

# CP Violation and $B$ Physics at the LHC

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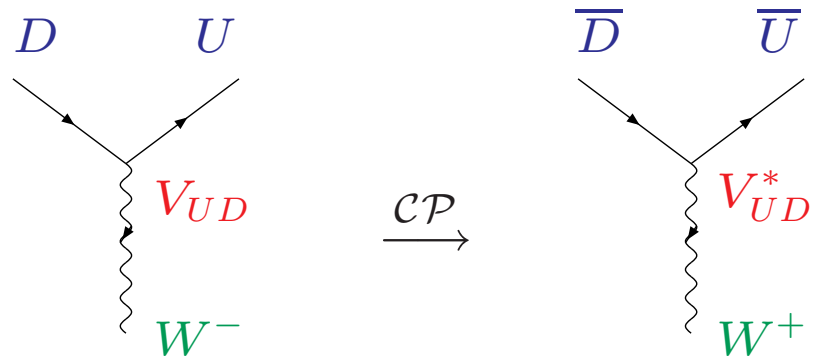
*CERN, Department of Physics, Theory Division*

HQL 2006, Munich, Germany, 16–20 October 2006

- Setting the Stage
- A Brief Look at the Current  $B$ -Factory Data
- Key Targets of the  $B$  Physics Programme at the LHC
- Conclusions and Outlook

# Setting the Stage

- Standard Model (SM):  $\rightarrow$  Kobayashi–Maskawa mechanism of CP violation:



Recent review: R.F., *J. Phys.* **G32** (2006) R71 [hep-ph/0512253]

# Why Study Flavour Physics & CP Violation?

- New Physics (NP): → typically new patterns in the flavour sector
  - SUSY scenarios;
  - left–right–symmetric models;
  - models with extra  $Z'$  bosons;
  - scenarios with extra dimensions;
  - “little Higgs” scenarios ...
- $\nu$  masses: → origin beyond the Standard Model (SM)!
  - CP violation in the neutrino sector?
  - Connection with quark-flavour physics?
- Cosmology: → baryon asymmetry suggests new CP violation!
  - Could be associated with very high energy scales:
    - \* attractive mechanism: “leptogenesis”, involving new CP-violating sources in the decays of heavy Majorana neutrinos.
  - But could also be accessible in the laboratory ...

# Challenging the Standard Model through Flavour Studies

Before searching for NP, we have to understand the SM picture!

- Key problem:

◇ *impact of strong interactions* → “hadronic” uncertainties

– Famous example:  $\text{Re}(\varepsilon'/\varepsilon)_K$ , measuring “direct” CPV in  $K$  decays.

- Prospects for the “good old”  $K$ -meson system [CPV in '64:  $\varepsilon_K \sim 10^{-3}$ ]:

– Clean tests of the SM are offered by  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  and  $K_L \rightarrow \pi^0 \nu \bar{\nu}$ , as their hadronic pieces can be fixed through  $K \rightarrow \pi \ell \bar{\nu}$  decays!

– These “rare” decays are *absent* at the tree level of the SM, i.e. originate there exclusively from loops, with BRs =  $\mathcal{O}(10^{-10})$  → challenging<sup>1</sup>

- The  $B$ -meson system is a *particularly promising probe*: → our focus

– Offers various strategies: simply speaking, there are *many*  $B$  decays!

– Search for clean SM relations that could be spoiled by NP ...

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<sup>1</sup>Plans to measure  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  at the SPS (CERN) and  $K_L \rightarrow \pi^0 \nu \bar{\nu}$  at E391 (KEK/J-PARC).

# Where to Study $B$ -Meson Decays?

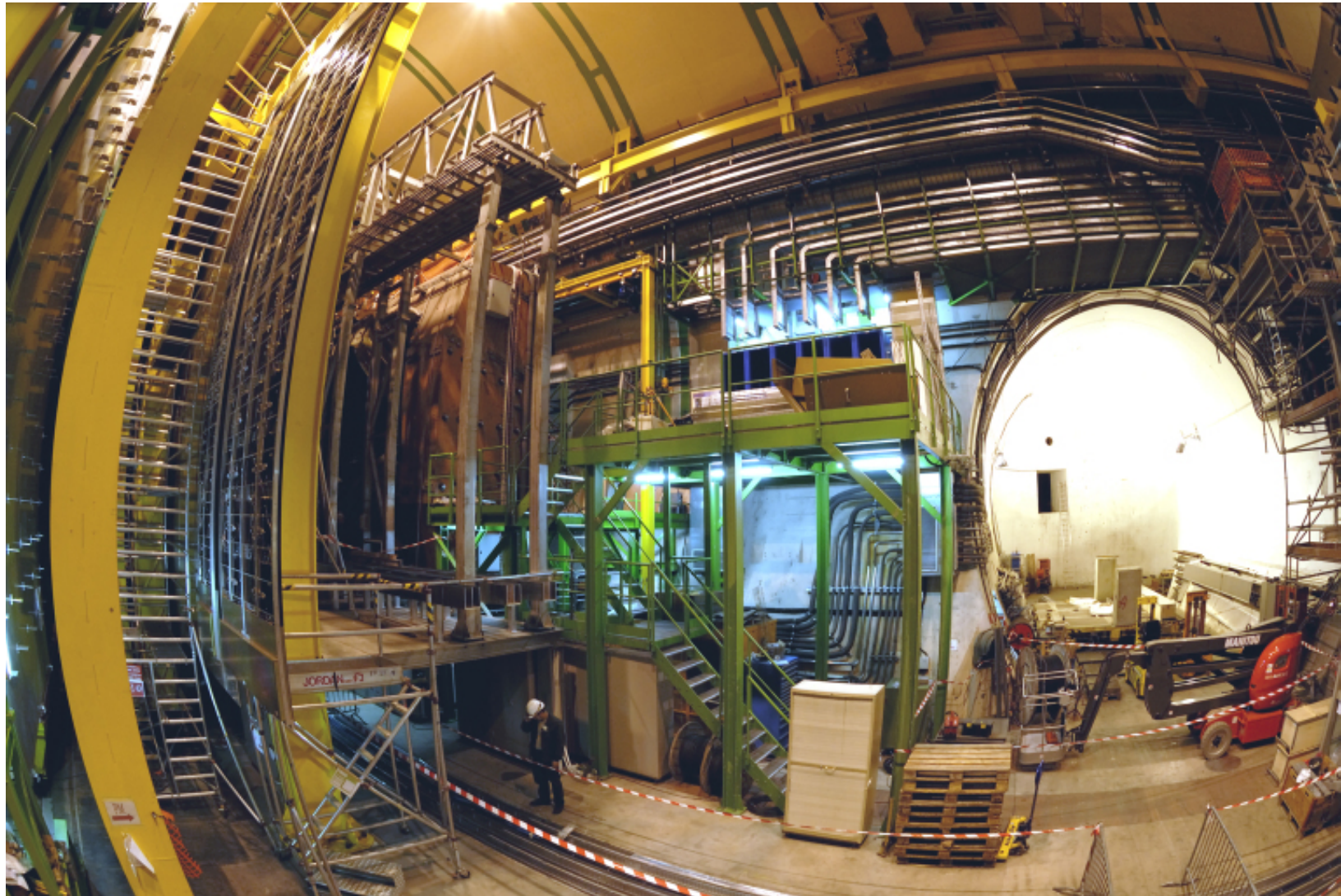
- $B$  factories: asymmetric  $e^+e^-$  colliders @  $\Upsilon(4S) \rightarrow B_d^0 \bar{B}_d^0, B_u^+ B_u^-$ 
  - PEP-II with the *Babar* experiment (SLAC);
  - KEK-B with the *Belle* experiment (KEK):
    - { could well establish CP violation in the  $B$  system;  
many interesting results with  $\sum \mathcal{O}(10^9)$   $B\bar{B}$  pairs ...
  - Discussion of a super- $B$  factory, with increase of luminosity by  $\mathcal{O}(10^2)$ .
- Hadron colliders: → produce also  $B_s$  mesons,<sup>2</sup> as well as  $B_c, \Lambda_b, \dots$ 
  - Tevatron: CDF and D0 have reported first  $B_{(s)}$ -decay results ...
  - ... to be continued at the LHC  $\gtrsim$  2007:

ATLAS & CMS (can also address some  $B$  physics)

⊕ *dedicated*  $B$ -decay experiment: LHCb

<sup>2</sup>Recently, data at  $\Upsilon(5S)$  were taken by Belle, allowing also access to  $B_s$  decays [hep-ex/0610003].

- A recent picture of the LHCb experiment @ CERN:



# Central Target: Unitarity Triangle (UT)

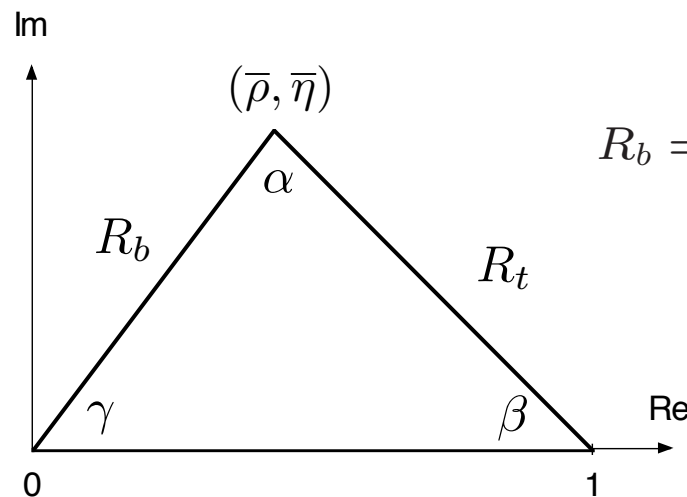
- Application of the Wolfenstein parametrization: [Wolfenstein (1984)]

$$\hat{V}_{\text{CKM}} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

→ phenomenological expansion in  $\lambda \equiv |V_{us}| = 0.22$  [from  $K \rightarrow \pi\ell\bar{\nu}_\ell$ ]

- Unitarity of the CKM matrix:

$$\hat{V}_{\text{CKM}}^\dagger \cdot \hat{V}_{\text{CKM}} = \hat{1} = \hat{V}_{\text{CKM}} \cdot \hat{V}_{\text{CKM}}^\dagger \Rightarrow$$



$$R_b = \left(1 - \frac{\lambda^2}{2}\right) \frac{1}{\lambda} \left| \frac{V_{ub}}{V_{cb}} \right|$$

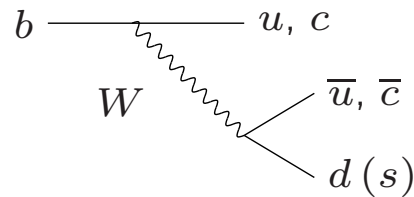
$$R_t = \frac{1}{\lambda} \left| \frac{V_{td}}{V_{cb}} \right|$$

$$\bar{\rho} \equiv (1 - \lambda^2/2)\rho, \quad \bar{\eta} \equiv (1 - \lambda^2/2)\eta$$

→ NLO corrections  
[Buras *et al.* (1994)]

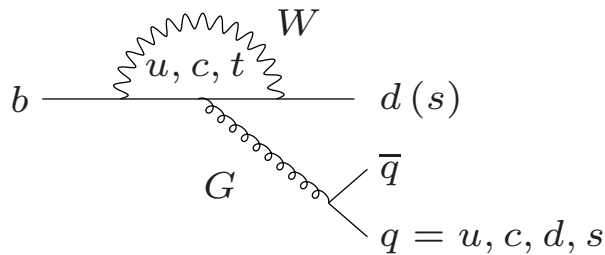
# Key Processes for CP Violation: Non-Leptonic $B$ Decays

- Tree diagrams:

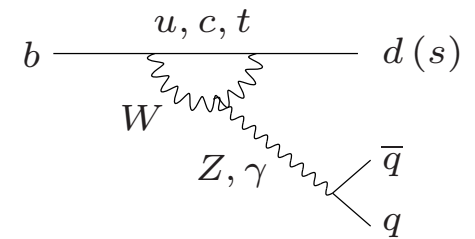
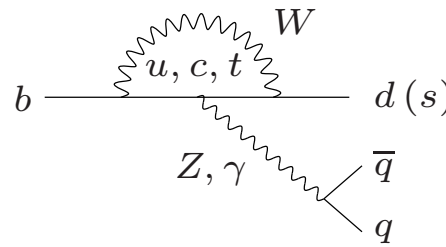


- Penguin diagrams:

- ◊ QCD penguins:



- ◊ Electroweak (EW) penguins:



- The calculation of the decay amplitudes is theoretically very challenging:

$$A(B \rightarrow f) \sim \sum_k \underbrace{C_k(\mu)}_{\text{pert. QCD}} \times \underbrace{\langle f | Q_k(\mu) | B \rangle}_{\text{"unknown"}}$$

[Details and recent progress → talk by Martin Beneke]



... but calculation of  $\langle f | Q_k(\mu) | B \rangle$  can be circumvented:

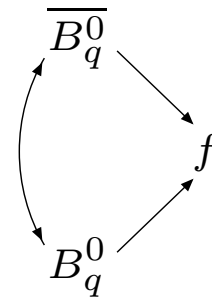
- Amplitude relations allow us in fortunate cases to eliminate the hadronic matrix elements ( $\rightarrow$  typically strategies to determine the UT angle  $\gamma$ ):

- Exact relations: class of pure “tree” decays (e.g.  $B \rightarrow DK$ ).
- Approximate relations, which follow from the flavour symmetries of strong interactions, i.e.  $SU(2)$  isospin or  $SU(3)_F$ :

$$B \rightarrow \pi\pi, B \rightarrow \pi K, B_{(s)} \rightarrow KK.$$

- Decays of neutral  $B_d$  and  $B_s$  mesons:

Interference effects through  $B_q^0 - \bar{B}_q^0$  mixing:



- Lead to “mixing-induced” CP violation  $\mathcal{A}_{\text{CP}}^{\text{mix}}$ !
- If one CKM amplitude dominates:

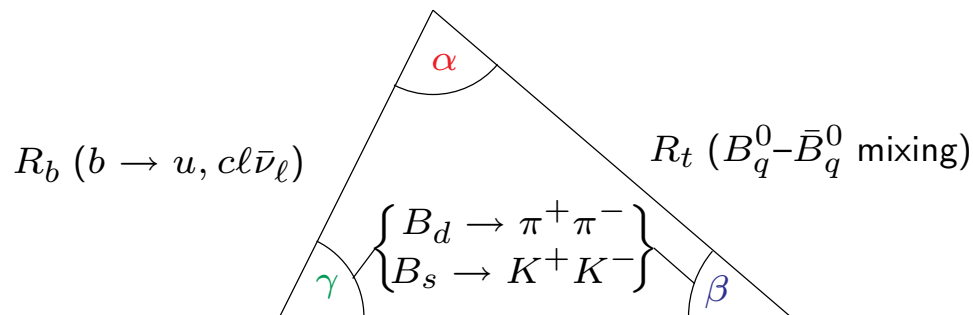
$\Rightarrow$  *hadronic matrix elements cancel!*

\* Example:  $B_d^0 \rightarrow J/\psi K_S \Rightarrow \sin 2\beta$  [Bigi, Carter & Sanda ('80–'81)]

# A Brief Roadmap of Quark-Flavour Physics

- CP-B studies through various processes and strategies:

$$B \rightarrow \pi\pi \text{ (isospin), } B \rightarrow \rho\pi, B \rightarrow \rho\rho$$



$$B \rightarrow \pi K \text{ (penguins)}$$

$$B_d \rightarrow \psi K_S \text{ (} B_s \rightarrow \psi\phi : \phi_s \approx 0 \text{)}$$

$$\left. \begin{array}{l} B_u^\pm \rightarrow K^\pm D \\ B_d \rightarrow K^{*0} D \\ B_c^\pm \rightarrow D_s^\pm D \end{array} \right\} \text{ only trees}$$

$$B_d \rightarrow \phi K_S \text{ (pure penguin)}$$

$$\left. \begin{array}{l} B_d \rightarrow D^{(*)\pm} \pi^\mp : \gamma + 2\beta \\ B_s \rightarrow D_s^\pm K^\mp : \gamma + \phi_s \end{array} \right\} \text{ only trees}$$

- Moreover “rare” decays:  $B \rightarrow X_s \gamma, B_{d,s} \rightarrow \mu^+ \mu^-, K \rightarrow \pi \nu \bar{\nu}, \dots$ 
  - Originate from loop processes in the SM. [ $\rightarrow$  talk by A. Weiler]
  - Interesting correlations with CP-B studies.

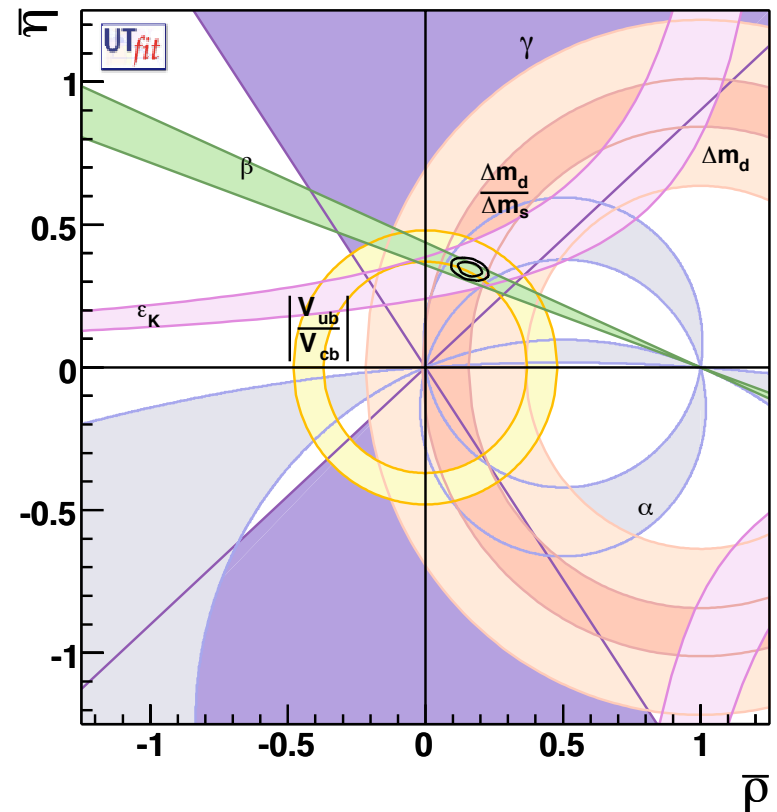
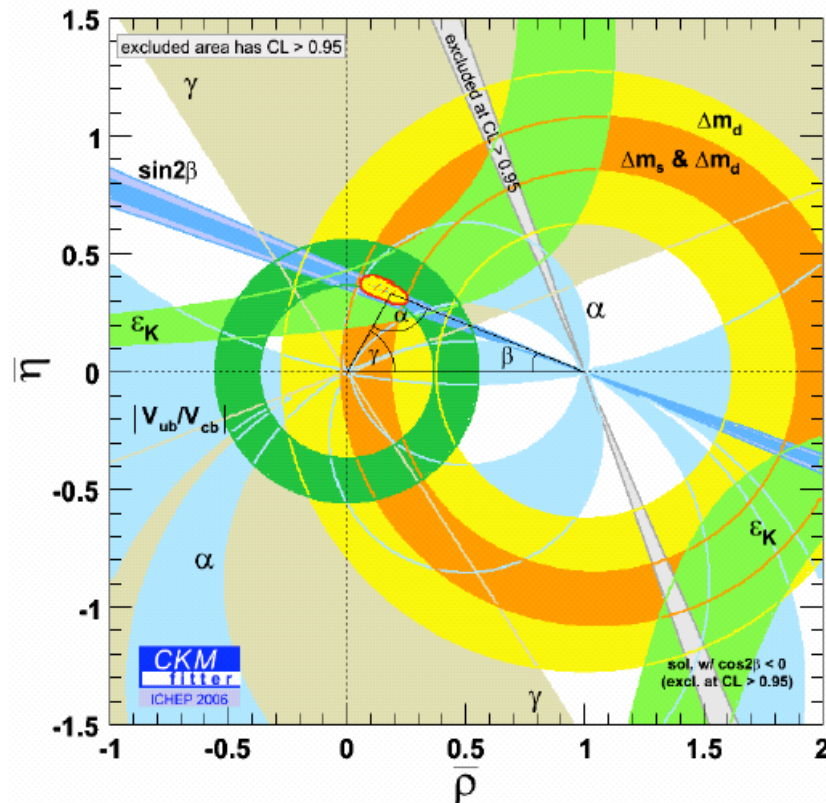
New Physics

$\Rightarrow$

Discrepancies

# Status of the Unitarity Triangle

- Two competing groups: → many plots & correlations ...
  - *CKMfitter* Collaboration [<http://ckmfitter.in2p3.fr/>];
  - *UTfit* Collaboration [<http://www.utfit.org/>]:



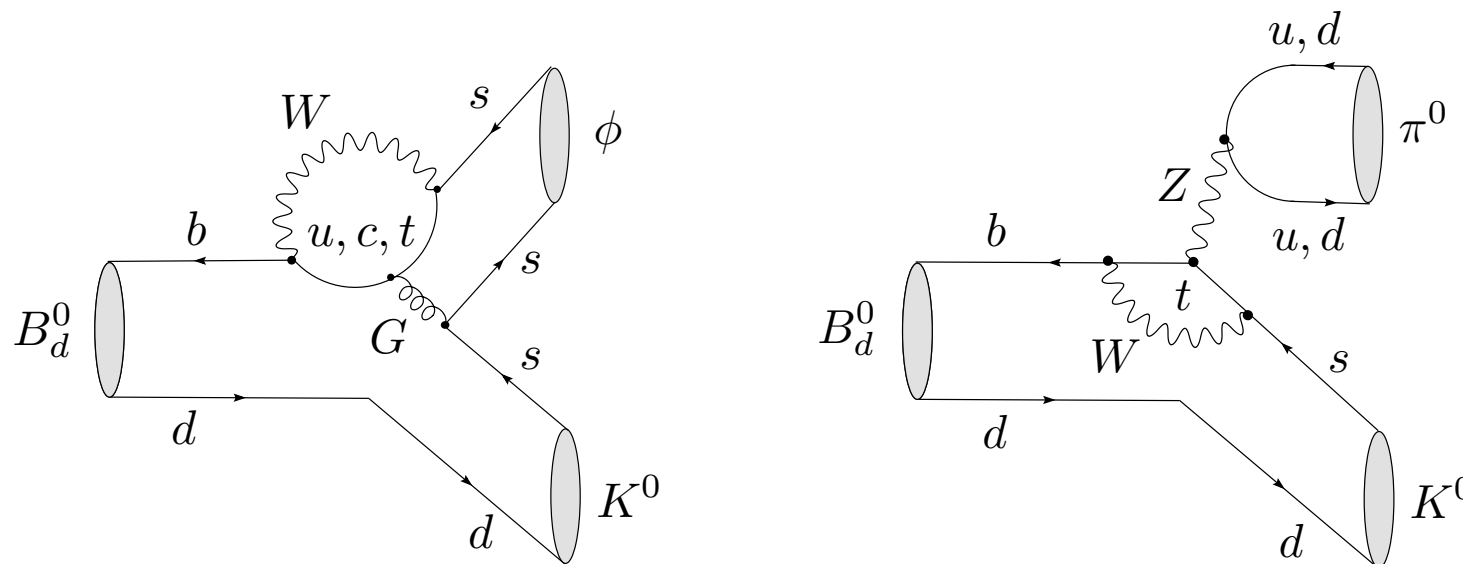
⇒ impressive global agreement with KM, but no longer “perfect” ...

A Brief Look  
at the Current  
*B*-Factory Data:

Two popular avenues for New Physics to manifest itself ...

# 1. New Physics @ Amplitude Level:

- Typically *small* effects if SM tree processes play the dominant rôle.
- Potentially *large* effects in the penguin sector through new particles in the loops or new contributions at the tree level: e.g. SUSY,  $Z'$  models.



→ hot topics ...

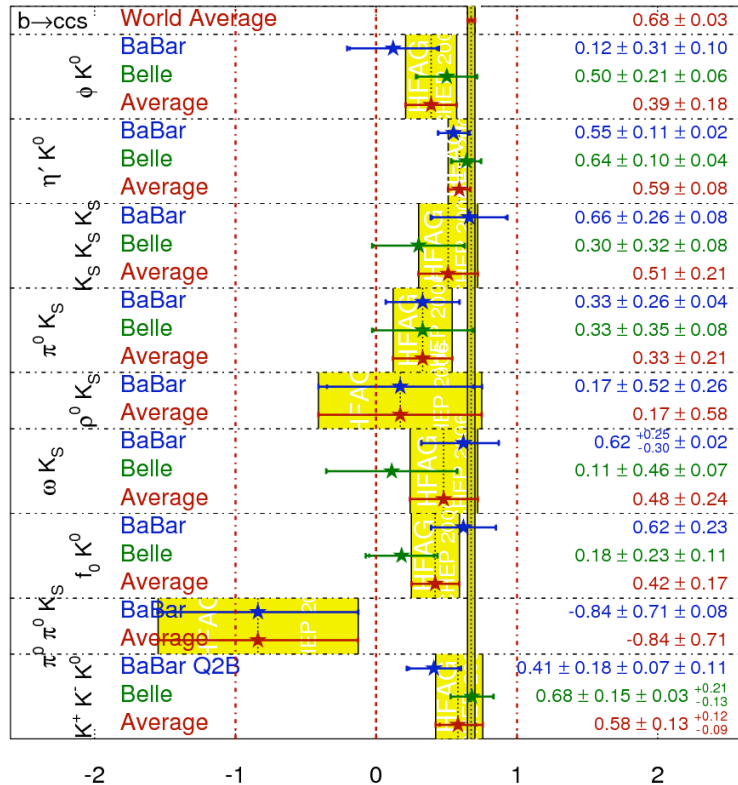
# CP Violation in $b \rightarrow s$ Penguin Modes

- $B_d \rightarrow \phi K_S$  is the key example: amplitude structure of the SM  $\Rightarrow$

$$(\sin 2\beta)_{\phi K_S} = (\sin 2\beta)_{\psi K_S} + \mathcal{O}(\lambda^2), \quad \mathcal{A}_{\text{CP}}^{\text{dir}}(B_d \rightarrow \phi K_S) = 0 + \mathcal{O}(\lambda^2)$$

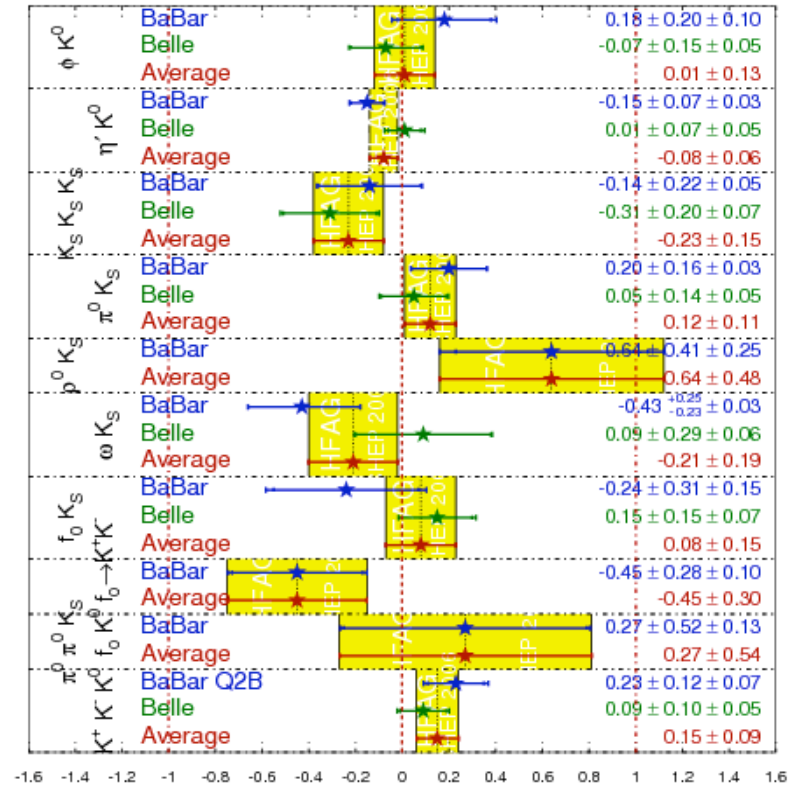
Preliminary

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}}) \quad \text{HFAG ICHEP 2006 PRELIMINARY}$$



$$C_f = -A_f$$

HFAG ICHEP 2006 PRELIMINARY

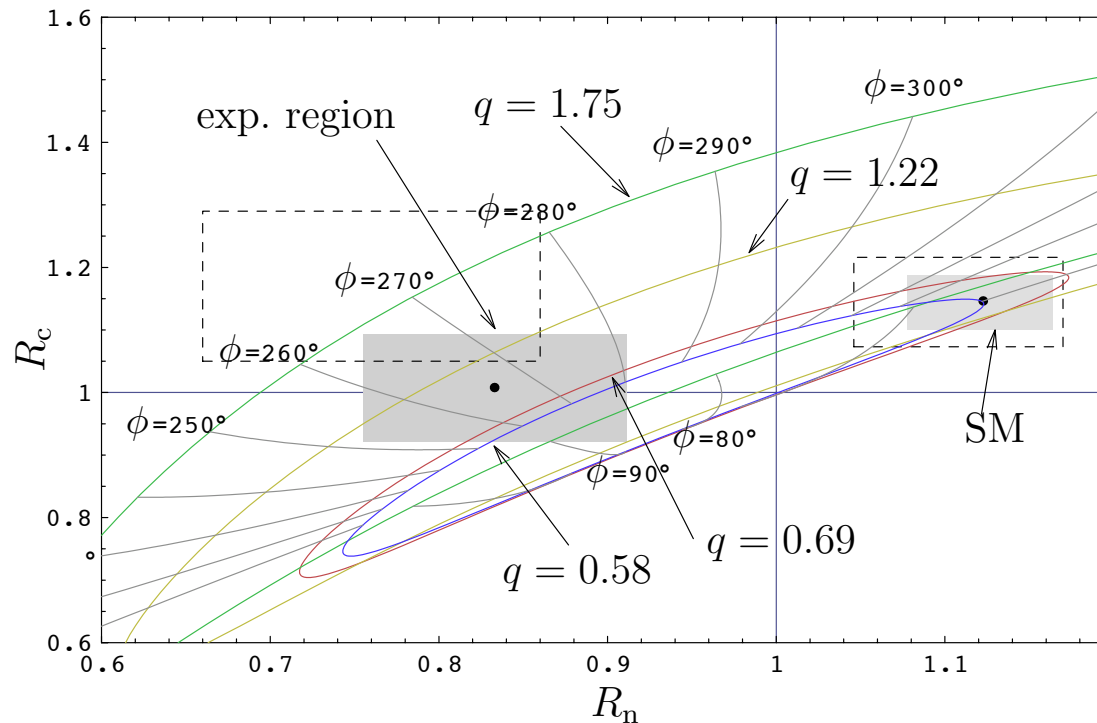


NP could be present, but still cannot be resolved  $\rightarrow$  stay tuned ...

# The $B \rightarrow \pi K$ Puzzle

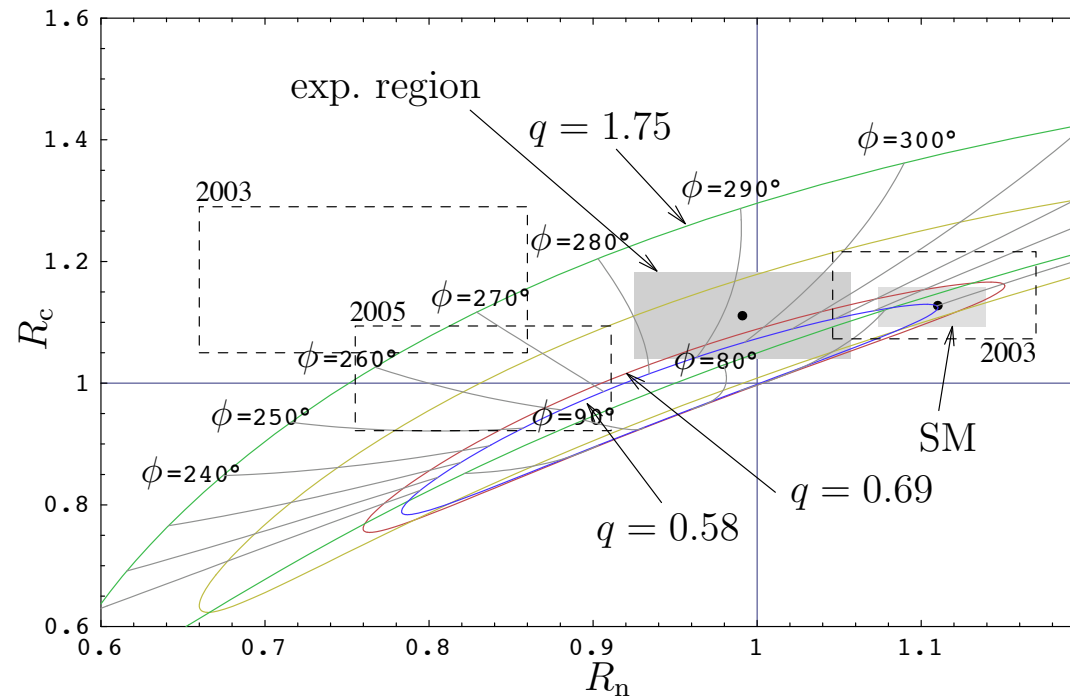
- Observables with a sizeable impact of EW penguins:  $\rightarrow$  parameters  $q, \phi$

$$\left. \begin{aligned}
 R_c &\equiv 2 \left[ \frac{\text{BR}(B^+ \rightarrow \pi^0 K^+) + \text{BR}(B^- \rightarrow \pi^0 K^-)}{\text{BR}(B^+ \rightarrow \pi^+ K^0) + \text{BR}(B^- \rightarrow \pi^- \bar{K}^0)} \right] \\
 R_n &\equiv \frac{1}{2} \left[ \frac{\text{BR}(B_d^0 \rightarrow \pi^- K^+) + \text{BR}(\bar{B}_d^0 \rightarrow \pi^+ K^-)}{\text{BR}(B_d^0 \rightarrow \pi^0 K^0) + \text{BR}(\bar{B}_d^0 \rightarrow \pi^0 \bar{K}^0)} \right]
 \end{aligned} \right\} \rightarrow \text{NP in EWPs!}$$



[A.J. Buras, R.F., F. Schwab & S. Recksiegel ('03-'05)]

- (Preliminary) Status after ICHEP '06:



- The SM prediction is very stable, with further reduced errors!
- The  $B$ -factory data have moved quite a bit towards the SM.
- Suggested by constraints from rare  $B \rightarrow X_s \ell^+ \ell^-$  decays ...

- Furthermore puzzling CP asymmetries:  $B_d^0 \rightarrow \pi^0 K_S$ ,  $B^\pm \rightarrow \pi^0 K^\pm$ .

⊕ correlations with rare  $B$  and  $K$  decays

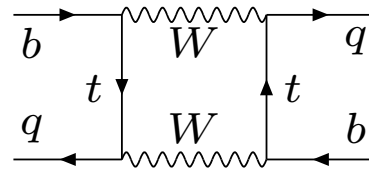
NP could be present, but still cannot be resolved

 → stay tuned ...



## 2. New Physics in $B_q^0-\bar{B}_q^0$ mixing:

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- NP particles in boxes or tree contributions (e.g. SUSY,  $Z'$  models):

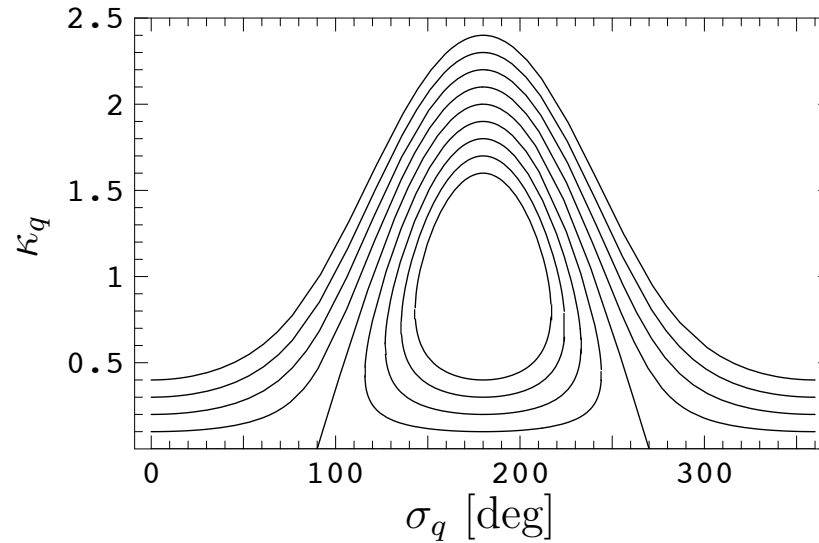
$$\boxed{M_{12}^q = M_{12}^{q,\text{SM}} (1 + \kappa_q e^{i\sigma_q})} \Rightarrow$$

- Mass difference:  $\Delta M_q = \Delta M_q^{\text{SM}} |1 + \kappa_q e^{i\sigma_q}|$
- Mixing phase:  $\phi_q = \phi_q^{\text{SM}} + \phi_q^{\text{NP}} = \phi_q^{\text{SM}} + \arg(1 + \kappa_q e^{i\sigma_q})$

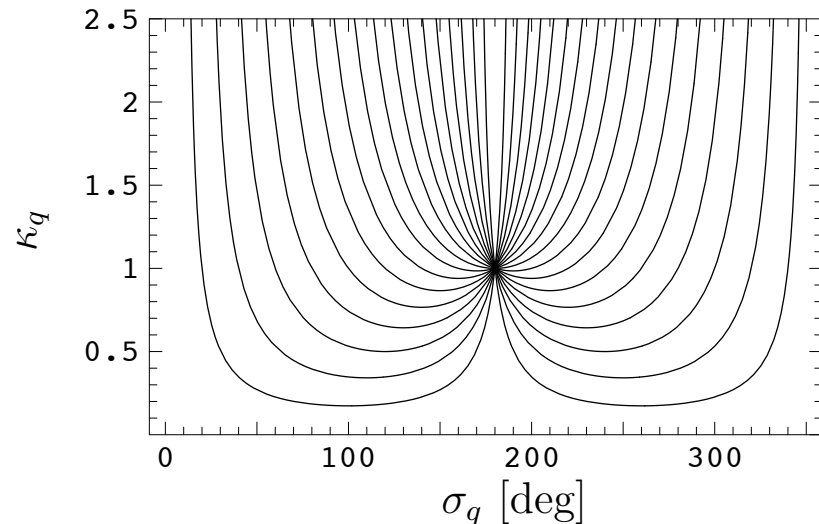
[Details: P. Ball & R.F., hep-ph/0604249]

# Constraints in the NP Space of $B_q^0-\bar{B}_q^0$ Mixing

- Contours in the  $\sigma_q-\kappa_q$  plane following from  $\rho_q \equiv \Delta M_q/\Delta M_q^{\text{SM}}$ :



- Contours in the  $\sigma_q-\kappa_q$  plane following from the NP phase  $\phi_q^{\text{NP}}$ :



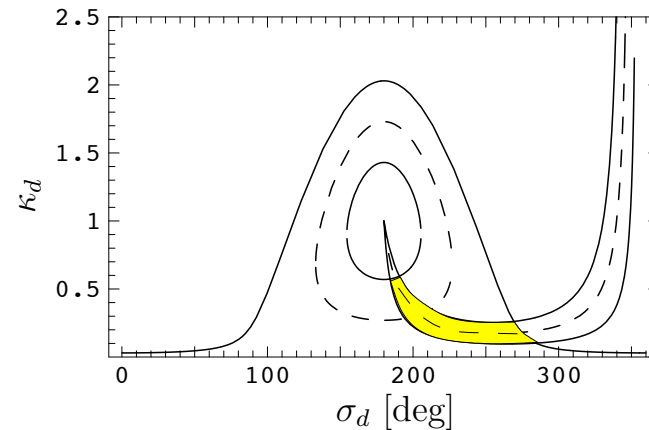
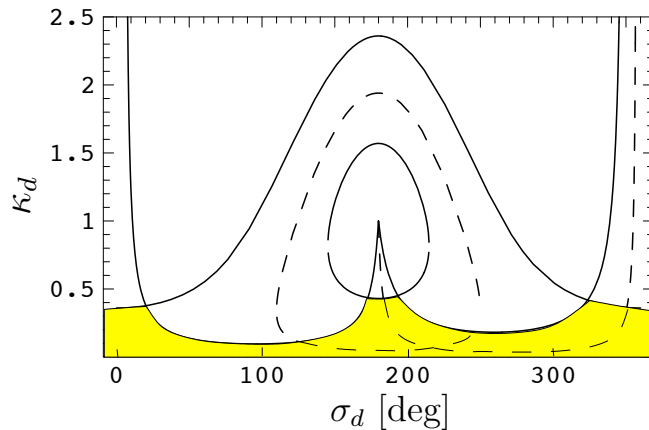
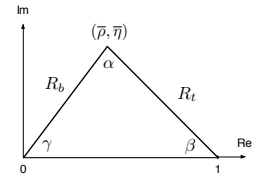
# Implications of the $B$ -Factory Data for the $B_d$ System

- Determination of  $\rho_d = \Delta M_d / \Delta M_d^{\text{SM}}$ :  $\rightarrow$   $\Delta M_d^{\text{SM}}$  required, involving ...

- CKM parameter  $|V_{td}^* V_{tb}|$ :  $\rightarrow$  governed by  $\gamma$ , if unitarity is used.
- Hadronic parameter  $f_{B_d}^2 \hat{B}_{B_d}$ : lattice  $\rightarrow$  two benchmark sets:
  - \* JLQCD results (2 flavours of dynamical light Wilson quarks).
  - \*  $f_{B_d}$  from HPQCD (3 dynamical flavours) with  $\hat{B}_{B_d}$  from JLQCD.

- Determination of the NP phase:  $\rightarrow$   $\phi_d^{\text{NP}} = (2\beta)_{\psi K_S} - (2\beta)_{\text{tree}}$

- $\phi_d^{\text{NP}}$  is governed by  $R_b \propto |V_{ub}/V_{cb}|$ ;
- Unfortunately, discrepancy between  $|V_{ub}|_{\text{excl}}$  and  $|V_{ub}|_{\text{incl}}$  ...



JLQCD and  $\phi_d^{\text{NP}}|_{\text{excl}} = -(2.5 \pm 8.0)^\circ$       (HP+JL)QCD and  $\phi_d^{\text{NP}}|_{\text{incl}} = -(10.1 \pm 4.6)^\circ$

# Key Targets of the *B* Physics Programme at the LHC

→ high statistics and *complementarity* to *B* factories:

*fully exploit the  $B_s$ -meson system!*

# General Features of the $B_s$ System

- Rapid  $B_s^0-\bar{B}_s^0$  oscillations:  $\Delta M_s \stackrel{\text{SM}}{=} \mathcal{O}(20 \text{ ps}^{-1}) \gg \Delta M_d \stackrel{\text{exp}}{=} 0.5 \text{ ps}^{-1}$

$\Rightarrow$  challenging to resolve them experimentally!

- The width difference  $\Delta\Gamma_s$  is expected to be of  $\mathcal{O}(10\%)$ : [ $\rightarrow$  talk by A. Lenz]

– Experimental status:  $B_s \rightarrow J/\psi\phi$  @ Tevatron  $\Rightarrow$

$$\frac{\Delta\Gamma_s}{\Gamma_s} = \left\{ \begin{array}{ll} 0.24_{-0.38}^{+0.28+0.03} & [\text{D0 ('05)}] \\ 0.65_{-0.33}^{+0.25} \pm 0.01 & [\text{CDF ('05)}] \end{array} \right\} \xrightarrow{\text{LHCb}} \boxed{\text{precision} \sim 0.01}$$

– May provide interesting CPV studies through “untagged” rates:

$$\langle \Gamma(B_s(t) \rightarrow f) \rangle \equiv \Gamma(B_s^0(t) \rightarrow f) + \Gamma(\bar{B}_s^0(t) \rightarrow f)$$

\* The rapidly oscillating  $\Delta M_s t$  terms cancel!

\* Various “untagged” strategies were proposed.

[Dunietz ('95); R.F. & Dunietz ('96); Dunietz, Dighe & R.F. ('99); ...]

- The CP-violating phase of  $B_s^0-\bar{B}_s^0$  mixing is *tiny* in the SM:

$$\boxed{\phi_s \stackrel{\text{SM}}{=} -2\lambda^2\eta \approx -2^\circ} \Rightarrow \text{interesting for NP searches (see below)!}$$

# Hot News of this Spring:

- Signals for  $B_s^0-\bar{B}_s^0$  mixing at the Tevatron:
  - For many years, only lower bounds on  $\Delta M_s$  were available from the LEP (CERN) experiments and SLD (SLAC)!
  - Finally, the value of  $\Delta M_s$  could be pinned down: [ $\rightarrow$  talk by S. Menzemer]
    - \* D0:  $\Rightarrow$  two-sided bound  $17 \text{ ps}^{-1} < \Delta M_s < 21 \text{ ps}^{-1}$  (90% C.L.)  
 $\Rightarrow 2.5 \sigma$  signal at  $\Delta M_s = 19 \text{ ps}^{-1}$
    - \* CDF:  $\Delta M_s = [17.77 \pm 0.10(\text{stat}) \pm 0.07(\text{syst})] \text{ ps}^{-1} \gtrsim 5\sigma$
- These new results have already triggered considerable theoretical activity:

M. Carena *et al.*, hep-ph/0603106; M. Ciuchini and L. Silvestrini, hep-ph/0603114; L. Velasco-Sevilla, hep-ph/0603115; M. Endo and S. Mishima, hep-ph/0603251; M. Blanke *et al.*, hep-ph/0604057; Z. Ligeti, M. Papucci and G. Perez, hep-ph/0604112; J. Foster, K.I. Okumura and L. Roszkowski, hep-ph/0604121; K. Cheung *et al.*, hep-ph/0604223; G. Isidori and P. Paradisi, hep-ph/0605012; S. Khalil, hep-ph/0605021; Y. Grossman, Y. Nir and G. Raz, hep-ph/0605028; S. Baek, J.H. Jeon and C.S. Kim, hep-ph/0607113; ...

# Space for NP

in the

$B_s$ -Meson System:

$$M_{12}^s = M_{12}^{s,\text{SM}} (1 + \kappa_s e^{i\sigma_s})$$

→ in analogy to the  $B_d$  system ...

[Details: P. Ball & R.F., hep-ph/0604249]

# Constraints on NP through $\Delta M_s$

- CKM unitarity and Wolfenstein expansion:  $|V_{ts}^* V_{tb}| = |V_{cb}| [1 + \mathcal{O}(\lambda^2)]$

$\Rightarrow$  no information on  $\gamma$  and  $R_b$  needed (in contrast to  $\Delta M_d$ )!

- Numerical results:

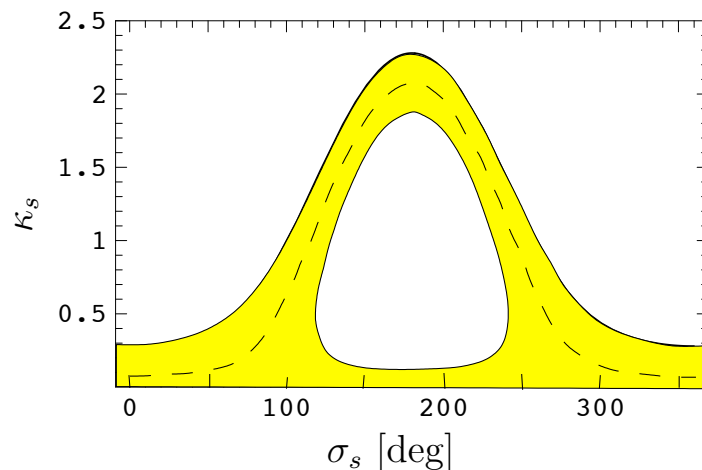
$$\Delta M_s^{\text{SM}} \Big|_{\text{JLQCD}} = (16.1 \pm 2.8) \text{ ps}^{-1}$$

$$\rho_s \equiv \Delta M_s / \Delta M_s^{\text{SM}} \Big|_{\text{JLQCD}} = 1.08_{-0.01}^{+0.03}(\text{exp}) \pm 0.19(\text{th})$$

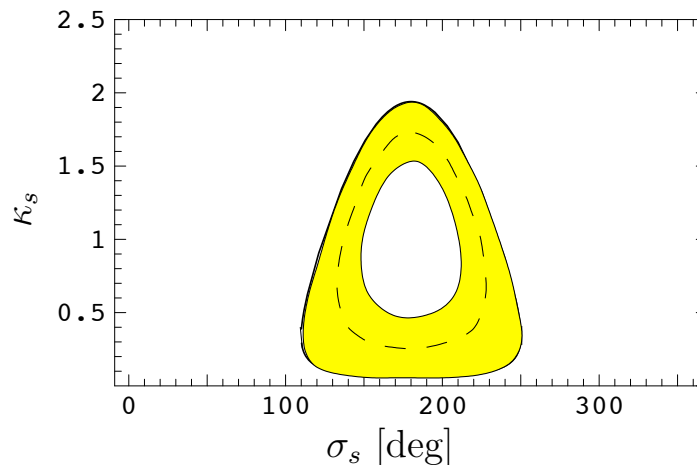
$$\Delta M_s^{\text{SM}} \Big|_{(\text{HP+JL})\text{QCD}} = (23.4 \pm 3.8) \text{ ps}^{-1}$$

$$\rho_s \Big|_{(\text{HP+JL})\text{QCD}} = 0.74_{-0.01}^{+0.02}(\text{exp}) \pm 0.18(\text{th})$$

- Allowed regions in the  $\sigma_s - \kappa_s$  plane:



JLQCD



(HP+JL)QCD



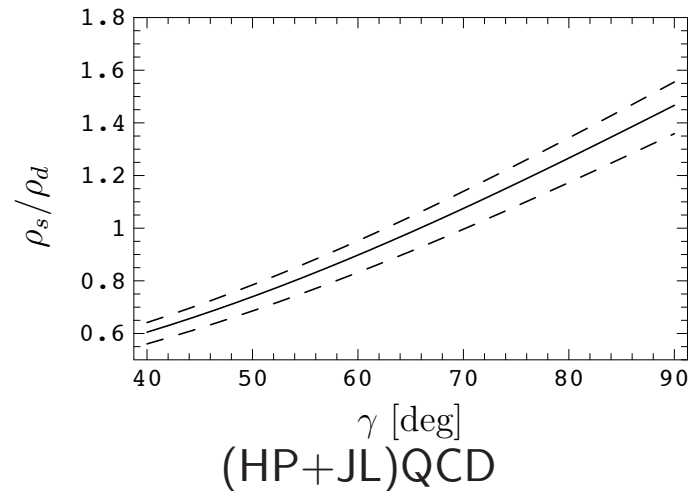
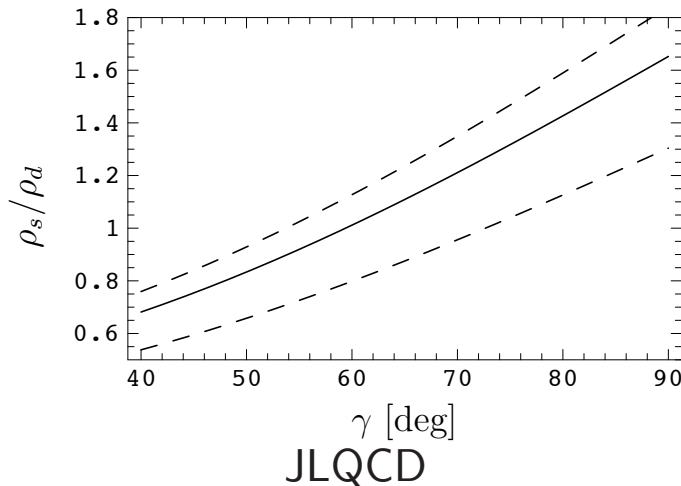
# Constraints on NP through $\Delta M_s$ and $\Delta M_d$

- The ratio  $\Delta M_s/\Delta M_d$  involves just an  $SU(3)$ -breaking parameter:

$$\xi \equiv \frac{f_{B_s} \hat{B}_{B_s}^{1/2}}{f_{B_d} \hat{B}_{B_d}^{1/2}} \rightarrow \text{reduced th. uncertainty as compared to } f_{B_q} \hat{B}_{B_q}^{1/2}.$$

- Usually determination of UT side  $R_t$ . Different avenue (CKM unitarity):<sup>3</sup>

$$\frac{\rho_s}{\rho_d} = \lambda^2 \underbrace{\left[1 - 2R_b \cos \gamma + R_b^2\right]}_{=R_t^2} \left[1 + \mathcal{O}(\lambda^2)\right] \frac{1}{\xi^2} \frac{M_{B_d} \Delta M_s}{M_{B_s} \Delta M_d}$$



$$\rightarrow \left. \frac{\rho_s}{\rho_d} \right|_{2010} = 1.07 \pm 0.09(\gamma)_{-0.08}^{+0.06}(\xi) = 1.07 \pm 0.12 \Rightarrow \boxed{! ?}$$

<sup>3</sup>Scenario for 2010:  $\gamma = (65 \pm 20)^\circ \xrightarrow{\text{LHCb}} (70 \pm 5)^\circ$  with (HP+JL)QCD lattice values.

# Golden Process to Search

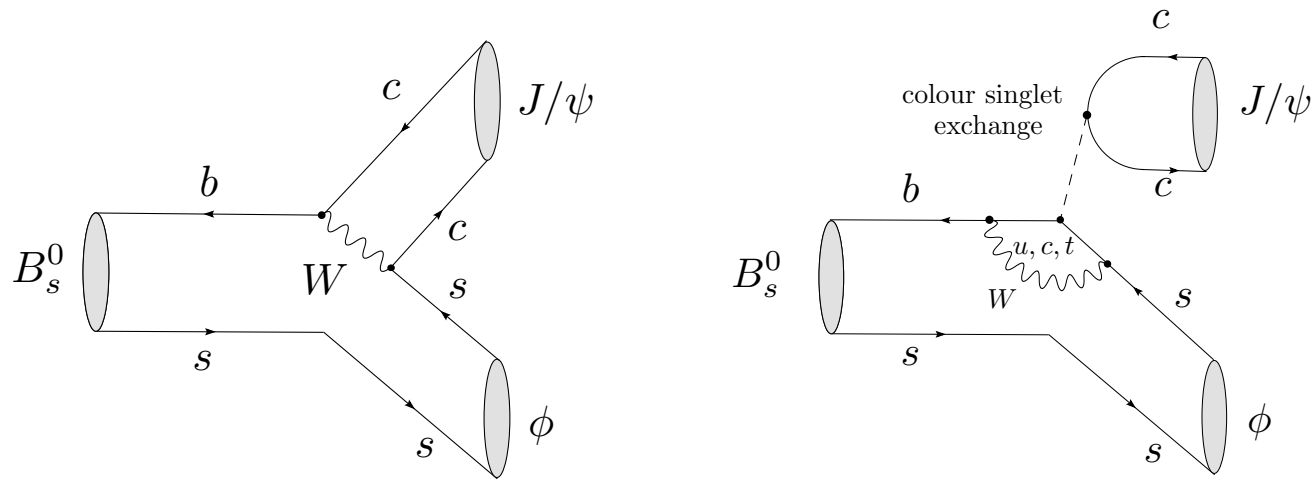
for NP in  $B_s^0 - \bar{B}_s^0$  Mixing:

$$B_s^0 \rightarrow J/\psi\phi$$

$\rightarrow B_s^0$  counterpart of  $B_d^0 \rightarrow J/\psi K_S \dots$

[Dighe, Dunietz & R.F. (1999); Dunietz, R.F. & Nierste (2001)]

## Let's have a closer look ...



- There is an important difference with respect to  $B_d^0 \rightarrow J/\psi K_S$ :

final state is an admixture of different CP eigenstates!

- Angular distribution of the  $J/\psi[\rightarrow \ell^+\ell^-]\phi[\rightarrow K^+K^-]$  decay products:

$\Rightarrow$  the different CP eigenstates can be disentangled!

- Linear polarization amplitudes:  $A_0(t), A_{\parallel}(t), A_{\perp}(t)$

- $A_0(t)$  and  $A_{\parallel}(t)$  correspond to CP-even final-state configurations;
- $A_{\perp}(t)$  describes a CP-odd final-state configuration.

# Simple: Time-Dependent One-Angle Distribution

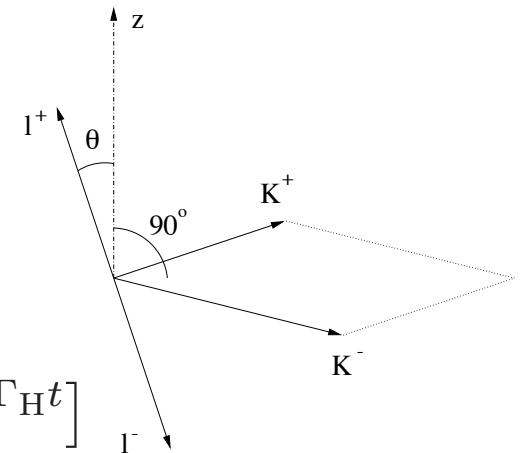
$$\frac{d\Gamma(t)}{d \cos \Theta} \propto \underbrace{(|A_0(t)|^2 + |A_{\parallel}(t)|^2)}_{\text{CP even}} \frac{3}{8} (1 + \cos^2 \Theta) + \underbrace{|A_{\perp}(t)|^2}_{\text{CP odd}} \frac{3}{4} \sin^2 \Theta$$

- The angular dependence allows us to extract the following observables:

$$P_+(t) \equiv |A_0(t)|^2 + |A_{\parallel}(t)|^2, \quad P_-(t) \equiv |A_{\perp}(t)|^2$$

- Untagged data samples: → untagged rates ...

$$P_{\pm}(t) + \bar{P}_{\pm}(t) \propto [(1 \pm \cos \phi_s) e^{-\Gamma_L t} + (1 \mp \cos \phi_s) e^{-\Gamma_H t}]$$



- Tagged data samples: → CP asymmetries ...

$$\frac{P_{\pm}(t) - \bar{P}_{\pm}(t)}{P_{\pm}(t) + \bar{P}_{\pm}(t)} = \pm \frac{2 \sin(\Delta M_s t) \sin \phi_s}{(1 \pm \cos \phi_s) e^{+\Delta \Gamma_s t/2} + (1 \mp \cos \phi_s) e^{-\Delta \Gamma_s t/2}}$$

## Comments

$$\boxed{\phi_s = -2\lambda^2 R_b \sin \gamma + \phi_s^{\text{NP}} \approx \phi_s^{\text{NP}}} \Rightarrow$$

- CP-violating NP effects would be indicated by the following features:
  - The *untagged* observables depend on *two* exponentials;
  - *sizeable* values of the CP-violating asymmetries.
- These general features hold also for the full *three-angle* distribution:
  - Much more involved than one-angle case [Dighe, Dunietz & R.F. (1999)].
  - But provides additional information through the following terms:
$$\text{Re}\{A_0^*(t)A_{\parallel}(t)\}, \quad \text{Im}\{A_f^*(t)A_{\perp}(t)\} \quad (f \in \{0, \parallel\}).$$
  - No experimental draw-back with respect to the one-angle case!
- Following these lines,  $\Delta\Gamma_s$  (see above) and  $\phi_s$  can be extracted:
  - Note:  $\Delta\Gamma_s = \Delta\Gamma_s^{\text{SM}} \cos \phi_s$  [Grossman (1996)]  $\Rightarrow$  *reduction* of  $\Delta\Gamma_s$ .

# News from the Tevatron & Reach at the LHC

- Very recent (preliminary) analysis by D0: [D0Conference note 5144 ('06)]

– Untagged, time-dependent three-angle  $B_s \rightarrow J/\psi\phi$  distribution:

$$\Rightarrow \phi_s = -0.79 \pm 0.56 \text{ (stat.)} \pm 0.01 \text{ (syst.)} = -(45 \pm 32 \pm 0.6)^\circ$$

– Imposing also constraints from semilept.  $B$  decays: [D0note 5144-Conf ('06)]

$$\Rightarrow \phi_s = -0.56_{-0.41}^{+0.44} = -(32_{-23}^{+25})^\circ$$

$\Rightarrow$  still not stringently constrained, but very accessible @ LHC ...

- Experimental reach at the LHC: [O. Schneider, M. Smizanska, T. Speer]

– LHCb:  $\sigma_{\text{stat}}(\sin \phi_s) \approx 0.031$  (1 year, i.e.  $2 \text{ fb}^{-1}$ ) [0.013 (5 years)];

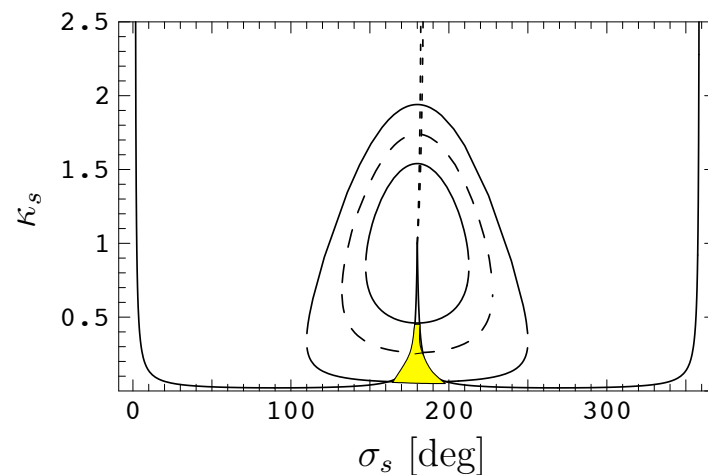
– ATLAS & CMS: expect uncertainties of  $\mathcal{O}(0.1)$  (1 year, i.e.  $10 \text{ fb}^{-1}$ ).

# Impact of CP Violation Measurements on $\sigma_s, \kappa_s$

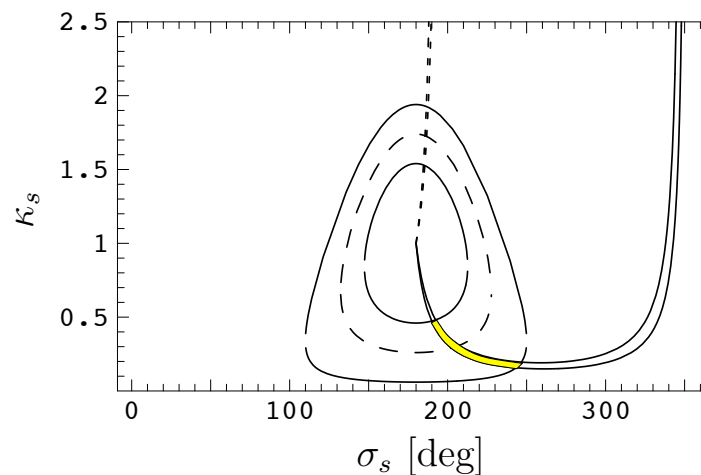
- Illustration through two scenarios ( $\sim 2010$ ):

(i)  $(\sin \phi_s)_{\text{exp}} = -0.04 \pm 0.02$ : corresponds to the SM;

(ii)  $(\sin \phi_s)_{\text{exp}} = -0.20 \pm 0.02$ :  $\rightarrow$  NP @  $10\sigma$  [corresponds to the “tension” in the UT fits for  $\kappa_s = \kappa_d, \sigma_s = \sigma_d \rightarrow$  “magnification” in the  $B_s$  system]



SM scenario (i)



NP scenario (ii)

- Remarks:

- It is very challenging to establish NP without new CP-violating effects.
- But the data still leave a lot of space for such effects in specific NP scenarios (SUSY,  $Z'$ , ...), which could be detected at the LHC!

[Details: P. Ball & R.F., hep-ph/0604249  $\oplus$  references therein]

# Further Benchmark Decays

for the

LHCb Experiment

→ very rich physics programme ...



# Two Major Lines of Research

## 1. Precision measurements of $\gamma$ :

- Tree strategies, with expected sensitivities after 1 year of taking data:

- $B_s^0 \rightarrow D_s^\mp K^\pm$ :  $\sigma_\gamma \sim 14^\circ$

- $B_d^0 \rightarrow D^0 K^*$ :  $\sigma_\gamma \sim 8^\circ$  ... to be compared with the

- $B^\pm \rightarrow D^0 K^\pm$ :  $\sigma_\gamma \sim 5^\circ$

current  $B$ -factory data:  $\gamma|_{D^{(*)}K^{(*)}} = \begin{cases} (62_{-25}^{+35})^\circ & \text{(CKMfitter)} \\ (65 \pm 20)^\circ & \text{(UTfit)} \end{cases}$

- Decays with penguin contributions:

- $B_s^0 \rightarrow K^+ K^-$  and  $B_d^0 \rightarrow \pi^+ \pi^-$ :  $\sigma_\gamma \sim 5^\circ$

- $B_s^0 \rightarrow D_s^+ D_s^-$  and  $B_d^0 \rightarrow D_d^+ D_d^-$

## 2. Analyses of rare decays which are absent at the SM tree level:

- $B_s^0 \rightarrow \mu^+ \mu^-$ ,  $B_d^0 \rightarrow \mu^+ \mu^-$

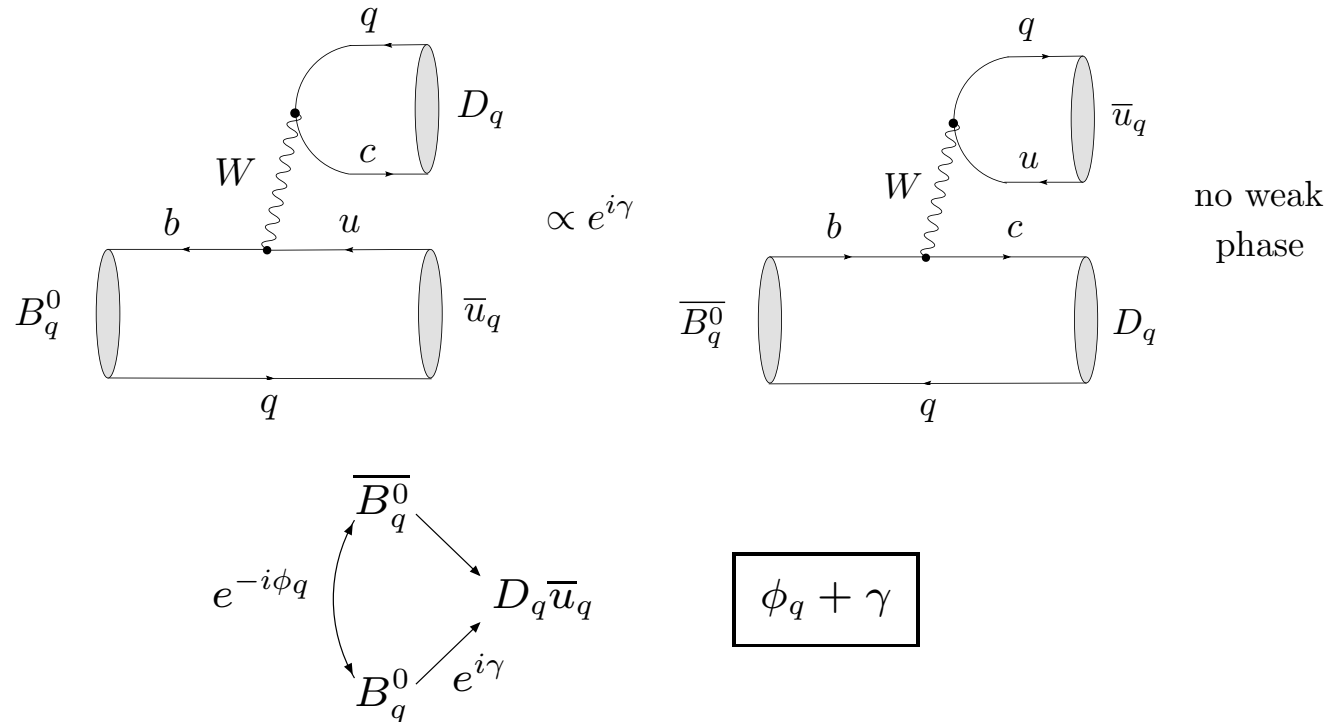
- $B_d^0 \rightarrow K^{*0} \mu^+ \mu^-$ ,  $B_s^0 \rightarrow \phi \mu^+ \mu^-$ ; ...

→ let's have a closer look at some decays ...

[For a recent experimental overview, see A. Schopper, hep-ex/0605113]

# CP Violation in $B_s \rightarrow D_s^\pm K^\mp$ and $B_d \rightarrow D^\pm \pi^\mp$

- General case:



- $q = s$ :  $D_s \in \{D_s^+, D_s^{*+}, \dots\}$ ,  $u_s \in \{K^+, K^{*+}, \dots\}$ :

→ hadronic parameter  $X_s e^{i\delta_s} \propto R_b \Rightarrow$  large interference effects!

- $q = d$ :  $D_d \in \{D^+, D^{*+}, \dots\}$ ,  $u_d \in \{\pi^+, \rho^+, \dots\}$ :

→ hadronic parameter  $X_d e^{i\delta_d} \propto -\lambda^2 R_b \Rightarrow$  tiny interference effects!

- $\cos(\Delta M_q t)$  and  $\sin(\Delta M_q t)$  terms of the time-dependent decay rates:

$$\Rightarrow \boxed{\text{theoretically clean determination of } \phi_q + \gamma} \quad \phi_q \text{ known} \longrightarrow \boxed{\gamma}$$

[Dunietz & Sachs (1988); Aleksan, Dunietz & Kayser (1992); Dunietz (1998); ...]

- However, there are also problems:

- We encounter an *eightfold* discrete ambiguity for  $\phi_q + \gamma$ !?
- In the  $q = d$  case, an additional input is required to extract  $X_d$  since  $\mathcal{O}(X_d^2)$  interference effects would have to be resolved  $\rightarrow$  *impossilbe* ...

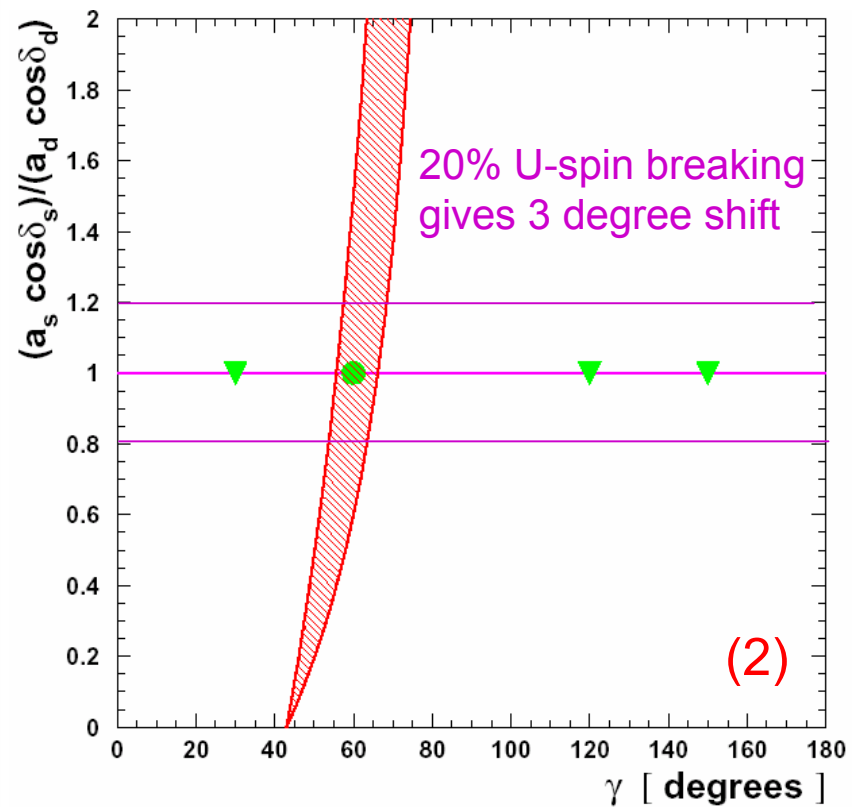
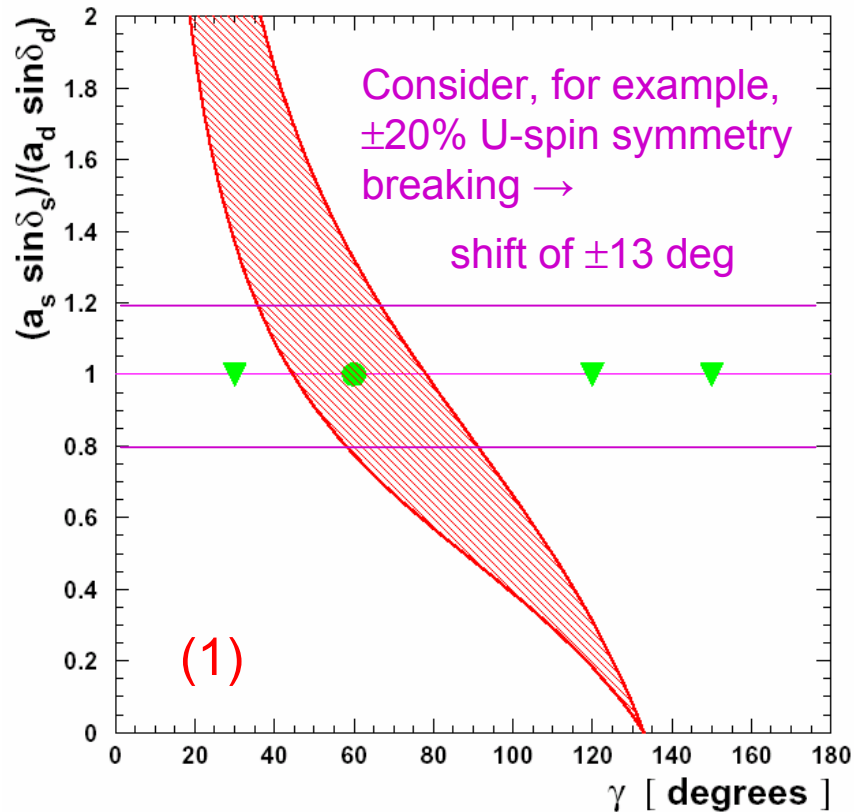
- Combined analysis of  $B_s^0 \rightarrow D_s^{(*)+} K^-$  and  $B_d^0 \rightarrow D^{(*)+} \pi^-$ : [R.F. (2003)]

$$\boxed{s \leftrightarrow d} \Rightarrow U\text{-spin symmetry provides an interesting playground:}^4$$

- An *unambiguous* value of  $\gamma$  can be extracted from the observables!
- To this end,  $X_d$  has *not* to be fixed, and  $X_s$  may *only* enter through a  $1 + X_s^2$  correction, which is determined through *untagged*  $B_s$  rates!
- Promising first studies by LHCb:  $\rightarrow$

<sup>4</sup>The  $U$ -spin is an  $SU(2)$  subgroup of the  $SU(3)_F$  flavour-symmetry group, connecting  $d$  and  $s$  quarks in analogy to the conventional isospin symmetry, which relates  $d$  and  $u$  quarks to each other.

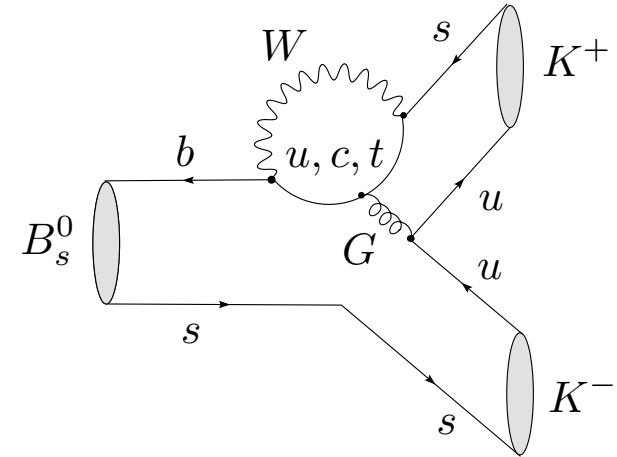
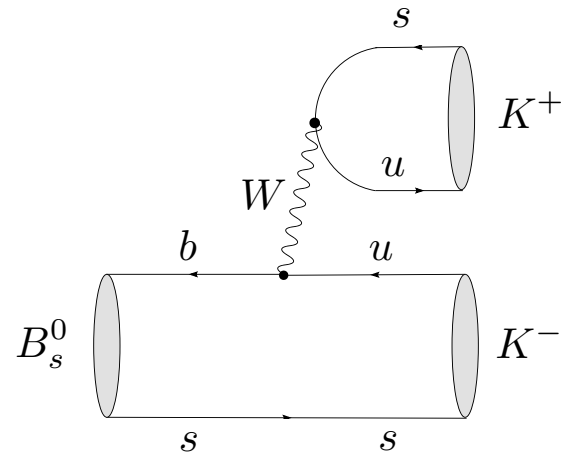
# Full U-Spin Symmetry: 5 years



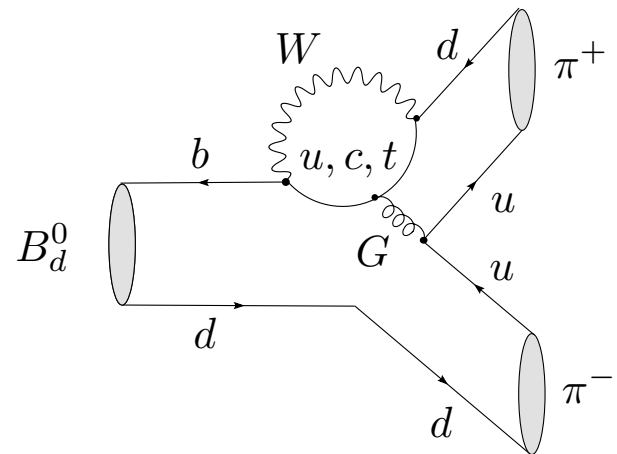
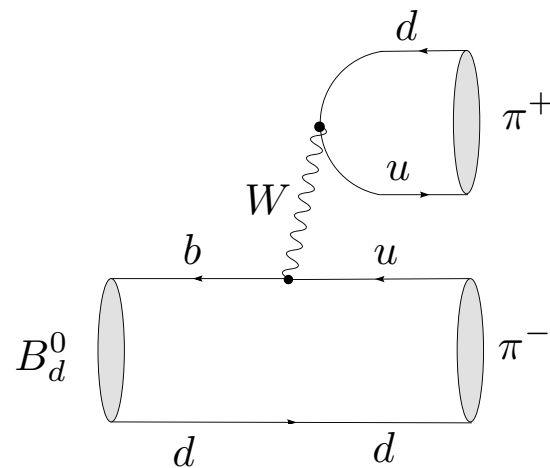
Both expressions now giving very interesting precision on  $\gamma$ .  
Right hand plot has precision of 5 degrees, and small systematic.  
Ambiguous solutions now excluded.

# The $B_s \rightarrow K^+K^-$ , $B_d \rightarrow \pi^+\pi^-$ System

- $B_s^0 \rightarrow K^+K^-$ :



- $B_d^0 \rightarrow \pi^+\pi^-$ :



$$\Rightarrow \boxed{s \leftrightarrow d}$$

- Structure of the decay amplitudes in the Standard Model:

$$A(B_d^0 \rightarrow \pi^+ \pi^-) \propto \left[ e^{i\gamma} - d e^{i\theta} \right]$$

$$A(B_s^0 \rightarrow K^+ K^-) \propto \left[ e^{i\gamma} + \left( \frac{1 - \lambda^2}{\lambda^2} \right) d' e^{i\theta'} \right]$$

$$d e^{i\theta} = \frac{\text{“penguin”}}{\text{“tree”}} \Big|_{B_d \rightarrow \pi^+ \pi^-}, \quad d' e^{i\theta'} = \frac{\text{“penguin”}}{\text{“tree”}} \Big|_{B_s \rightarrow K^+ K^-}$$

[ $d, d'$ : real hadronic parameters;  $\theta, \theta'$ : strong phases]

- General form of the CP asymmetries (time-dependent rate asymmetries):

$$\mathcal{A}_{\text{CP}}^{\text{dir}}(B_d \rightarrow \pi^+ \pi^-) = G_1(d, \theta, \gamma), \quad \mathcal{A}_{\text{CP}}^{\text{mix}}(B_d \rightarrow \pi^+ \pi^-) = G_2(d, \theta, \gamma, \phi_d)$$

$$\mathcal{A}_{\text{CP}}^{\text{dir}}(B_s \rightarrow K^+ K^-) = G'_1(d', \theta', \gamma), \quad \mathcal{A}_{\text{CP}}^{\text{mix}}(B_s \rightarrow K^+ K^-) = G'_2(d', \theta', \gamma, \phi_s)$$

- $\phi_d = 2\beta$  (from  $B_d \rightarrow J/\psi K_S$ ) and  $\phi_s \approx 0$  are known parameters:

$$- \mathcal{A}_{\text{CP}}^{\text{dir}}(B_d \rightarrow \pi^+ \pi^-) \quad \& \quad \mathcal{A}_{\text{CP}}^{\text{mix}}(B_d \rightarrow \pi^+ \pi^-): \Rightarrow \boxed{d = d(\gamma)} \quad (\text{clean!})$$

$$- \mathcal{A}_{\text{CP}}^{\text{dir}}(B_s \rightarrow K^+ K^-) \quad \& \quad \mathcal{A}_{\text{CP}}^{\text{mix}}(B_s \rightarrow K^+ K^-): \Rightarrow \boxed{d' = d'(\gamma)} \quad (\text{clean!})$$

- Example:

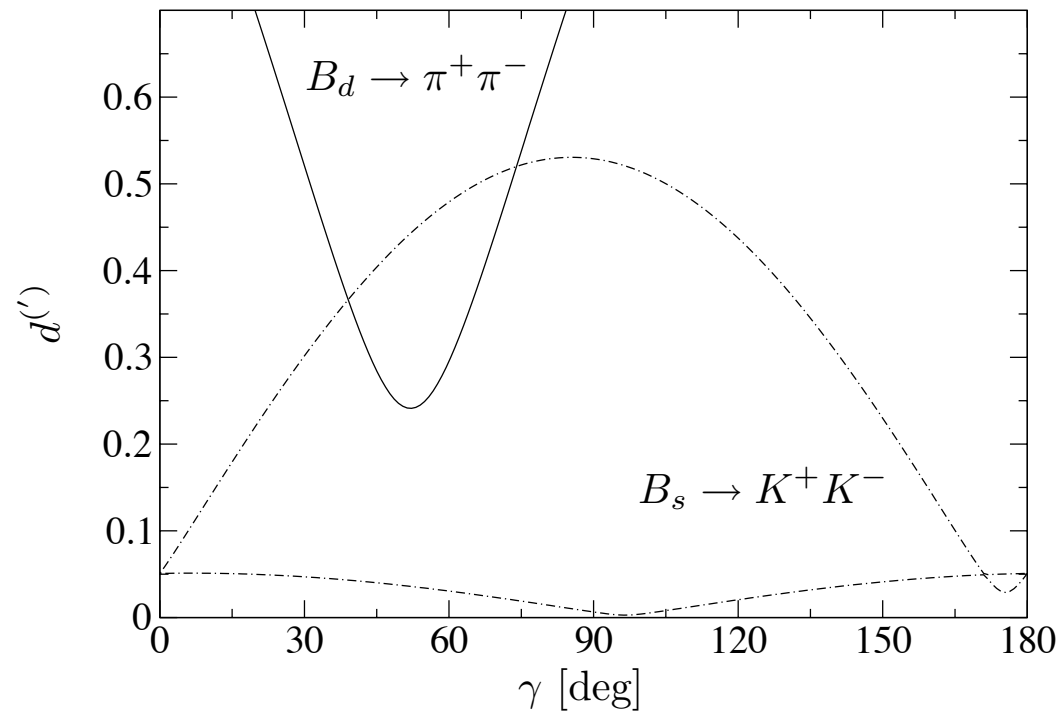
- Input parameter:

- \*  $\phi_d = 43.4^\circ$ ,  $\phi_s = -2^\circ$ ,  $\gamma = 74^\circ$ ,  $d = d' = 0.52$ ,  $\theta = \theta' = 146^\circ$

- CP asymmetries:

- \*  $B_d \rightarrow \pi^+ \pi^-$ :  $\mathcal{A}_{\text{CP}}^{\text{dir}} = -0.37$ ,  $\mathcal{A}_{\text{CP}}^{\text{mix}} = +0.50$

- \*  $B_s \rightarrow K^+ K^-$ :  $\mathcal{A}_{\text{CP}}^{\text{dir}} = +0.12$ ,  $\mathcal{A}_{\text{CP}}^{\text{mix}} = -0.19$



- The decays  $B_d \rightarrow \pi^+\pi^-$  and  $B_s \rightarrow K^+K^-$  are related to each other through the interchange of all down and strange quarks:

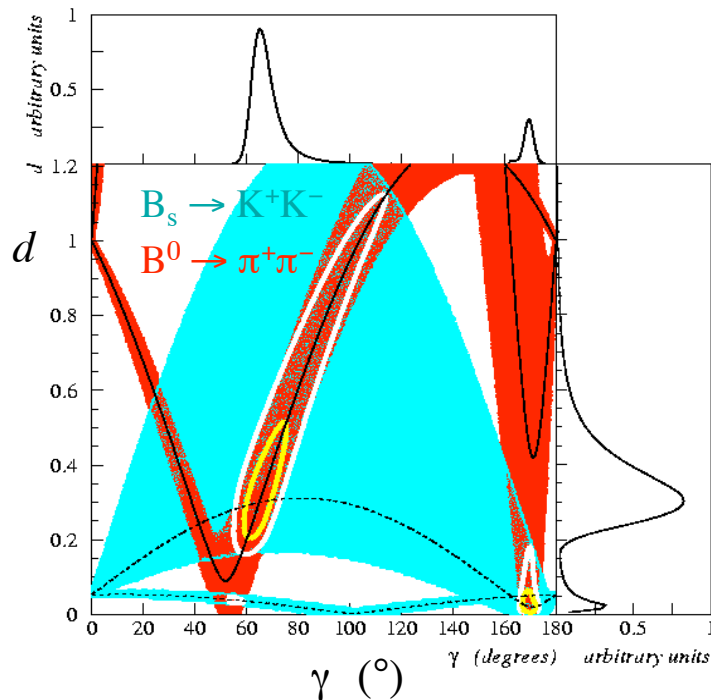
$$U\text{-spin symmetry} \Rightarrow d = d', \quad \theta = \theta'$$

–  $d = d'$ :  $\Rightarrow$  determination of  $\gamma, d, \theta, \theta'$

[R.F. (1999)]

–  $\theta = \theta'$ :  $\Rightarrow$  test of the  $U$ -spin symmetry!

- Detailed experimental feasibility studies show that the  $B_s \rightarrow K^+K^-$ ,  $B_d \rightarrow \pi^+\pi^-$  strategy is very promising for LHCb:



$\rightarrow$  experimental accuracy for  $\gamma$  of a few degrees!

[ CERN-LHCb/2003-123 & 124; talk by A. Sarti at Flavour LHC Workshop, October '06, CERN ]



- Recent news from the Tevatron: [CDF Collaboration, hep-ex/0607021]

Observation of  $B_s \rightarrow K^+ K^-$  @ CDF

- $236 \pm 32$  events were seen, which correspond to the branching ratio

$$\text{BR}(B_s \rightarrow K^+ K^-) = (33 \pm 5.7 \pm 6.7) \times 10^{-6};$$

update @ BEAUTY '06:  $\rightarrow (24.4 \pm 1.4 \pm 4.6) \times 10^{-6}$ .

- Theoretical prediction: [Buras, R.F. Schwab & Recksiegel ('04)]

- Requires the knowledge of an  $SU(3)$ -breaking form-factor ratio (which cancels in  $d e^{i\theta} = d' e^{i\theta'}$ ) [QCD sum rules: Khodjamirian et al. ('03)].

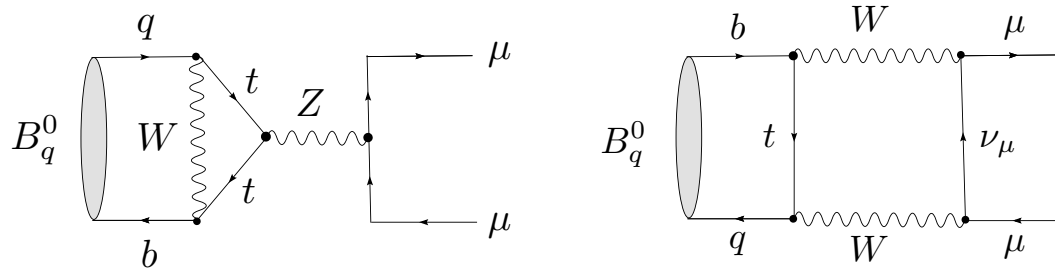
- Dynamical assumptions (small annihilation) and  $B_d \rightarrow \pi^\mp K^\pm$  data:

$$\Rightarrow \text{BR}(B_s \rightarrow K^+ K^-) = (35 \pm 7) \times 10^{-6}$$

$\Rightarrow$  good agreement!

# The Rare Decays $B_q \rightarrow \mu^+ \mu^-$ ( $q \in \{d, s\}$ )

- Originate from  $Z$  penguins and box diagrams in the Standard Model:



- Corresponding low-energy effective Hamiltonian: [Buchalla & Buras (1993)]

$$\mathcal{H}_{\text{eff}} = -\frac{G_F}{\sqrt{2}} \left[ \frac{\alpha}{2\pi \sin^2 \Theta_W} \right] V_{tb}^* V_{tq} \eta_Y Y_0(x_t) (\bar{b}q)_{V-A} (\bar{\mu}\mu)_{V-A}$$

- $\alpha$ : QED coupling;  $\Theta_W$ : Weinberg angle.
- $\eta_Y$ : short-distance QCD corrections (calculated ...)
- $Y_0(x_t \equiv m_t^2/M_W^2)$ : Inami–Lim function, with top-quark dependence.
- Hadronic matrix element:  $\rightarrow$  very simple situation:
  - Only the matrix element  $\langle 0 | (\bar{b}q)_{V-A} | B_q^0 \rangle$  is required:  $f_{B_q}$

$\Rightarrow$  belong to the cleanest rare  $B$  decays!

- Most recent SM predictions: [Blanke, Buras, Guadagnoli, Tarantino ('06)]

→ use the data for the  $\Delta M_q$  to reduce the hadronic uncertainties:

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) = (3.35 \pm 0.32) \times 10^{-9}$$

$$\text{BR}(B_d \rightarrow \mu^+ \mu^-) = (1.03 \pm 0.09) \times 10^{-10}$$

- Most recent experimental upper bounds from the Tevatron:

– CDF collaboration @ 95% C.L.: [CDF Public Note 8176 (2006)]

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) < 1.0 \times 10^{-7}, \quad \text{BR}(B_d \rightarrow \mu^+ \mu^-) < 3.0 \times 10^{-8}$$

– D0 collaboration @ 90% C.L. (95% C.L.): [D0note 5009-CONF (2006)]

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) < 1.9 (2.3) \times 10^{-7}$$

⇒ still a long way to go (?) → LHC (background under study)

- However, NP may significantly enhance  $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$ :

– In SUSY scenarios:  $\text{BR} \sim (\tan \beta)^6 \rightarrow$  dramatic enhancement (!);

[see, e.g., Foster *et al.* and Isidori & Paride ('06) for recent analyses]

– NP with modified EW penguin sector: sizeable enhancement.

# The Rare Decay $B_d^0 \rightarrow K^{*0} \mu^+ \mu^-$

- Key observable for NP searches:

Forward–Backward Asymmetry

$$A_{\text{FB}}(\hat{s}) = \frac{1}{d\Gamma/d\hat{s}} \left[ \int_0^1 d(\cos\theta) \frac{d^2\Gamma}{d\hat{s} d(\cos\theta)} - \int_{-1}^0 d(\cos\theta) \frac{d^2\Gamma}{d\hat{s} d(\cos\theta)} \right]$$

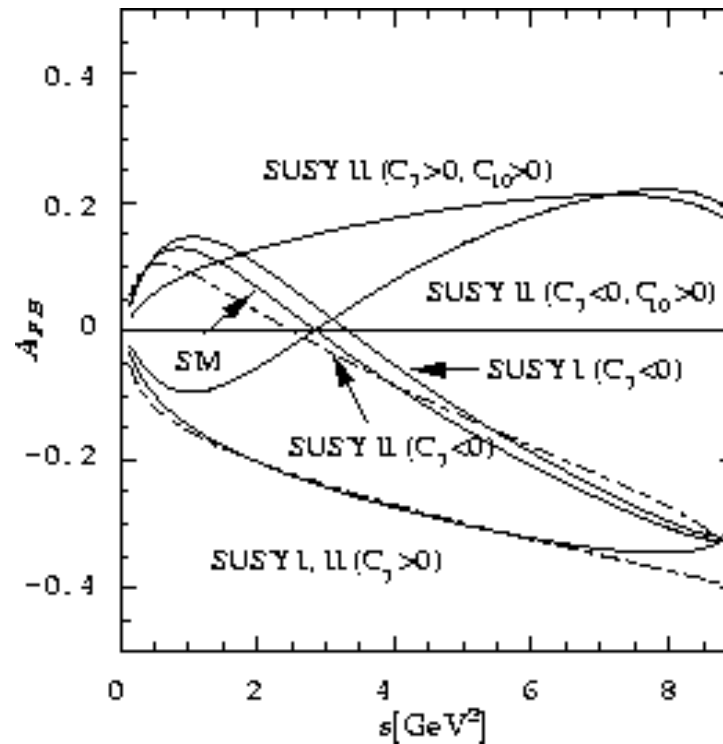
- $\theta$  is the angle between the  $B_d^0$  momentum and that of the  $\mu^+$  in the dilepton centre-of-mass system,
- and  $\hat{s} = s/M_B^2$ , with  $s = (p_{\mu^+} + p_{\mu^-})^2$ .

- Particularly interesting:

$$A_{\text{FB}}(\hat{s}_0)|_{\text{SM}} = 0$$

[Burdman ('98); Ali *et al.* ('00); ...]

- The value of  $\hat{s}_0$  is very robust with respect to hadronic uncertainties!
- SUSY extensions of the SM:
  - may yield  $A_{\text{FB}}(\hat{s})$  of opposite sign or without a zero point →



[A. Ali *et al.*, *Phys. Rev.* **D61** (2000) 074024]

- Sensitivity at the LHC:

- LHCb:  $\sim 4400$  decays/year, yielding  $\Delta\hat{s}_0 = 0.06$  after one year.
- ATLAS will collect about 1000  $B^0 \rightarrow K^{*0}\mu^+\mu^-$  decays per year.

- Other  $b \rightarrow s\mu^+\mu^-$  decays under study:  $\Lambda_b \rightarrow \Lambda\mu^+\mu^-$ ,  $B_s^0 \rightarrow \phi\mu^+\mu^-$  ...

- Current  $B$ -factory data: inclusive  $b \rightarrow sl^+\ell^-$  BRs and the integrated asymmetries  $\int A_{FB}$  in accordance with SM, but still large uncertainties.

# Conclusions and Outlook (I)

- Tremendous progress in  $B$  physics during the recent years:

Fruitful interplay between theory and experiment

- $e^+e^-$   $B$  factories: have already produced  $\sum \mathcal{O}(10^9)$   $B\bar{B}$  pairs;
- Tevatron: has recently succeeded in observing  $B_s^0-\bar{B}_s^0$  mixing.

- Status in October 2006:

- The data agree globally with the Kobayashi–Maskawa picture!
- But we have also hints for discrepancies:  $\rightarrow$  first signals of NP??

- New perspectives for  $B$ -decay studies @ LHC  $\gtrsim$  autumn 2007:

- Large statistics and full exploitation of the  $B_s$  physics potential, thereby complementing the physics programme of the  $e^+e^-$   $B$  factories.
- Precision determinations of  $\gamma$ :  $\rightarrow$  key ingredients for NP searches!
- Powerful studies of rare decays:  $B_{s,d} \rightarrow \mu^+\mu^-$ , ...

$\rightarrow$  much more stringent CKM consistency tests!

## Conclusions and Outlook (II)

*Flavour physics & CP violation in direct context with LHC*

- Main goals of the ATLAS and CMS experiments:

- Exploration of the mechanism of EW symmetry breaking: Higgs!?
- Production and observation of *new* particles ...
- Then back to questions of dark matter, baryon asymmetry ...
  - ⊕ complementary and further studies at ILC/CLIC

- Synergy with the flavour sector:<sup>5</sup>

$B \oplus K, D$ , top physics & lepton/neutrino sector

- If discovery of new particles, which kind of new physics?
- Insights into the corresponding new flavour structures and possible new sources of CP violation through studies of flavour processes.
- Sensitivity on very high energy scales of new physics through precision measurements, also if NP particles cannot be produced at the LHC ...

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<sup>5</sup>Topic of CERN Workshop: <http://flavlhq.web.cern.ch/flavlhq/>