

# **SUSY Mass Resolution Studies Progress Report**

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# Outline

- The Colorado SUSY group
- SUSY parameter points and masses
- Simulation tools
- Endpoint method studies
- Determining masses by minimizing  $\chi^2$
- Current status and future work

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# SUSY FastMC Studies at CU Boulder

Many undergraduates contribute to SUSY and calorimetry studies at CU.

Those that have contributed to this presentation include:

Chris Geraci	Paul Steinbrecher	Elliot Smith
Maria Gulda	Kyle Miller	Jack Gill

<http://hep-www.colorado.edu/SUSY>

<http://hep-www.colorado.edu/~nlc>

# SUSY FastMC Studies at CU Boulder

Our task:

- Attempt reconstruction of SUSY masses using fast MC detector simulation

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- Attempt reconstruction of SUSY masses using fast MC detector simulation
- Determine whether measurements are attainable
- Determine whether changes in detector or accelerator design might help with measurements

- The Colorado SUSY group
- **SUSY parameter points and masses**
- Simulation tools
- Endpoint method studies
- Determining masses by minimizing  $\chi^2$
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# The SUSY Parameter points

Nine separate parameter points chosen for studies: SPS1-9

- 6 mSUGRA parameter points
- 2 GMSB points
- 1 AMSB point

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We have focused on SPS1 and several other mSUGRA points

# The SUSY Parameter points

	mSUGRA					
	SPS1	SPS2	SPS3	SPS4	SPS5	SPS6
$M_0$	100	1450	90	400	150	150
$M_{1/2}$	250	300	400	300	300	300
$A_0$	-100	0	0	0	-1000	0
$\tan(\beta)$	10	10	10	50	5	10
$\mu$	352.39	124.77	508.59	377.03	639.80	393.09

	GMSB			AMSB
	SPS7	SPS8		SPS9
$\Lambda$	40,000	100,000	$M_0$	400
$M_{mes}$	80,000	200,000	$M_{3/2}$	60000
$N_5$	3	1	$\tan(\beta)$	10
$\tan(\beta)$	15	15	$\mu$	869.90
$\mu$	300.03	398.31		

# The SUSY Masses

	minimal SUGRA						GMSB		AMSB
	SPS1	SPS2	SPS3	SPS4	SPS5	SPS6	SPS7	SPS8	SPS9
$\tilde{\chi}_1^0$	96.05	79.54	160.55	118.66	119.51	117.50	161.65	137.19	175.51
$\tilde{\chi}_2^0$	176.82	135.34	296.95	218.14	226.33	215.54	260.06	252.33	549.03
$\tilde{\chi}_3^0$	358.81	140.84	512.87	383.91	642.83	398.70	306.26	404.00	874.37
$\tilde{\chi}_4^0$	377.81	269.45	529.57	401.08	652.95	418.06	379.94	426.28	875.97
$\tilde{\chi}_1^+$	176.38	104.03	296.85	218.06	226.33	215.20	256.33	252.03	175.67
$\tilde{\chi}_2^+$	378.23	269.03	529.51	402.28	652.68	418.19	379.45	426.47	877.22
$h^0$	113.97	115.71	116.95	115.39	119.79	114.71	113.57	114.83	114.83
$H^0$	394.15	1444.10	573.03	404.63	694.03	457.84	378.37	515.01	912.56
$A^0$	393.63	1442.95	572.42	404.43	693.86	457.26	377.89	514.49	911.74
$H^+$	401.77	1446.18	578.30	416.28	698.49	464.40	386.70	521.17	915.83
$\tilde{\nu}_e$	186.00	1454.17	275.99	441.22	244.52	243.25	249.06	347.61	309.71
$\tilde{e}_R^-$	142.97	1451.69	178.33	416.54	191.45	191.30	127.43	175.87	303.01
$\tilde{e}_L^-$	202.14	1456.33	287.11	448.40	256.30	255.81	261.47	356.61	319.66
$\tilde{\tau}_1^-$	133.22	1439.46	170.59	267.61	180.67	184.34	120.45	169.42	271.28
$\tilde{\tau}_2^-$	206.13	1450.38	289.22	414.91	257.86	258.31	263.40	357.59	322.54
$\tilde{t}_1$	379.11	1003.88	623.83	530.58	220.74	474.12	779.09	957.65	1005.17
$\tilde{t}_2$	574.71	1307.41	819.54	695.88	644.65	659.73	863.00	1058.68	1128.80
$\tilde{b}_1$	491.91	1296.56	757.50	606.86	535.86	589.80	822.17	1021.90	1112.07
$\tilde{b}_2$	524.59	1520.09	791.35	706.45	622.99	623.42	843.35	1048.26	1232.88
$\tilde{u}_R$	520.45	1530.08	791.78	715.10	624.49	621.87	830.54	1033.16	1227.35
$\tilde{u}_L$	537.25	1532.70	816.57	730.24	641.82	638.97	859.66	1080.25	1218.09
$\tilde{g}$	595.19	784.37	914.26	721.03	710.31	708.58	926.04	820.50	1275.18

# The SUSY Masses

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# Simulation Tools

## Event Generation:

- ISAJET - SUSY and Standard Model background
- HERWIG -  $e^+e^- \rightarrow e^+e^-\gamma^*\gamma^*$
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## Analysis

- ROOT

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# Endpoint Method Overview

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$$X \rightarrow Y + Z$$

$$E(X) = 250 GeV$$

$$E(Z) = \gamma(E_{Z,cm} + \beta P_{Z,cm} \cos(\theta))$$

Energy of visible (particle  $Z$ ) follows a uniform distribution between an  $E_{max}$  and  $E_{min}$ .

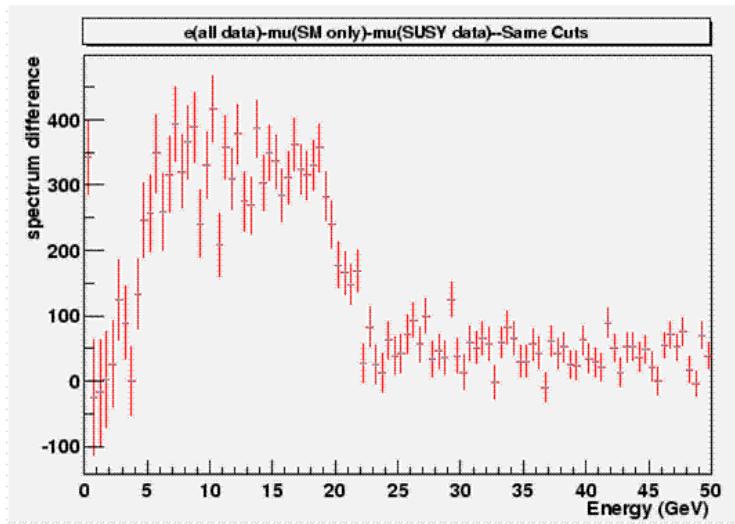
# Endpoint method - Example: SPS1 $\tilde{\nu}_e \bar{\tilde{\nu}}_e$

$$e^+ e^- \rightarrow \tilde{\nu}_e \bar{\tilde{\nu}}_e$$

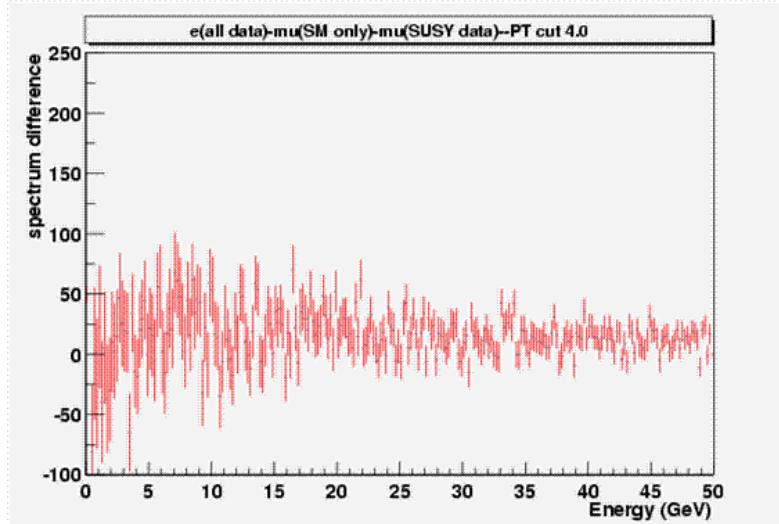
$$\tilde{\nu}_e \rightarrow \tilde{\chi}_1^0 \nu (87.9\%)$$

$$\tilde{\nu}_e \rightarrow \tilde{\chi}_1^+ e^- (8.9\%)$$

left polarization



right polarization



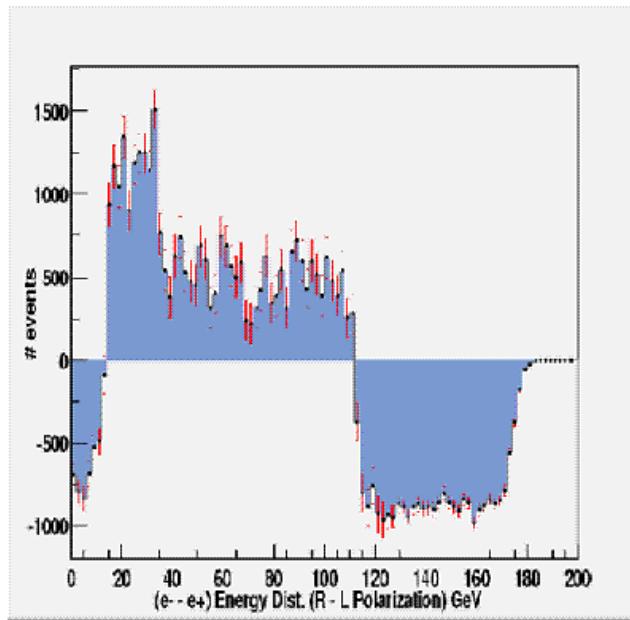
# Endpoint method - SPS1 $\tilde{\nu}_e \bar{\tilde{\nu}}_e$ - Results

	$E_{low}$	$E_{high}$
No Brems	$4.11 \pm 0.04$	$21.10 \pm 0.09$
Brems	$4.22 \pm 0.08$	$20.40 \pm 0.12$

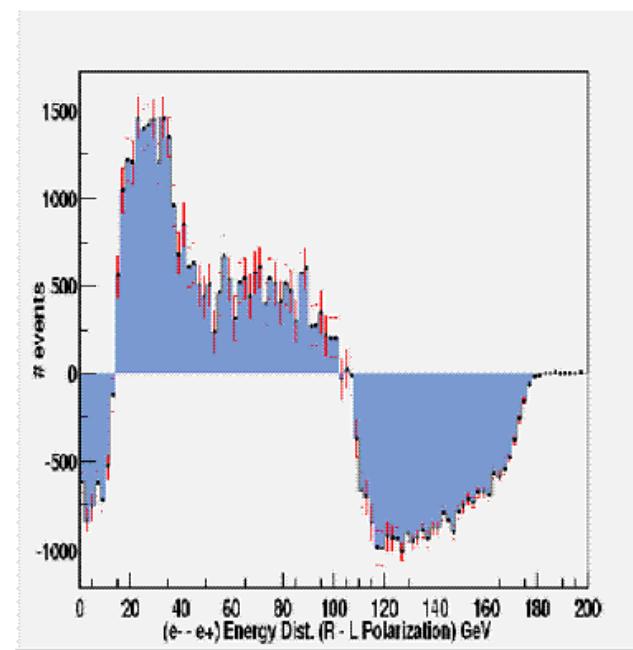
	$M_{\tilde{\nu}_e}$	$M_{\tilde{\chi}_1^0}$
Input	186.00	176.38
No Brems	$184.7 \pm 0.7$	$175.1 \pm 0.7$
Brems	$188.4 \pm 0.7$	$178.9 \pm 0.7$

# Endpoint method and Beam/Bremsstrahlung

No Bremsstrahlung



With Bremsstrahlung



Bremsstrahlung and beamstrahlung destroy the energy endpoints. However, the energy distribution is still highly dependent upon the particle masses.

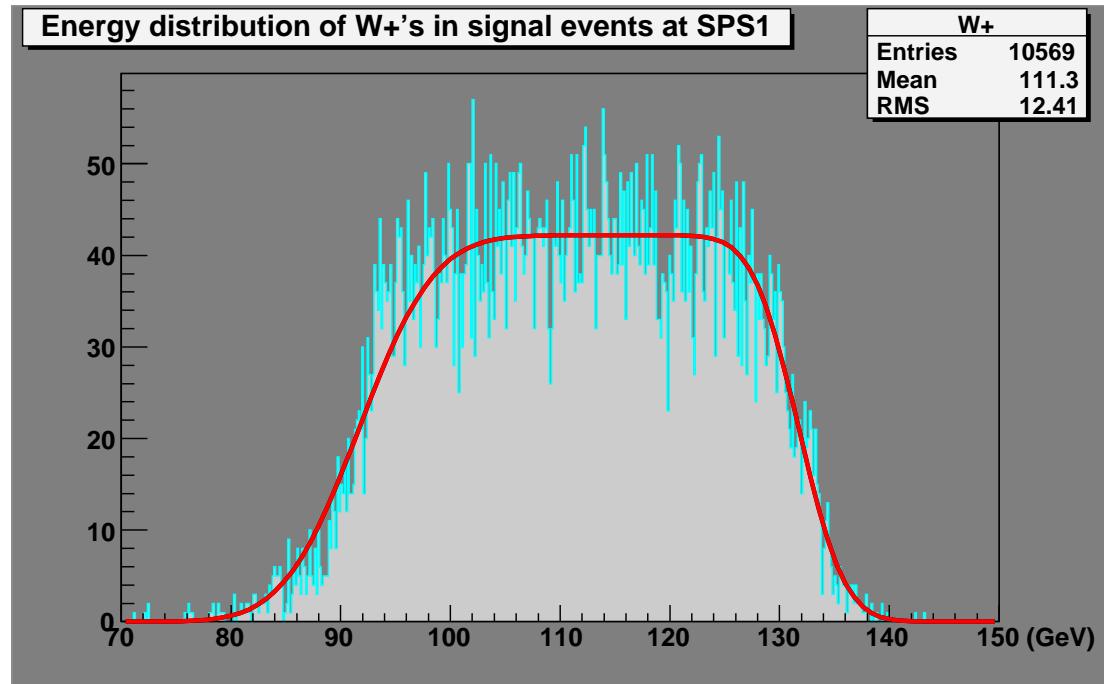
# Endpoint method - $\tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0$

$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-$$

$$\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 W^\pm$$

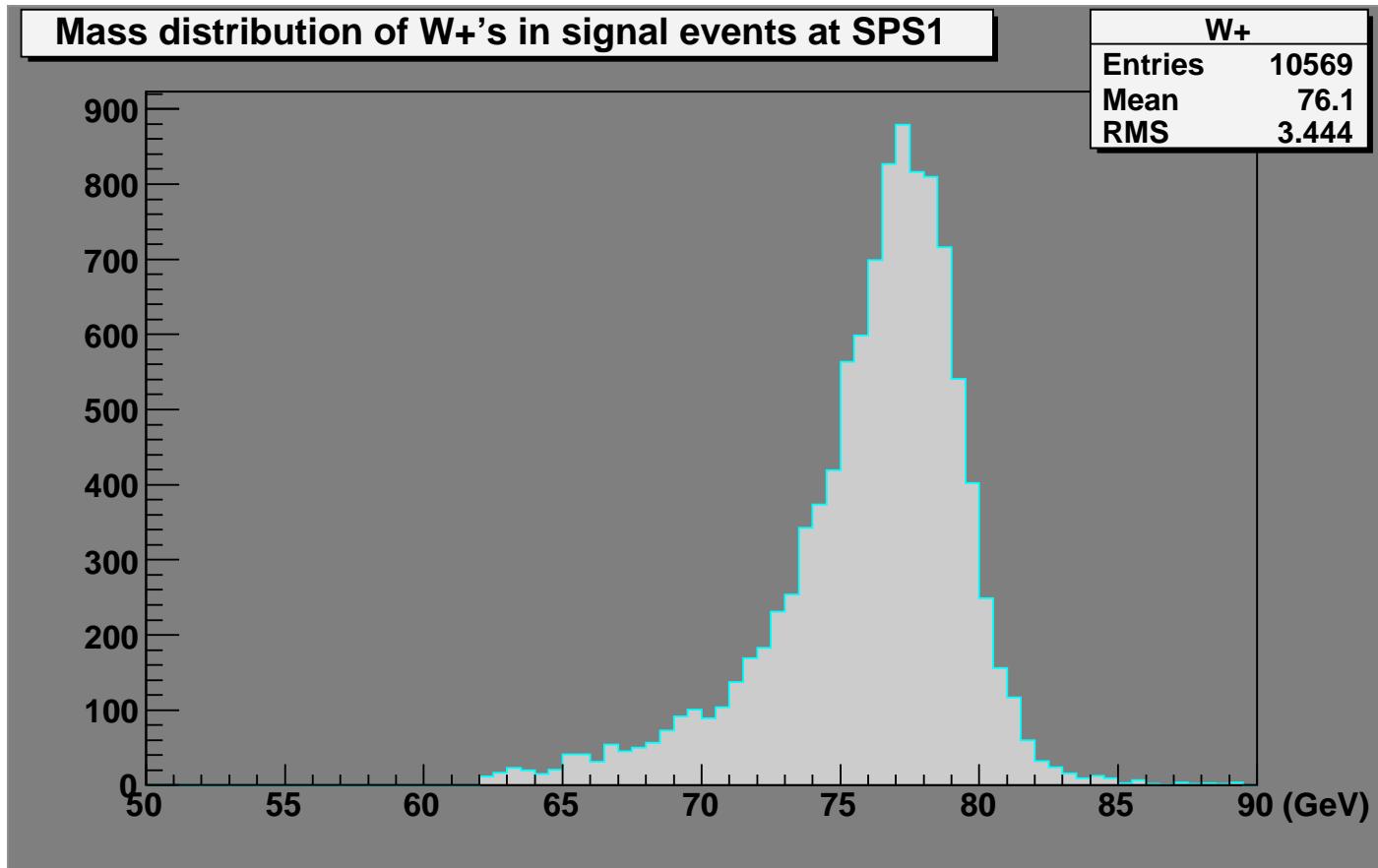
$$W^\pm \rightarrow \ell^\pm \nu_\ell$$

$$W^\mp \rightarrow q\bar{q}'$$



	Reconstructed Mass	MC Mass
$\tilde{\chi}_1^0$	$101.0 \pm 0.3$ (statistical)	95.185
$\tilde{\chi}_1^\pm$	$186.8 \pm 0.5$ (statistical)	180.374

# Endpoint method - $\tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0$



Bias in  $W$  mass reconstruction affects reconstruction of gaugino mass

# Endpoint Method - Conclusions

- 2-body decays provide a distinct signal for SUSY searches
- The endpoint method can be used to make a rough first calculation of the mass
- Brems-/beamstrahlung make precision measurements impossible
- Precision measurements are impossible in the best case when the visible particle is a W or Z

SUSY signals are distinct enough to yield precision mass measurements

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# Measuring Masses by $\chi^2$ Analysis

- Use ISAJET to create one year of SUSY, SM data
- Determine cuts to isolate signal
- Compare energy distribution to distribution using different input masses
  - Each variation uses 10 years of data in order to minimize uncertainty in histogram bin size
- Best mass for 1-year data set corresponds to minimum  $\chi^2$
- Uncertainty is the change in mass which causes a change of 1 in  $\chi^2$

# $\chi^2$ Analysis - SPS6 $\tilde{\nu}_e \bar{\tilde{\nu}}_e$

$$e^+ e^- \rightarrow \tilde{\nu}_e \bar{\tilde{\nu}}_e$$

$$\tilde{\nu}_e \rightarrow \tilde{\chi}_1^0 \nu_e; \bar{\tilde{\nu}}_e \rightarrow \tilde{\chi}_1^- e^+$$

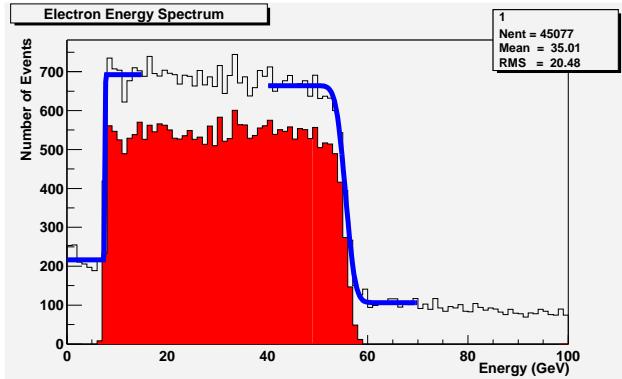
$$\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 W^- \rightarrow hadrons$$

Cuts:

- number of particles
- reconstructed W mass
- energy of W

# $\chi^2$ Analysis - SPS6 $\tilde{\nu}_e \bar{\tilde{\nu}}_e$

No Bremsstrahlung

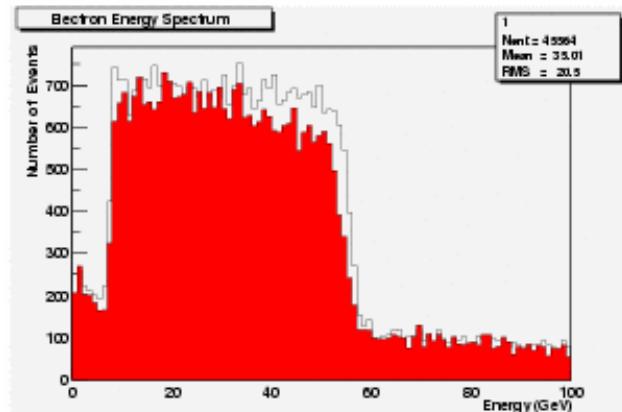


	Recon Mass	MC Mass
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$\tilde{\nu}_e$	$243.6 \pm 0.5$	243.85
$\tilde{\chi}_1^\pm$	$222.1 \pm 0.5$	222.38

red = signal

With Bremsstrahlung



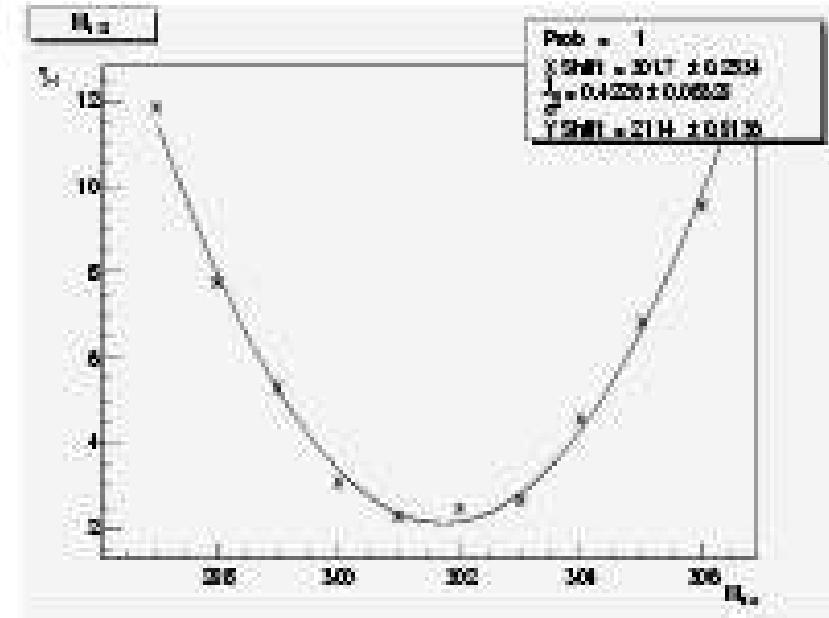
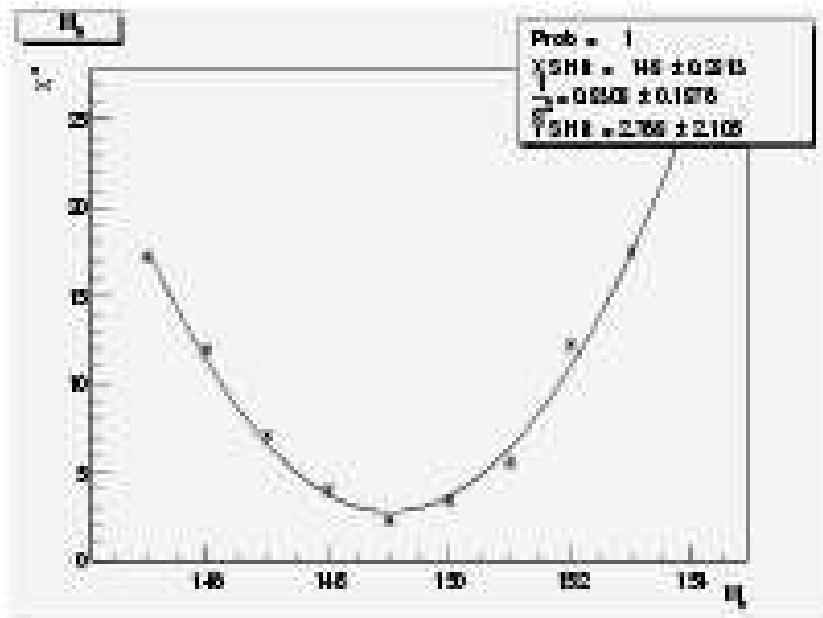
	Recon Mass	MC Mass
--	------------	---------

$\tilde{\nu}_e$	$248.9 \pm 0.8$	243.85
$\tilde{\chi}_1^\pm$	$227.4 \pm 0.4$	222.38

red = bremsstrahlung

# $\chi^2$ Analysis - SPS6 $\tilde{\nu}_e \bar{\tilde{\nu}}_e$

- $\chi^2$  of the distribution varies as a function of  $M_0$  and  $M_{1/2}$



Recon Mass    MC Mass

$\tilde{\nu}_e$

$243.6 \pm 0.1$

243.85

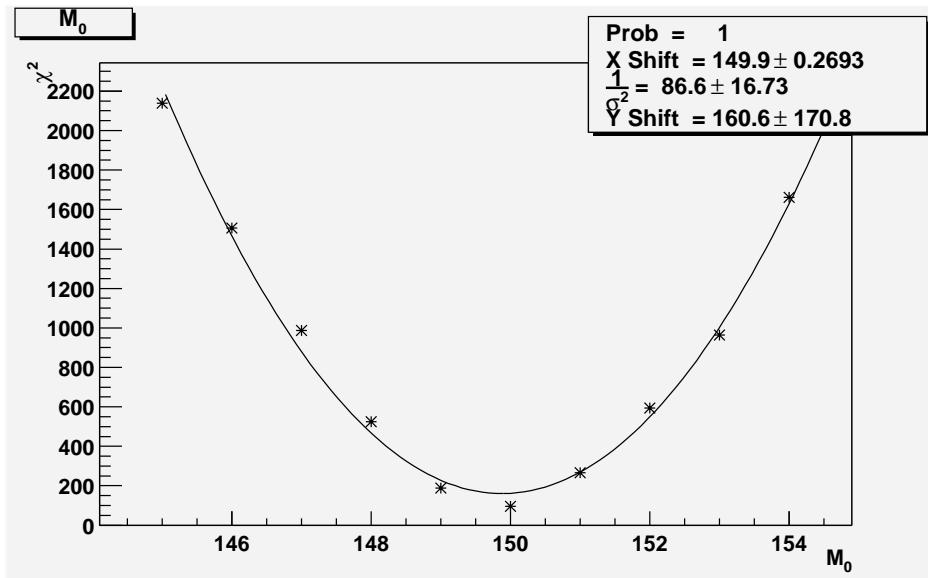
$\tilde{\chi}_1^\pm$

$222.4 \pm 0.3$

222.38

# $\chi^2$ Analysis - SPS6 $\tilde{\nu}_e \bar{\tilde{\nu}}_e$

- Similar analysis as at SPS6:



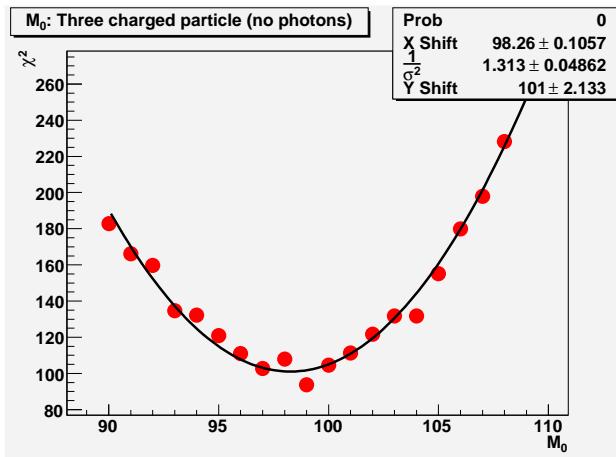
Recon Mass    MC Mass

$\tilde{\nu}_e$        $244.8 \pm 0.1$       245.9

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# Current Status and Future Work

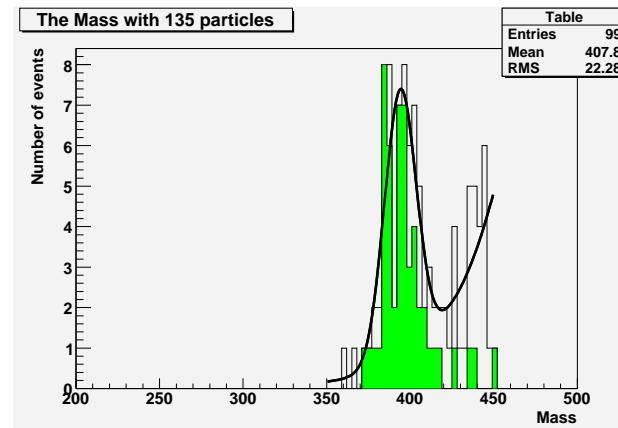
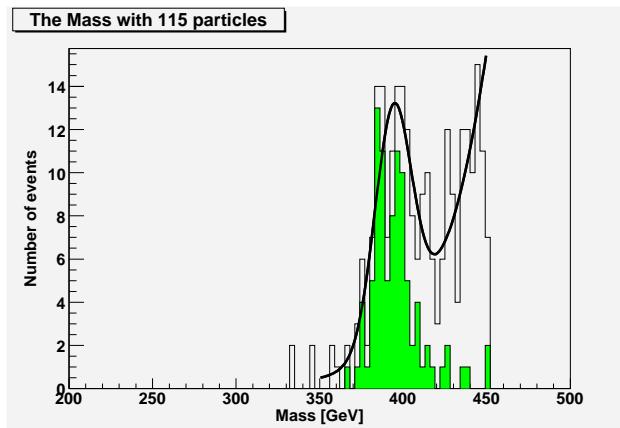
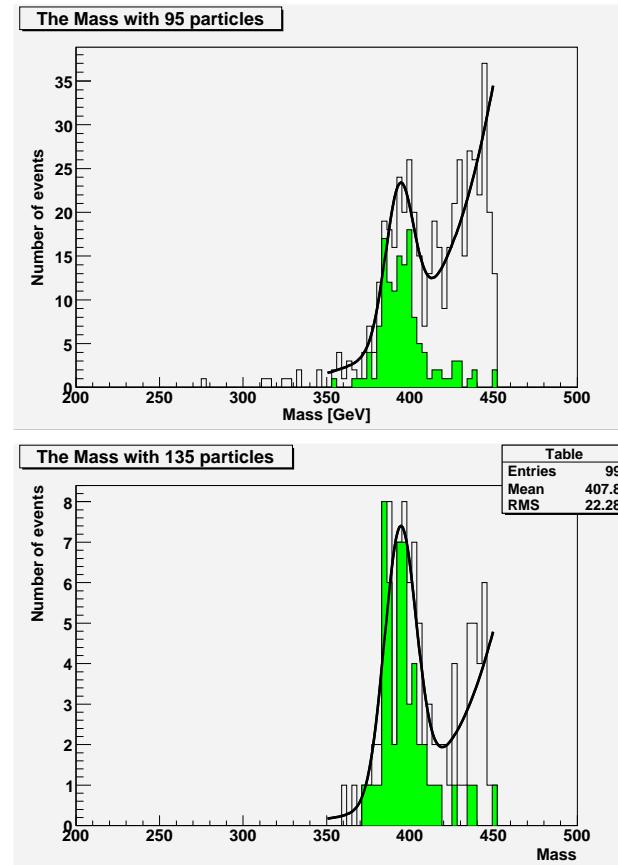
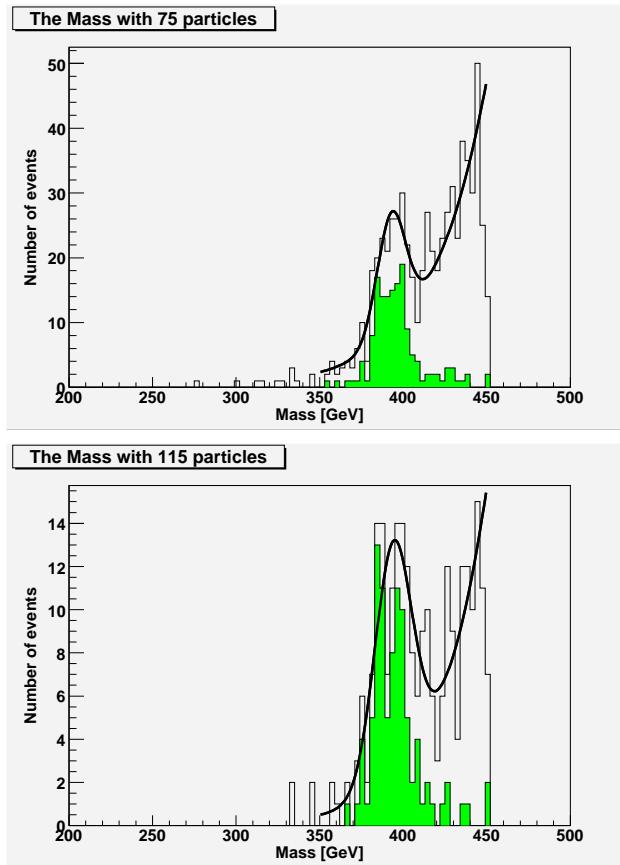
- Signal analysis is an ongoing process



Three-prong taus produce energy distributions that may yield successful mass determination.

# Current Status and Future Work

- Signal analysis is an ongoing process



$H+ \rightarrow t\bar{b}$  at 1 TeV produces a significant mass peak.

# Snowmass Mountain, CO - 14092'

