

The Discovery Potential of rare K and B decays

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Indirect measurements

Lessons from the **past**:

rare low energy processes like ΔM_K (charm), $B_d - \bar{B}_d$ osc. and EWPT (top), can tell us a lot about heavy particles prior to their discovery

'60 ΔM_K

'87 ARGUS at Desy ΔM_{B_d}

'9x LEP

'99-now Belle/Babar

Present

SM works remarkably well, surprisingly also in the least understood sector: the flavor sector

Future

In order to test NP indirectly we need **theoretically very clean** observables, preferably with **small SM** contribution.



Flavour in the SM

Yukawas are responsible for flavour transitions

$$\mathcal{L}_{\text{Yukawa}} = \bar{Q}_L Y_D D_R H + \bar{Q}_L Y_U U_R (H)_c$$

$$Y_D = (m_d, m_s, m_b)/v$$

$$Y_U = V_{\text{CKM}}^\dagger (m_u, m_c, m_t)/v$$

$m_t \gg m_i$ and V_{CKM} has a hierarchical structure

There are no FCNCs on tree level.

Flavour change is small

$$Y_D = (m_d, m_s, m_b)/v$$

$$Y_U = V_{\text{CKM}}^\dagger (m_u, m_c, m_t)/v$$

$$Y_U \approx \begin{pmatrix} 10^{-5} & -0.002 & 0.007 + 0.004i \\ 10^{-6} & 0.007 & -0.04 + 0.0008i \\ 10^{-8} + 10^{-7}i & 0.0003 & 0.96 \end{pmatrix}$$

We have no idea why Y_U and Y_D are the way they are.

Generally, NP models are struggling since we have **no theory of flavour**.

We want NP to show up at around a TeV (Higgs stabilization).

K-K mixing e.g. shows no generic flavour violation up to 10^3 TeV.

Flavour precision tests

General structure of a decay rate



Energy scale

$$\Gamma = (\text{non-pert. QCD}) \times \text{QCD RG} \times (V_{\text{ckm}} \text{ SM short dist.} + \text{NP})$$



theoretical uncertainty

Three strategies for precision tests:

- 1) hadronic uncertainties cancel in asymmetries $A_{\text{CP}}^{\text{mix}}(B_s \rightarrow \psi\phi)$
partial cancelation: $Br(B_q \rightarrow \mu^+ \mu^-) / \Delta M_q$
- 2) hadronic matrix element from Experiment ($K \rightarrow \pi \bar{\nu} \nu$)
- 3) inclusive, non-perturbative $\sim (\Lambda_{\text{QCD}}/m_b)^2$ ($B \rightarrow X_s \gamma$)

FCNCs in the SM

interesting Flavour channels

$$s \rightarrow d \sim \lambda^5 \quad \Delta M_K, \epsilon_K, \epsilon'/\epsilon, K_L \rightarrow \pi^0 \bar{l}l, K \rightarrow \pi \bar{\nu}\nu$$

$$b \rightarrow d \sim \lambda^3 \quad \Delta M_d, B_d \rightarrow \mu^+ \mu^-, B \rightarrow X_d \gamma$$

$$b \rightarrow s \sim \lambda^2 \quad \Delta M_s, B_s \rightarrow \mu^+ \mu^-, B \rightarrow X_s l^+ l^-, \\ B \rightarrow X_s \gamma \quad A_{FB}(B \rightarrow X_s l^+ l^-) \\ B \rightarrow K^* \gamma$$

theoretical error

$$< 15 \% \quad < 10\% \quad < 5\%$$



increasing
SM contribution

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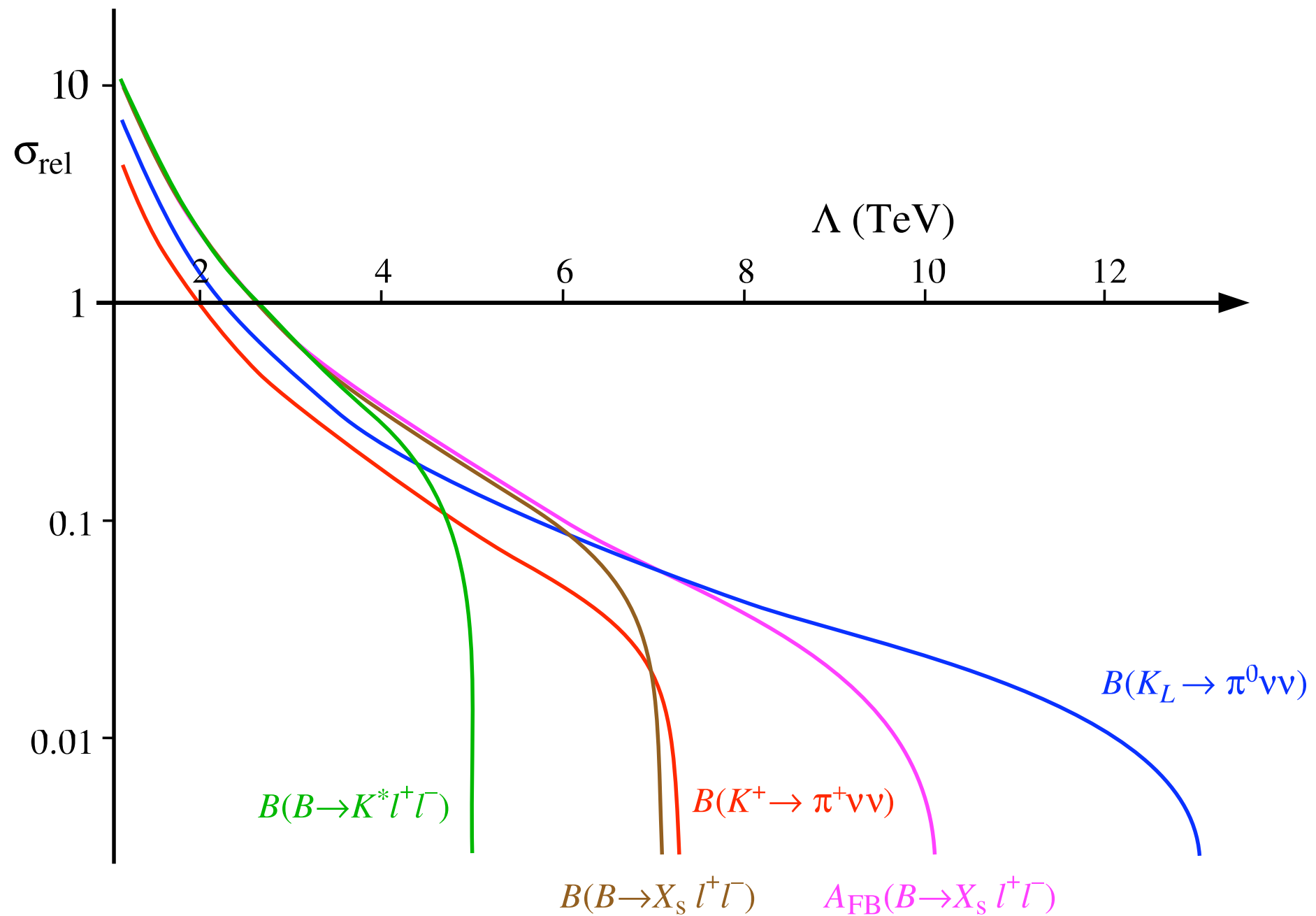
< 5%



increasing
SM contribution

Comparison of sensitivities

D'Ambrosio, Giudice, Isidori, Strumia '02; Buras, Bryman, Isidori, Littenberg '05



plan of the talk

- Interesting NP flavour observables of the future
- rare Kaon decays: the four golden modes, status of the SM calculation, NP searches
- $B \rightarrow X_s \gamma$ (new result)
- rare B decays and large $\tan\beta$
- Conclusions

4 golden modes

$$Br(K_L \rightarrow \pi^0 \mu^+ \mu^-)$$

$$Br(K_L \rightarrow \pi^0 e^+ e^-)$$

$$Br(K^+ \rightarrow \pi^+ \nu \bar{\nu})$$

$$Br(K_L \rightarrow \pi^0 \nu \bar{\nu})$$



24 carat

4 golden modes

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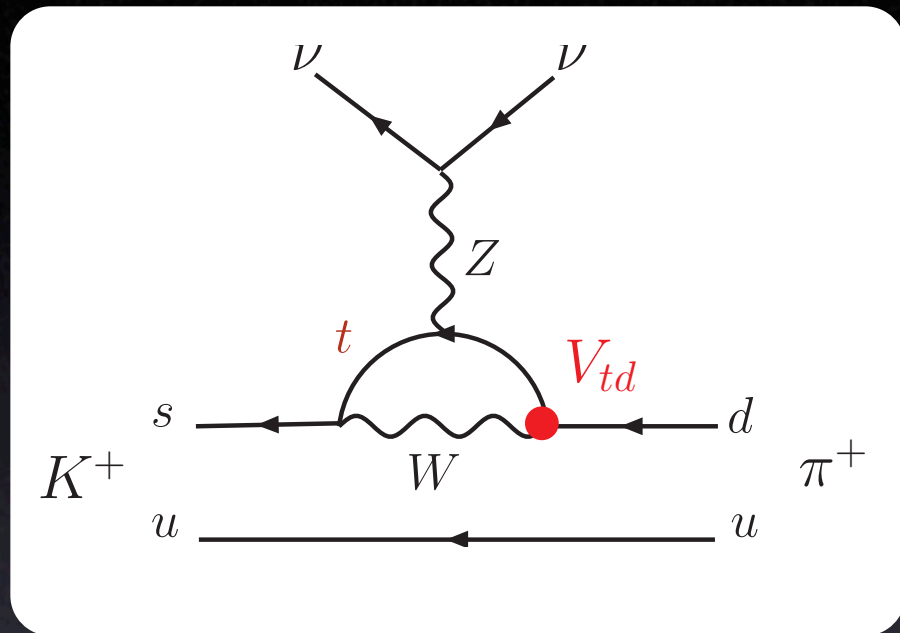
60-€!



$$K_L \rightarrow \pi^0 \nu \bar{\nu}$$

$$K^+ \rightarrow \pi^+ \nu \bar{\nu}$$

Potential of $K \rightarrow \pi \nu \bar{\nu}$



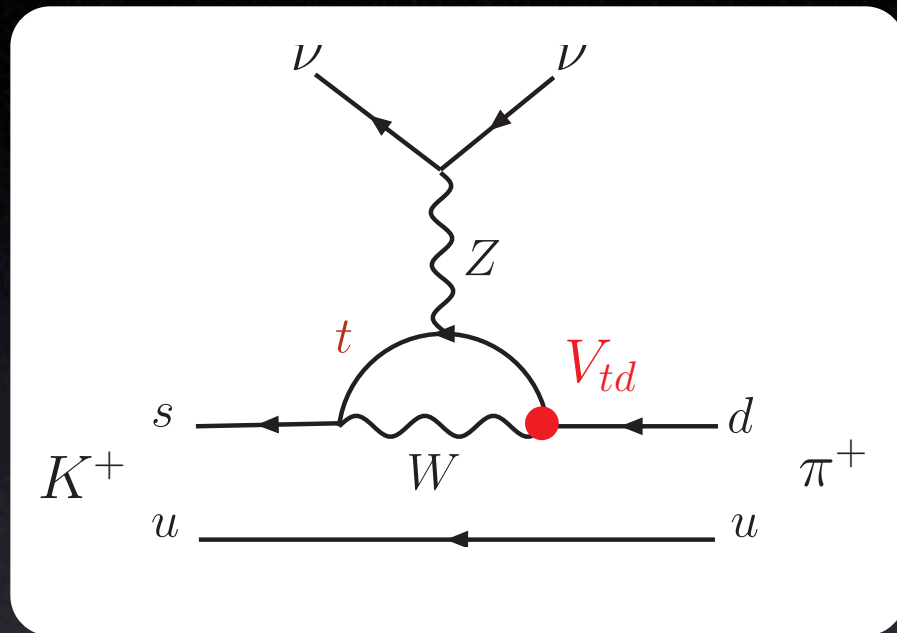
+ box

Dominated by short distance contributions

o $\sigma(K^+)_{\text{theory}} \sim 4\%$

o $\sigma(K_L)_{\text{theory}} \sim 2\%$

Potential of $K \rightarrow \pi \nu \bar{\nu}$



+ box

$$A(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = B_+ \left(\lambda_c \tilde{P}_c + \lambda_t X(v) \right)$$

$$A(K_L \rightarrow \pi^0 \nu \bar{\nu}) = B_L \text{Im} [\lambda_t X(v)]$$

$$\lambda_t = V_{ts}^* V_{td} \quad \lambda_c = V_{cs}^* V_{cd}$$

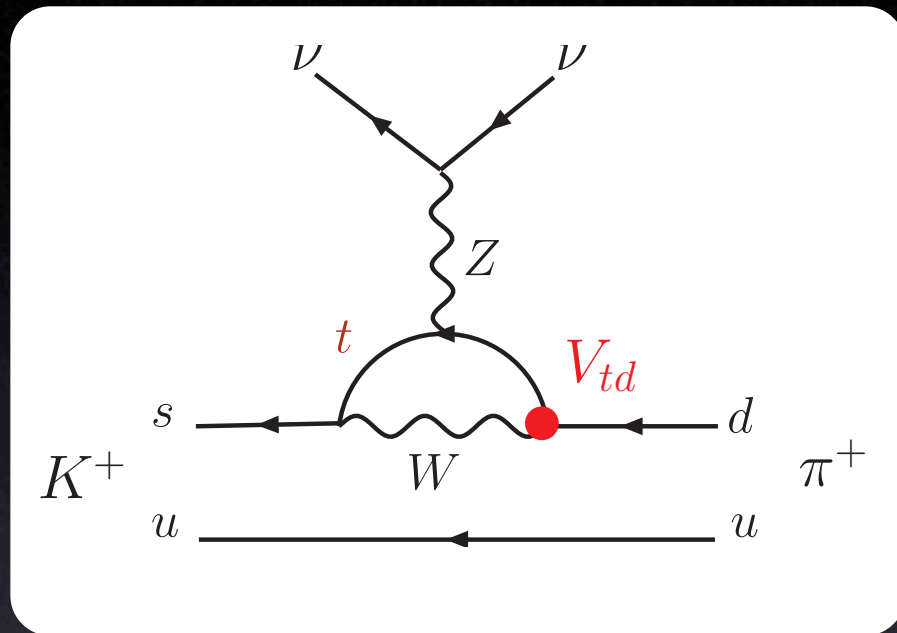
B_+ and B_L from $K^+ \rightarrow \pi^0 e^+ \nu$

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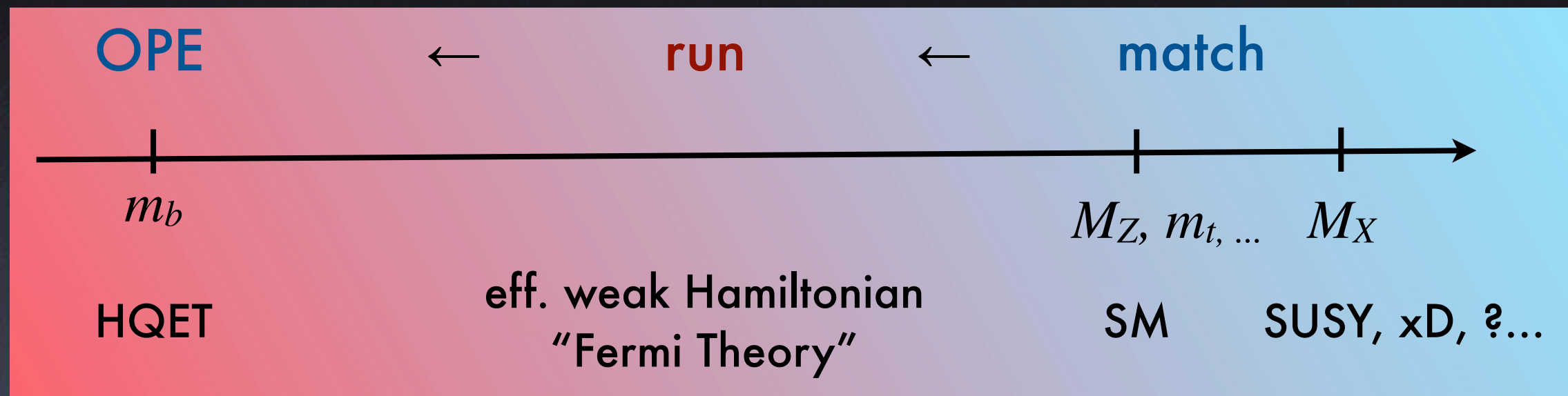
pure short-distance

Dominated by short distance contributions

o $\sigma(K^+)_{\text{theory}} \sim 4\%$

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SM Calculation



General properties

$$\mathcal{L}_{\text{eff}}^{(6)} = \frac{4G_F}{\sqrt{2}} \frac{\alpha}{2\pi s_W^2} \sum_{i=u,c,t} C^i(\mu) Q_\nu^{(6)}$$
$$Q_\nu^{(6)} = \sum_{l=e,\mu,\tau} (\bar{s}_L \gamma_\mu d_L) (\bar{\nu}_{lL} \gamma^\mu \nu_{lL})$$

$$C^i(M_W) \propto m_i^2 V_{is}^* V_{id} \propto \begin{cases} \Lambda_{\text{QCD}}^2 \lambda & \mathbf{u} \\ m_c^2 (\lambda + i\lambda^5) & \mathbf{c} \\ m_t^2 (\lambda^5 + i\lambda^5) & \mathbf{t} \end{cases}$$

- * Z penguin is $SU(2)_L$ breaking: powerlike GIM
- * large CPV phase in dominant top contribution
- * charm effects:
 - 1) **negligible** in K_L : $O(m_c^2/m_t^2) \ll 1$ for dominant direct CPV-Amplitude
 - 2) **small** in $K^+ \sim 30\%$ (\rightarrow next to next slide)

SM prediction of $K_L \rightarrow \pi^0 \nu \bar{\nu}$

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = \kappa_L \left[\frac{\text{Im}(V_{ts}^* V_{td})}{\lambda^5} X \right]^2$$

$$\kappa_L = r_{K_L} \frac{3\alpha^2 \mathcal{B}(K^+ \rightarrow \pi^0 e^+ \nu_e) \tau(K_L)}{2\pi^2 s_W^4 \tau(K^+)}$$

- * short distance dominated (>99%)
- * very small theoretical error ~ 2%
- * 85% of total error CKM input
- * precise and direct measurement of amount of CPV in SM

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = (2.93 \pm 0.44) \times 10^{-11}$$

Buras, Gorbahn, Haisch, Nierste '06

$$\text{Br}_{\text{exp}} / \text{Br}_{\text{SM}} < 2.86 \cdot 10^4 \text{ (90\% C.L.) E391}$$

KTEV, E391a (soon to be improved!)

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$$X = 1.46 \pm 0.04 \quad (\text{NLO})$$

t

Buchalla & Buras '93, '99;
Misiak & Urban '99

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Buchalla & Buras '93, '99;
Misiak & Urban '99

$$r_{K_L} = 0.944 \pm 0.028 \quad \text{isospin}$$

Marciano & Parsa '96

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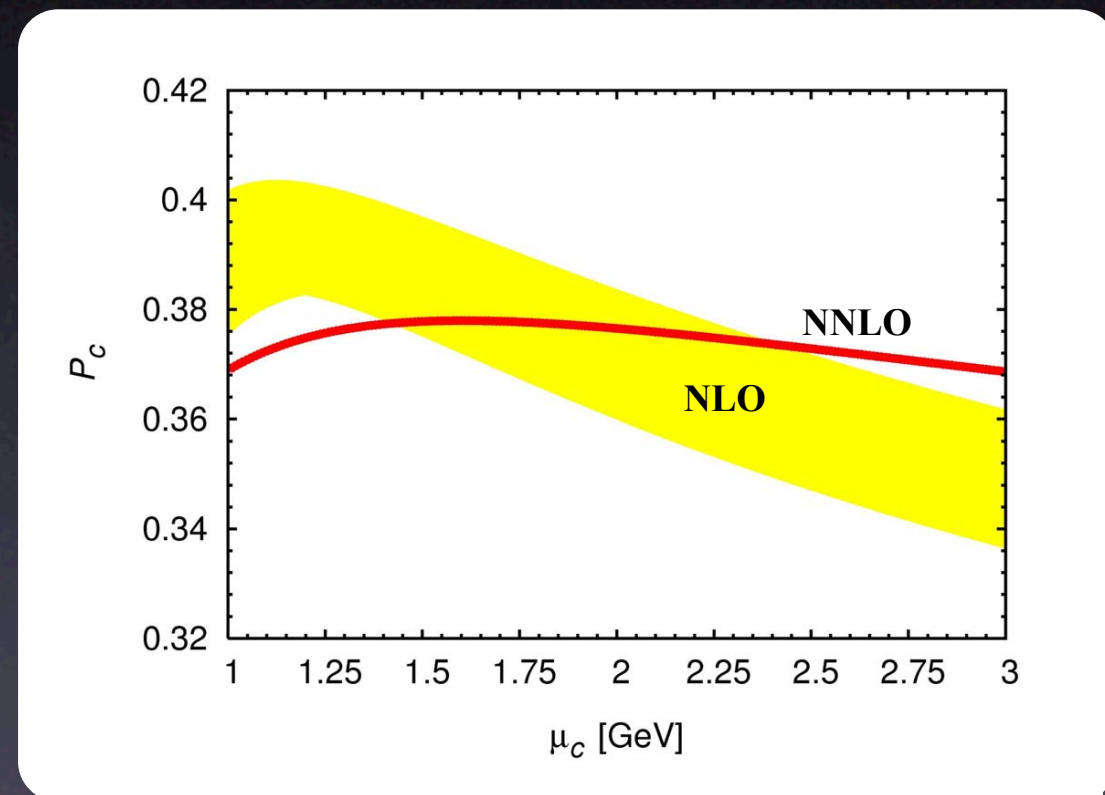
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* P_c error now dominated by Δm_c
Buras, Gorbahn, Haisch, Nierste '05

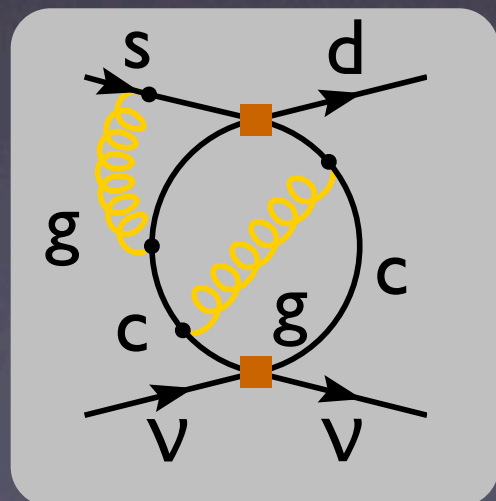
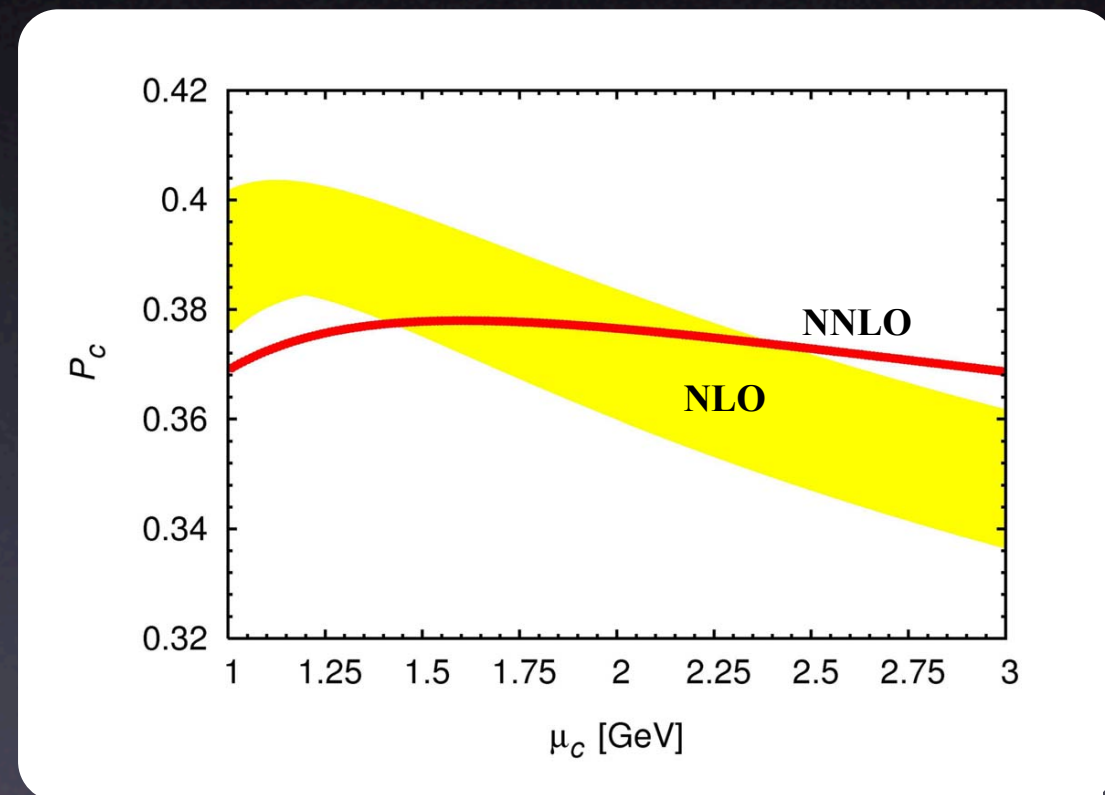


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$$P_c^{\text{NLO}} = 0.369 \pm 0.033 \pm 0.037 \pm 0.009 \approx 0.37 \pm 0.07$$

Buchalla, Buras '94

$$P_c^{\text{NNLO}} = 0.375 \pm 0.031 \pm 0.009 \pm 0.009 \approx 0.38 \pm 0.04$$

Buras, Gorbahn, Haisch, Nierste '05

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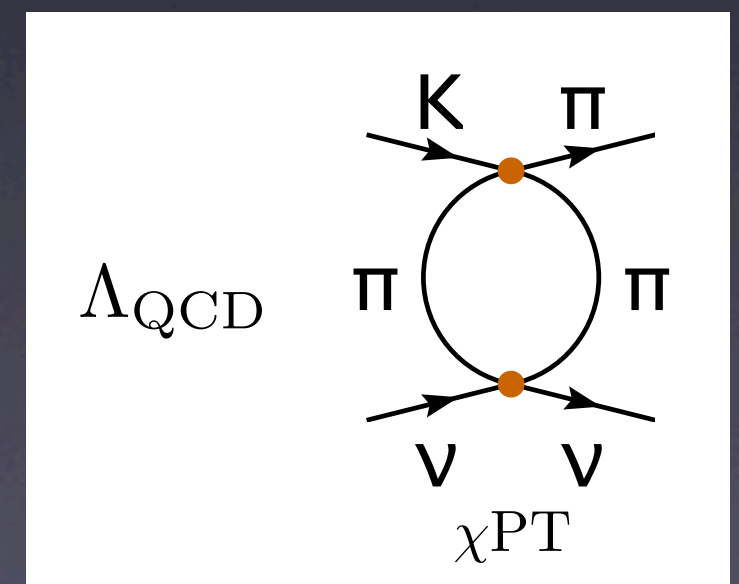
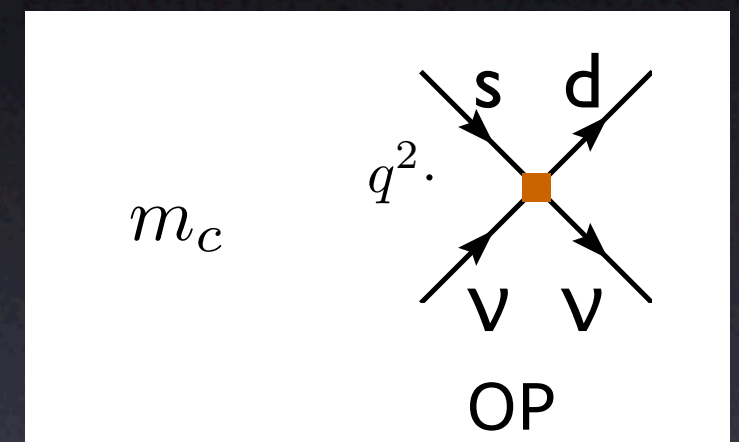
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Buras, Gorbahn, Haisch, Nierste '05

* LD and dim8 effects in δP_c are $\sim \pi^2 F_\pi^2/m_c^2 \sim 10\%$ of charm contribution, 6% enhancement of Br_{K^+} Isidori, Mescia & Smith '05

* LQCD could improve accuracy to 1-2%
Isidori, Martinelli & Turchetti '05



$$\delta P_c = 0.04 \pm 0.02$$

SM prediction for $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.0 \pm 1.1) \times 10^{11}$$

Buras, Gorbahn, Haisch, Nierste '05

- * theoretical error of QCD corrections to the charm contribution P_c factor ~ 4 smaller thanks to NNLO calculation

$$\mathcal{B}_{\text{exp}}^+ = \left(14.7_{-8.9}^{+13.0} \right) \times 10^{11}$$

E787 (2), E949 (I)

- * P_c error now dominated by Δm_c
Buras, Gorbahn, Haisch, Nierste '05

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MFV

SM Yukawa couplings are the only source of flavour violation.

All flavour violation is proportional to V_{CKM} .

Strong correlations between K and B physics.

K^+ and K_L in specific MFV models

- Littlest Higgs: slight suppression Buras, Uhlig, Poschenrieder '05
- Universal ED: <9-10% enhancement Buras, AW, Spranger '03
- CMFV MSSM: 0...40% suppression Buras, Gambino, Gorbahn, Jäger, Silvestrini '00

General pattern:

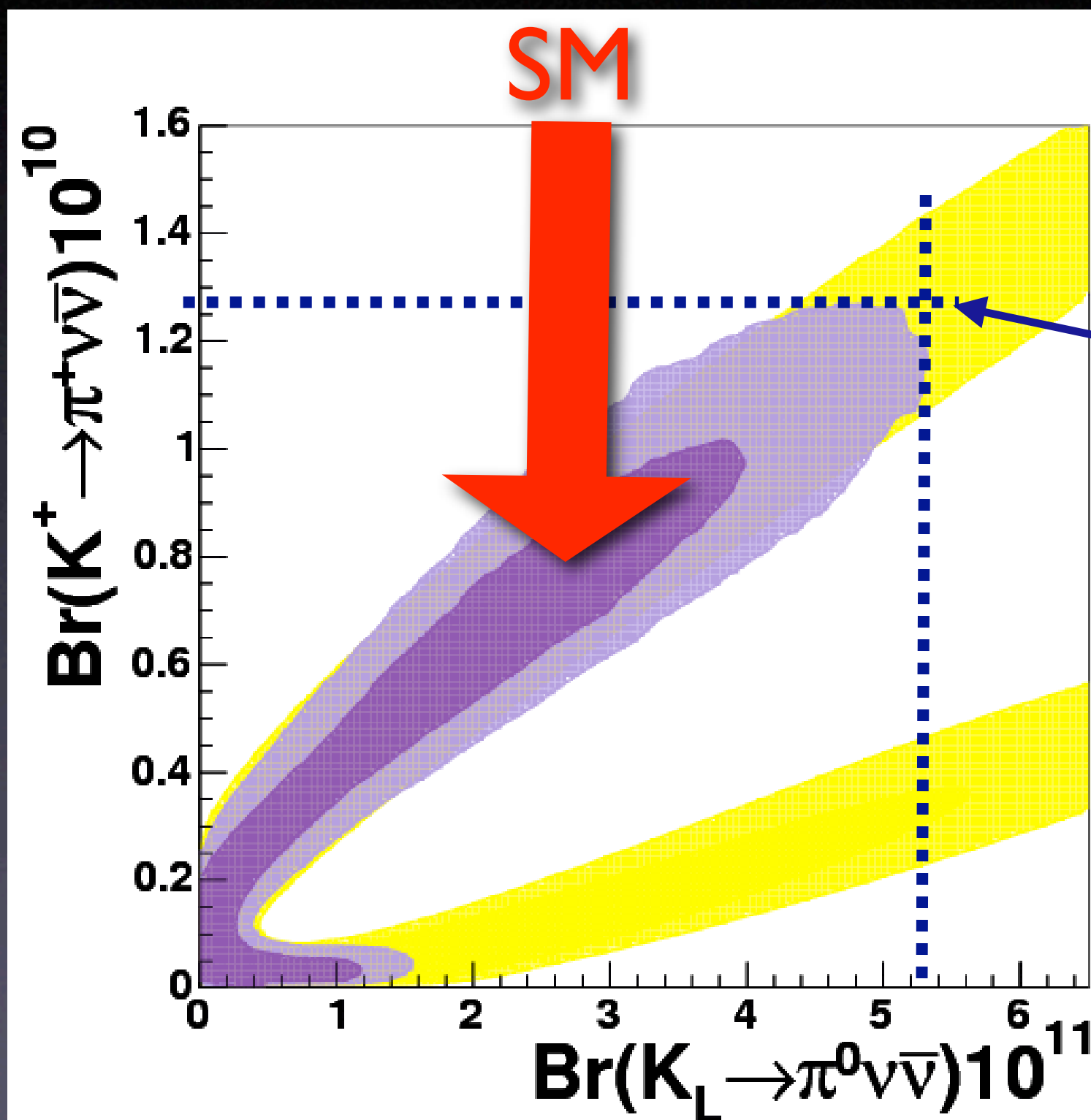
Buras, Blanke '06

NP contribution to ΔM_d interferes constructively with SM
 $\Delta F = 2$ Amplitude S in the above models and

$$\left(\frac{V_{td}^{NP}}{V_{td}^{SM}} \right)^2 = \frac{S^{SM}}{S^{SM} + |\Delta S^{NP}|} < 1$$

$Br(K)_{exp} > Br(K)_{SM}$ immediately falsifies most MFV models!


MFV upper bound



model independent

95% C.L. upper bound

Bona, Buras, Bobeth, Ewerth,
Pierini, Silvestrini, AW '05

Universal CKM fit from 
Bona et. al '05

using universal UTfit +
 $B \rightarrow X_s \gamma + B \rightarrow X_s l^+ l^-$

MFV upper bounds

Bona, Buras, Bobeth, Ewerth, Pierini, Silvestrini, AW (05)

Branching Ratios	MFV (95%)	SM (95%)	SM (68%)	Exp
$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \cdot 10^{11}$	<11.9	<10.9	8.3 ± 1.2	$14.7^{+13.0}_{-8.9}$
$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \cdot 10^{11}$	<4.6	<4.2	3.1 ± 0.6	<2.86 10^4 (90% C.L.) E391
$\text{Br}(B \rightarrow X_S \nu \bar{\nu}) \cdot 10^5$	<5.2	<4.1	3.7 ± 0.2	<64
$\text{Br}(B_s \rightarrow \mu^+ \mu^-) \cdot 10^9$	<7.4	<5.9	3.7 ± 1.0	<80 (90% C.L.) CDF
$\text{Br}(B_d \rightarrow \mu^+ \mu^-) \cdot 10^{10}$	<2.2	<1.8	1.1 ± 0.4	< $1.6 \cdot 10^3$

BNL AGS E787, E949

<2.86 10^4 (90% C.L.) E391

<80 (90% C.L.) CDF

low/moderate $\tan\beta$!

Beyond MFV

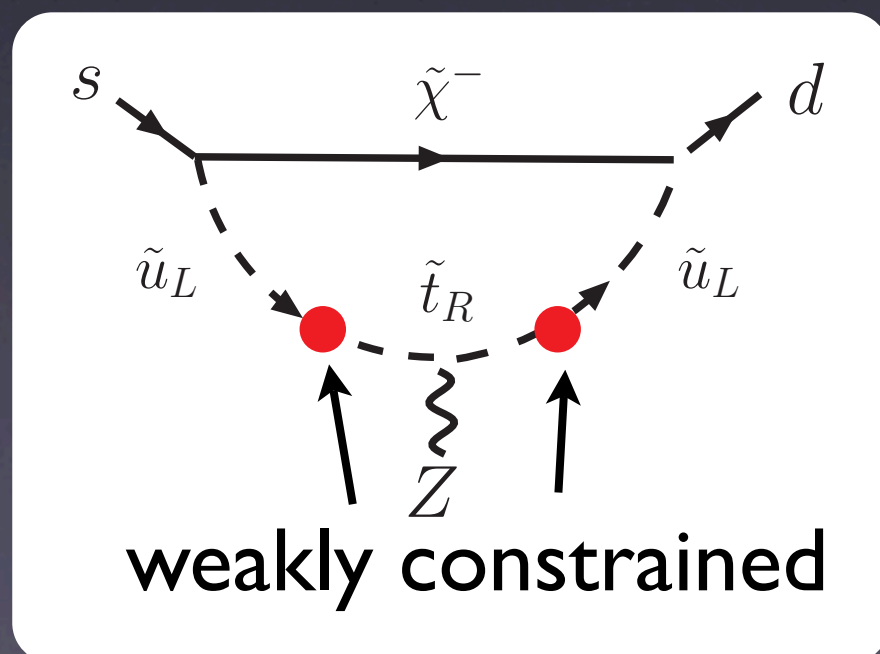
rare K decays are a very sensitive probe
for non-MFV flavour violation since

$$(s \rightarrow d) \sim \lambda^5$$

suppression is not built in the model anymore.

Generic MSSM

- Flavor structure probes Susy breaking mechanism
- Room for sizable deviations even if $\Delta F=2$ sector agrees well with SM
- very sensitive to new sources of flavor symmetry breaking due to λ^5 suppression of SM amplitude



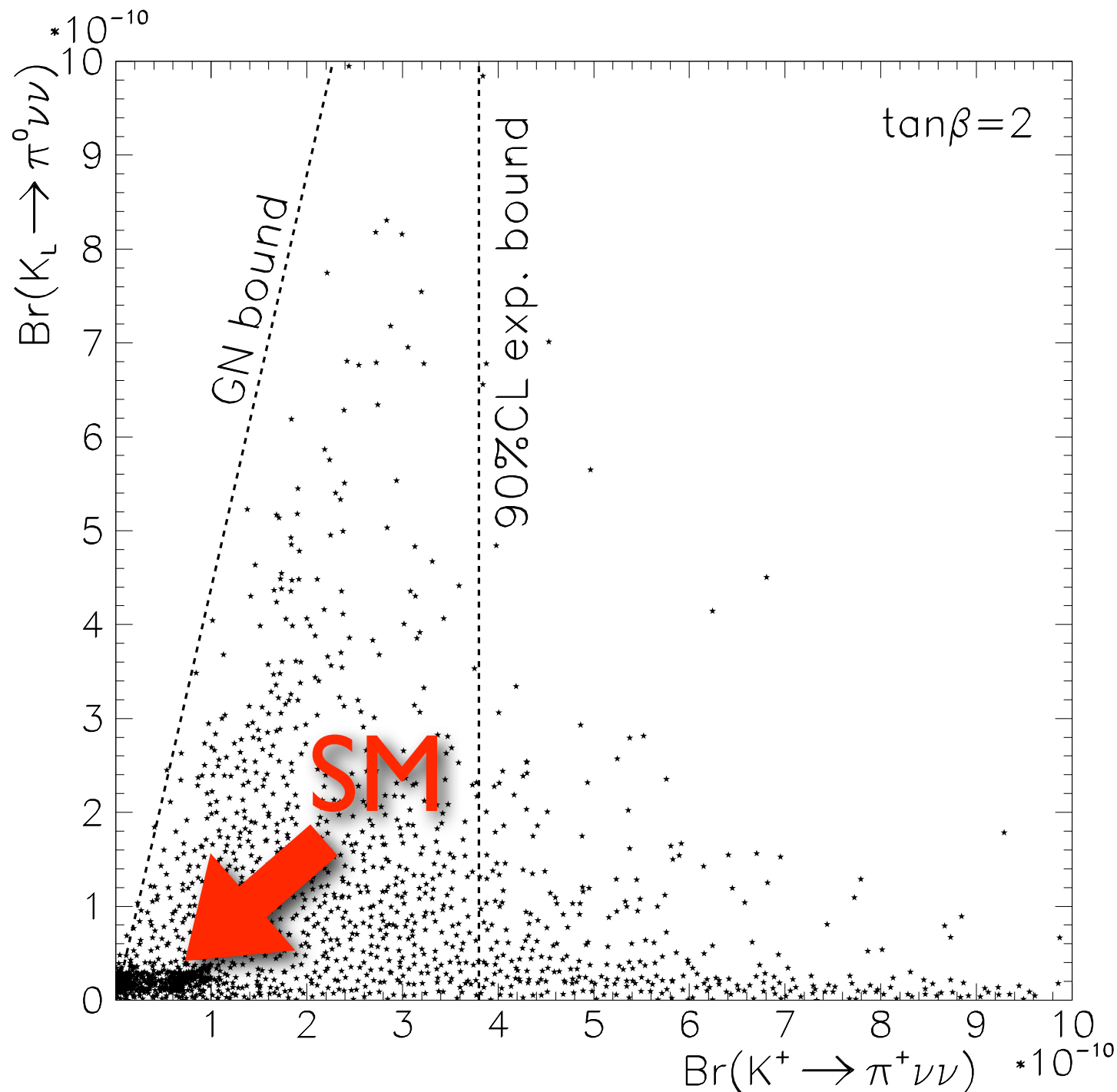
$$\text{Amplitude } \cancel{\text{SU}(2)_L} \propto \frac{1}{M_Z^2} V_{Z \bar{s}d}$$

$$\tilde{X}_{\text{SUSY}}^{(\text{peng})} \propto \frac{(M_{LR}^2)_{d't} (M_{LR}^2)_{s't}^*}{M_{\text{SUSY}}^4}$$

small $\tan\beta$

Generic MSSM

Buras, Ewerth, Jäger, Rosiek '04



includes all present constraints

$\Delta M_K, \epsilon_K, b \rightarrow s\gamma, \dots$

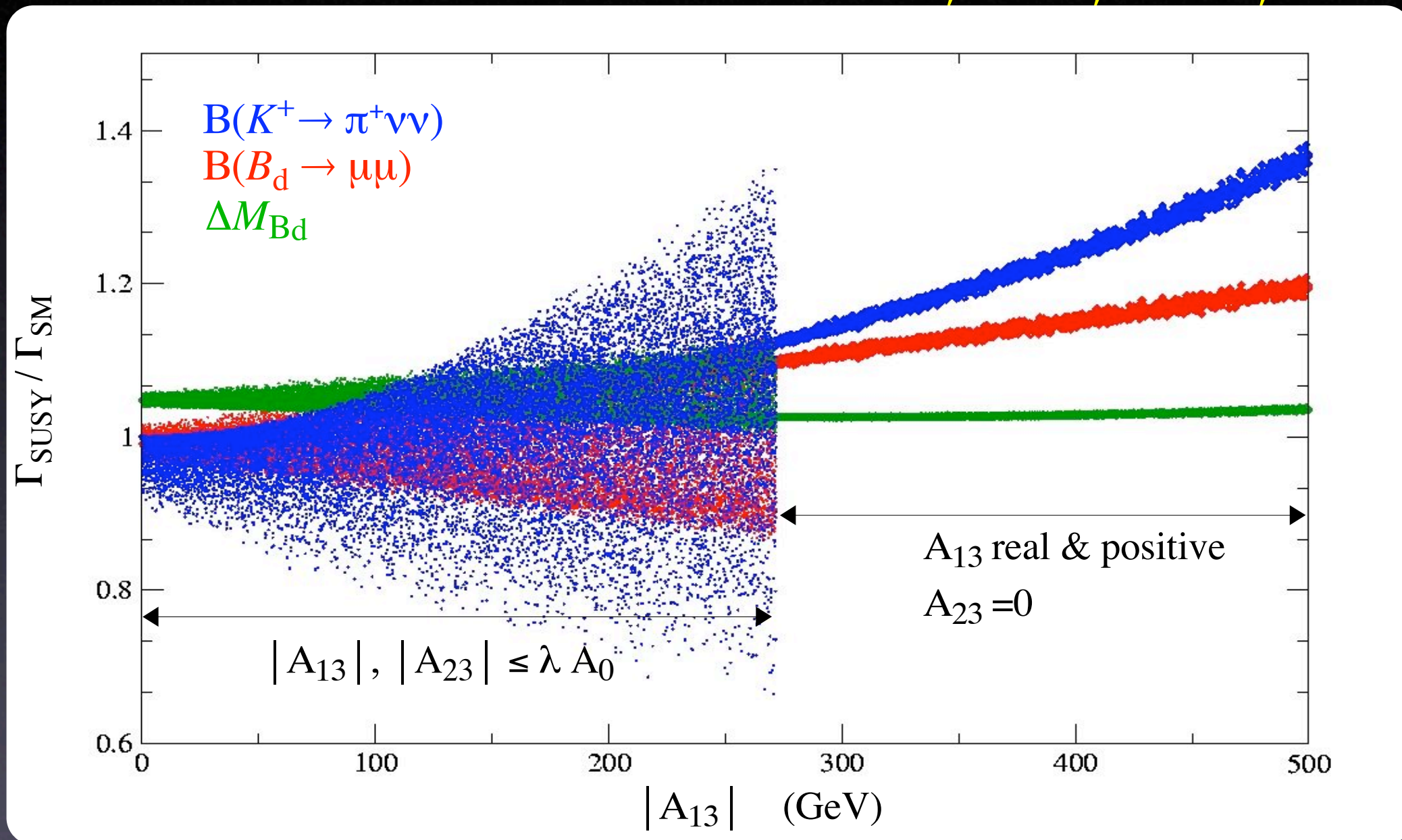
saturation of
Grossman-Nir bound

K_L could be 20-30x
enhanced

in reach of E39 Ia

Generic MSSM II

Isidori, Mescia, Paradisi, Smith, Trine '06



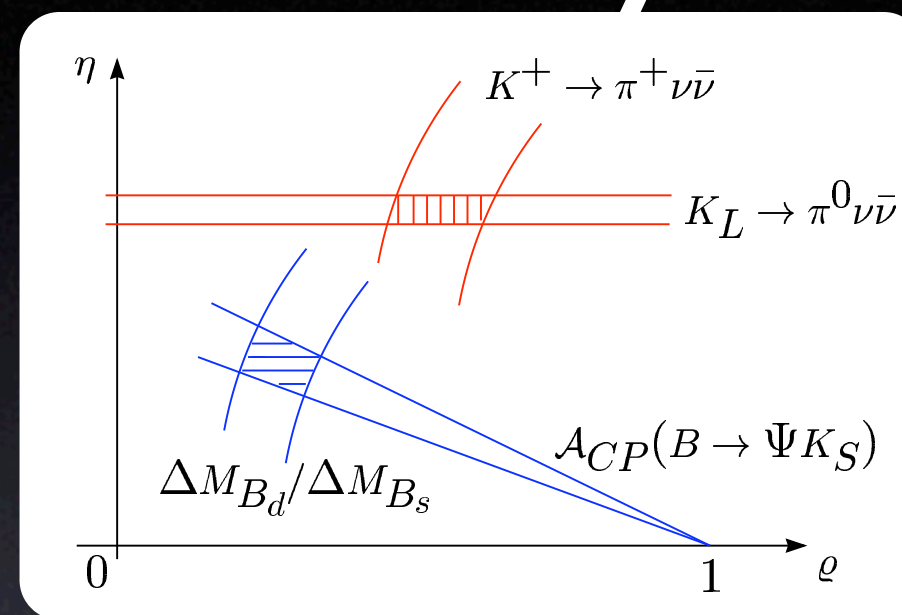
K^+ best probe of up-type trilinear soft Susy breaking terms

$$\mathcal{L}_{\text{soft}} \subset (A^U Y^U)_{ij} Q_L^i U_R^j \phi$$

CKM and rare K decays

$$(\sin 2\beta)_{\psi K_S} = (\sin 2\beta)_{\pi\nu\bar{\nu}}$$

test of the ‘golden relation’



Could help improve the knowledge of CKM parameters

However, **more interesting** is the **201x** scenario:

- * CKM known to great precision independent of NP from Belle, BaBar, LHCb, SuperB, ...
- * SM prediction for K^+ , K_L together with a 10% measurement allows precision test of the flavor structure of NP

Status of $K_L \rightarrow \pi^0 l^+ l^-$

Buchalla, D'Ambrosio, Isidori; Isidori, Smith, Unterdorfer '04, Smith, Mescia, Trine '06

$$Br(K_L \rightarrow \pi^0 l^+ l^-) = \left[C_{\text{mix}}^l + C_{\text{int}}^l \left(\frac{\text{Im}\lambda_t}{10^{-4}} \right) + C_{\text{dir}}^l \left(\frac{\text{Im}\lambda_t}{10^{-4}} \right)^2 + C_{\text{CPC}}^l \right] \cdot 10^{-12}$$

indirect
CPV

interference of
direct and indirect

direct
CPV

CP
conserving

substantial progress in
theory precision
associated with light quark
loops

experimental input from NA48

$$C_{\text{dir}}^e = (4.62 \pm 0.24)(\omega_{7V}^2 + \omega_{7A}^2) \quad C_{\text{dir}}^\mu = (1.09 \pm 0.05)(\omega_{7V}^2 + 2.32\omega_{7A}^2)$$

$$C_{\text{int}}^e = (11.3 \pm 0.3)\omega_{7V},$$

$$C_{\text{int}}^\mu = (2.63 \pm 0.06)\omega_{7V},$$

$$C_{\text{mix}}^e = 14.5 \pm 0.05,$$

$$C_{\text{mix}}^\mu = 3.36 \pm 0.20,$$

$$C_{\text{CPC}}^e \simeq 0,$$

$$C_{\text{CPC}}^\mu = 5.2 \pm 1.6,$$

$$Br(K_L \rightarrow \pi^0 \mu^+ \mu^-) = (1.5 \pm 0.3) \cdot 10^{-11}$$

$$Br(K_L \rightarrow \pi^0 e^+ e^-) = (3.7_{-0.9}^{+1.1}) \cdot 10^{-11}$$

Exp:

@ 90% C.L.

$$< 2.8 \cdot 10^{-10}$$

KTEV '00

$$< 3.8 \cdot 10^{-10}$$

KTEV '03

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Direct CPV amplitude:

- * clean probe of independent NP structures and CPV beyond SM
- * important if beyond-MFV NP is found

Status of $K_L \rightarrow \pi^0 l^+ l^-$

Buchalla, D'Ambrosio, Isidori; Isidori, Smith, Unterdorfer '04, Smith, Mescia, Trine '06

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indirect
CPV

interference of
direct and indirect

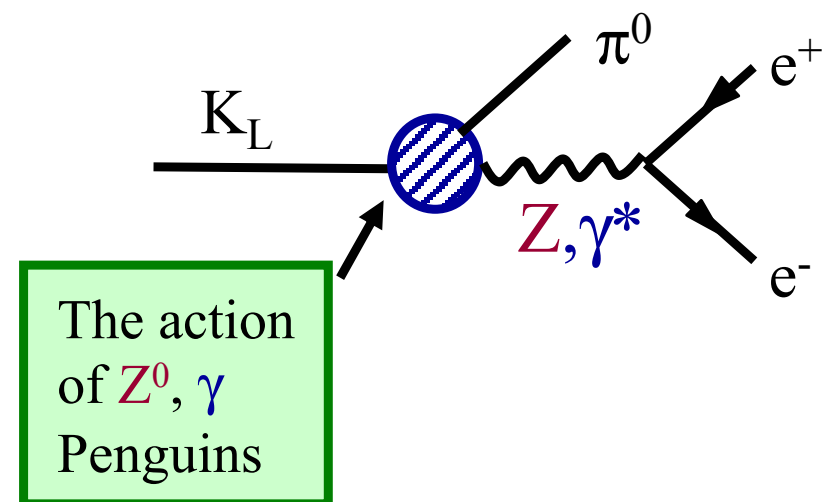
direct
CPV

CP
conserving

NP

Direct CPV amplitude:

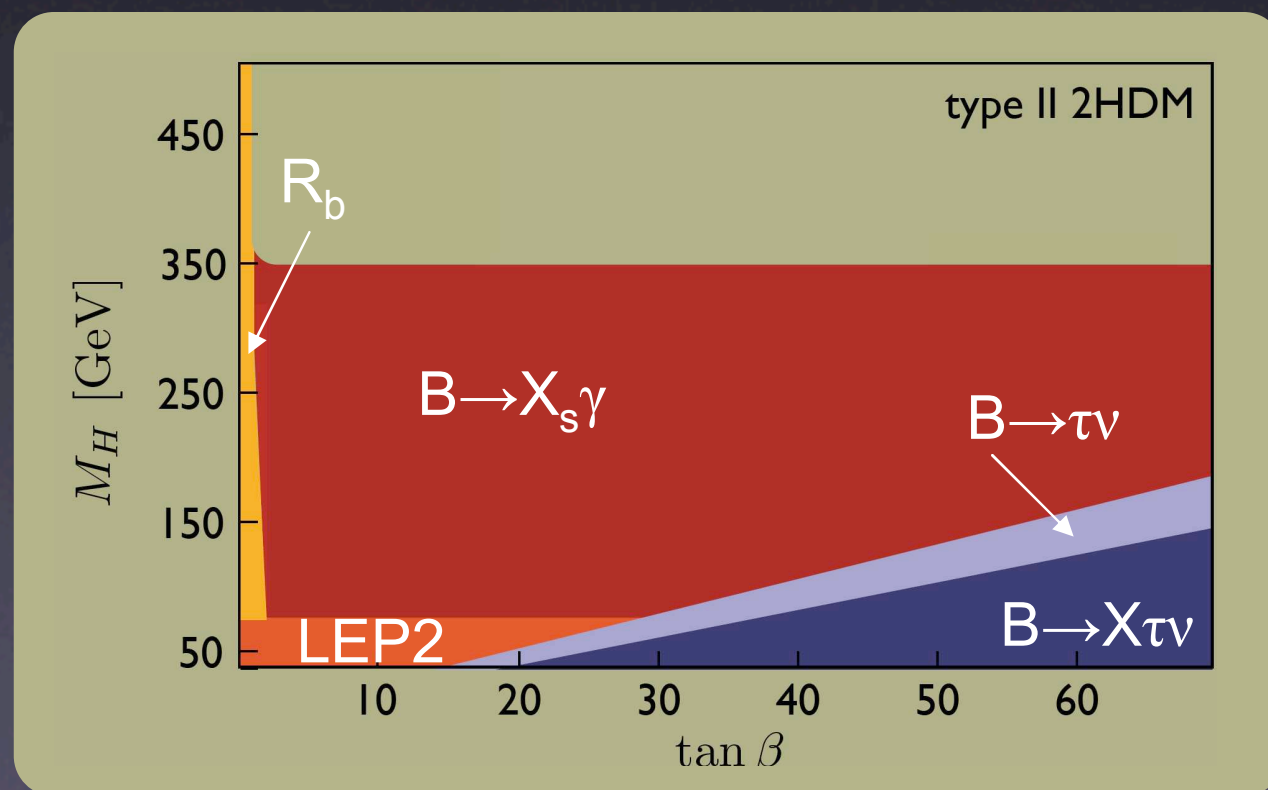
- * clean probe of independent NP structures and CPV beyond SM
- * important if beyond-MFV NP is found



$$Q_\nu, Q_{9V}, Q_{10A}$$

$$B \rightarrow X_s \gamma$$

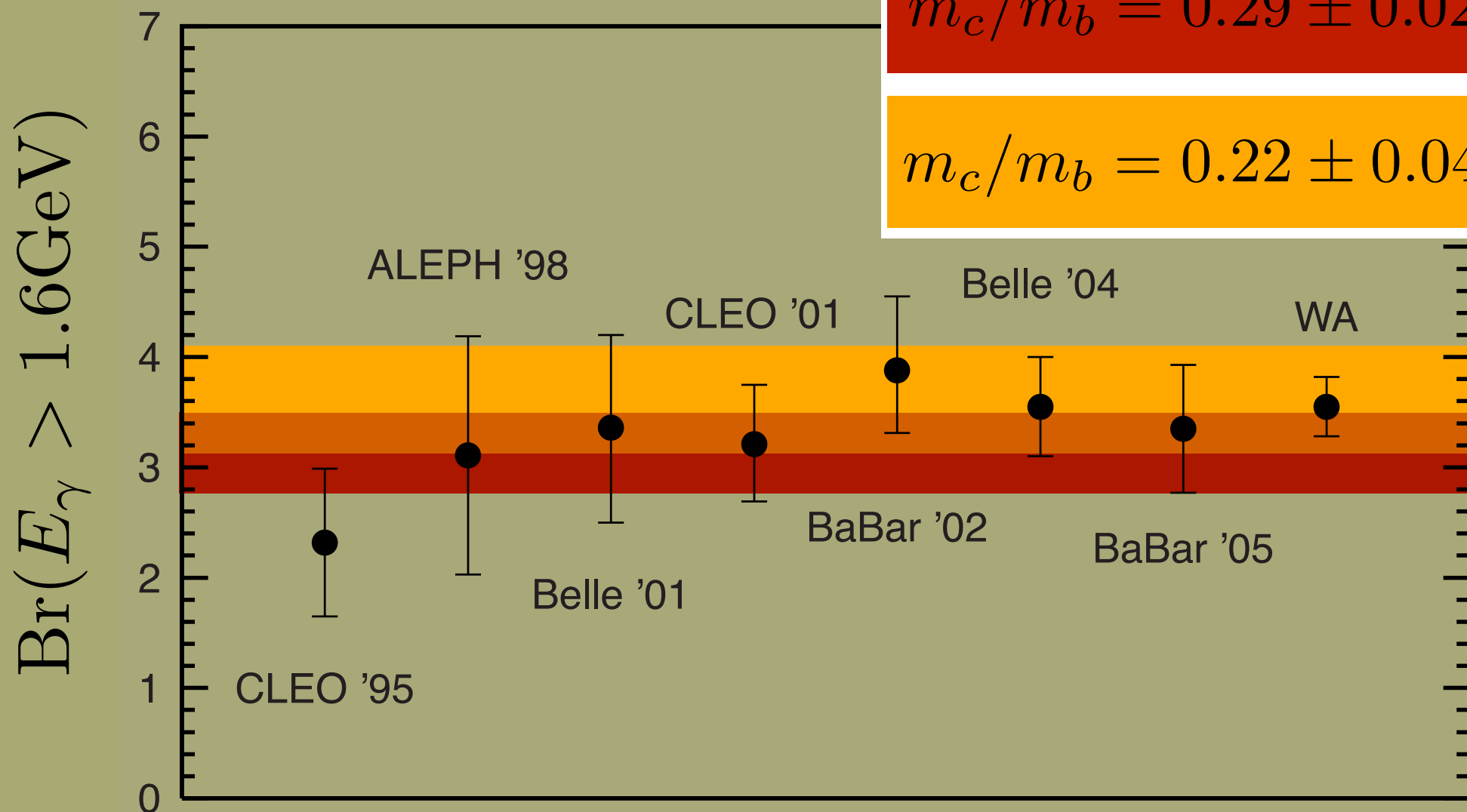
new NNLO results



$$B \rightarrow X_s \gamma$$

Charm mass dependence enters first at NLO:

Strong scheme ambiguity in m_c/m_b only be resolved at **NNLO**



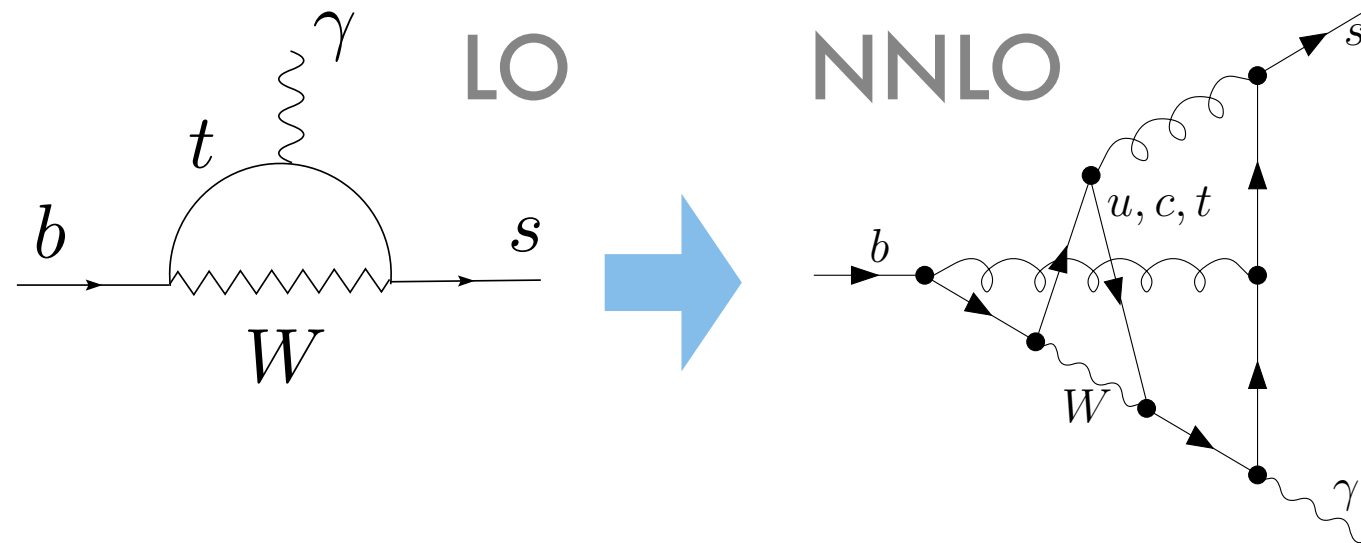
$$m_c/m_b = 0.29 \pm 0.02 \text{ (pole mass)}$$

$$m_c/m_b = 0.22 \pm 0.04 \text{ (}\overline{\text{MS}}\text{)}$$

(old NLO)

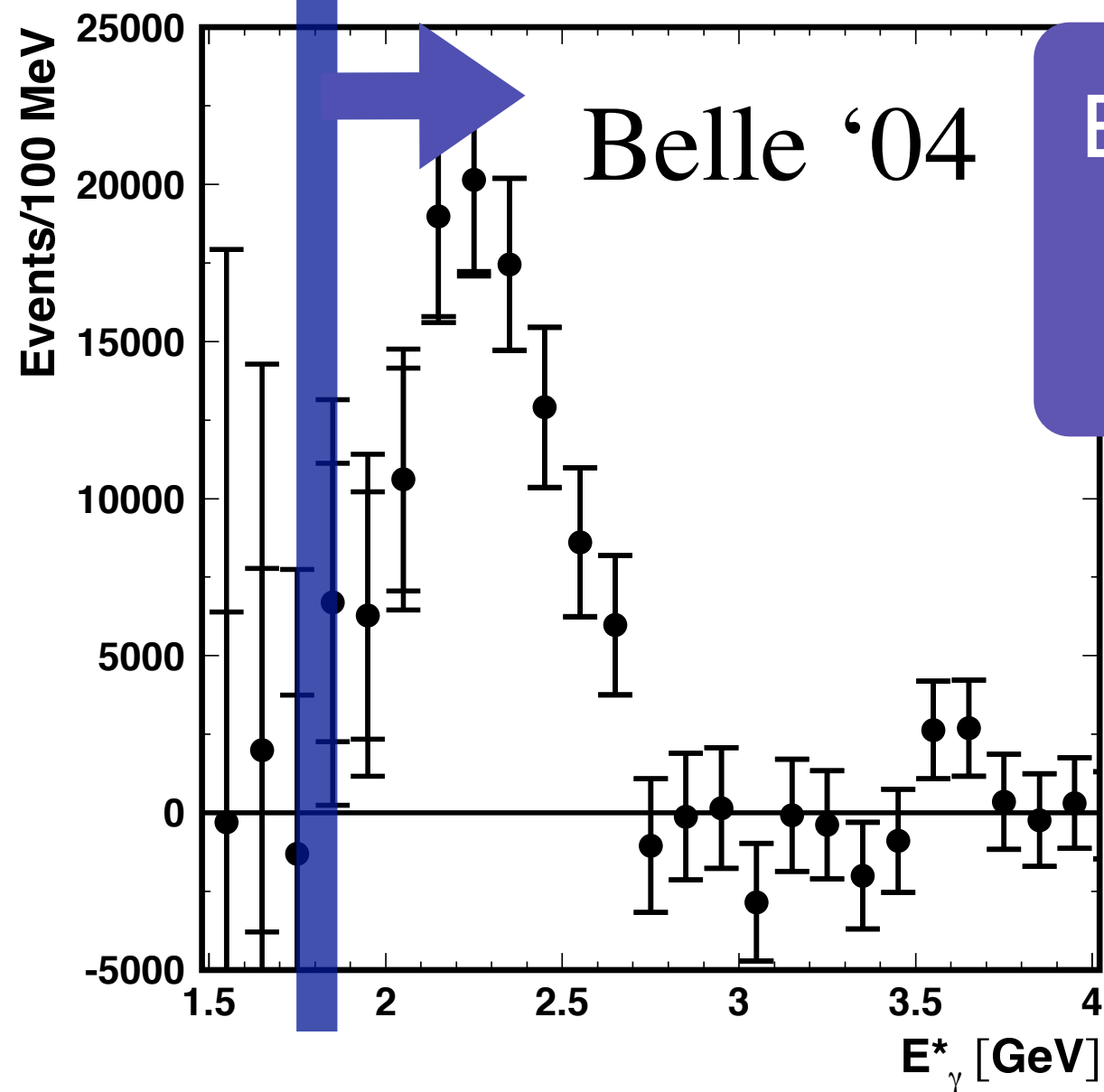
very involved calculation

M. Misiak,^{1,2} H. M. Asatrian,³ K. Bieri,⁴ M. Czakon,⁵ A. Czarnecki,⁶ T. Ewerth,⁴ A. Ferroglia,⁷ P. Gambino,⁸ M. Gorbahn,⁹ C. Greub,⁴ U. Haisch,¹⁰ A. Hovhannisyan,³ T. Hurth,^{2,11} A. Mitov,¹² V. Poghosyan,³ M. Ślusarczyk,⁶ and M. Steinhauser⁹



- 1) 3-loop matching (complete)
- 2) 3 and 4-loop mixing (almost)
- 3) most difficult: 3-loop matrix element (interpolation between $m_c/m_b \gg 1$ and $\alpha_s^2 n_F$ approximation)

Cut in photon energy



$E_\gamma > 1.8$ GeV
to suppress
background

BaBar $E_\gamma > 1.9$ GeV, CLEO $E_\gamma > 2.0$ GeV

Cut in photon energy

with cut $E_0 > E_\gamma$ three relevant scales: Neubert '04; Becher, Neubert '06

(hard) m_b

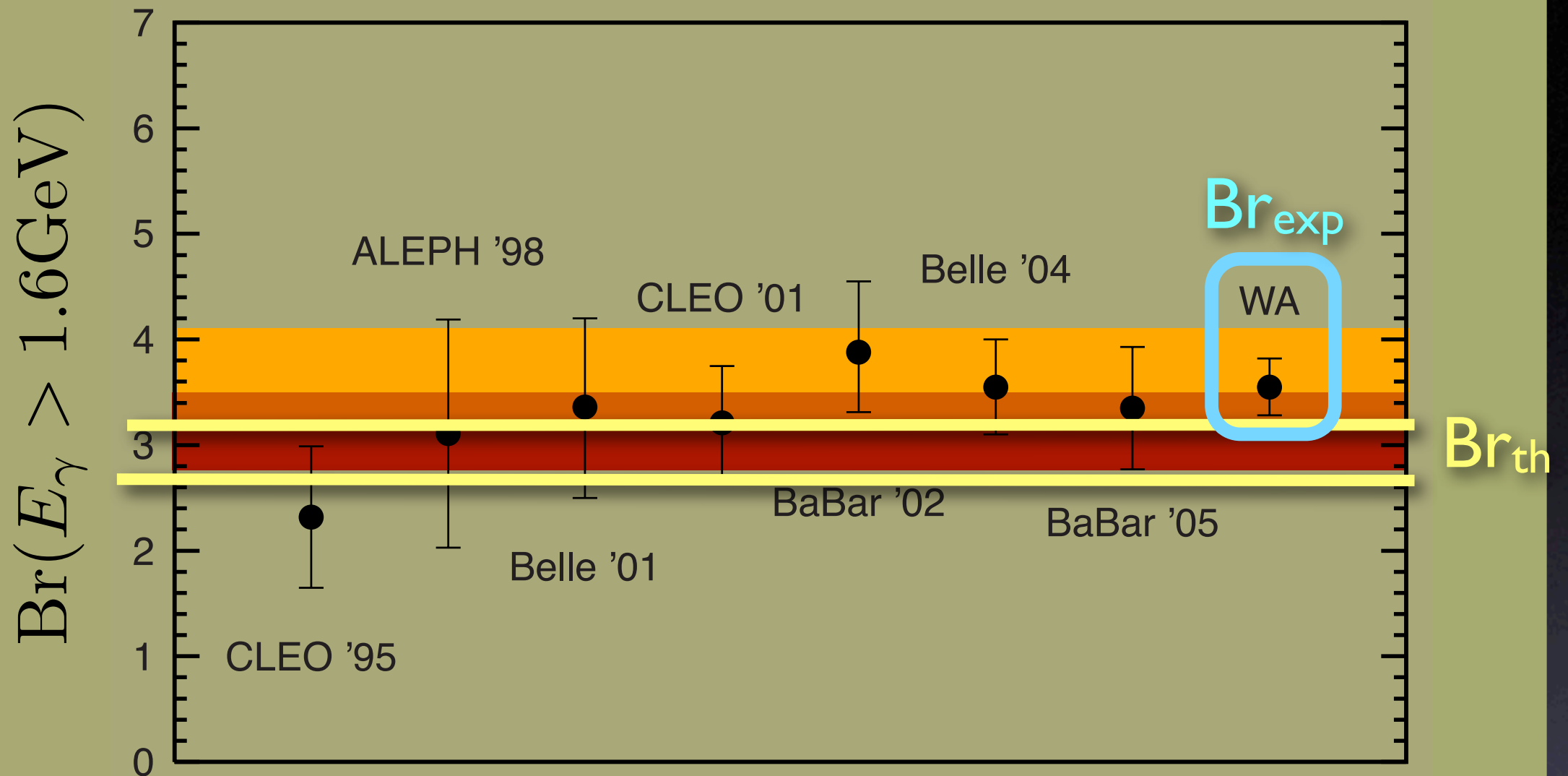
(jet) $(\Delta m_b)^{1/2}$

(soft) $\Delta = m_b - 2E_0 \approx 1 \text{ GeV}$

OPE in terms of $(\Lambda_{\text{QCD}}/\Delta)^n$ and $\alpha_s(\Delta)$

$$\Gamma \sim \underbrace{H^2}_{\text{hard}} \underbrace{J}_{\text{jet}} \otimes \underbrace{S}_{\text{soft}}$$

calculate NNLO corrections to multiscale OPE to resum large logarithms



$$\frac{\text{Br}(\bar{B} \rightarrow X_s \gamma)_{\text{exp}}}{\text{Br}(\bar{B} \rightarrow X_s \gamma)_{\text{th}}} = 1.19 \pm 0.09_{\text{exp}} \pm 0.10_{\text{th}}$$

NNLO estimate of Becher/Neubert '06 including effect of photon energy cut using the recent NNLO result of Misiak et. al '06

MFV MSSM at large $\tan\beta$

Hall, Ratazzi, Sarid

Babu, Kolda

Chankowski, Slawianowska

Bobeth, Ewerth, Krüger, Urban

Huang, Liao, Yan, Zhu

Isidori, Retico

Dedes, Dreiner, Nierste

Dedes, Pilaftis

Chankowski, Rosiek

Foster, Okumura, Roszkowski

Key players

Specific pattern:

Babu, Kolda '02

$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) \sim (\tan\beta)^6$$

$$\Delta M_s \sim (\Delta M_s)^{\text{SM}} - c (\tan\beta)^4$$

Buras, Chankowski, Rosiek, Slawianowska '02

$$\text{Br}(B_u \rightarrow \tau \nu) \sim \text{Br}(B_u \rightarrow \tau \nu)^{\text{SM}} - d (\tan\beta)^2 \quad \text{Isidori, Paradisi '06}$$

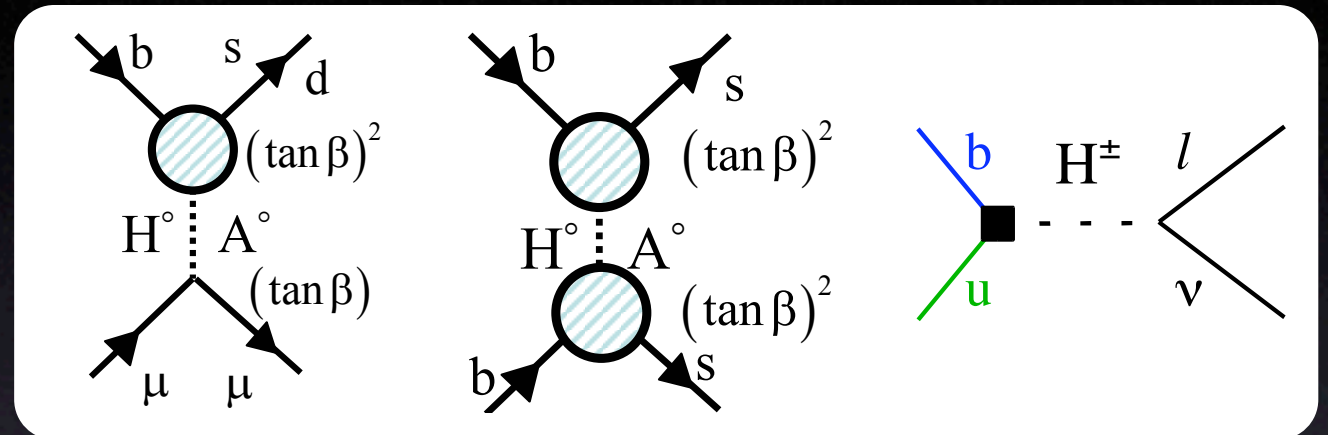
$\text{Br}(B \rightarrow X_s \gamma)$ chargino and H^\pm contributions tend to cancel for $A_U < 0$.

using UTfit '05 and CDF/D0 result; UTfit '06 -> 0.96

$$(\Delta M_s)^{\text{exp}} / (\Delta M_s)^{\text{SM}} = 0.8 \pm 0.12$$

$$R_{\text{BTV}} = (\text{Br}(B_u \rightarrow \tau \nu))^{\text{exp}} / (\text{Br}(B_u \rightarrow \tau \nu))^{\text{SM}} = 0.7 \pm 0.3$$

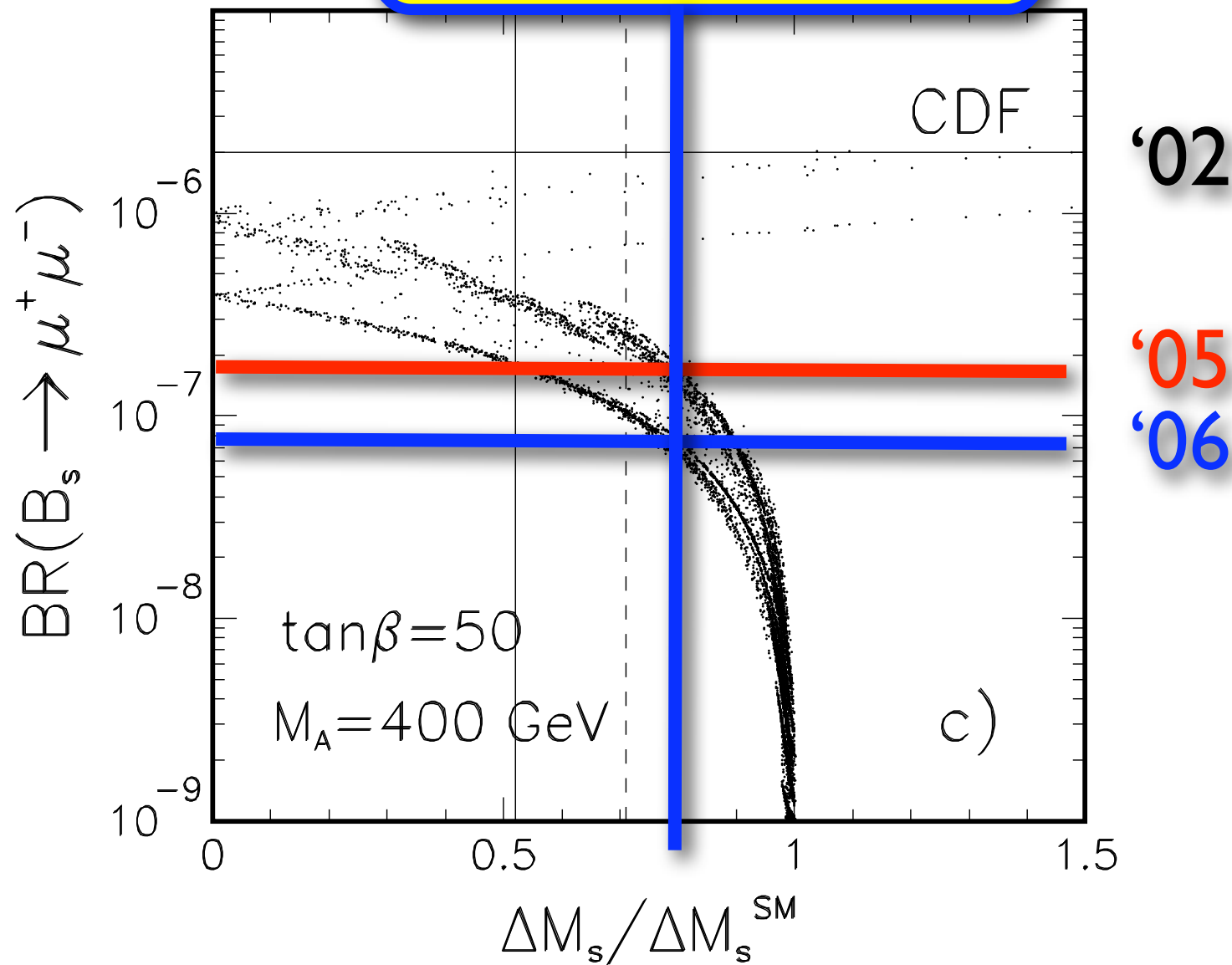
pre-ICHEP 06, post-ICHEP -> R=0.85



$B_s \rightarrow \mu^+ \mu^-$ vs. ΔM_s

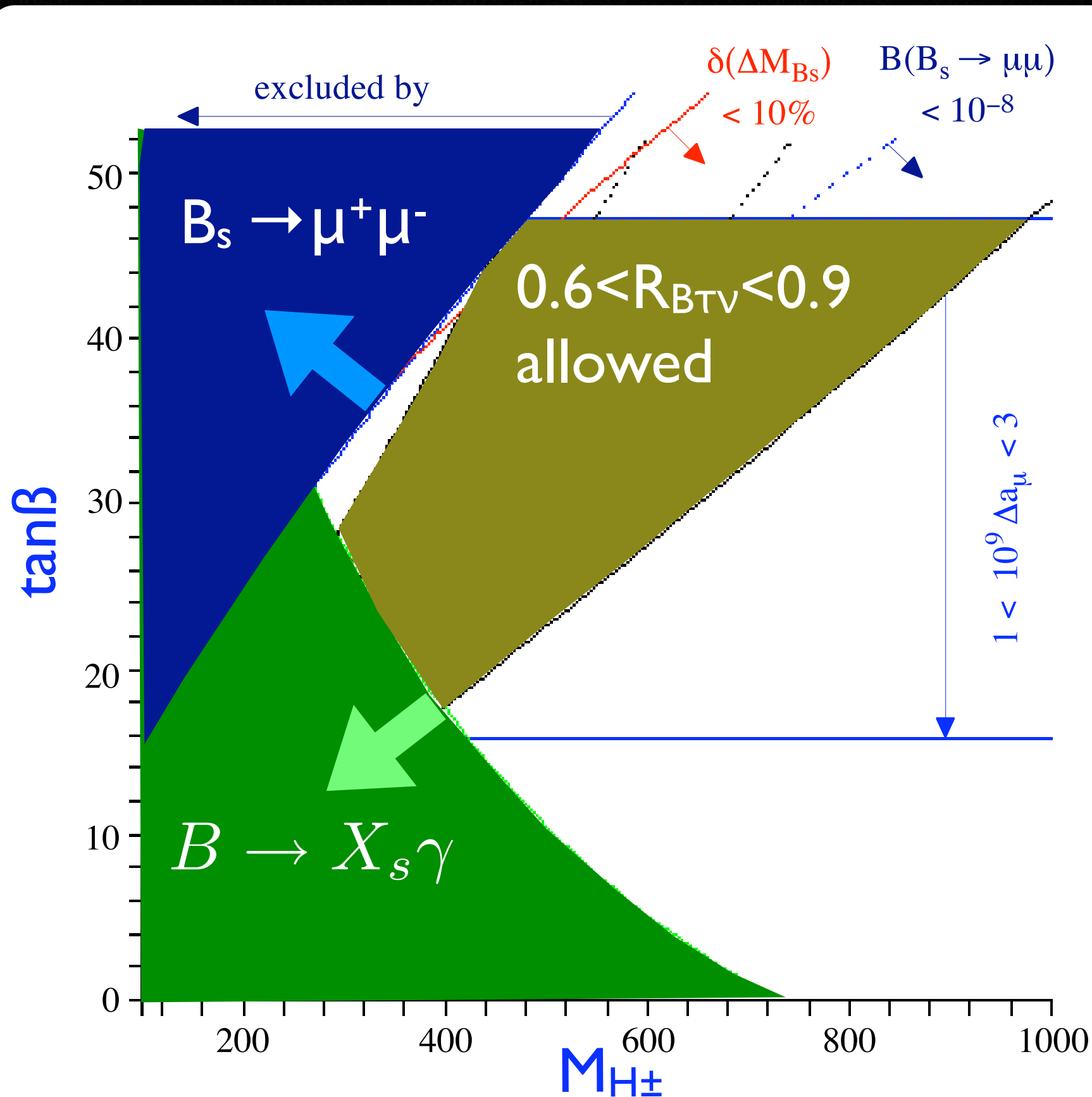
Buras, Chankowski, Rosiek, Slawianowska '02

$$(\Delta M_s)^{\text{exp}} / (\Delta M_s)^{\text{SM}}$$



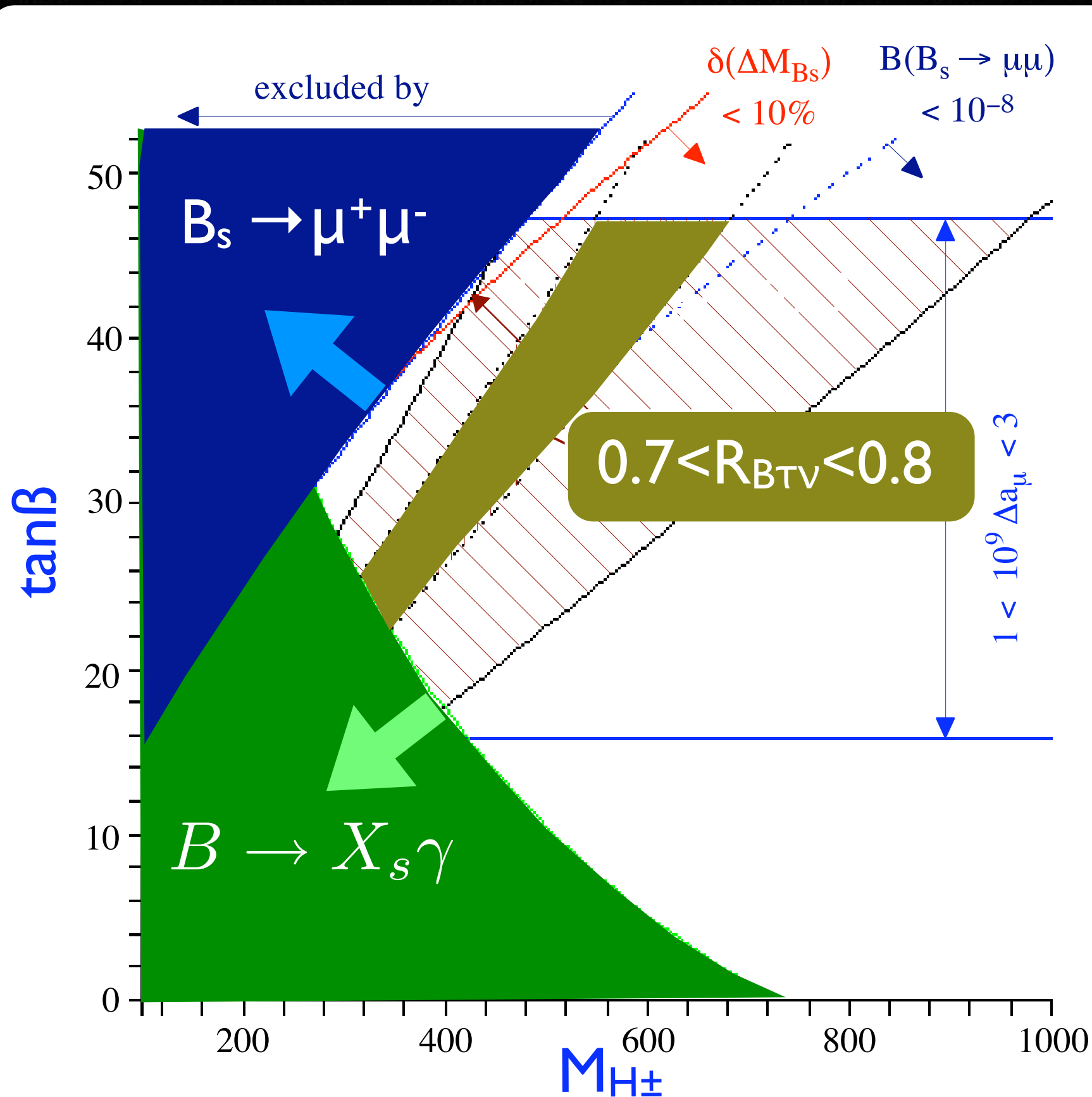
MFV-MSSM and large $\tan\beta$

Isidori, Paradisi '06



MFV-MSSM and large $\tan\beta$

Isidori, Paradisi '06



Outlook and conclusions

- We are puzzled by the flavour problem
- Rare K decays are very sensitive probe into TeV scale flavour violation. Best test of MFV and generically expect large deviations in non-MFV scenarios.
- Beginning of the era of precision flavour tests of NP
- Very interesting NP scenario Little Higgs with T parity: see [C. Tarantino's talk](#) for a discussion of the signatures.
- Theorist's nirvana: measure $K \rightarrow \pi \bar{\nu} \nu$ and $B_s \rightarrow \mu^+ \mu^-$

