

# *D* and *D<sub>s</sub>* Decays and Dalitz Analyses

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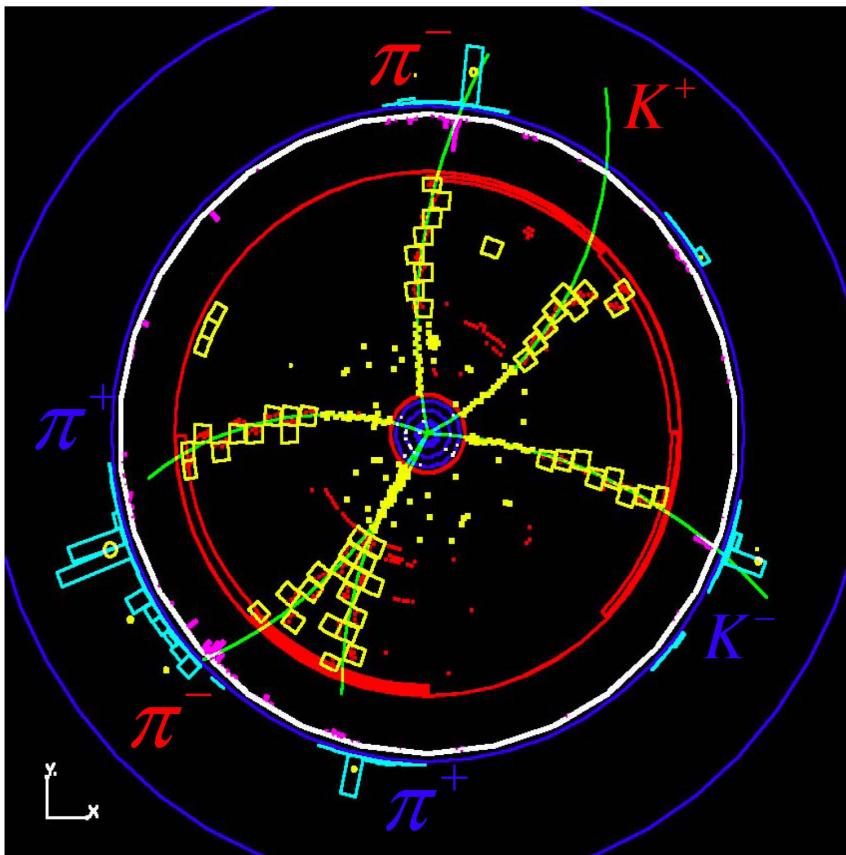
- Absolute  $D^0$  and  $D^+$  Branching Fractions
- Cabibbo Suppressed  $D^0$  and  $D^+$  Decays
- Doubly Cabibbo Suppressed  $D^0$  and  $D^+$  Decays
- Absolute  $D_s$  Branching Fractions
- Inclusive  $D^0$ ,  $D^+$ , and  $D_s$  decays to  $s\bar{s}$
- Dalitz Analyses
- Summary and Conclusions



Heavy Quarks and Leptons 2006  
München October 18, 2006

# $e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$ Events and Analyses

$e^+e^- \rightarrow \psi(3770) \rightarrow D^+D^-$   
 $D^+ \rightarrow K^-\pi^+\pi^+$  and  $D^- \rightarrow K^+\pi^-\pi^-$



- CLEO-c uses  $D^+$  and  $D^0$  decays from  $e^+e^- \rightarrow \psi(3770) \rightarrow D^+D^-$  or  $D^0\bar{D}^0$ 
  - No additional pions produced
  - Extremely clean events
- Leptonic, semileptonic, and key hadronic branching fractions measured with a double tagging technique
  - Other branching fractions measured relative to a reference mode, usually  $D^0 \rightarrow K^-\pi^+$  or  $D^+ \rightarrow K^-\pi^+\pi^+$
- Absolute branching fractions for key Cabibbo Favored hadronic modes were published with  $56 \text{ pb}^{-1}$  of data.
  - Preliminary update with  $281 \text{ pb}^{-1}$  reported for the first time here
- Some other branching ratios utilizing  $281 \text{ pb}^{-1}$  already published or submitted for publication

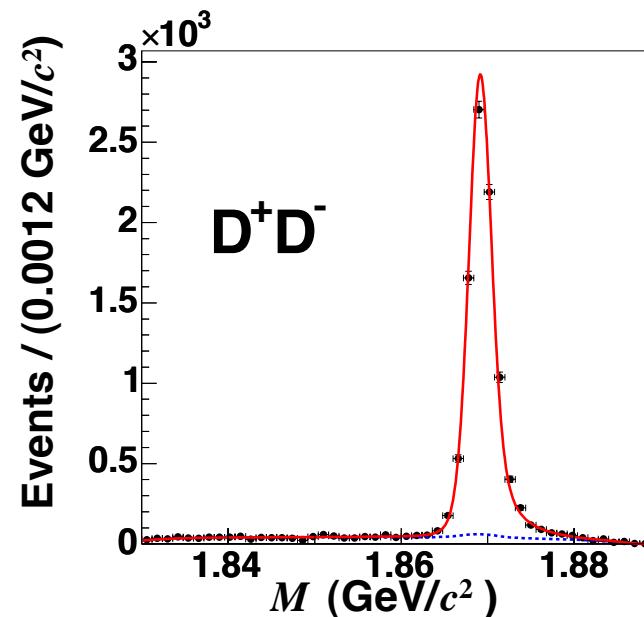
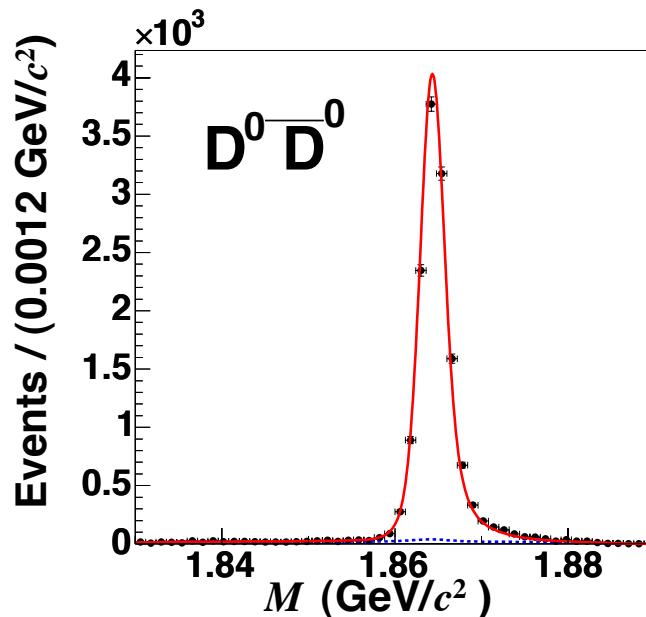
# Absolute $D^0$ and $D^+$ Hadronic Branching Fractions

Utilize technique pioneered by MARK III

- Single Tag (ST) Yields  $D \rightarrow i$  and  $\bar{D} \rightarrow X$   $N_i = N_{D\bar{D}} \mathcal{B}_i \epsilon_i$
  - Double Tag (DT) Yields  $D \rightarrow i$  and  $\bar{D} \rightarrow \bar{j}$   $N_{i\bar{j}} = N_{D\bar{D}} \mathcal{B}_i \mathcal{B}_{\bar{j}} \epsilon_{i\bar{j}}$ 
    - Obtain ST and DT yields from fits to beam constrained mass distributions
    - Compute branching fractions and  $N_{D\bar{D}}$
- $$\mathcal{B}_i = \frac{N_{i\bar{j}}}{N_{\bar{j}}} \frac{\epsilon_{\bar{j}}}{\epsilon_{i\bar{j}}} \quad \text{and} \quad N_{D\bar{D}} = \frac{N_i N_{\bar{j}}}{N_{i\bar{j}}} \frac{\epsilon_{i\bar{j}}}{\epsilon_i \epsilon_{\bar{j}}}$$
- Do a  $\chi^2$  fit including all yields and all errors – correlated and uncorrelated.

Yields from  $281 \text{ pb}^{-1}$

- ST all modes: 230,225  $D^0/\bar{D}^0$
- DT all modes:  $13,575 \pm 120$   $D^0\bar{D}^0$
- DT all modes: 167,086  $D^+/D^-$
- DT all modes:  $8,867 \pm 97$   $D^+D^-$

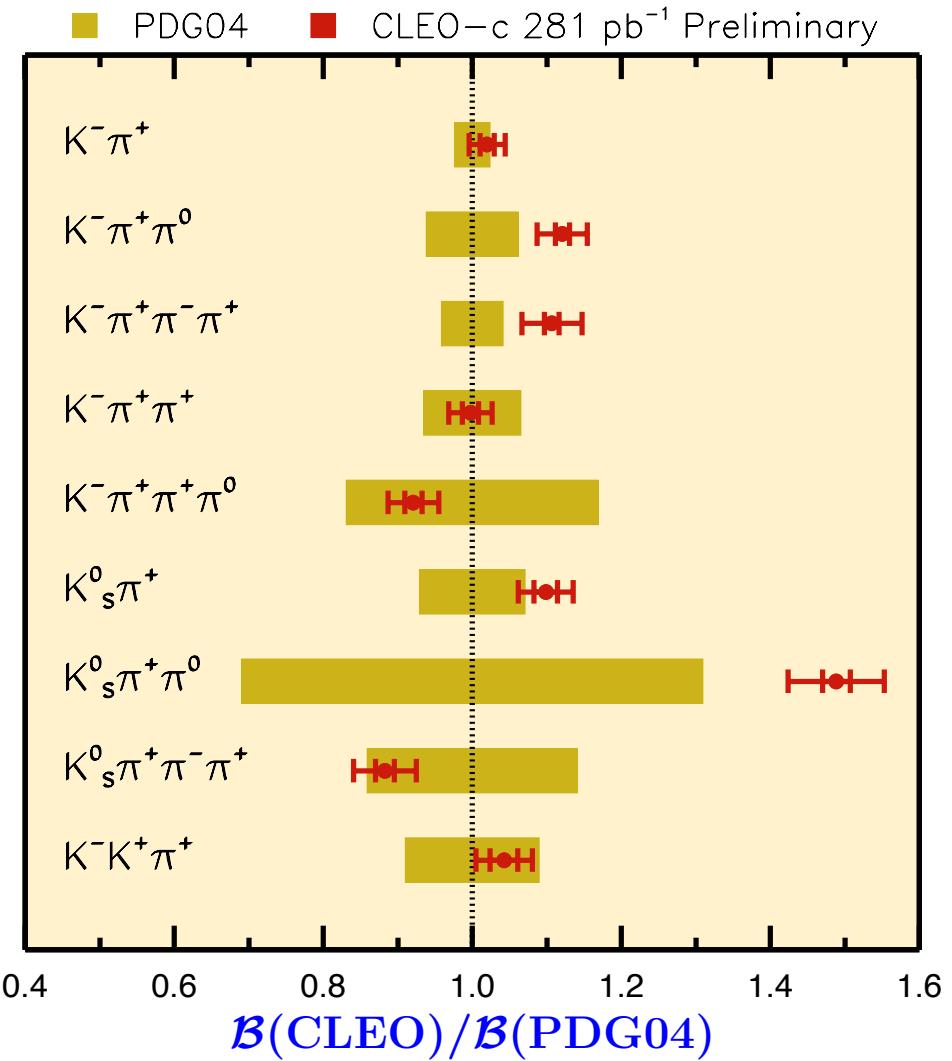


# Absolute Hadronic $D^0$ and $D^+$ Branching Fractions

CLEO-c 281 pb $^{-1}$  Preliminary

| Mode                                   | $\mathcal{B}$ (%)        |
|--|--------------------------|
| $D^0 \rightarrow K^-\pi^+$             | $3.87 \pm 0.04 \pm 0.08$ |
| $D^0 \rightarrow K^-\pi^+\pi^0$        | $14.6 \pm 0.1 \pm 0.4$   |
| $D^0 \rightarrow K^-\pi^+\pi^+\pi^-$   | $8.3 \pm 0.1 \pm 0.3$    |
| $D^+ \rightarrow K^-\pi^+\pi^+$        | $9.2 \pm 0.1 \pm 0.2$    |
| $D^+ \rightarrow K^-\pi^+\pi^+\pi^0$   | $6.0 \pm 0.1 \pm 0.2$    |
| $D^+ \rightarrow K_S^0\pi^+$           | $1.55 \pm 0.02 \pm 0.05$ |
| $D^+ \rightarrow K_S^0\pi^+\pi^0$      | $7.2 \pm 0.1 \pm 0.3$    |
| $D^+ \rightarrow K_S^0\pi^+\pi^+\pi^-$ | $3.13 \pm 0.05 \pm 0.14$ |
| $D^+ \rightarrow K^+K^-\pi^+$          | $0.93 \pm 0.02 \pm 0.03$ |

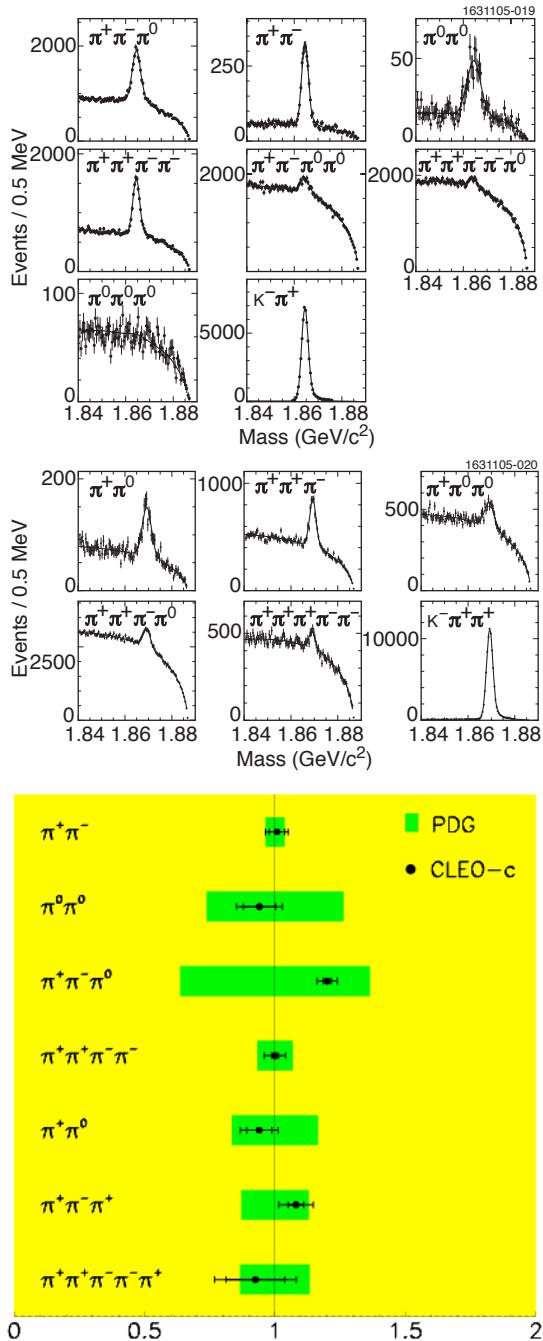
- Systematic errors dominate!
  - Conservative now – little change from 56 pb $^{-1}$  results
  - Expect some improvement
- Final State Radiation included in efficiency MC
  - Without FSR in MC  $\mathcal{B}$ 's would decrease by  $\lesssim 2\%$



Compare to PDG04 because PDG06 includes CLEO-c 56 pb $^{-1}$  in averages

2% for  $\mathcal{B}(D^0 \rightarrow K^-\pi^+)$

# Singly-Cabibbo-Suppressed $D^0$ and $D^+$ Decays to Pions



CLEO-c  $281 \text{ pb}^{-1}$

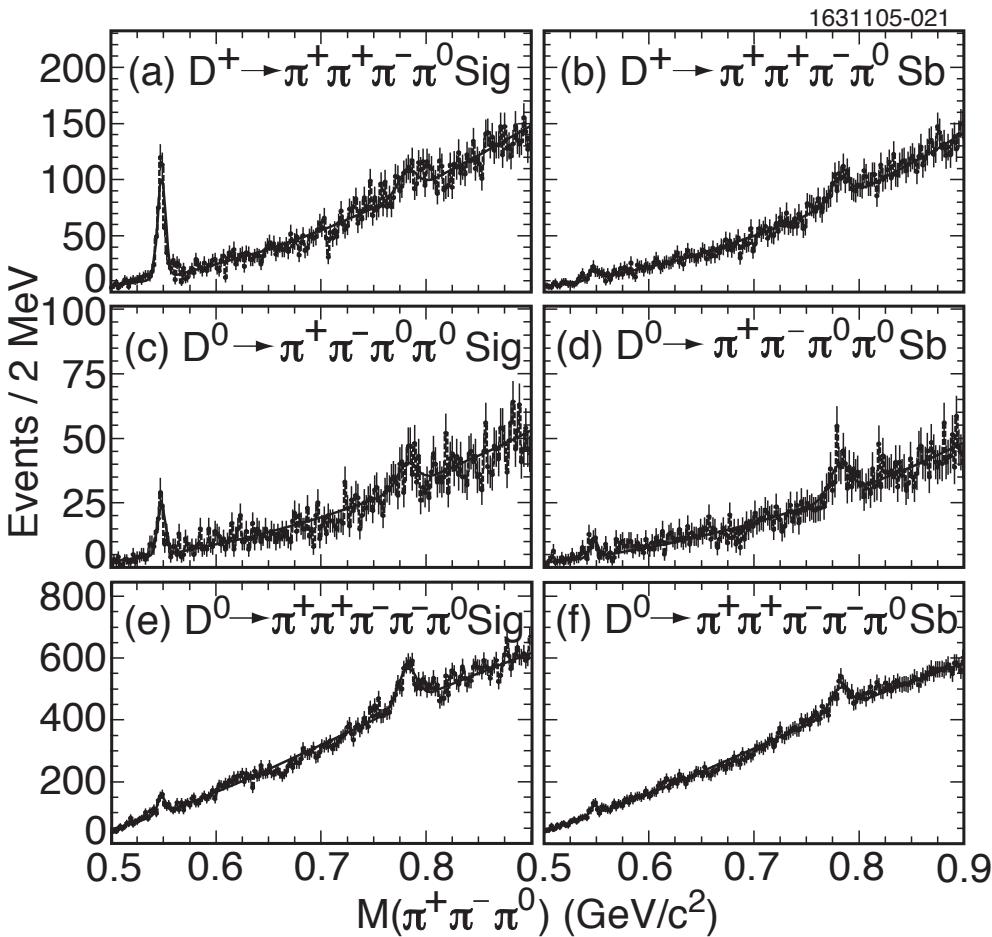
| Mode                        | CLEO-c $\mathcal{B}$ ( $10^{-3}$ ) | PDG04 $\mathcal{B}$ ( $10^{-3}$ ) |
|-----------------------------|------------------------------------|-----------------------------------|
| $\pi^+\pi^-$                | $1.39 \pm 0.04 \pm 0.03$           | $1.38 \pm 0.05$                   |
| $\pi^0\pi^0$                | $0.79 \pm 0.05 \pm 0.04$           | $0.84 \pm 0.22$                   |
| $\pi^+\pi^-\pi^0$           | $13.2 \pm 0.2 \pm 0.5$             | $11 \pm 4$                        |
| $\pi^+\pi^-\pi^+\pi^-$      | $7.3 \pm 0.1 \pm 0.3$              | $7.3 \pm 0.5$                     |
| $\pi^+\pi^-\pi^0\pi^0$      | $9.9 \pm 0.6 \pm 0.7$              | —                                 |
| $\pi^+\pi^-\pi^+\pi^-\pi^0$ | $4.1 \pm 0.5 \pm 0.2$              | —                                 |
| $\pi^+\pi^0$                | $1.25 \pm 0.06 \pm 0.08$           | $1.33 \pm 0.22$                   |
| $\pi^+\pi^+\pi^-$           | $3.35 \pm 0.10 \pm 0.20$           | $3.1 \pm 0.4$                     |
| $\pi^+\pi^0\pi^0$           | $4.8 \pm 0.3 \pm 0.4$              | —                                 |
| $\pi^+\pi^+\pi^-\pi^0$      | $11.6 \pm 0.4 \pm 0.7$             | —                                 |
| $\pi^+\pi^-\pi^+\pi^-\pi^+$ | $1.60 \pm 0.18 \pm 0.17$           | $1.82 \pm 0.25$                   |

- Reference branching fractions used (CLEO-c and PDG 2004 averages)
  - $\mathcal{B}(D^0 \rightarrow K^-\pi^+) = (3.84 \pm 0.07)\%$
  - $\mathcal{B}(D^+ \rightarrow K^-\pi^+\pi^+) = (9.4 \pm 0.3)\%$

BaBar  $\mathcal{B}(D^+ \rightarrow \pi^+\pi^0)$  with DCSD  $\mathcal{B}(D^+ \rightarrow K^+\pi^0)$

# Singly-Cabibbo-Suppressed $D^0$ and $D^+$ Decays to Pions

## Searches for $\eta$ and $\omega$ in multipion $D^0$ and $D^+$ decays



Look for net  $M(\pi^+ \pi^- \pi^0)$  signals  
in signal and sideband regions of  
 $\Delta E \equiv E(D) - E_{beam}$

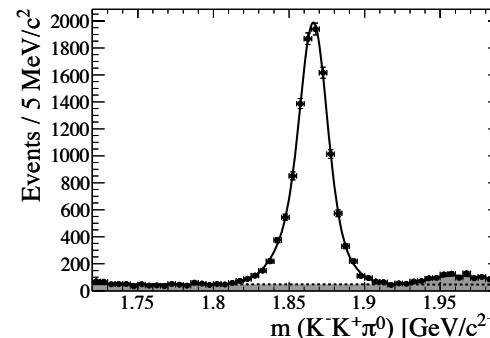
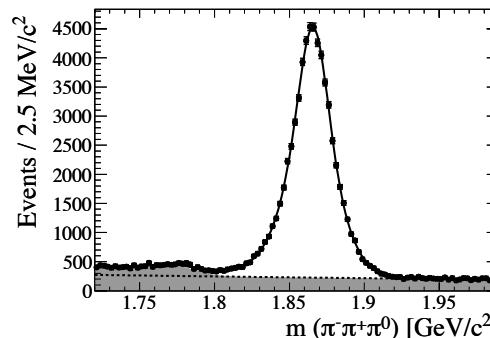
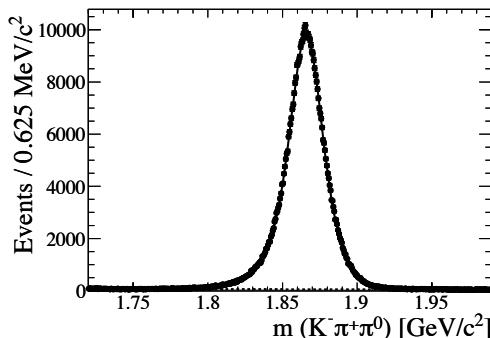
| Mode                 | $\mathcal{B} (10^{-3})$  |
|----------------------|--------------------------|
| $\eta \pi^0$         | $0.62 \pm 0.14 \pm 0.05$ |
| $\eta \pi^+$         | $3.61 \pm 0.25 \pm 0.26$ |
| $\eta \pi^+ \pi^-$   | $< 1.9$ (90% CL)         |
| $\omega \pi^0$       | $< 0.26$ (90% CL)        |
| $\omega \pi^+$       | $< 0.34$ (90% CL)        |
| $\omega \pi^+ \pi^-$ | $1.7 \pm 0.5 \pm 0.2$    |

### Isospin Amplitudes in $D \rightarrow \pi\pi$ decay

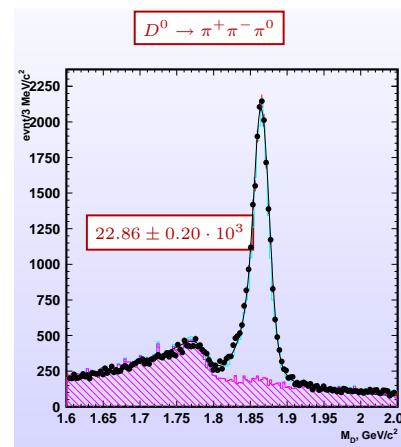
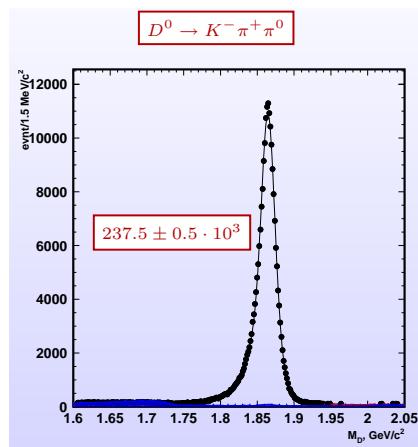
- Amplitudes  $A_0$  and  $A_2$  for  $D \rightarrow \pi\pi$  to  $I = 0, 2$  states
- Determine  $A_2/A_0 = 0.420 \pm 0.014 \pm 0.001$  and  $\delta = (86.4 \pm 2.8 \pm 3.3)^\circ$  (relative phase) from  $\mathcal{B}(\pi^+\pi^-)$ ,  $\mathcal{B}(\pi^0\pi^0)$ , and  $\mathcal{B}(\pi^+\pi^0)$
- Indicates that final state interactions are important in  $D \rightarrow \pi\pi$  decay

# Singly-Cabibbo-Suppressed $D^0$ Decays

BaBar



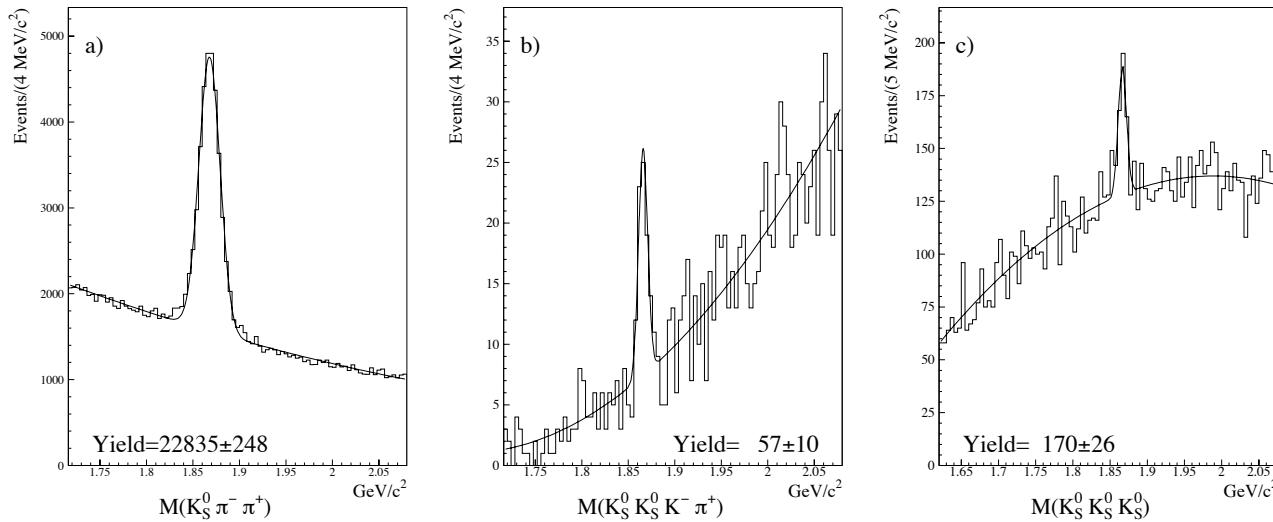
Belle



- Note: different x-axes
- BaBar:  $D^{*+} \rightarrow D^0\pi^+$  tag
- Belle: Uglov ICHEP06
- Used  $\mathcal{B}(D^0 \rightarrow K^-\pi^+\pi^0)$  from PDG 2006

|  | $\mathcal{B}(D^0 \rightarrow \pi^+\pi^-\pi^0)$         | Luminosity            |
|--|--|-----------------------|
| BaBar  | $(1.493 \pm 0.008 \pm 0.018 \pm 0.053) \times 10^{-2}$ | $232 \text{ fb}^{-1}$ |
| CLEO-c   | $(1.32 \pm 0.02 \pm 0.05 \pm 0.02) \times 10^{-2}$     | $281 \text{ pb}^{-1}$ |
| Belle Preliminary                                | $(1.40 \pm 0.01 \pm 0.04 \pm 0.05) \times 10^{-2}$     |                       |
| $\mathcal{B}(D^0 \rightarrow K^-\bar{K}^+\pi^0)$ |  |                       |
| BaBar  | $(0.334 \pm 0.004 \pm 0.006 \pm 0.012) \times 10^{-2}$ |                       |
| PDG 2006   | $(0.13 \pm 0.04) \times 10^{-2}$                       |                       |

# FOCUS Multi-Kaon Modes



| Mode  | FOCUS $\mathcal{B}$ ( $10^{-3}$ ) |      |
|---|-----------------------------------|------|
| $D^0 \rightarrow K^0 \bar{K}^0$             | $0.86 \pm 0.19 \pm 0.10 \pm 0.05$ | SCSD |
| $D^0 \rightarrow K^- K^+ \pi^+ \pi^-$       | $2.20 \pm 0.08 \pm 0.06 \pm 0.09$ | SCSD |
| $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$   | $1.24 \pm 0.21 \pm 0.13 \pm 0.07$ | SCSD |
| $D^0 \rightarrow K_S^0 K_S^0 K^\pm \pi^\mp$ | $0.63 \pm 0.11 \pm 0.06 \pm 0.04$ | CF   |
| $D^0 \rightarrow K_S^0 K_S^0 K_S^0$         | $1.07 \pm 0.16 \pm 0.16 \pm 0.06$ | CF   |

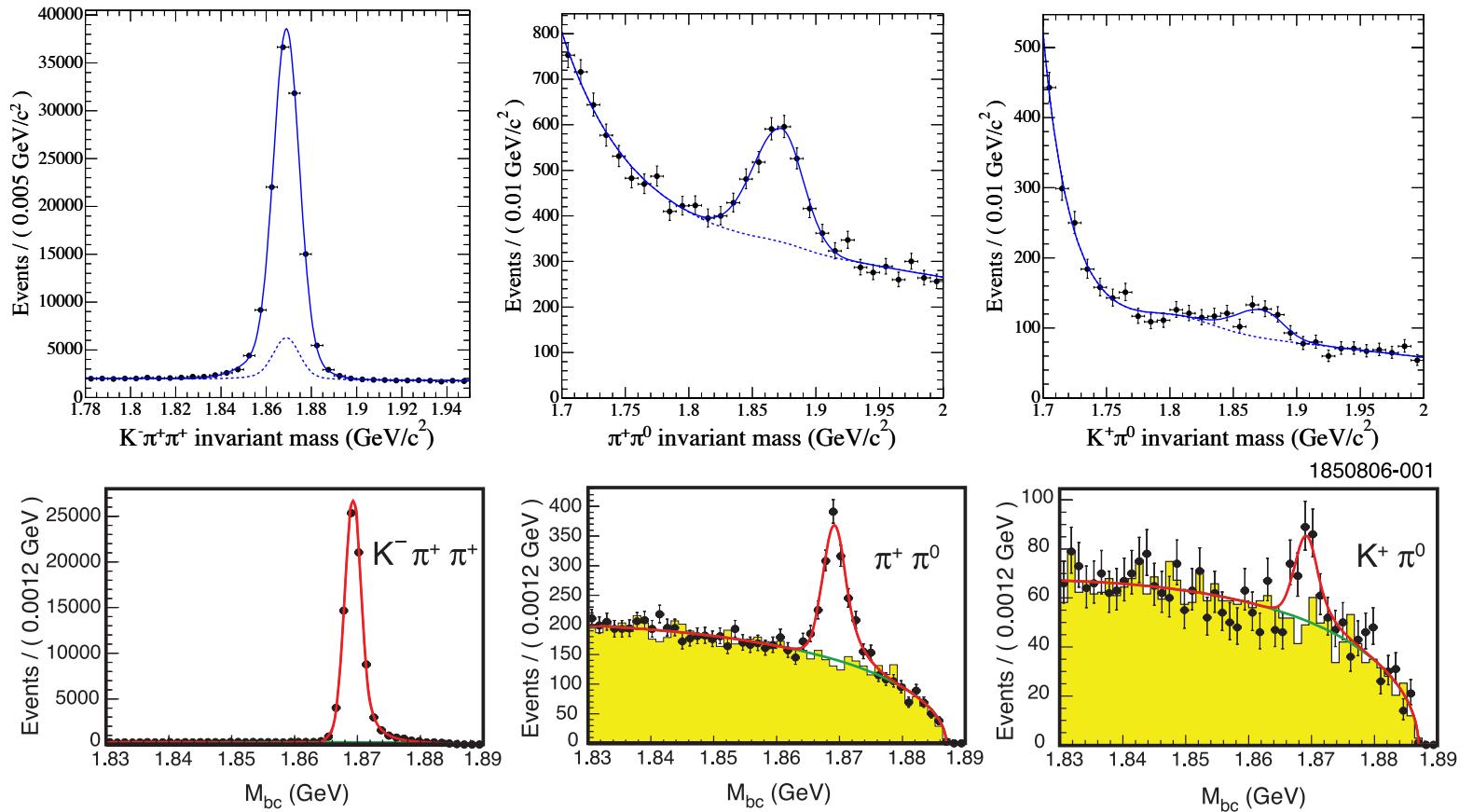
Used reference branching fractions from PDG 06

- $\mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-)$  for  $D^0 \rightarrow K^- K^+ \pi^+ \pi^-$  decay
- $\mathcal{B}(D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-)$  for all other modes

Dalitz Analysis of  $D^0 \rightarrow K^- K^+ \pi^+ \pi^-$  later

# Doubly-Cabibbo-Suppressed $D$ Decays

BaBar  
 $K^+\pi^0$  First  
 Observation



CLEO-c

$$D^+ \rightarrow \pi^+\pi^0 \text{ (SCSD)}$$

Collaboration

$$\mathcal{B}_{\text{mode}}/\mathcal{B}_{\text{ref}}$$

BaBar

$$(1.33 \pm 0.11 \pm 0.09) \times 10^{-2}$$

$$D^+ \rightarrow K^+\pi^0 \text{ (DCSD)}$$

$$\mathcal{B}_{\text{mode}}/\mathcal{B}_{\text{ref}}$$

CLEO-c

$$(1.33 \pm 0.07 \pm 0.06) \times 10^{-2}$$

$$(2.68 \pm 0.50 \pm 0.26) \times 10^{-3}$$

$$(2.40 \pm 0.38 \pm 0.16) \times 10^{-3}$$

(The CLEO-c result for  $D^+ \rightarrow \pi^+\pi^0$  is from the SCSD analysis.)

# Comparison of $D \rightarrow K_S^0\pi$ and $D \rightarrow K_L^0\pi$ Decay Rates

Cabibbo-Favored and Doubly-Cabibbo-Suppressed amplitudes for  $D \rightarrow K^0\pi$ .

- Observed final states are  $K_S^0$  and  $K_L^0$
- Interference between CF and DCS amplitudes can lead to different rates for  $D \rightarrow K_S^0\pi$  and  $D \rightarrow K_L^0\pi$   
(Bigi and Yamamoto)
- Reconstruct  $D \rightarrow K_L^0\pi$  from missing mass

$$R(D) \equiv \frac{\mathcal{B}(D \rightarrow K_S^0\pi) - \mathcal{B}(D \rightarrow K_L^0\pi)}{\mathcal{B}(D \rightarrow K_S^0\pi) + \mathcal{B}(D \rightarrow K_L^0\pi)}$$

CLEO-c Preliminary

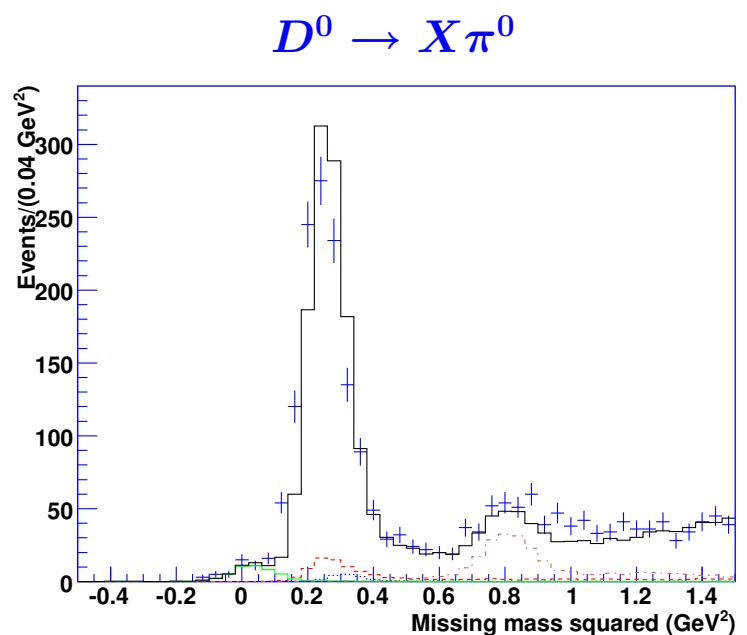
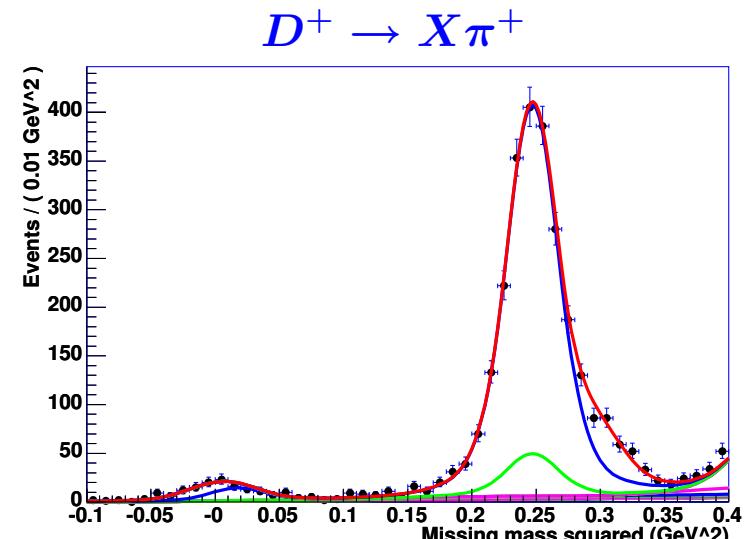
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$$R(D^+) \quad 0.030 \pm 0.023 \pm 0.025$$

$$R(D^0) \quad 0.122 \pm 0.024 \pm 0.030$$

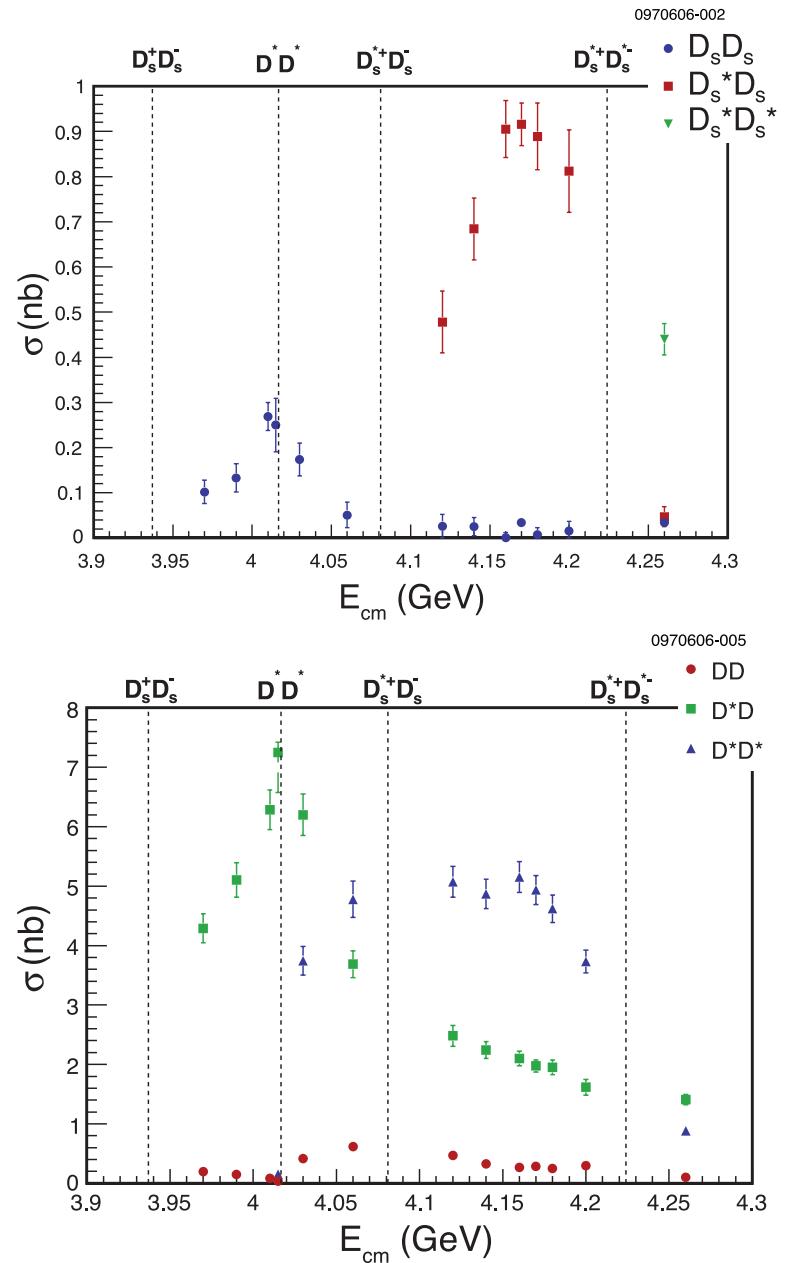
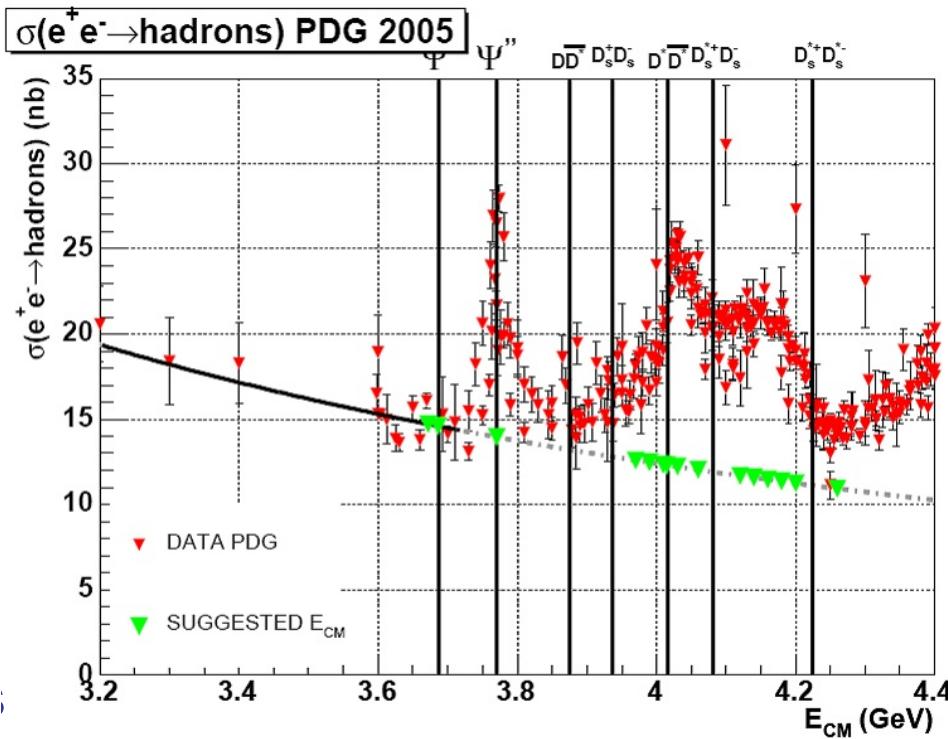

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- U-spin and SU(3) predict  
 $R(D^0) = 2 \tan^2(\theta_c)$  which gives  
 $R(D^0) = 0.109 \pm 0.001$
- $R(D^+)$  not so simple:  
 $D^+ \rightarrow \bar{K}^0\pi^+$  external & internal spectator  
 $D^+ \rightarrow K^0\pi^+$  external spectator & annihilation



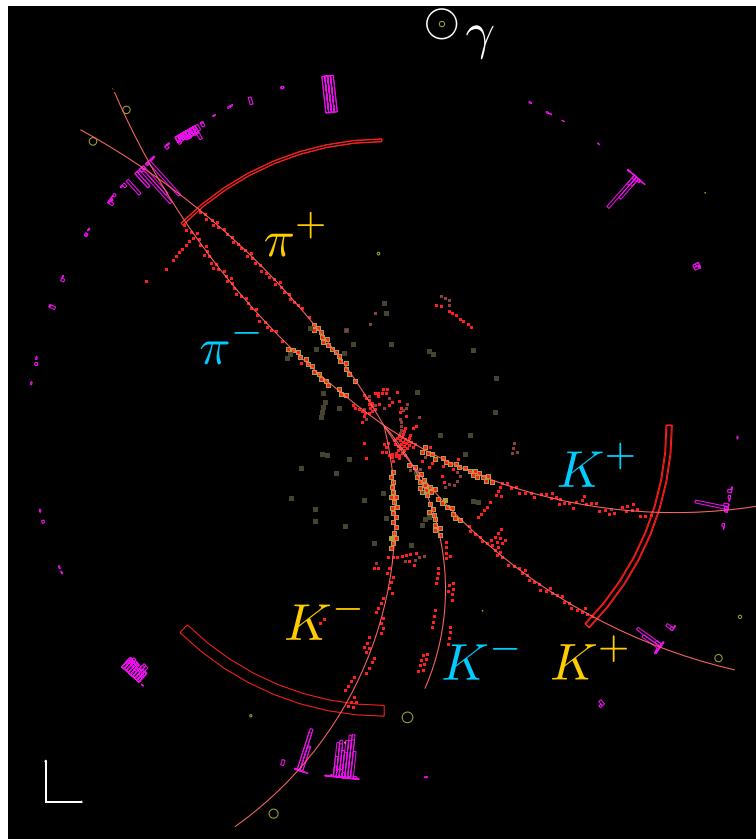
# $D_s$ Production Cross Section

- Little was known about the composition of  $\sigma(e^+e^-)$  above  $E_{cm} = 3.8$  GeV.
- CLEO scan with  $\sim 5 \text{ pb}^{-1}$  per point with fast turnaround and feedback
- More luminosity in the region around  $E_{cm} = 4.17$  GeV where  $D_s^\pm D_s^{*\mp}$  peaks
  - $\sigma(e^+e^- \rightarrow D_s^\pm D_s^{*\mp}) \approx 0.9 \text{ nb}$



# Selecting $D_s^\pm D_s^{*\mp}$ Events

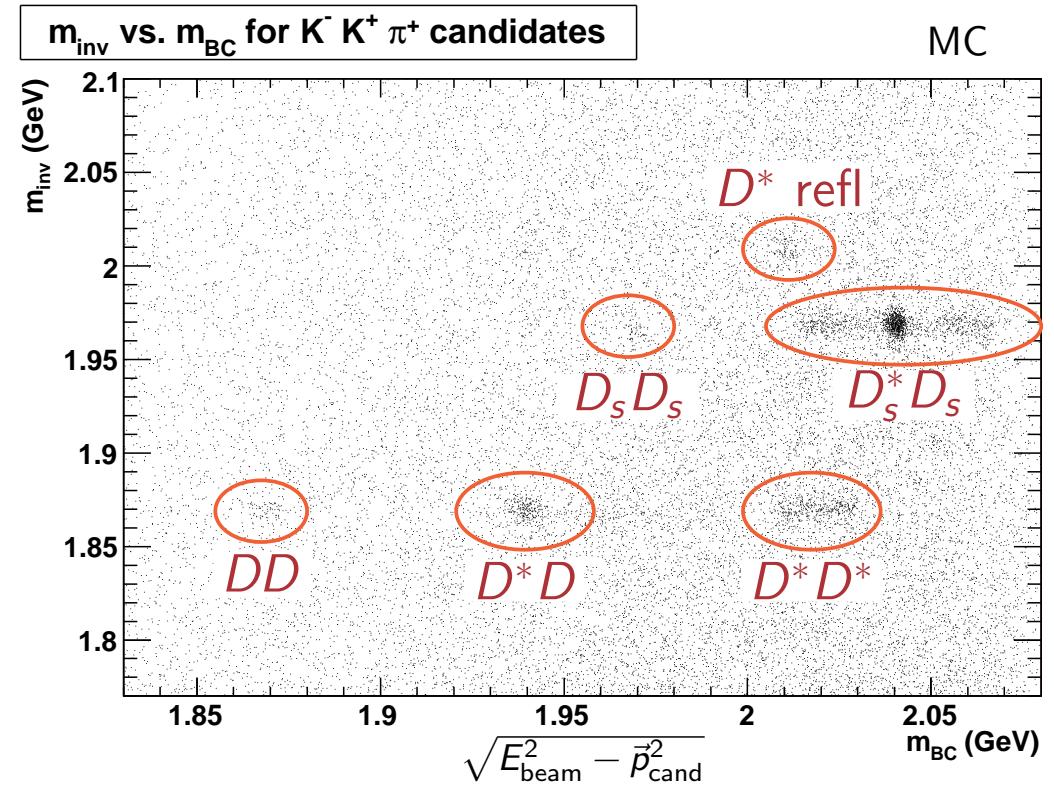
$$e^+ e^- \rightarrow D_s^* D_s \rightarrow D_s^+ D_s^- \gamma$$



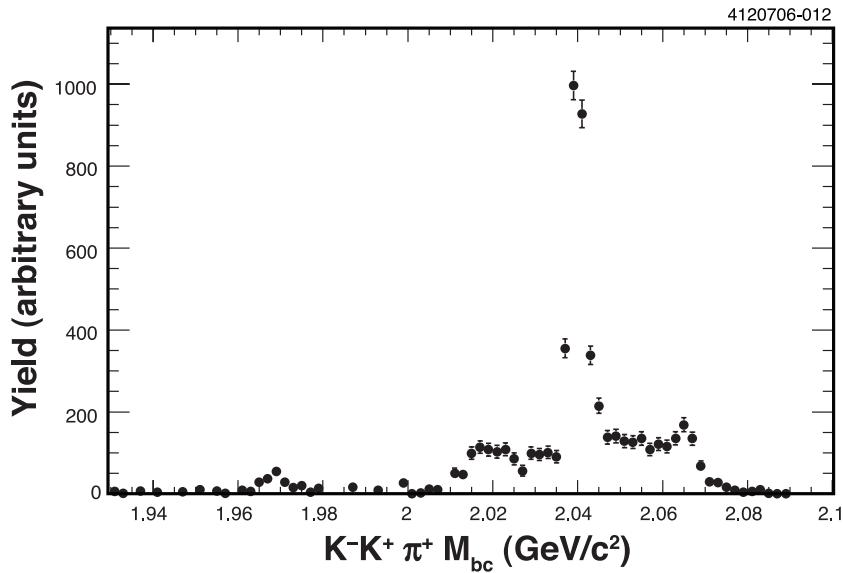
Ignore the  $\gamma$  or  $\pi^0$  from  $D_s^*$  decay

Select  $D_s^\pm D_s^{*\mp}$  events using:

- Candidate invariant mass  $m_{inv}$
- Candidate  $m_{BC}$  (a proxy for momentum)

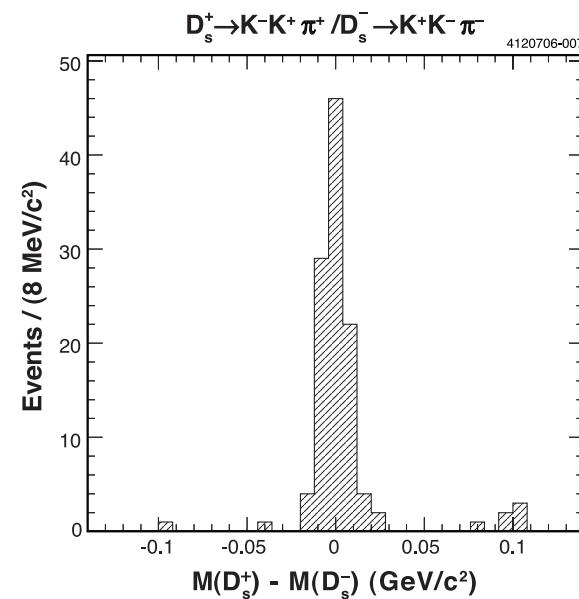
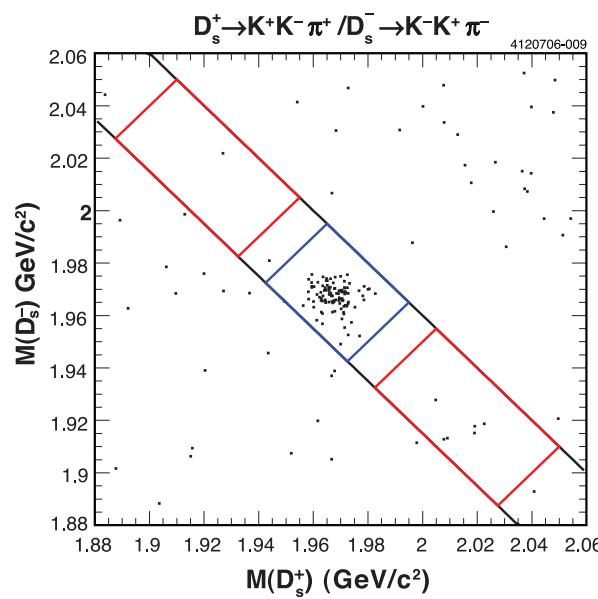
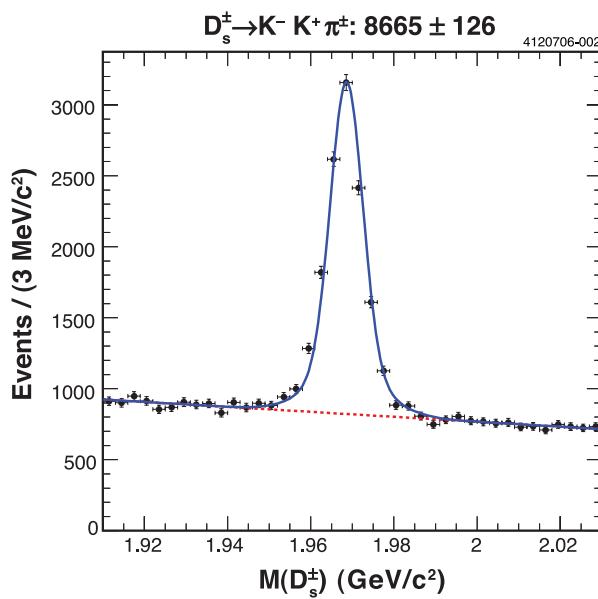


# Analyzing $D_s^\pm D_s^{*\mp}$ Events



Measuring ST and DT events:

- Require  $M_{bc} > 2.01 \text{ GeV}$
- Fit ST  $M(D_s)$  candidate invariant mass distribution
- Cut DT in  $M(D_s^-)$  vs  $M(D_s^+)$  plane
  - Blue box signal
  - Red boxes sidebands



# Absolute Hadronic $D_s$ Branching Fractions

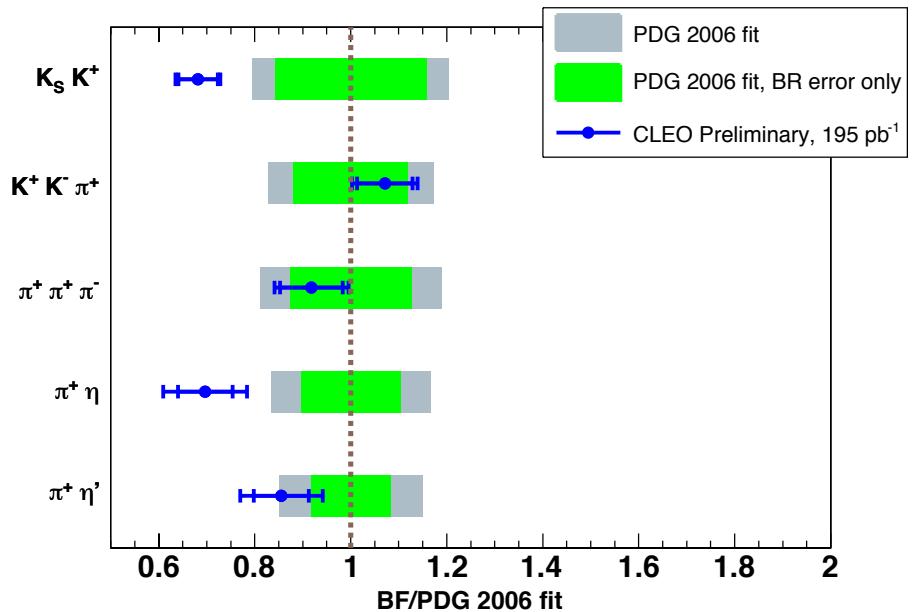
CLEO-c Preliminary

195 pb $^{-1}$  of data

| $D_s^+$ Mode          | $\mathcal{B}$ (%)        |
|-----------------------|--------------------------|
| $K_S K^+$             | $1.50 \pm 0.09 \pm 0.05$ |
| $K^- K^+ \pi^+$       | $5.57 \pm 0.30 \pm 0.19$ |
| $K^- K^+ \pi^+ \pi^0$ | $5.62 \pm 0.33 \pm 0.51$ |
| $\pi^+ \pi^+ \pi^-$   | $1.12 \pm 0.08 \pm 0.05$ |
| $\pi^+ \eta$          | $1.47 \pm 0.12 \pm 0.14$ |
| $\pi^+ \eta'$         | $4.02 \pm 0.27 \pm 0.30$ |

Additional 130 pb $^{-1}$  to be analyzed

Comparison with PDG 2006



Belle measures  $\mathcal{B}(D_s^+ \rightarrow K^- K^+ \pi^+)$  utilizing a partial reconstruction technique for  $e^+ e^- \rightarrow D_{s1} D_s^*$  events  
(R. Uglov ICHEP06)

| $\mathcal{B}(D_s^+ \rightarrow K^- K^+ \pi^+) (\%)$ |             |                          |
|---|-------------|--------------------------|
| CLEO  | Preliminary | $5.57 \pm 0.30 \pm 0.19$ |
| Belle   | Preliminary | $4.1 \pm 0.4 \pm 0.4$    |

# Partial $D_s^+ \rightarrow K^- K^+ \pi^+$ Branching Fractions

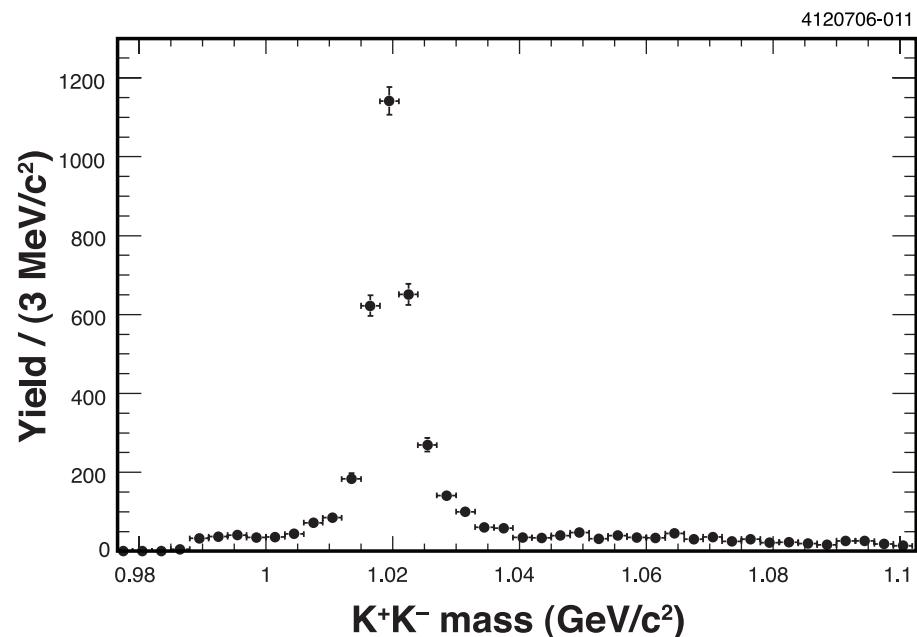
$\mathcal{B}(D_s^+ \rightarrow \phi\pi^+ \rightarrow K^- K^+ \pi^+)$  is one of the largest  $D_s$  branching fractions

- A branching fraction called  $\mathcal{B}(D_s^+ \rightarrow \phi\pi^+)$  has often been used as a reference branching fraction for  $D_s$  decays.
  - Derived from a narrow mass cut around the  $\phi$  peak in the  $M(K^+K^-)$  distribution in  $D_s^+ \rightarrow K^- K^+ \pi^+$  events.
- E687 has published and FOCUS has reported significant contributions from  $f_0(980)$  (or  $a_0(980)$ ) in the  $\phi\pi$  region of the  $D_s^+ \rightarrow K^- K^+ \pi^+$  Dalitz plot.
  - These scalar contributions ( $\sim 5\%$ ) under the  $\phi$  peak in  $M(K^+K^-)$  are comparable to current CLEO-c errors for  $\mathcal{B}_{\Delta M} \equiv \mathcal{B}(D_s^+ \rightarrow K^- K^+ \pi^+)$  with  $|M(K^- K^+) - M_\phi| < \Delta M$  MeV/c<sup>2</sup>.
- PDG and HEP community need to decide how to deal with this in the future

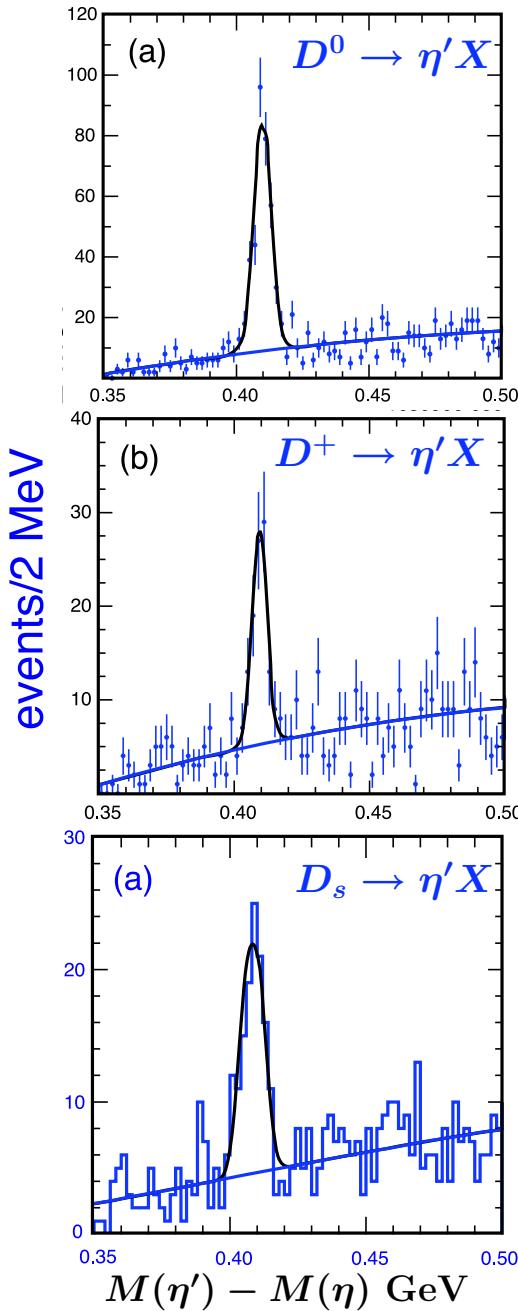
CLEO-c Preliminary

| $\mathcal{B}_{\Delta M}$ (%) |                          |
|------------------------------|--------------------------|
| $\mathcal{B}_{10}$           | $1.98 \pm 0.12 \pm 0.09$ |
| $\mathcal{B}_{20}$           | $2.25 \pm 0.13 \pm 0.12$ |
| PDG 06                       | $1.77 \pm 0.44$          |

PDG 06 unfolded from  
 $\mathcal{B}(\phi \rightarrow K^- K^+)$  and  
reported  $\mathcal{B}(D_s^+ \rightarrow \phi\pi^+)$



# CLEO-c Inclusive $D^0$ , $D^+$ , and $D_s$ decays to $s\bar{s}$



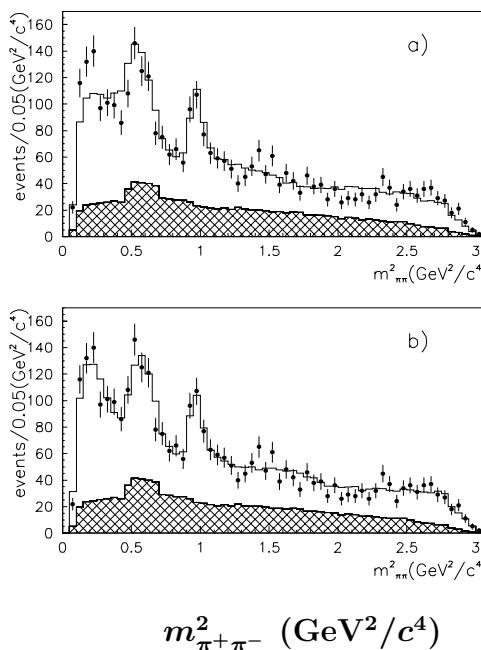
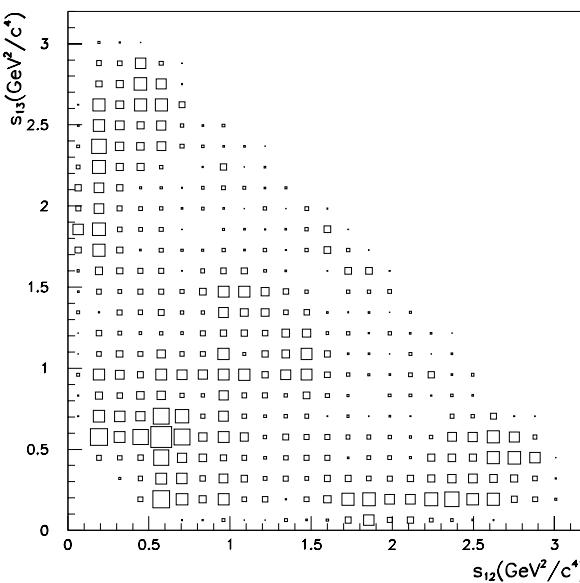
Inclusive  $D^0$ ,  $D^+$ , and  $D_s$  decays to  $\eta X$ ,  $\eta' X$ , and  $\phi X$

- For these  $s\bar{s}$  states larger branching fractions for  $D_s$  than for  $D^0$  and  $D^+$
- Fully reconstruct one  $D$  and then search for  $\eta$ ,  $\eta'$  and  $\phi$  from the other  $D$ .
- CLEO utilizes  
 $281 \text{ pb}^{-1}$  of  $\psi(3770)$  data for  $D^0$  and  $D^+$   
 $195 \text{ pb}^{-1}$  of  $E_{cm} \approx 4.17 \text{ GeV}$  data for  $D_s$

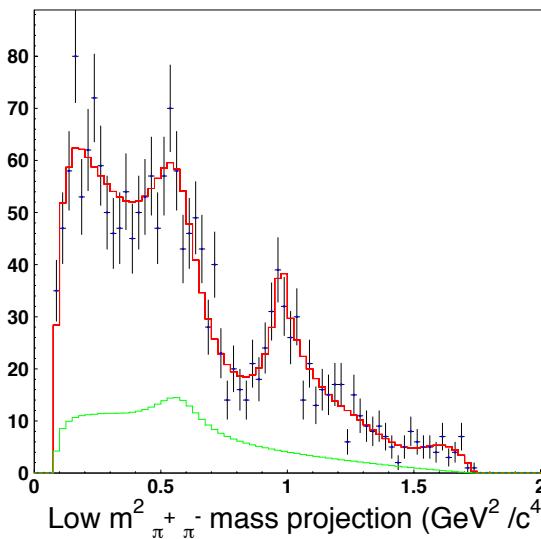
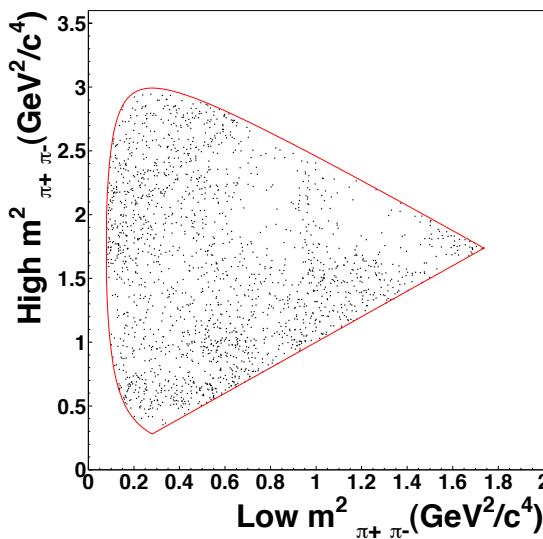
| Mode      | $\mathcal{B}(D^0) \text{ (%)}$ | $\mathcal{B}(D^+) \text{ (%)}$ | $\mathcal{B}(D_s^+) \text{ (%)}$ |
|-----------|--------------------------------|--------------------------------|----------------------------------|
| $\eta X$  | $9.5 \pm 0.4 \pm 0.8$          | $6.3 \pm 0.5 \pm 0.5$          | $23.5 \pm 3.1 \pm 2.0$           |
| $\eta' X$ | $2.48 \pm 0.17 \pm 0.21$       | $1.04 \pm 0.16 \pm 0.09$       | $8.7 \pm 1.9 \pm 0.8$            |
| $\phi X$  | $1.05 \pm 0.08 \pm 0.07$       | $1.03 \pm 0.10 \pm 0.07$       | $16.1 \pm 1.2 \pm 1.1$           |

- Qualitative observations:
  - $\eta'$  and  $\phi$  relatively rare in  $D^0$  and  $D^+$  decay
  - $\eta$  with lower mass and larger light quark content is produced at substantially higher rates in  $D^0$  &  $D^+$
  - $\phi$  rate higher in  $D_s$  decay than in  $D^0$  and  $D^+$  decay
  - can utilize higher  $\phi$  rates to separate  $D_s$  from  $D^0$  and  $D^+$  at  $\Upsilon(5S)$  and hadron colliders

# E791 and FOCUS Dalitz Analyses of $D^+ \rightarrow \pi^+\pi^+\pi^-$ Decays



$$m_{\pi^+\pi^-}^2 \text{ (GeV}^2/\text{c}^4\text{)}$$



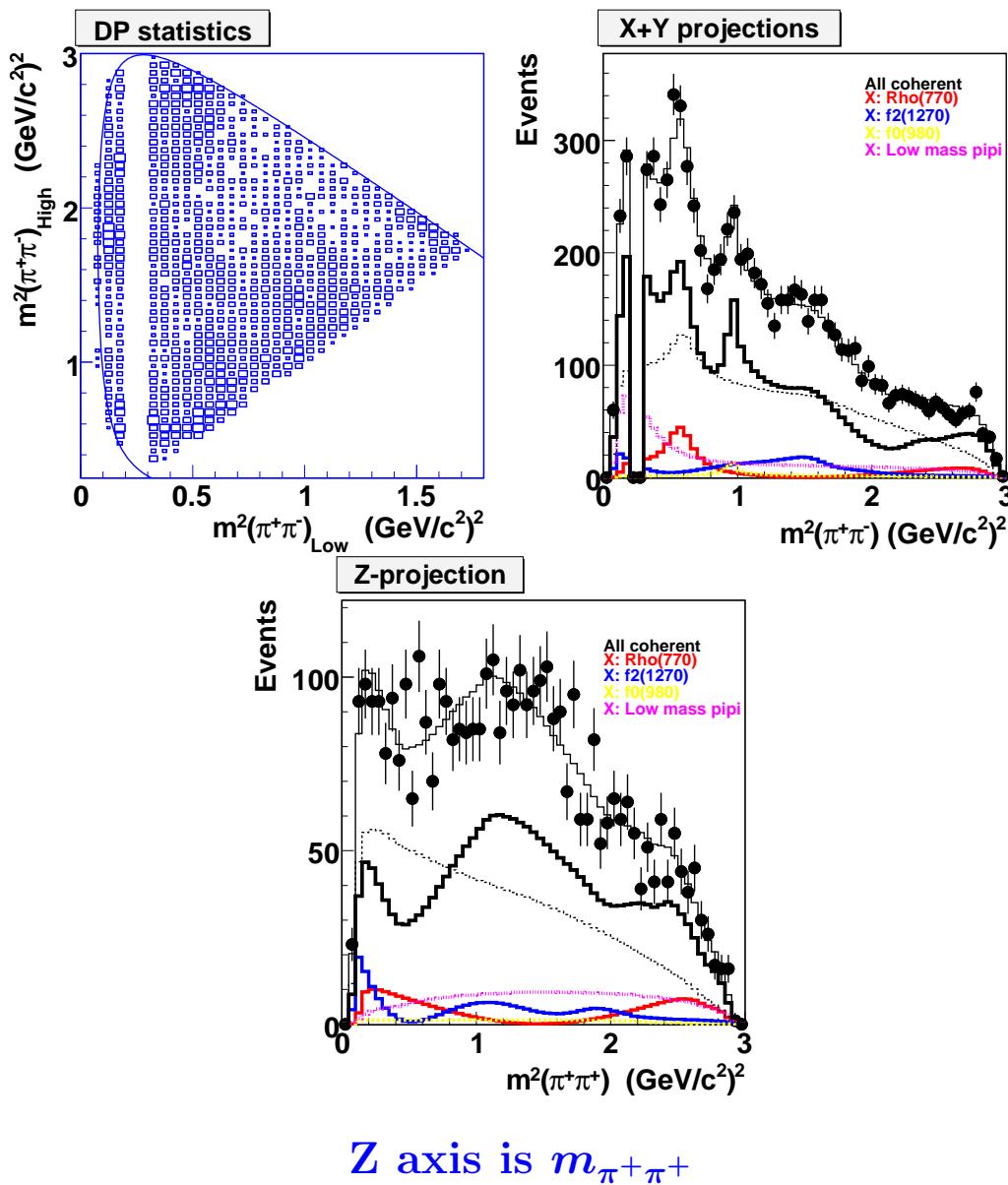
## E791 Dalitz Analysis

- $s_{12}$  and  $s_{13}$  are  $m_{\pi^+\pi^-}$
- Dalitz plot symmetrized about the line  $s_{12} = s_{13}$
- $\sigma^0\pi^+$  for low  $m_{\pi^+\pi^-}$  peak
  - (a) without  $\sigma^0\pi^+$
  - (b) with  $\sigma^0\pi^+$
- Also  $\rho^0\pi^+$ ,  $f_2(1270)\pi^+$ , ...

## FOCUS Dalitz Analysis

- Used K Matrix formalism
  - Low  $m_{\pi^+\pi^-}$  peak from combination of resonances,  $f_0(980)$ , ...
- Also  $\rho^0\pi^+$  and  $f_2(1270)\pi^+$

# CLEO-c Dalitz Analysis of $D^+ \rightarrow \pi^+\pi^+\pi^-$ Decays



## CLEO-c Preliminary

Isobar model like E791

- Removed  $K_S^0$  mass region
- $\sigma^0\pi^+$  for low  $m_{\pi^+\pi^-}$  peak
- Preliminary Fit Fraction results

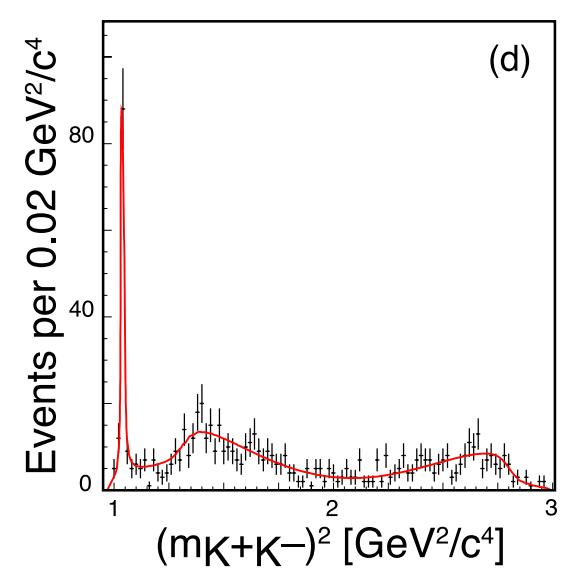
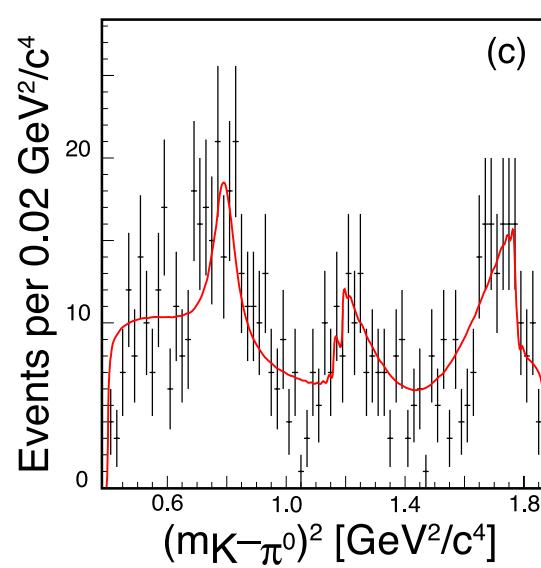
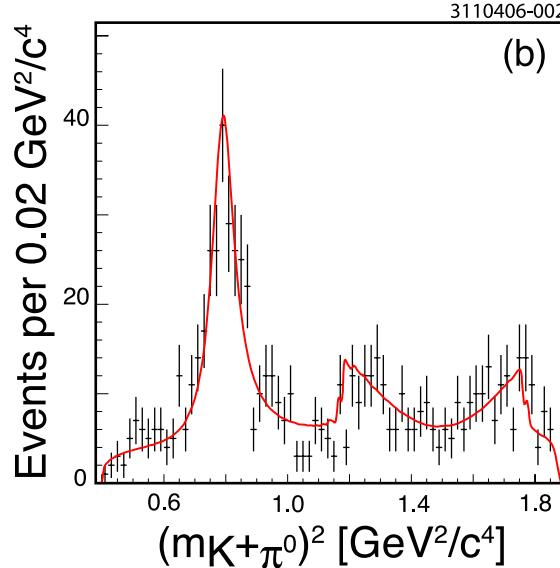
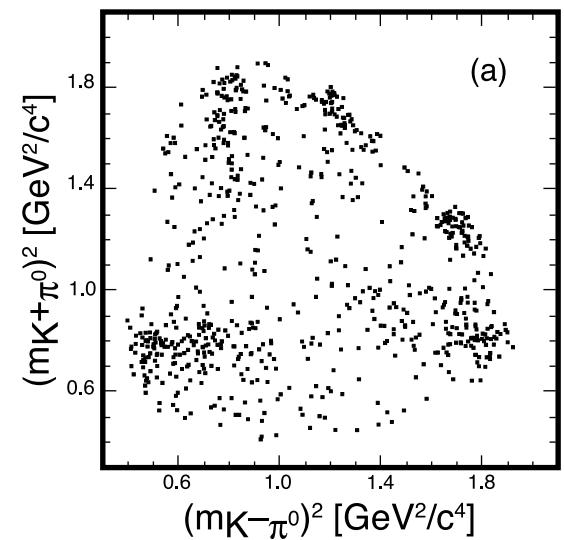
|                   | CLEO (%)       | E791 (%)       |
|-------------------|----------------|----------------|
| $\rho^0\pi^+$     | $20.0 \pm 2.5$ | $33.6 \pm 3.9$ |
| $\sigma^0\pi^+$   | $41.8 \pm 2.9$ | $46.3 \pm 9.2$ |
| $f_2(1270)\pi^+$  | $18.2 \pm 2.7$ | $19.4 \pm 2.5$ |
| $f_0(908)\pi^+$   | $4.1 \pm 0.9$  | $6.1 \pm 1.4$  |
| $f_0(1370)\pi^+$  | $2.6 \pm 1.9$  | $2.3 \pm 1.7$  |
| $f_0(1500)\pi^+$  | $3.4 \pm 1.3$  | —              |
| Non Res           | $< 3.5$        | $7.8 \pm 6.6$  |
| $\rho(1450)\pi^+$ | $< 2.4$        | $7.8 \pm 0.6$  |

E791 & CLEO-c general agreement  
Future: K-Matrix fit like FOCUS

# CLEO-III Dalitz Analysis of $D^0 \rightarrow K^+ K^- \pi^0$ Decays

CKM angle  $\gamma$  ( $\phi_3$ ) can be measured in  $B^\pm \rightarrow D^0(\bar{D}^0)K^\pm$  with  $D^0/\bar{D}^0$  decaying to  $K^{*+}K^-$  or  $K^{*-}K^+$

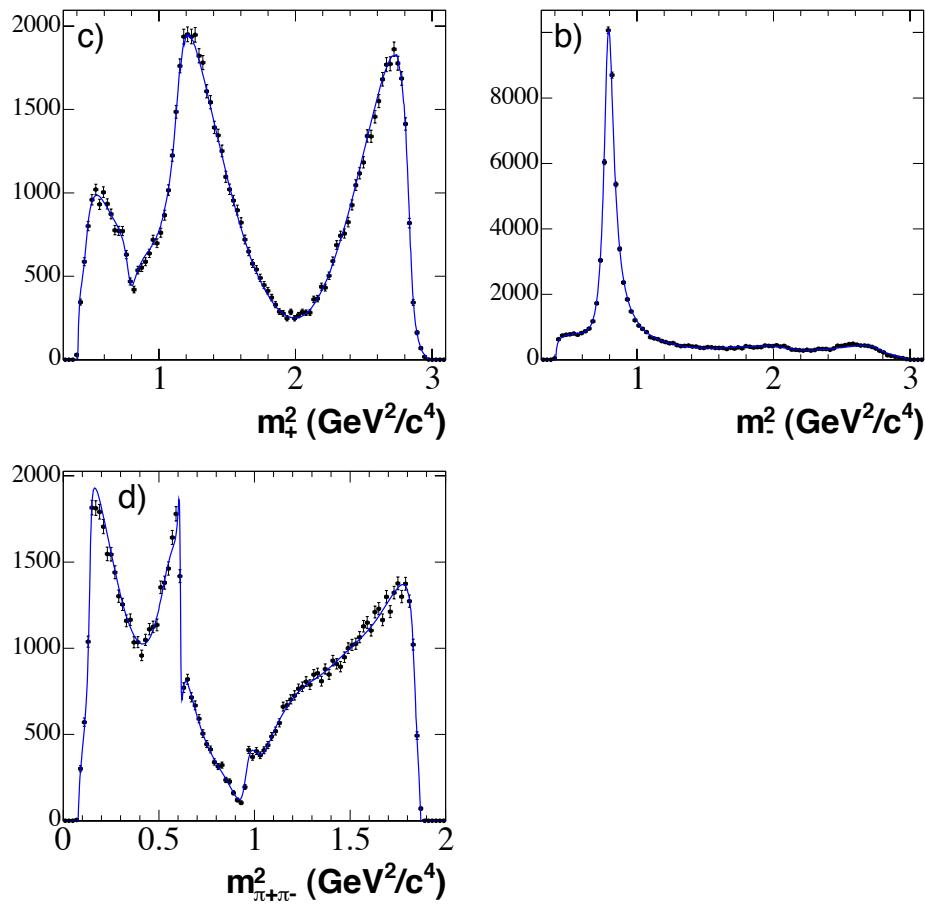
- Need relative complex amplitude for  $\bar{D}^0 \rightarrow K^{*+}K^-$  and  $D^0 \rightarrow K^{*+}K^-$
- Same as relative complex amplitude  $r_D e^{i\phi_D}$  for  $D^0 \rightarrow K^{*-}K^+$  and  $D^0 \rightarrow K^{*+}K^-$  (assuming  $CP$  conservation in these decays)
- CLEO finds:
  - $r_D = 0.52 \pm 0.05 \pm 0.04$
  - $\phi_D = 332^\circ \pm 8^\circ \pm 11^\circ$



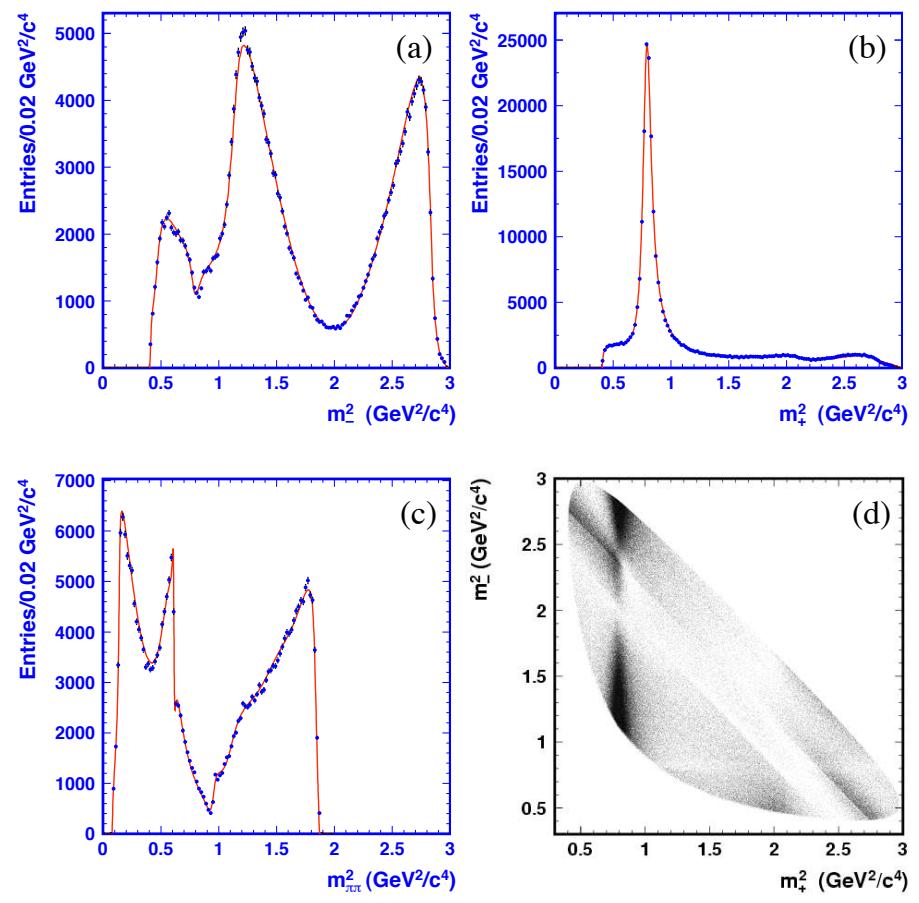
Projected fits

# Dalitz Analyses of $D \rightarrow K_S^0\pi^+\pi^-$ to Measure $\gamma$ or $\phi_3$

BaBar



Belle



$$D^0 \rightarrow K_S^0\pi^+\pi^- \text{ & } \bar{D}^0 \rightarrow K_S^0\pi^+\pi^-$$

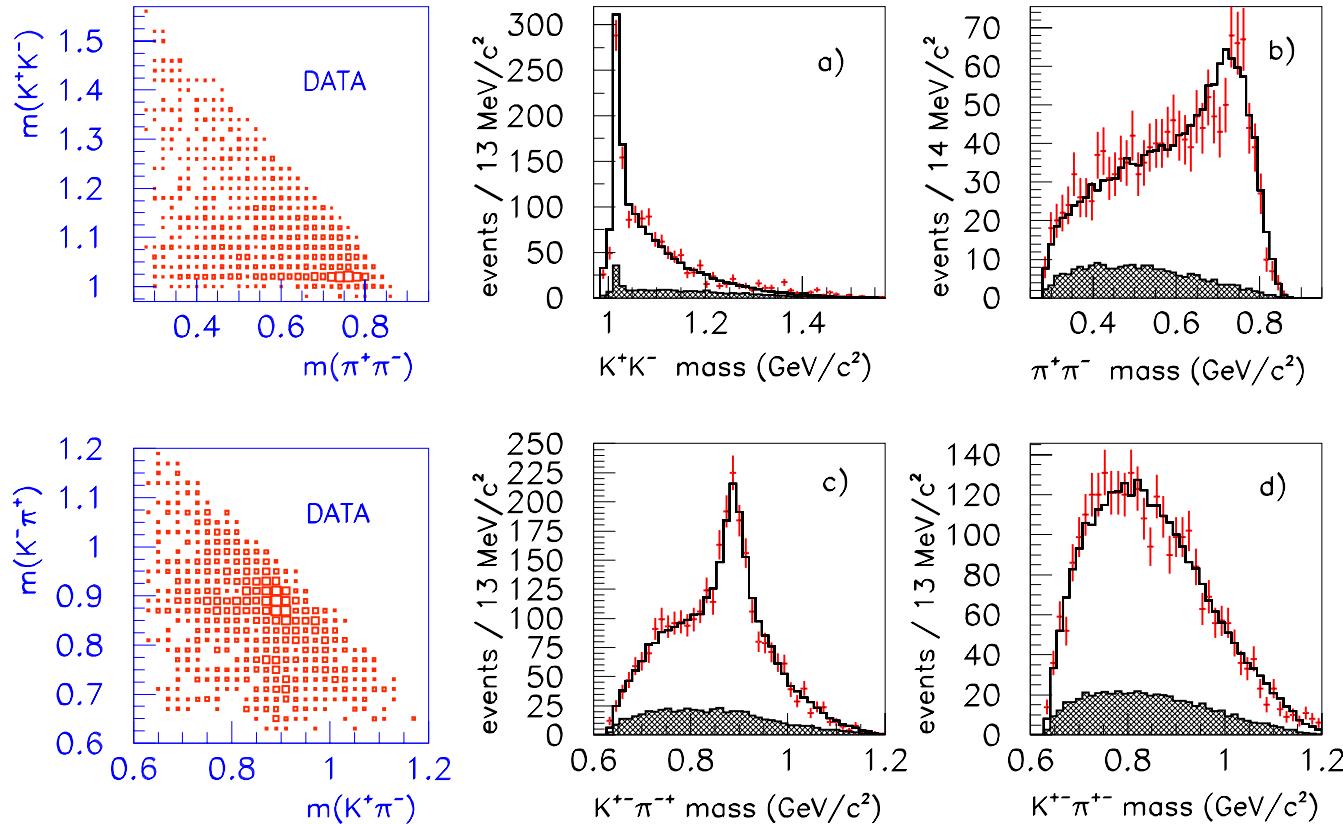
- Both fit data with isobar models
  - BaBar fit 17 two-body states
  - Belle fit 18 two-body states

Four states with Fit Fraction  $\gtrsim 10\%$

| State             | BaBar (%) | Belle (%) |
|-------------------|-----------|-----------|
| $K^*(892)^+\pi^-$ | 58.6      | 61.2      |
| $K_S^0\rho^0$     | 22.4      | 21.6      |
| $K_S^0\sigma$     | 9.3       | 9.8       |
| Non Res           | 7.3       | 9.7       |

# FOCUS Dalitz Analysis of $D^0 \rightarrow K^+K^-\pi^+\pi^-$ Decays

## Multiple Dalitz Plots from four-body decay



| Mode | Fit Fraction (%) |
|------|------------------|
|------|------------------|

$K_1(1270)^+K^-$        $33 \pm 6 \pm 4$

$K_1(1400)^+K^-$        $22 \pm 3 \pm 4$

$\phi\rho^0$        $29 \pm 2 \pm 1$

$K^*(1400)^0K^+\pi^-$        $11 \pm 1 \pm 1$

$f_0(980)\pi^+\pi^-$        $15 \pm 3 \pm 2$

## Summary and Conclusions

Advances in precision and discovery reach with BaBar, Belle, and CLEO-c

- Absolute  $D$  hadronic branching fractions from charm threshold CLEO-c
  - $281 \text{ pb}^{-1}$  Preliminary results for  $D^0$  and  $D^+$  limited by systematic errors
    - CF decay errors as low as  $\lesssim 3\%$
    - Now Final State Radiation must be considered; effects  $\lesssim 2\%$ 
      - Interesting problem for the PDG
  - $195 \text{ pb}^{-1}$  Preliminary results for  $D_s$  limited by statistics
    - CF decay errors as low as  $\lesssim 10\%$
    - Scalar  $K^+K^-$  contribution becoming significant in measurements of  $\mathcal{B}(D_s \rightarrow K^-K^+\pi^+)$  with  $M(K^+K^-)$  cut around the  $\phi$  peak
      - Need to define new reference branching fraction for  $D_s$  decays
- Many accurate branching ratio measurements from BaBar, Belle, and CLEO-c
  - BaBar and Belle are starting to dominate branching ratio measurements
- Dalitz analyses of  $D^+ \rightarrow \pi^+\pi^+\pi^-$ ,  $D^0 \rightarrow K^+K^-\pi^0$ , and  $D \rightarrow K_S^0\pi^+\pi^-$  decays, and three-body sub-modes from  $D^0 \rightarrow K^+K^-\pi^+\pi^-$  decays
  - Dalitz analyses of  $D \rightarrow K_S^0\pi^+\pi^-$  with huge statistics are byproducts of BaBar and Belle measurements of  $\gamma$  or  $\phi_3$ 
    - Expect BaBar and Belle to dominate future Dalitz  $D$  decay analyses
- Renaissance of hadronic  $D$  physics coming from CLEO-c at the charm threshold and BaBar and Belle at the beauty threshold!