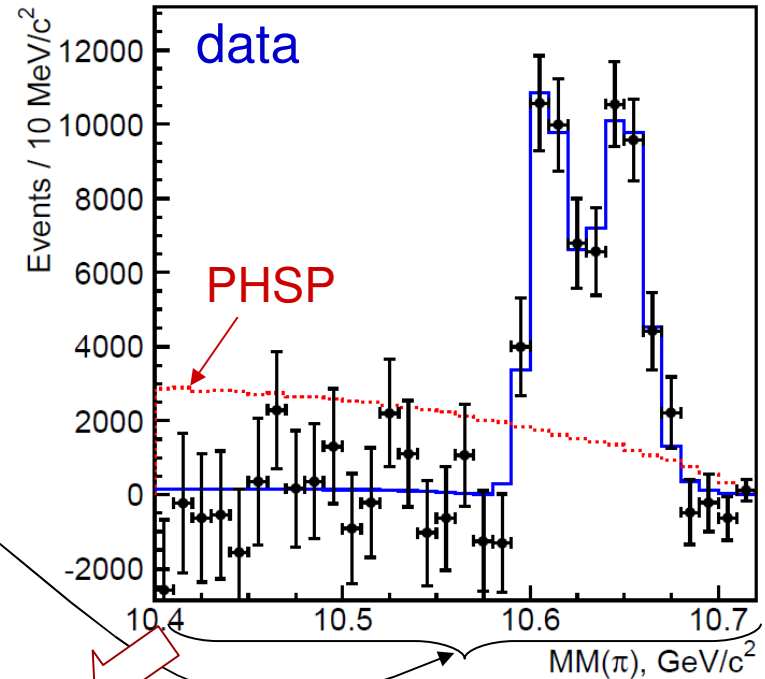
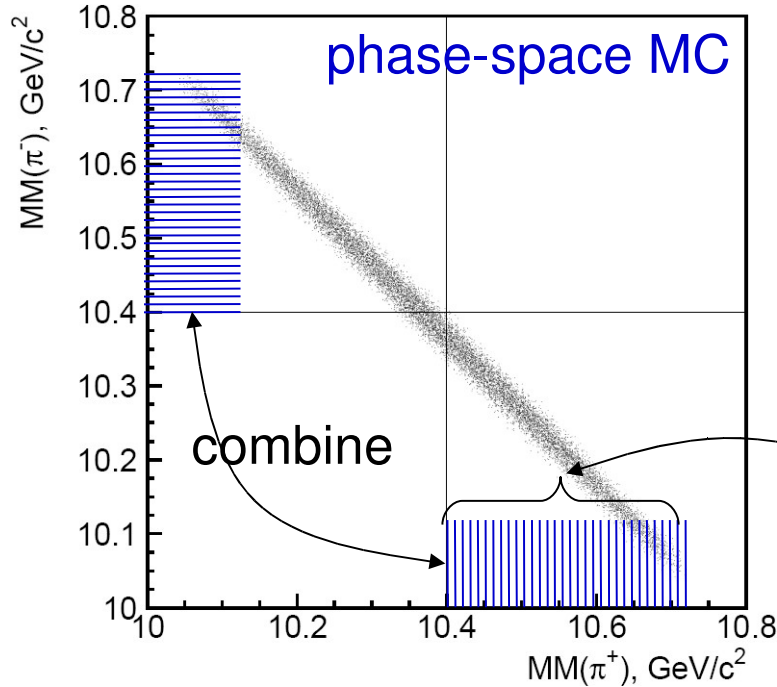
$$\frac{\Gamma(\Upsilon(5S) \rightarrow h_b(nP)\pi^+\pi^-)}{\Gamma(\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-)} = \begin{cases} 0.407 \pm 0.079^{+0.043}_{-0.076} & : h_b(1P) \\ 0.79 \pm 0.09^{+0.22}_{-0.10} & : h_b(2P) \end{cases}$$

Process with spin-flip is not suppressed
No h_b signal at $\Upsilon(4S)$

- Mechanism of $\Upsilon(5S) \rightarrow h_b(nP)\pi^+\pi^-$ decay is exotic!

Resonant substructure of $\Upsilon(5S) \rightarrow h_b(1P) \pi^+ \pi^-$

$P(h_b) = P_{\Upsilon(5S)} - P(\pi^+ \pi^-) \Rightarrow M(h_b \pi^+) = MM(\pi^-) \Rightarrow$ *measure $\Upsilon(5S) \rightarrow h_b \pi \pi$ yield in bins of $MM(\pi)$*



$$|BW(s, M_1, \Gamma_1) + ae^{i\phi} BW(s, M_1, \Gamma_1) + be^{i\psi}|^2 \frac{qP}{\sqrt{s}}$$

[preliminary]

$\sim \overline{B} B^*$ threshold

M (MeV/c²) Γ (MeV) a ϕ

$10605.1 \pm 2.2_{-1.0}^{+3.0}$	$11.4_{-3.9-1.2}^{+4.5+2.1}$	1	0
$10654.5 \pm 2.5_{-1.9}^{+1.0}$	$20.9_{-4.7-5.7}^{+5.4+2.1}$	$1.8_{-0.7-0.5}^{+1.0+0.1}$	188_{-58-9}^{+44+4}

$\sim B^* \overline{B}^*$ threshold

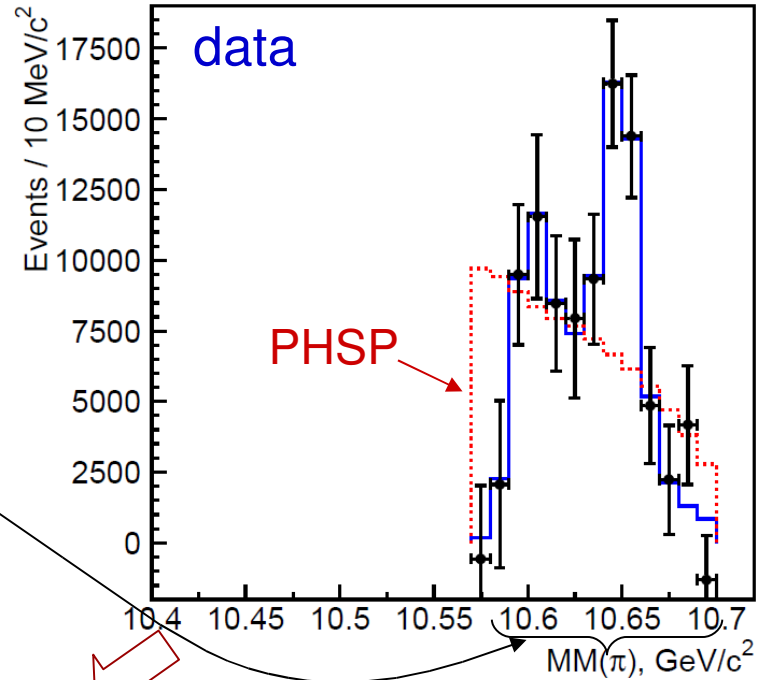
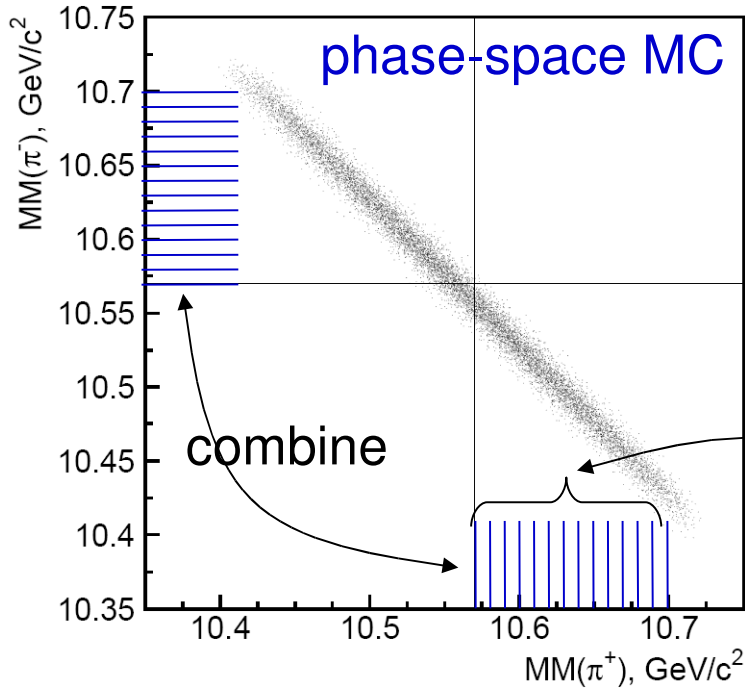
Significances

2 vs.1 : 7.4 σ (6.6 σ w/ syst)

2 vs.0 : 18 σ (16 σ w/ syst)

non-res. ~ 0

Resonant substructure of $\Upsilon(5S) \rightarrow h_b(2P) \pi^+ \pi^-$



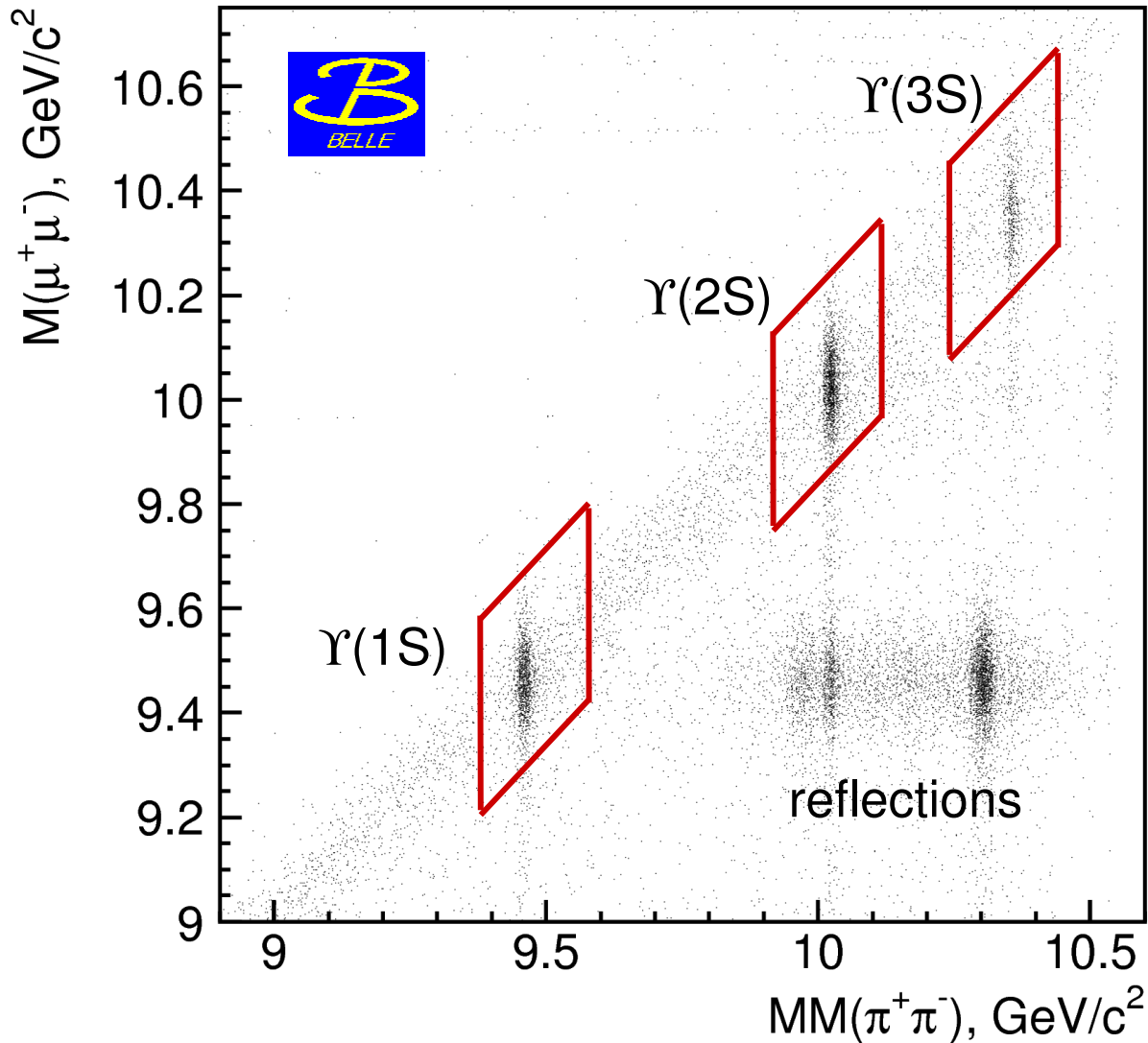
	$h_b(1P) \pi^+ \pi^-$	$h_b(2P) \pi^+ \pi^-$
M_1 (MeV/c ²)	$10605.1 \pm 2.2^{+3.0}_{-1.0}$	$10596 \pm 7^{+5}_{-2}$
Γ_1 (MeV)	$11.4^{+4.5+2.1}_{-3.9-1.2}$	16^{+16+13}_{-10-4}
M_2 (MeV/c ²)	$10654.5 \pm 2.5^{+1.0}_{-1.9}$	$10651 \pm 4 \pm 2$
Γ_2 (MeV)	$20.9^{+5.4+2.1}_{-4.7-5.7}$	12^{+11+8}_{-9-2}
a	$1.8^{+1.0+0.1}_{-0.7-0.5}$	$1.3^{+3.1+0.4}_{-1.1-0.7}$
ϕ (degree)	188^{+44+4}_{-58-9}	$255^{+56+12}_{-72-183}$
non - res	~ 0	~ 0

[preliminary]
Significances
 2 vs.1 : 2.7σ (1.9σ w/ syst)
 2 vs.0 : 6.3σ (4.7σ w/ syst)

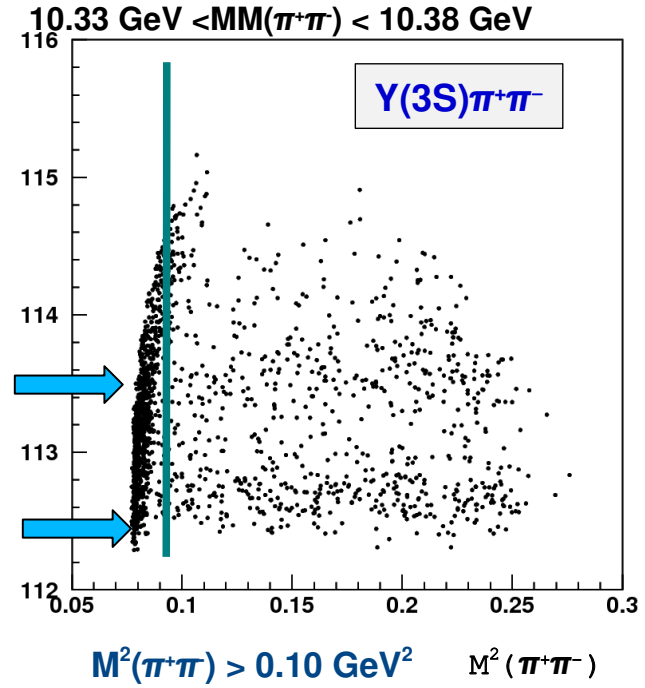
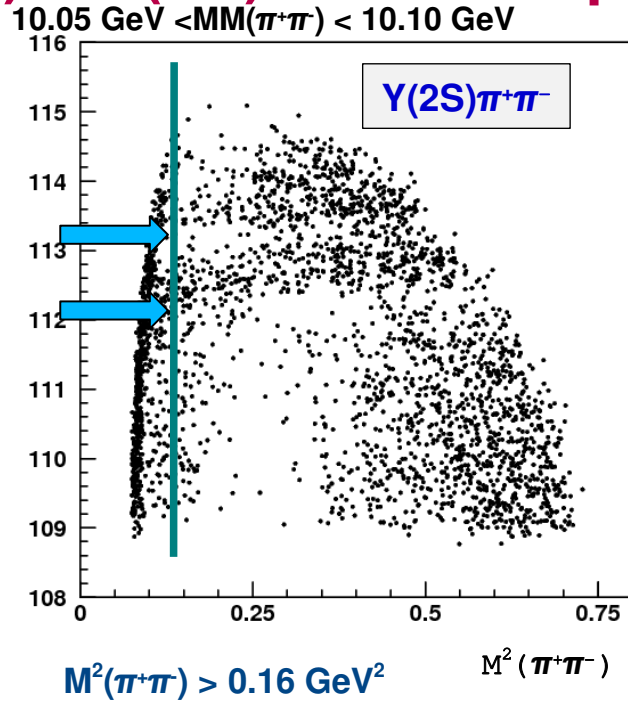
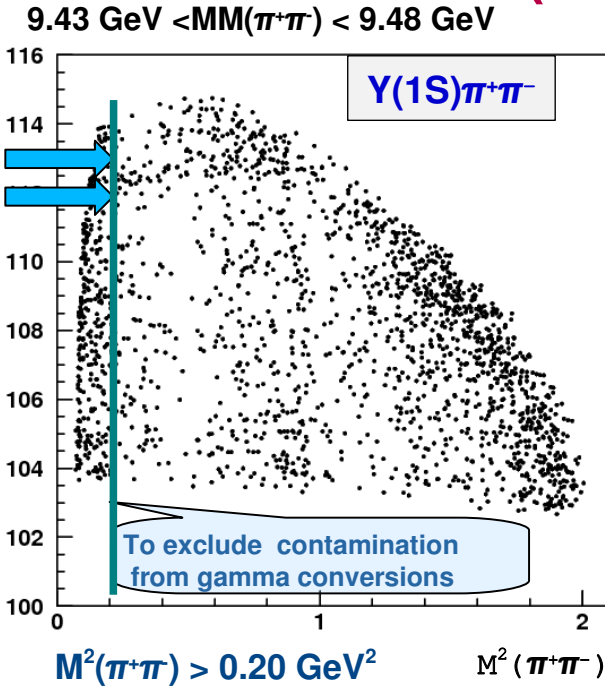
**Resonances parameters
 are consistent**

Exclusive $\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+\pi^-$

$$\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+\pi^- \quad (n = 1,2,3)$$
$$\Upsilon(nS) \rightarrow \mu^+\mu^-$$



$\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+\pi^-$ Dalitz plots



$$s_i \equiv M_{\pi_i \Upsilon}^2$$

Unbinned fit of DP with signal function:

Flatte $m=950 \text{ MeV}/c^2$

D-wave Breit-Wigner

$$S(s_1, s_2) = |A_{Z_{b1}} + A_{Z_{b2}} + A_{NR} + A_{f_0(980)} + A_{f_2(1275)}|^2$$

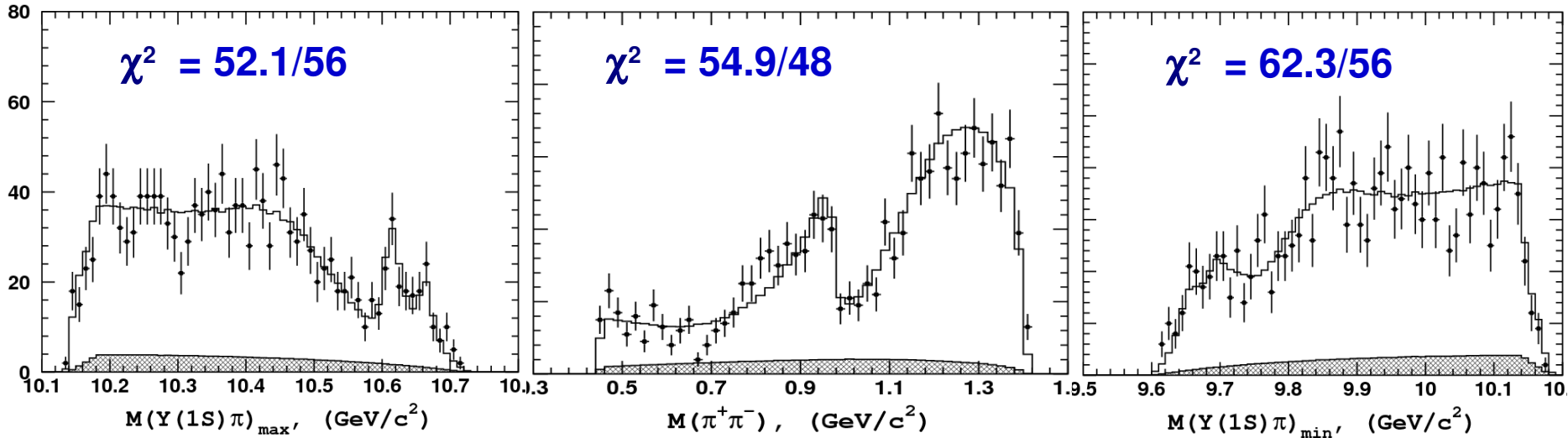
$$A_{Z_{bi}} = \frac{\sqrt{M_i \Gamma_i}}{M_i^2 - s_1 + iM_i \Gamma_i} + \frac{a_i e^{i\phi_i} \sqrt{M_i \Gamma_i}}{M_i^2 - s_2 + iM_i \Gamma_i}$$

$$A_{NR} = c_1 + c_2 m_{\pi\pi}^2$$

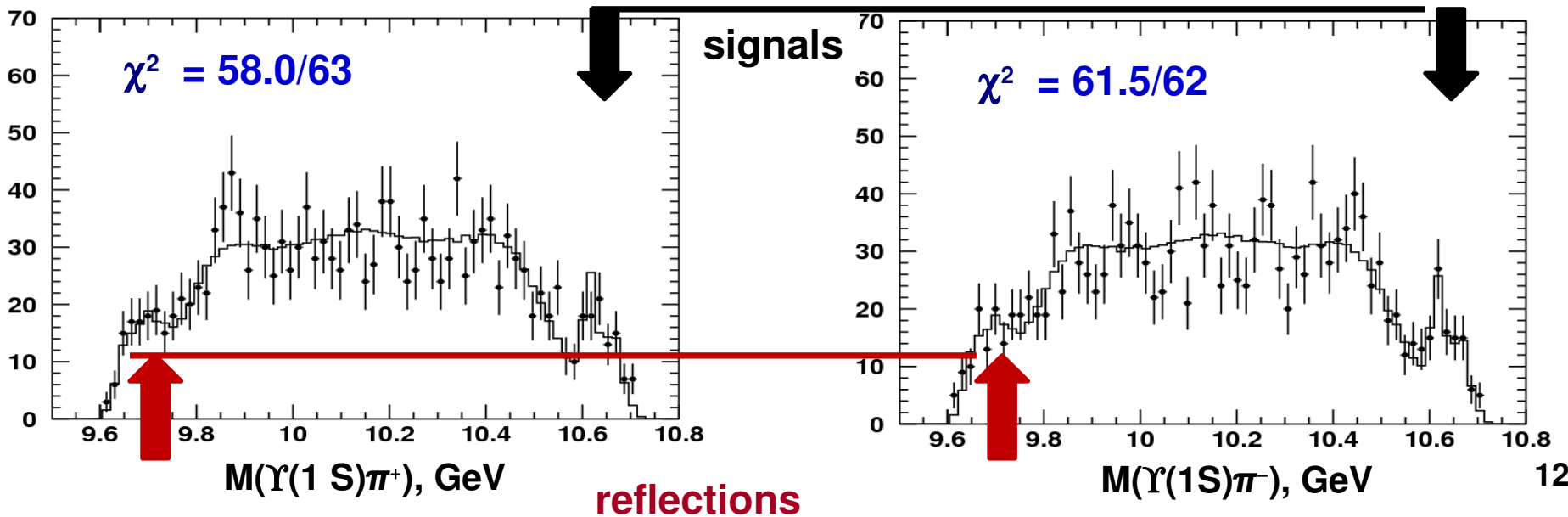
[1] M.B. Voloshin, Prog. Part. Nucl. Phys. 61:455, 2008.

[2] M.B. Voloshin, Phys. Rev. D74:054022, 2006.

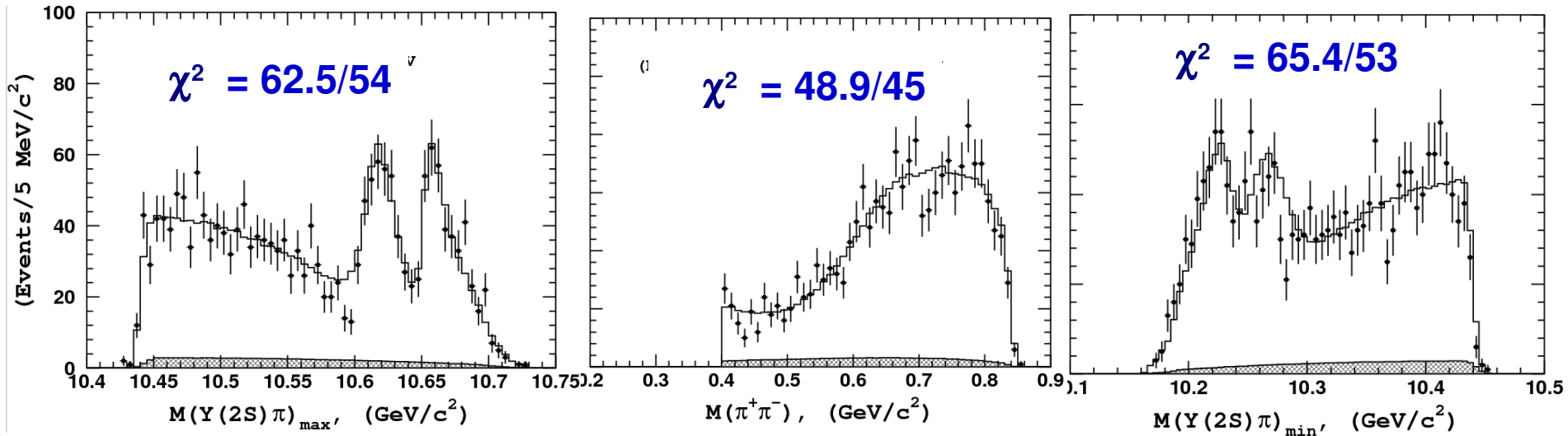
Results: $\Upsilon(1S)\pi^+\pi^-$



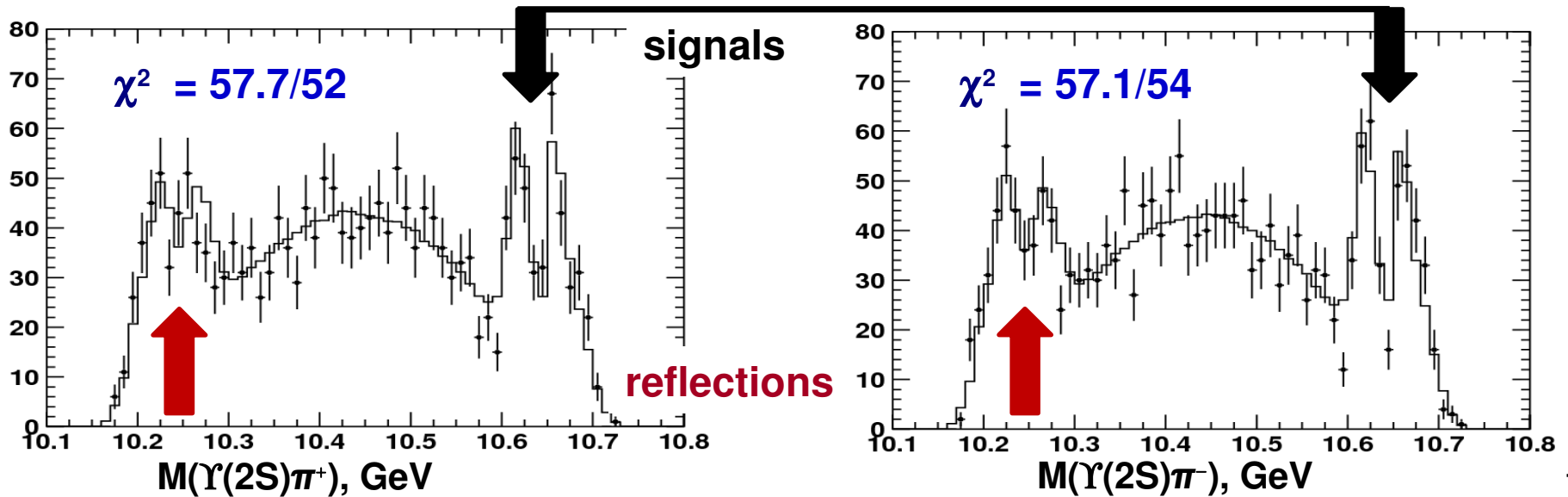
$M(\Upsilon(1S)\pi^+)$ and $M(\Upsilon(1S)\pi^-)$ projections:



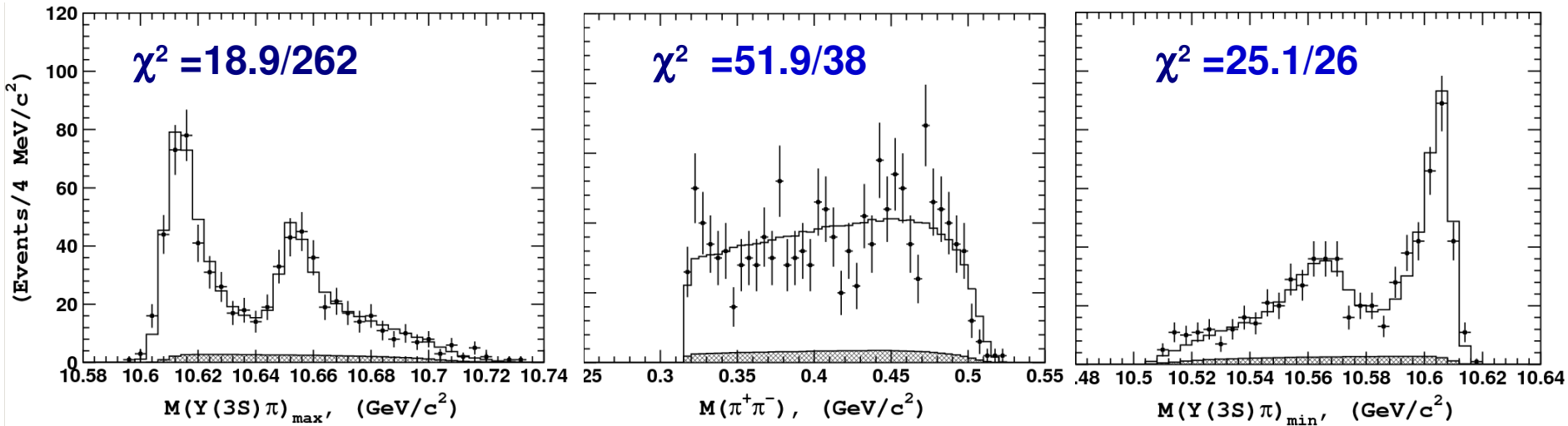
Results: $\Upsilon(2S)\pi^+\pi^-$



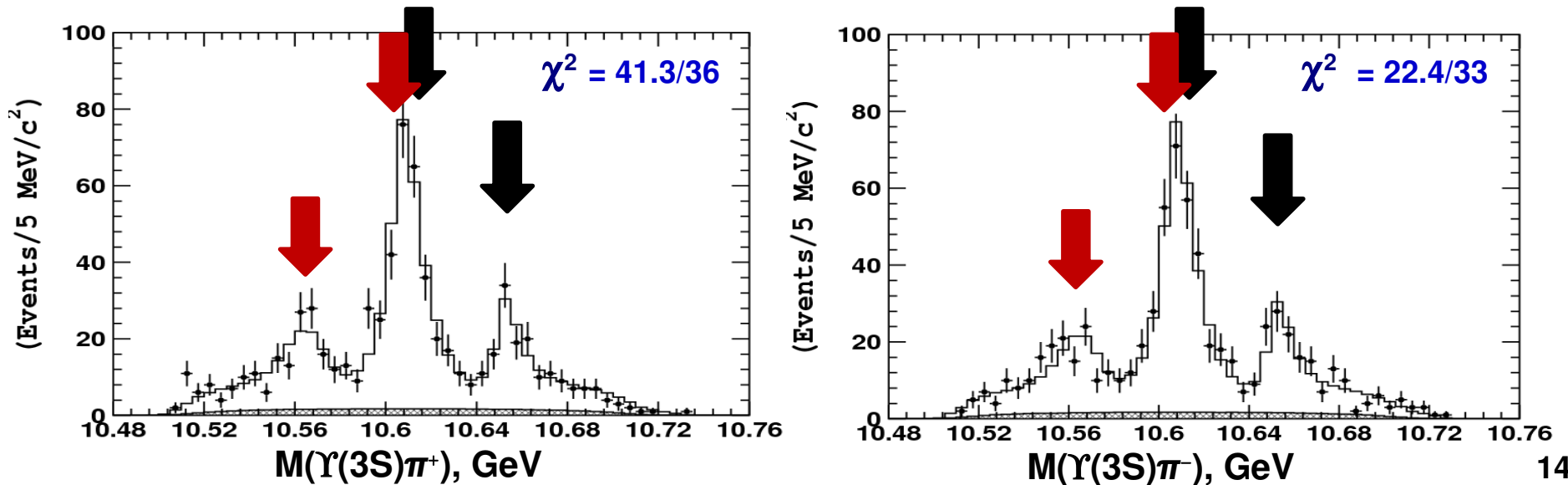
$M(\Upsilon(2S)\pi^+)$ and $M(\Upsilon(2S)\pi^-)$ projections:



Results: $\Upsilon(3S)\pi^+\pi^-$



$M(\Upsilon(3S)\pi^+)$ and $M(\Upsilon(3S)\pi^-)$ projections:



Fit results



[preliminary]

Final state	$\Upsilon(1S)\pi^+\pi^-$	$\Upsilon(2S)\pi^+\pi^-$	$\Upsilon(3S)\pi^+\pi^-$	$h_b(1P)\pi^+\pi^-$	$h_b(2P)\pi^+\pi^-$
$M(Z_b(10610)), \text{ MeV}/c^2$	$10609 \pm 3 \pm 2$	$10616 \pm 2_{-4}^{+3}$	$10608 \pm 2_{-2}^{+5}$	$10605.1 \pm 2.2_{-1.0}^{+3.0}$	$10596 \pm 7_{-2}^{+5}$
$\Gamma(Z_b(10610)), \text{ MeV}$	$22.9 \pm 7.3 \pm 2$	$21.1 \pm 4_{-3}^{+2}$	$12.2 \pm 1.7 \pm 4$	$11.4_{-3.9}^{+4.5} {}_{-1.2}^{+2.1}$	$16_{-10}^{+16} {}_{-4}^{+13}$
$M(Z_b(10650)), \text{ MeV}/c^2$	$10660 \pm 6 \pm 2$	$10653 \pm 2 \pm 2$	$10652 \pm 2 \pm 2$	$10654.5 \pm 2.5_{-1.9}^{+1.0}$	$10651 \pm 4 \pm 2$
$\Gamma(Z_b(10650)), \text{ MeV}$	$12 \pm 10 \pm 3$	$16.4 \pm 3.6_{-6}^{+4}$	$10.9 \pm 2.6_{-2}^{+4}$	$20.9_{-4.7}^{+5.4} {}_{-5.7}^{+2.1}$	$12_{-9}^{+11} {}_{-2}^{+8}$
Rel. amplitude	$0.59 \pm 0.19_{-0.03}^{+0.09}$	$0.91 \pm 0.11_{-0.03}^{+0.04}$	$0.73 \pm 0.10_{-0.05}^{+0.15}$	$1.8_{-0.7}^{+1.0} {}_{-0.5}^{+0.1}$	$1.3_{-1.1}^{+3.1} {}_{-0.7}^{+0.4}$
Rel. phase, degrees	$53 \pm 61_{-50}^{+5}$	$-20 \pm 18_{-9}^{+14}$	$6 \pm 24_{-59}^{+23}$	$188_{-58}^{+44} {}_{-9}^{+4}$	$255_{-72}^{+56} {}_{-183}^{+12}$

Masses, widths, relative amplitudes are consistent

Relative phases are swapped for Υ and h_b final states \Leftarrow expectation from a 'molecular' model

$Z_b(10610)$
 $M=10608.4 \pm 2.0 \text{ MeV}$
 $\Gamma=15.6 \pm 2.5 \text{ MeV}$

$Z_b(10650)$
 $M=10653.2 \pm 1.5 \text{ MeV}$
 $\Gamma=14.4 \pm 3.2 \text{ MeV}$

Summary of parameters of charged Z_b states

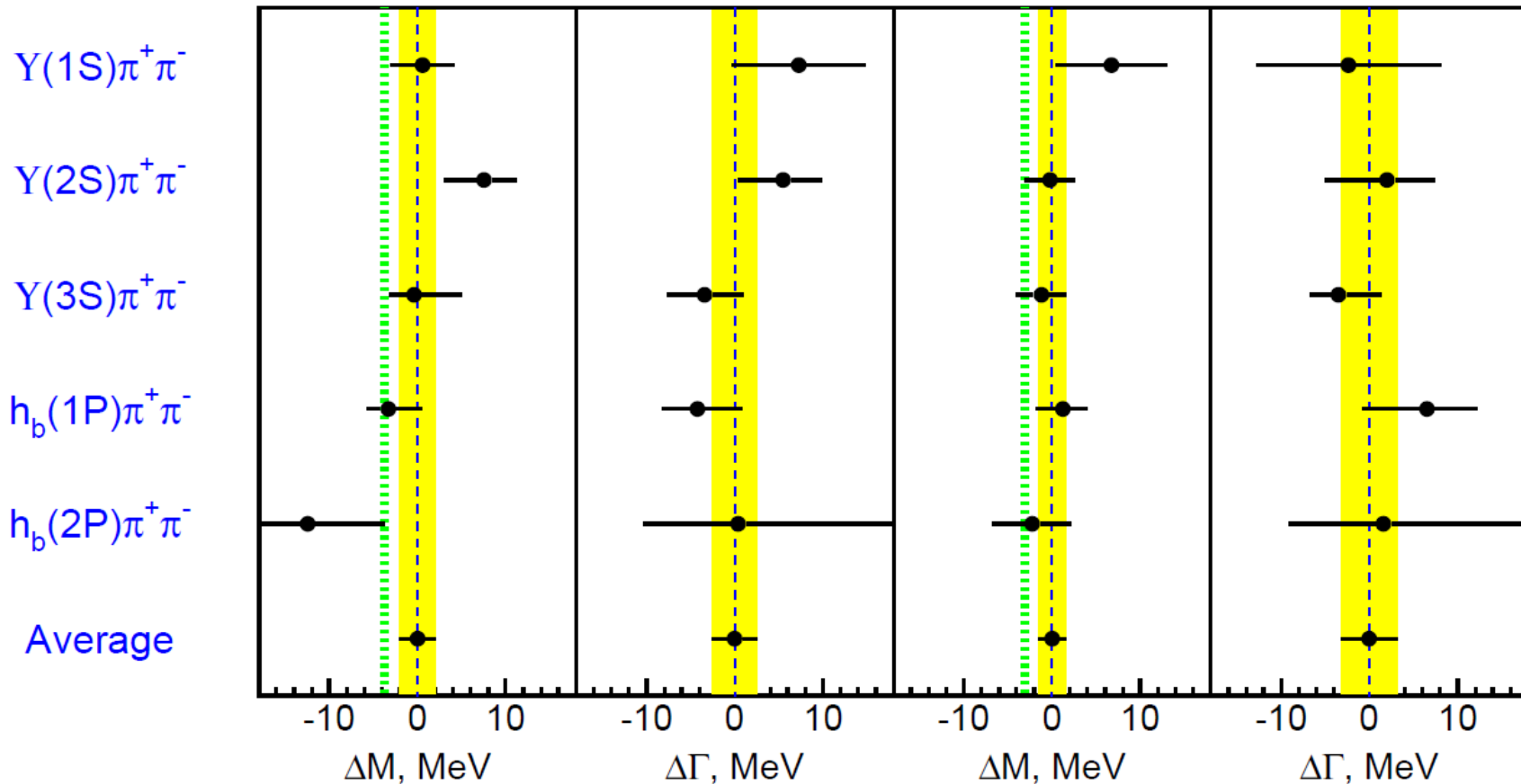


$\sim \overline{B}B^*$ threshold

$Z_b(10610)$

$\sim \overline{B^*}B^*$ threshold

$Z_b(10650)$ [preliminary]



$Z_b(10610)$

$M=10608.4 \pm 2.0$ MeV

$\Gamma=15.6 \pm 2.5$ MeV

$Z_b(10650)$

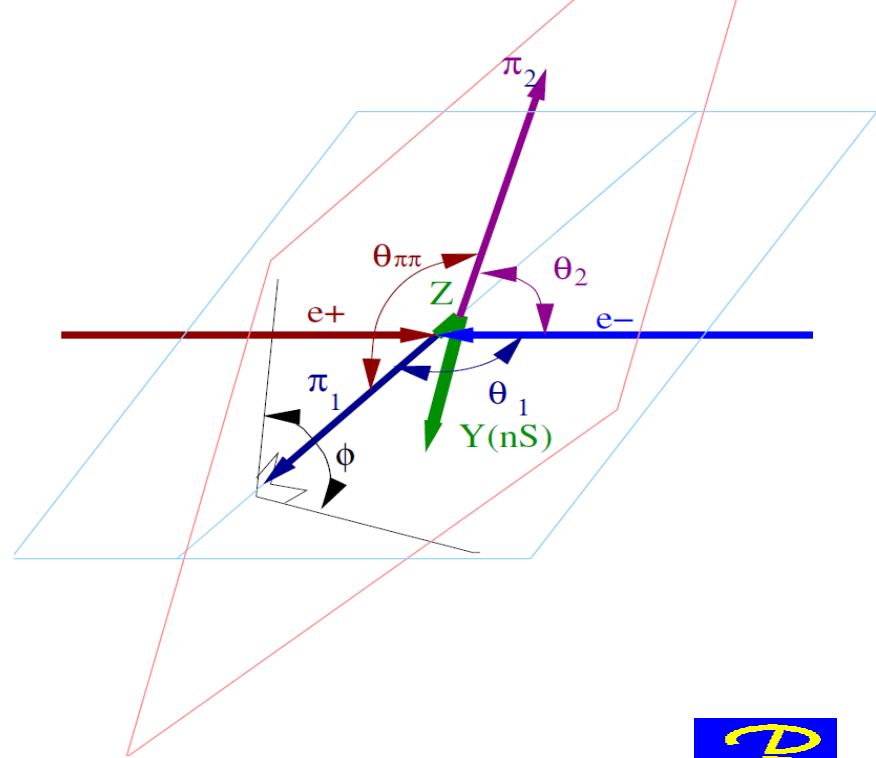
$M=10653.2 \pm 1.5$ MeV

$\Gamma=14.4 \pm 3.2$ MeV

Angular analysis

$$\Theta_i = \angle(\pi_i, e^+), \quad \theta_{\pi\pi} = \angle(\pi_1, \pi_2),$$

$$\phi = \angle[\text{plane}(\pi_1, e^+), \text{plane}(\pi_1, \pi_2)]$$



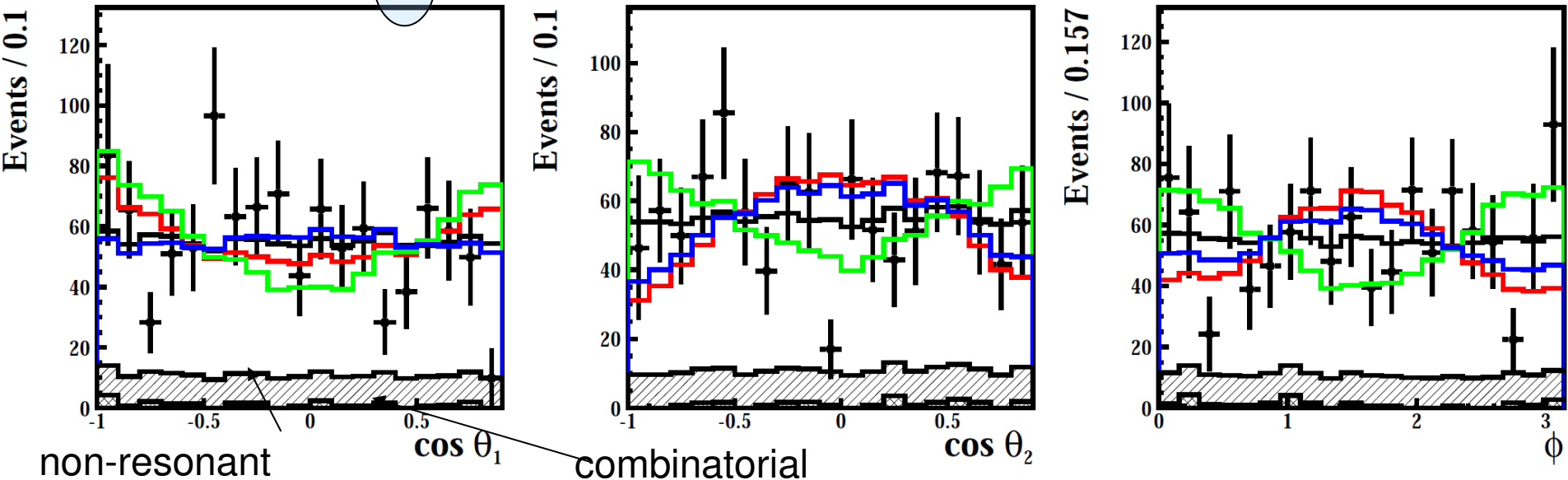
Cos $\theta_{\pi\pi}$ degraded by interference

Best discrimination:

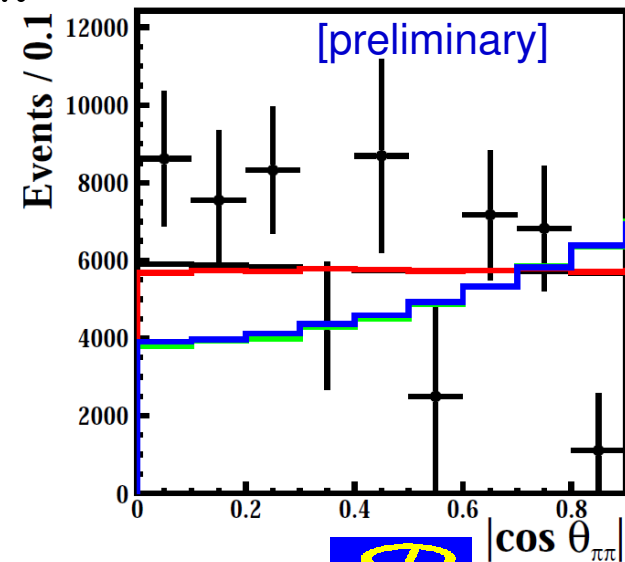
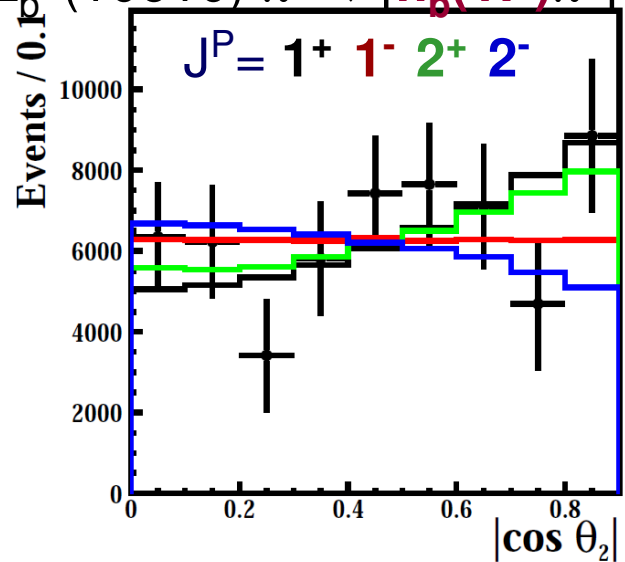
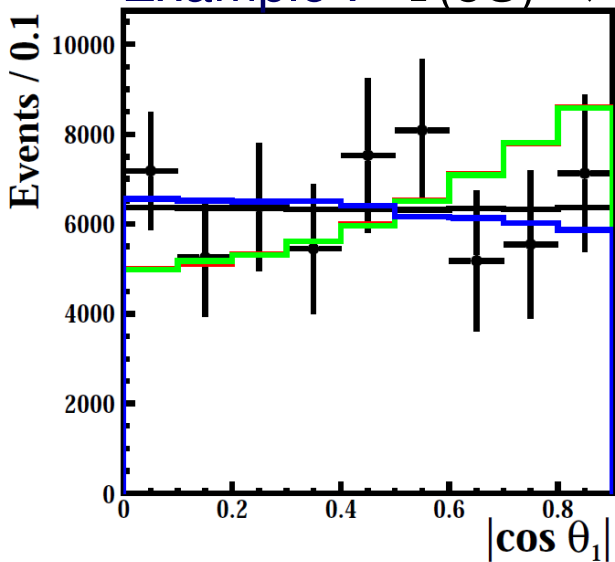
cos θ_2 for **1⁻** and **2⁻** ;

cos θ_1 for **2⁺**

Color coding: $J^P =$ **1⁺** **1⁻** **2⁺** **2⁻** (0^\pm is forbidden by parity conservation)



Example : $\Upsilon(5S) \rightarrow Z_b^+(10610) \pi^- \rightarrow [h_b(1P)\pi^+] \pi^-$



Best discrimination: $\cos\theta_2$ for 1^- ; $\cos\theta_{\pi\pi}$ for 2^+ and 2^-



Confidence Levels of angular fits to $\Upsilon(5S) \rightarrow Z_b^+ \pi^- \rightarrow [h_b(1P)\pi^+] \pi^-$ decay with hypothesis 1^+

	$\cos\theta_1$	$\cos\theta_2$	$\cos\theta_{\pi\pi}$
$Z_b(10610)$	84%	37%	1.1%
$Z_b(10650)$	15%	63%	7.2%

Probabilities at which different J^P hypotheses are disfavored compared to 1^+

J^P	$Z_b(10610)$			$Z_b(10650)$		
	$\Upsilon(2S)\pi^+\pi^-$	$\Upsilon(3S)\pi^+\pi^-$	$h_b(1P)\pi^+\pi^-$	$\Upsilon(2S)\pi^+\pi^-$	$\Upsilon(3S)\pi^+\pi^-$	$h_b(1P)\pi^+\pi^-$
1^-	3.6σ	0.3σ	0.3σ	3.7σ	2.6σ	2.7σ
2^+	4.3σ	3.5σ	4.3σ	4.4σ	2.7σ	2.1σ
2^-	2.7σ	2.8σ		2.9σ	2.6σ	

1+ assignment is favorable.

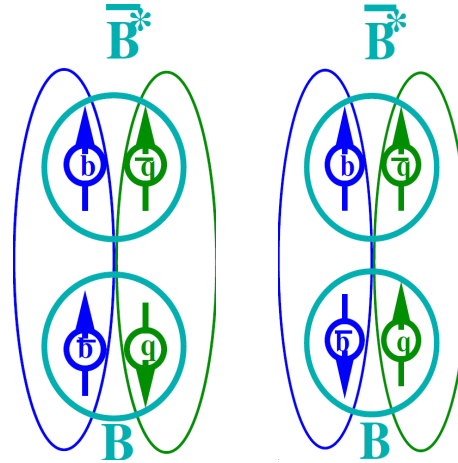
1-, 2+, 2- are disfavored at typically 3σ level.

Possible nature of Z_b 's

B^*B and B^*B^* S-wave molecules

$$|Z_b'\rangle = \frac{1}{\sqrt{2}} 0_{bb}^- \otimes 1_{Qq}^- - \frac{1}{\sqrt{2}} 1_{bb}^- \otimes 0_{Qq}^-$$

$$|Z_b\rangle = \frac{1}{\sqrt{2}} 0_{bb}^- \otimes 1_{Qq}^- + \frac{1}{\sqrt{2}} 1_{bb}^- \otimes 0_{Qq}^-$$



Masses of Z_b are close to $B^*B(*)$ thresholds

- Quantum number $J^P=1^+$
- Amplitude ratio $A[Z_b(10610)] / A[Z_b(10650)] \sim 1$
- Relative phase ~ 0 for Υ and $\sim 180^\circ$ for h_b .
- Explains why $h_b\pi\pi$ is unsuppressed relative to $\Upsilon\pi\pi$.
- **Additional measurements in B^*B and B^*B^* mode should be done**
- **Existence of other molecular states is predicted**

Summary



arXiv:1103.3419

-First observation of $h_b(1P)$ and $h_b(2P)$ in $\Upsilon(5S) \rightarrow \pi^+\pi^- h_b$

Masses consistent with CoG of χ_{bJ} states

-First observation of two charged bottomonium-like resonances in 5 different final states:

$h_b(1P)\pi^+\pi^-$, $h_b(2P)\pi^+\pi^-$, $\Upsilon(1S)\pi^+\pi^-$, $\Upsilon(2S)\pi^+\pi^-$, $\Upsilon(3S)\pi^+\pi^-$

[preliminary]

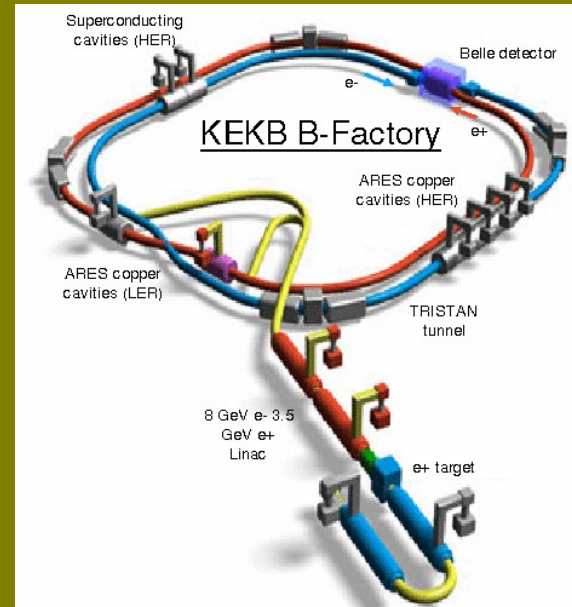
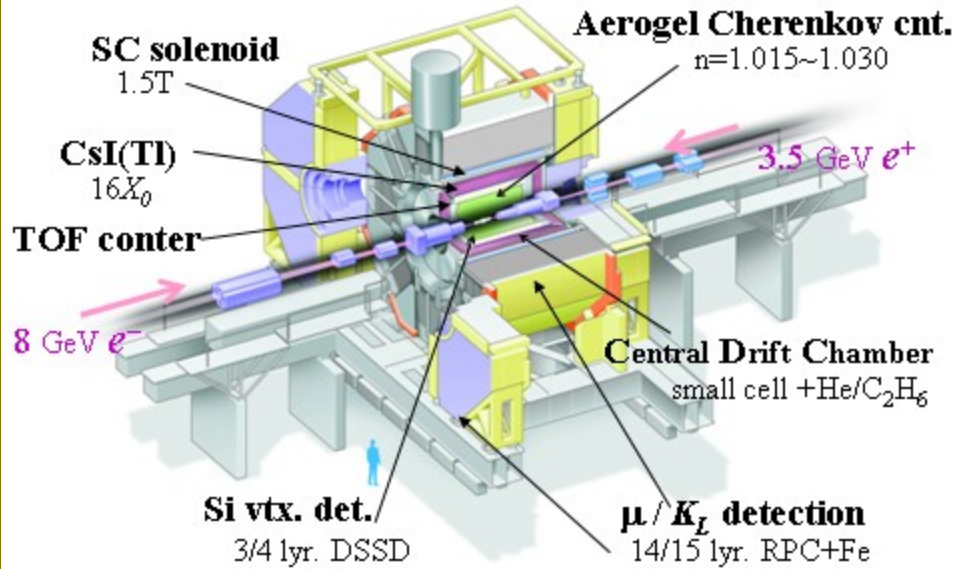
$Z_b(10610)$ $M = 10608.1 \pm 1.7 \text{ MeV}$
 $\Gamma = 15.5 \pm 2.4 \text{ MeV}$

$Z_b(10650)$ $M = 10653.3 \pm 1.5 \text{ MeV}$
 $\Gamma = 14.0 \pm 2.8 \text{ MeV}$

-Angular analysis favors $J^P=1^+$; other J^P are disfavored.

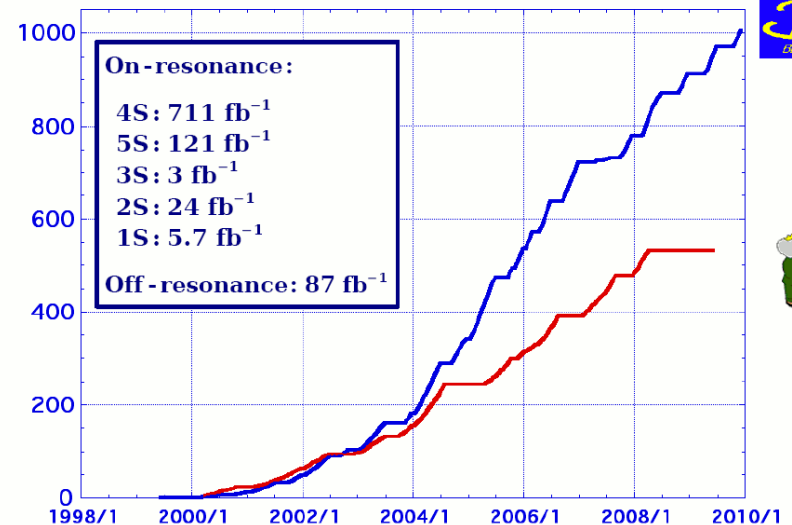
- Z_b properties are consistent with the B^*B and B^*B^* S-wave molecules .

Belle Detector

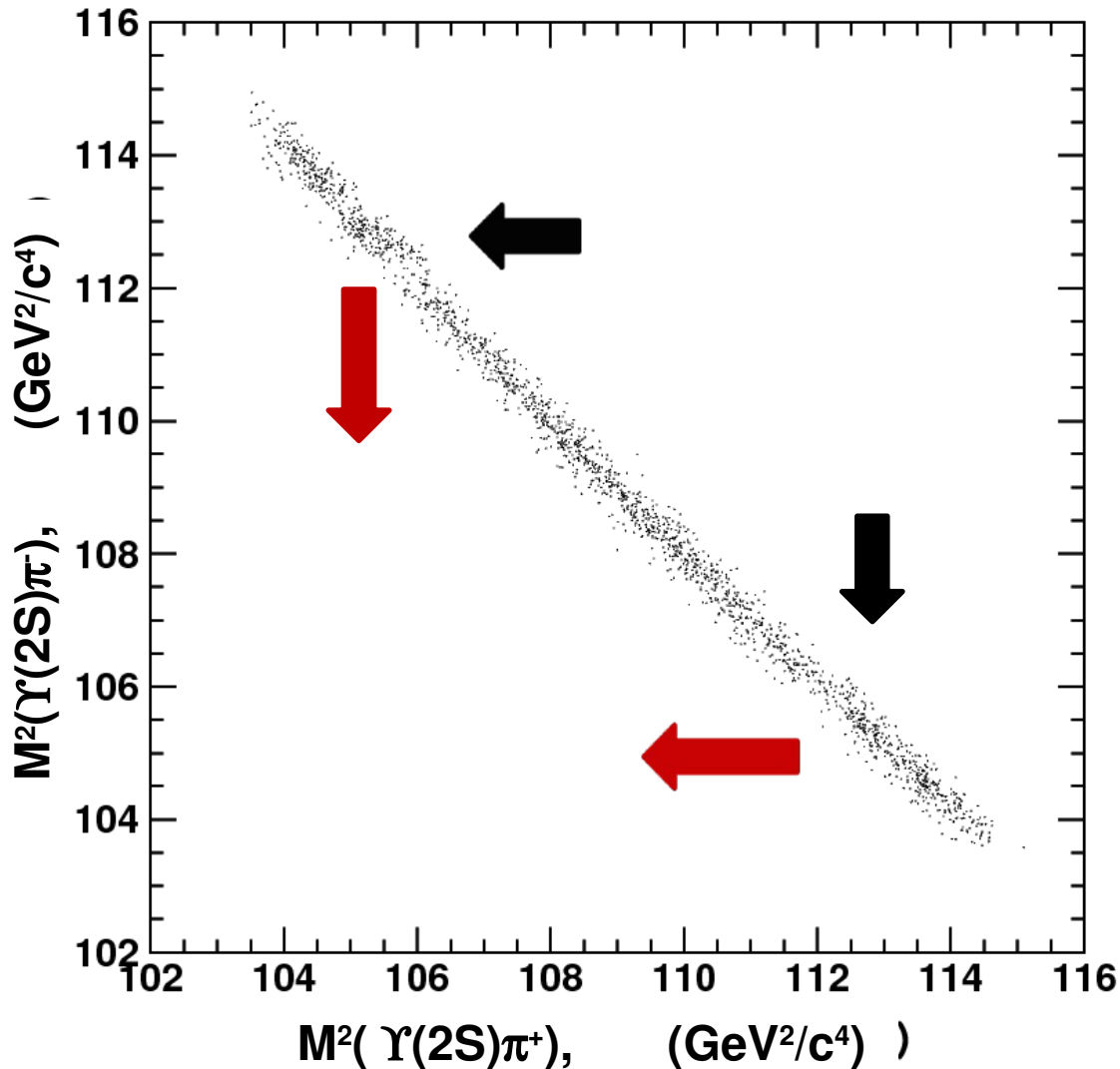


- $3.5\text{ GeV } e^+ \times 8.0\text{ GeV } e^-$.
- $\mathcal{L}_{\text{max}} = 2.1 \times 10^{34}\text{ cm}^{-2}\text{ s}^{-1}$
- Continuous injection
→ $1.1\text{ fb}^{-1}/\text{day}$.
- $\int \mathcal{L} dt \approx 1\text{ ab}^{-1}$

Integrated Luminosity



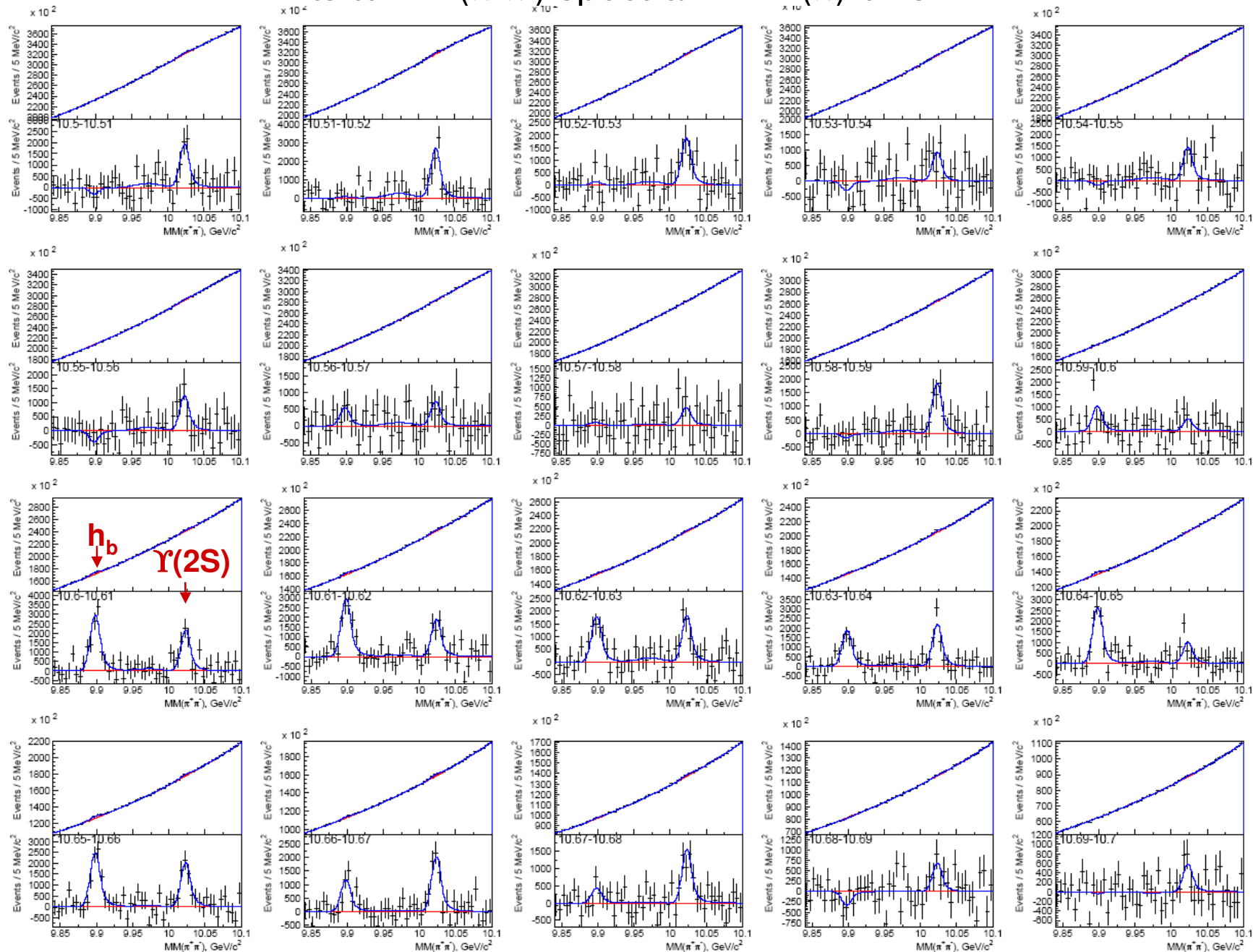
Dalitz Plot



If there is a signal in the $\Upsilon \pi$ system

It will also produce a signal like reflection on the other axis

Fits to MM($\pi^+\pi^-$) spectra in MM(π) bins

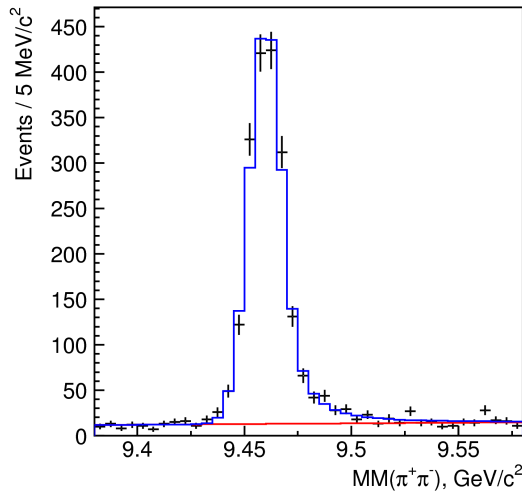


Calibration channels

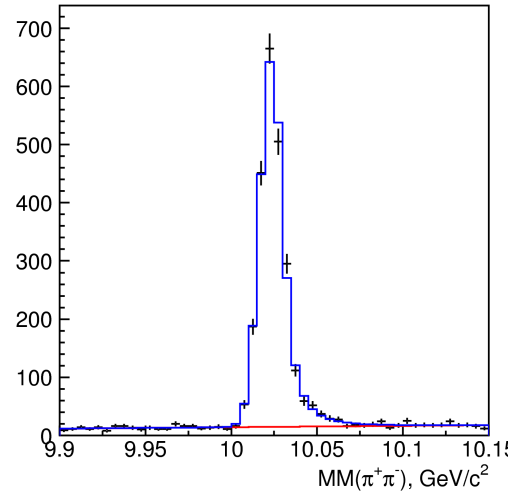
$$\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+ \pi^- \quad (n = 1, 2, 3)$$

$$\Upsilon(nS) \rightarrow \mu^+ \mu^-$$

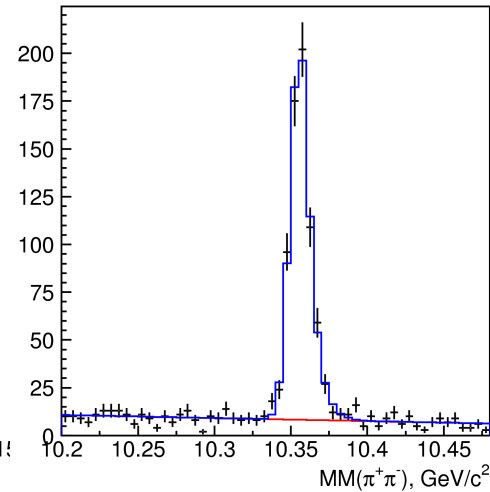
$\Upsilon(5S) \rightarrow \Upsilon(1S) \pi\pi$



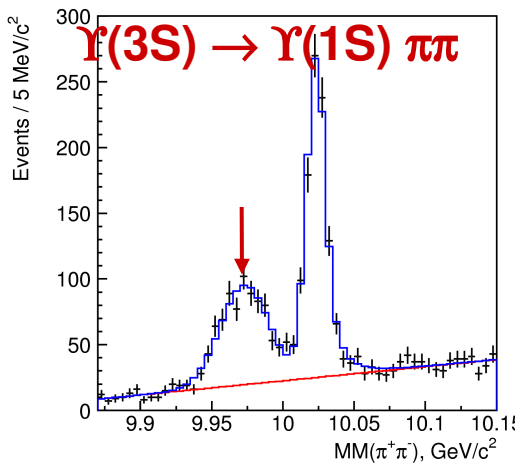
$\Upsilon(5S) \rightarrow \Upsilon(2S) \pi\pi$



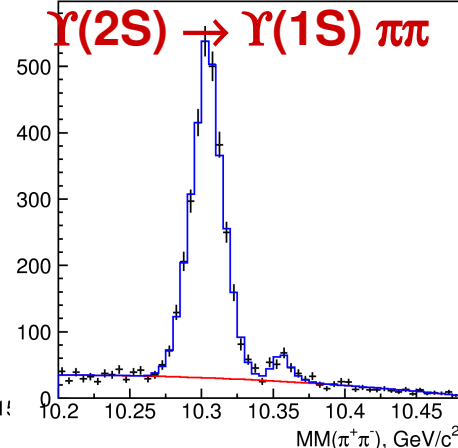
$\Upsilon(5S) \rightarrow \Upsilon(3S) \pi\pi$



$\Upsilon(3S) \rightarrow \Upsilon(1S) \pi\pi$



$\Upsilon(2S) \rightarrow \Upsilon(1S) \pi\pi$



⇒ Shapes of signals

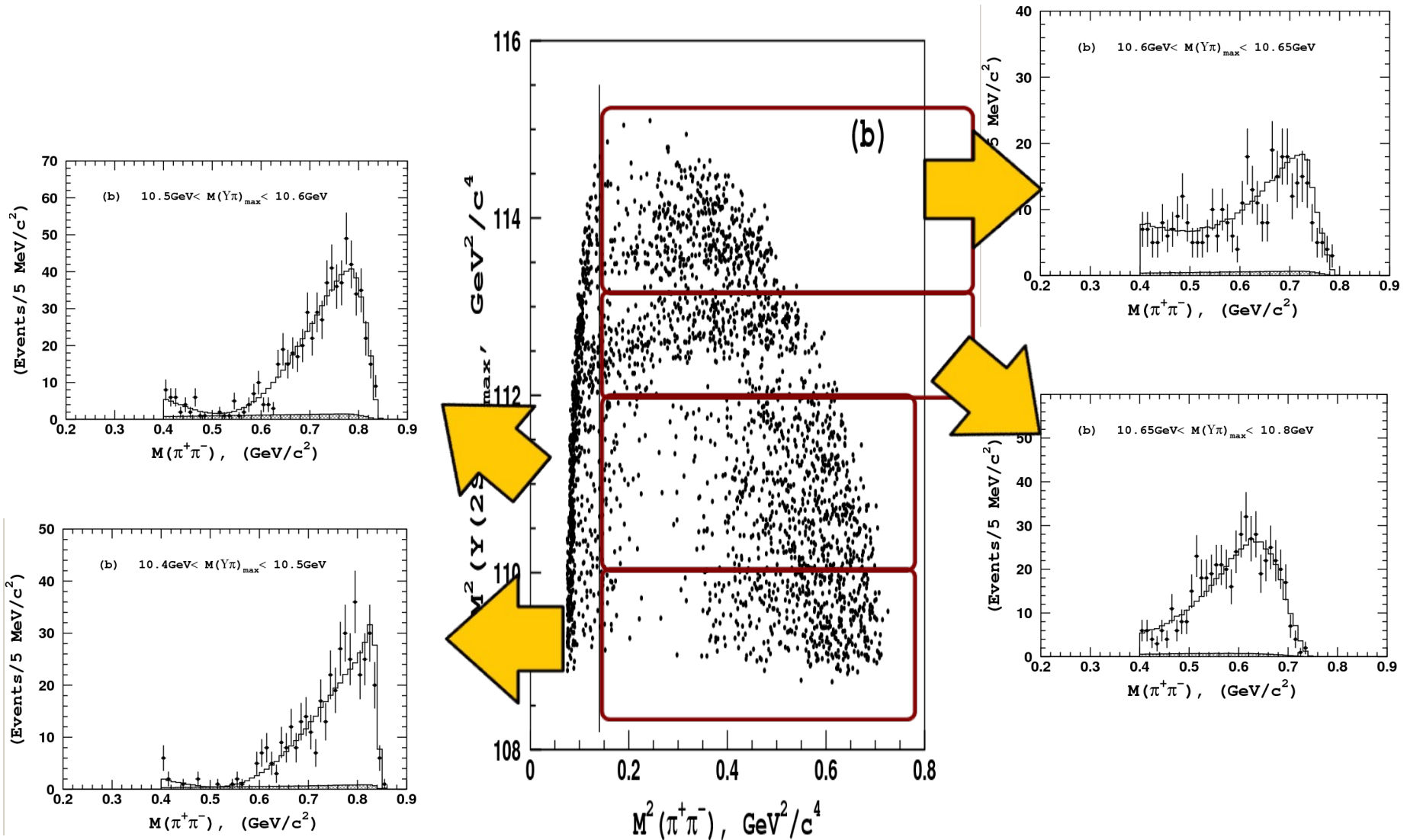
CrystalBall function

tail (8%) – ISR of soft γ

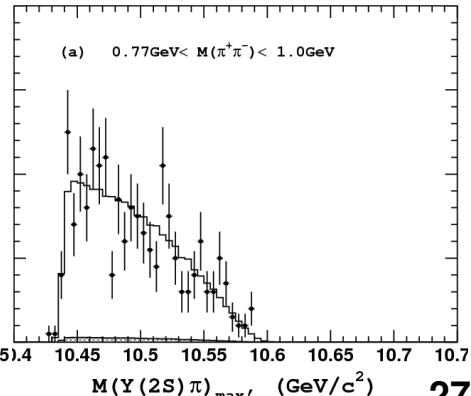
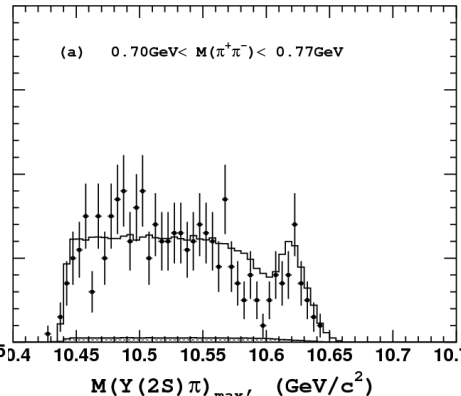
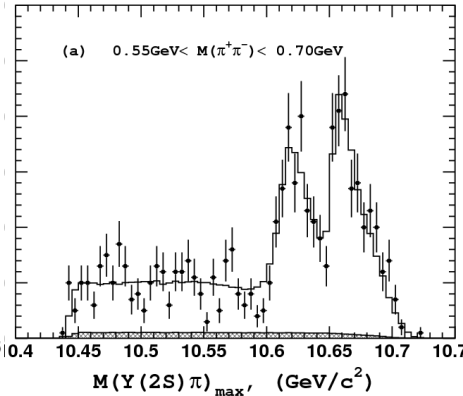
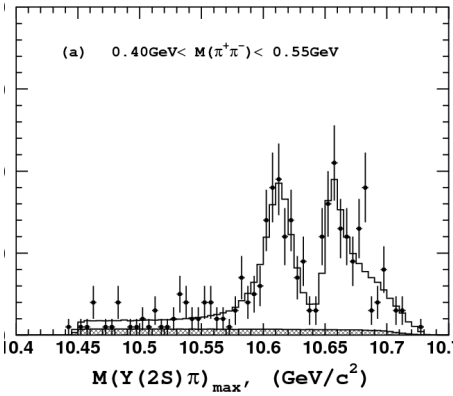
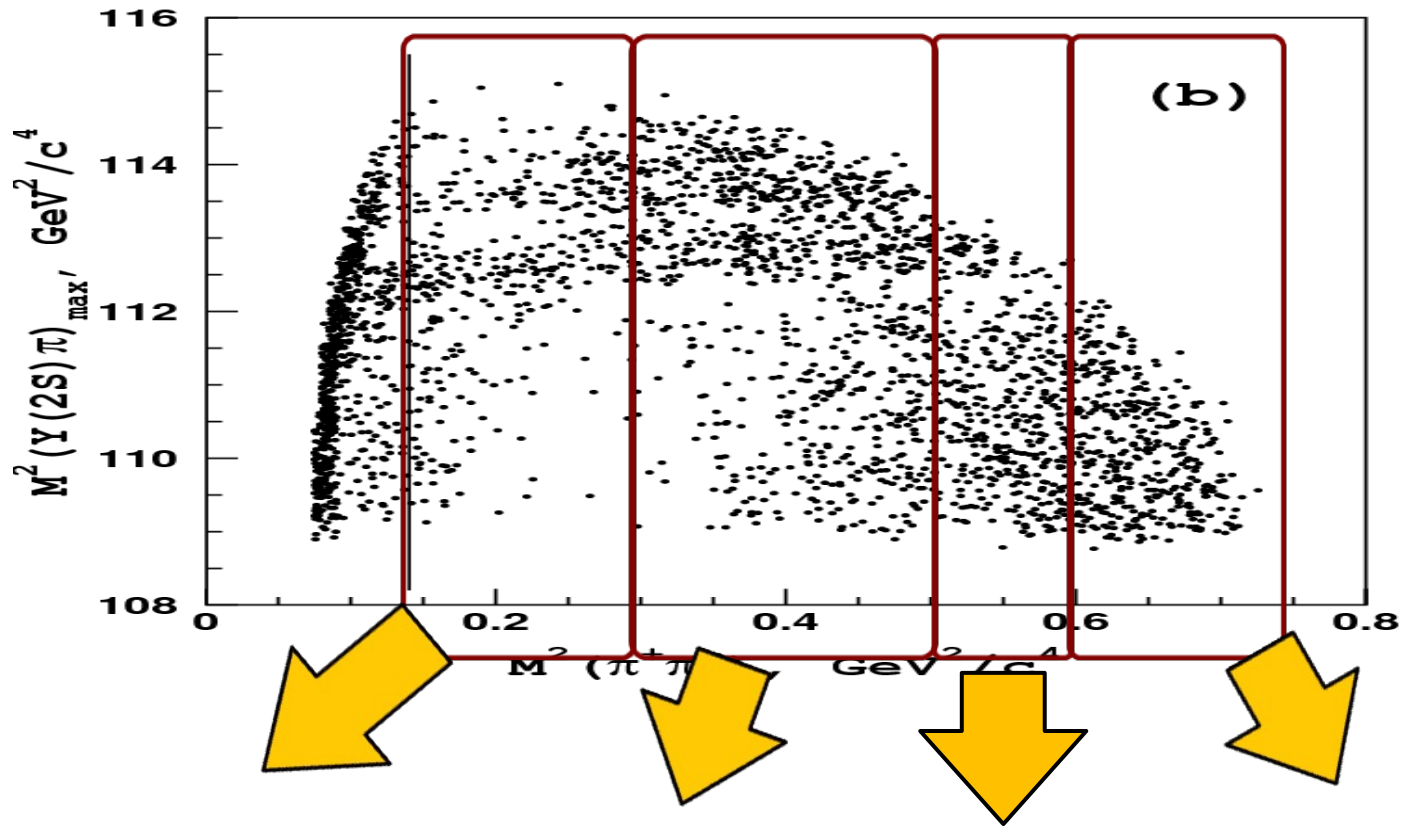
$\sigma = 5.7 - 7.5 \text{ MeV}$

⇒ Shapes of reflections

Results: $\Upsilon(2S)\pi^+\pi^-$



Results: $\Upsilon(2S)\pi^+\pi^-$



Expectations $\Upsilon(5S) \rightarrow Z_b \pi_1 \rightarrow [\Upsilon(2S) \pi_2] \pi_1$

1+ isotropic λ – beam direction

1- $\overline{|M_{tot}|^2} \propto p_1^2[p_2^2 - (\lambda p_2)^2] + 2(\mathbf{p}_1 \mathbf{p}_2)(\lambda p_1)(\lambda p_2)$

2+ $\overline{|M_{tot}|^2} \propto (\lambda[\mathbf{p}_1 \times \mathbf{p}_2])^2[2(\mathbf{p}_1 \mathbf{p}_2)^2 - \frac{1}{2}p_1^2 p_2^2] + \frac{1}{2}(p_1^2)^2(p_2^2)^2$
 $+ (\mathbf{p}_1 \mathbf{p}_2)^2[2(\mathbf{p}_1 \mathbf{p}_2)^2 - 2p_1^2 p_2^2 + \frac{1}{2}(\lambda p_1)^2 p_2^2]$.

2- $\overline{|M_{tot}|^2} \propto 6(\mathbf{p}_1 \mathbf{p}_2)^2 + 17p_1^2 p_2^2 - 9p_1^2 (\lambda p_2)^2 - 8p_2^2 (\lambda p_1)^2 + 12(\mathbf{p}_1 \mathbf{p}_2)(\lambda p_1)(\lambda p_2)$

many thanks to
A. Milstein
(BINP)

neglect Z_b recoil motion ($\beta < 0.02 \Rightarrow$ very good approximation)

also formulae for h_b are available

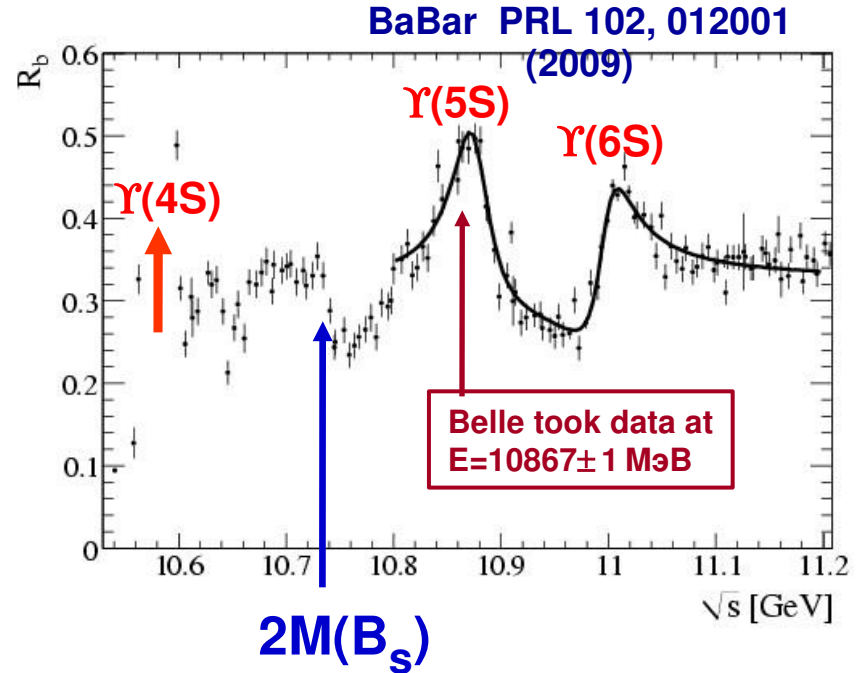
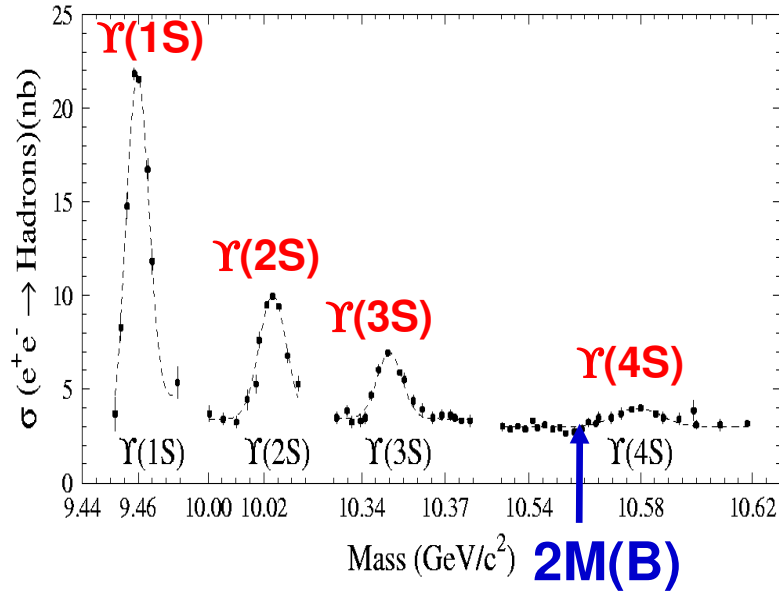
Consider 1D projections

θ_1, θ_2 – polar angles of 1st and 2nd pions

φ_p – angle btw planes defined by (1) π_1 & Z axis, (2) π_1 & π_2 .

Interference terms vanish after integration over other angular variables
 \Rightarrow subtraction of non-resonant contribution is possible.

e^+e^- hadronic cross-section

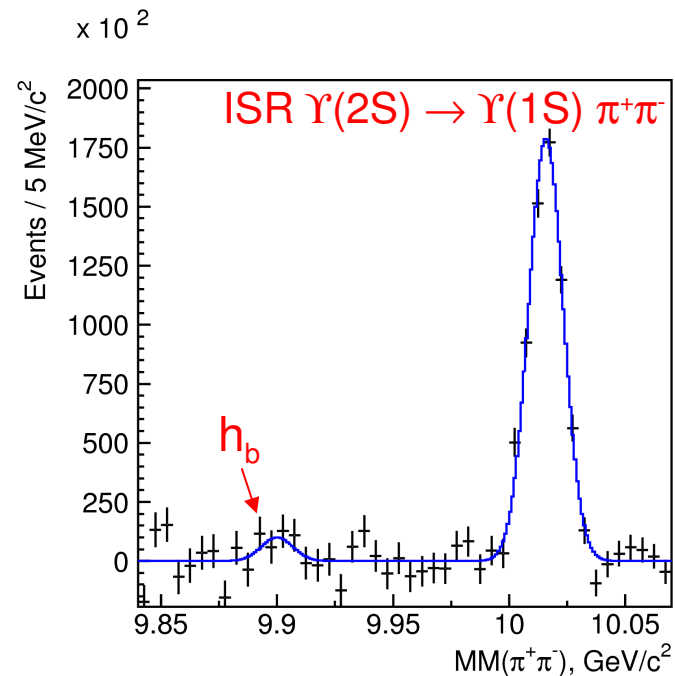
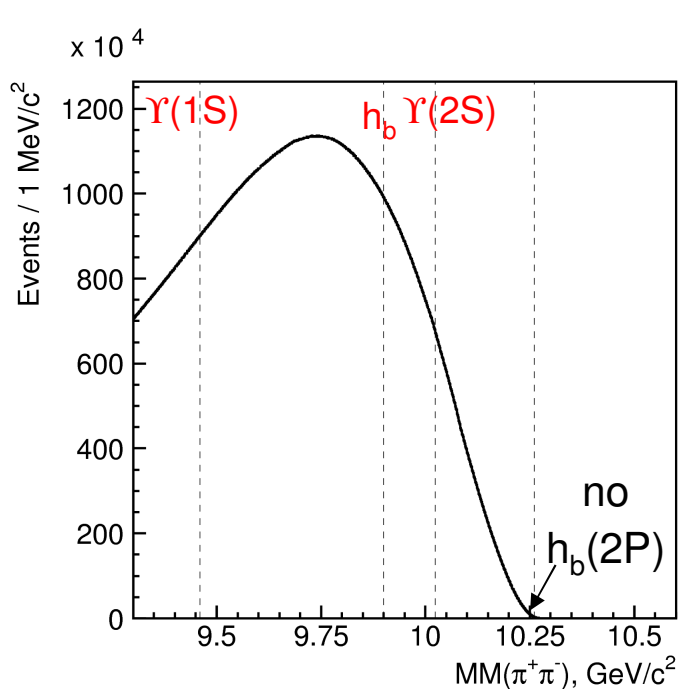


$e^+ e^- \rightarrow \gamma(4S) \rightarrow BB$, where B is B^+ or B^0

$e^+ e^- \rightarrow bb(\gamma(5S)) \rightarrow B^{(*)}B^{(*)}, B^{(*)}B^{(*)}\pi, BB\pi\pi, B_s^{(*)}B_s^{(*)}, \gamma(1S)\pi\pi, \gamma X \dots$

study

Search in $\Upsilon(4S)$ data



$L = 711\text{fb}^{-1}$ [$\times 6 \Upsilon(5S)$ sample]

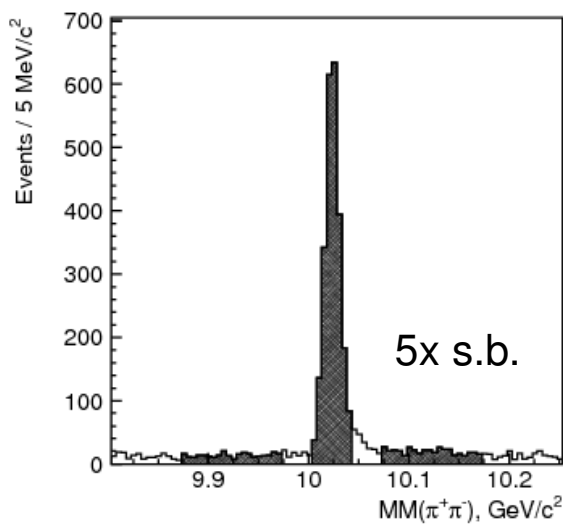
No significant signal of $h_b(1P)$: $(34 \pm 20) \times 10^3$ (1.7σ)

$\sigma[e^+e^- \rightarrow h_b(1P) \pi^+\pi^-] @ \Upsilon(4S) < 0.28$ at 90% C.L.

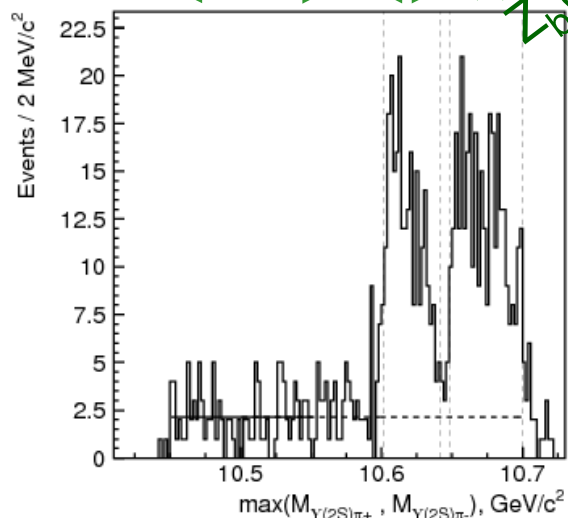
$\sigma[e^+e^- \rightarrow h_b(1P) \pi^+\pi^-] @ \Upsilon(5S)$

$\Rightarrow \Upsilon(4S)$ does not show anomalous properties

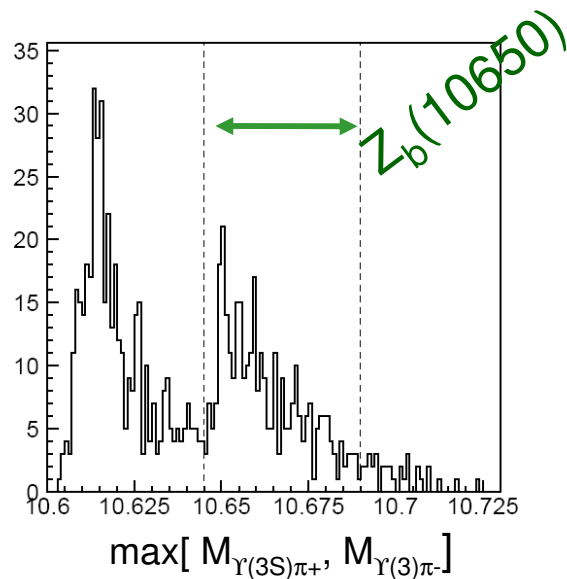
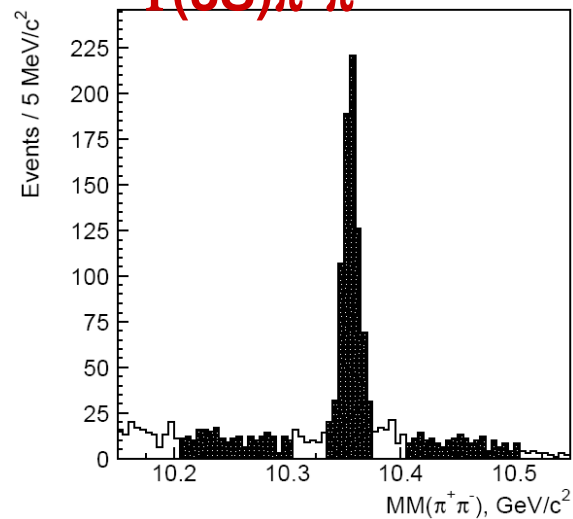
$\Upsilon(2S)\pi^+\pi^-$



non-resonant region
 $Z_b(10610)$
 $Z_b(10650)$



$\Upsilon(3S)\pi^+\pi^-$



Systematics

Results are stable

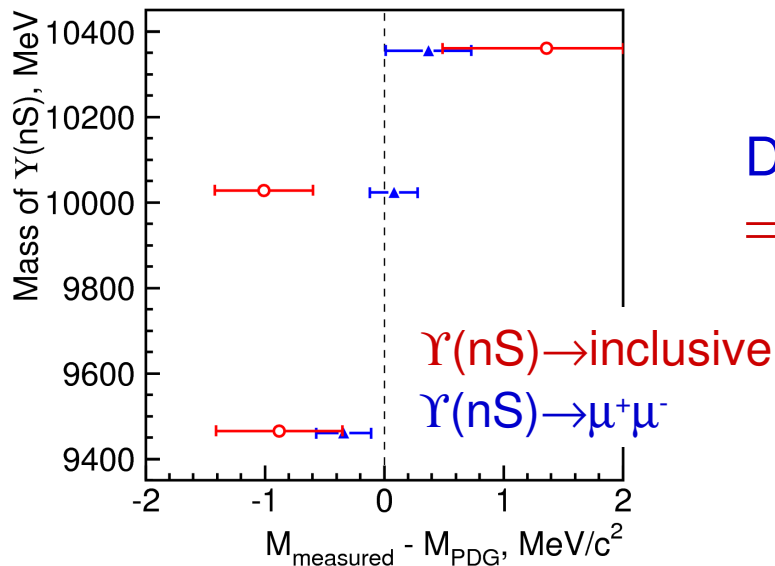
Significance w/ systematics

$h_b(1P)$ 5.5σ

$h_b(2P)$ 11.2σ

	Polynomial order	Fit range	Signal shape	Selection requirements
$N[h_b]$, 10^3	± 2.4	± 3.6	$+1.2$ -8.0	—
$M[h_b]$, MeV/c^2	$\pm .04$	$\pm .10$	$+0.04$ -0.20	$+.20$ $-.30$
$N[h_b(2P)]$, 10^3	± 2.2	± 2.6	$+23.$ -9.0	—
$M[h_b(2P)]$, MeV/c^2	$\pm .10$	$\pm .20$	$+1.0$ -0.0	$\pm .08$

$M_{\text{measured}} - M_{\text{PDG}}$ for reference channels



Deviations of reference channels from PDG

\Rightarrow additional uncertainty $\pm 1\text{MeV}$

local variations of background shape?

Confidence Levels of angular fits to
 $\Upsilon(5S) \rightarrow Z_b^+ \pi^- \rightarrow [h_b(1P)\pi^+] \pi^-$ decay with hypothesis 1^+

	$\cos \theta_1$	$\cos \theta_2$	$\cos \theta_{\pi\pi}$
$Z_b(10610)$	84%	37%	1.1%
$Z_b(10650)$	15%	63%	7.2%