

Analysis of Stop Quark with Small Stop-Neutralino Mass Difference at the ILC

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1-Introduction

- Scalar top studies for small visible energy in the detector.
- Theoretical motivation: Electroweak symmetry in particle physics and the nature of dark matter and baryogenesis in cosmology both suggest the existence of new symmetries within the reach of the next generation of colliders.
- Recently, the universe dark matter energy density has been precisely measured by the Wilkinson Microwave Anisotropy Probe (WMAP) to be $\Omega_{\text{CDM}} h^2 = 0.1126 \pm 0.0161 / -0.0181$.
- The super-symmetry with R parity conservation provides a stable neutral dark matter candidate, the Neutralino with mass and $\sigma \sim E.W$ energy scale.
- The Neutralino-Stop co-annihilation region is characterized by a small mass difference $M(\text{stop-neutralino}) = 15\text{-}30 \text{ GeV}$, with relic density compatible with the WMAP observation. ILC reach Complementary to LHC reach
- Of interest the stop decay into 2 soft charm jets and missing energy.
- Possible benchmark for vertex detectors and material budget.

2-Theoretical Motivation

- Electroweak Baryogenesis:

Sakharov Requirements:

- 1- Baryon Number Violation - (SM - Anomalous process)
- 2- C & CP violation - (SM-Quark CKM mixing)
- 3- Departure from Equilibrium - (SM-at EW phase transition)

Limitations of SM:

2) Not Enough CP violation & 3) $\rightarrow M_{Higgs} < 40 \text{ GeV}$, LEP Bound $M_{Higgs} > 114.4 \text{ GeV}$

$\rightarrow$ Supersymmetry with light scalar top, below the top mass: $m_{\tilde{t}_1} < m_t$

- Dark Matter

The Supersymmetric Lightest particle (LSP), the neutralino X^0_1 is a candidate

The annihilation cross-section $\sigma_a(X^0_1, X^0_1)$ too small

But for $m_{\tilde{t}_1} - m_{X^0_1} \sim 15\text{-}30 \text{ GeV}$, there is co-annihilation between the $\tilde{t}_1$ and the $X^0_1 \rightarrow \sigma_a(X^0_1, \tilde{t}_1) + \sigma_a(X^0_1, X^0_1)$ consistent with dark matter.

3-Signal And Background Cross-Sections (pb)

Process	$\sigma(\text{pb})$ - A. Freitas+Calvin(QCD)		
	Pr(0,0)	Pr(-80%,+60%)	Pr(+80%,-60%)
$\tilde{t} \tilde{t}^* M_{\tilde{t}_1}=120 \text{ GeV}$	0.115	0.153	0.187
$M_{\tilde{t}_1}=140 \text{ GeV}$	0.093	0.124	0.151
$M_{\tilde{t}_1}=180 \text{ GeV}$	0.049	0.065	0.079
$M_{\tilde{t}_1}=220 \text{ GeV}$	0.015	0.021	0.020
w^+w^-	8.55	24.54	0.77
$w\bar{e}v$	6.14	10.57	1.82
ZZ	0.49	1.02	0.44
eeZ	7.51	8.49	6.23
$t\bar{t}$	0.55	1.13	0.50
$qq, q\neq t$	13.14	25.35	14.85
$\gamma\gamma, p_T>5\text{GeV}$	936		

Table 1- $P(e^-)/P(e^+) = -80\%/+60\%$; $P(e^-)/P(e^+) = +80\%/-60\%$, $\sigma(eeZ)$ & $\sigma(W\bar{e}v)$ are from Grace and do not include Beamstrahlung/ISR The Signal is given for $\cos\theta_t = 0.5$

4- Selection $e^+ e^- \rightarrow \tilde{t}_1 \tilde{t}_1^* \rightarrow c \tilde{\chi}_0^1 \bar{c} \tilde{\chi}_0^1$

- Pythia with Simdet/Tesla was used for the simulations of both signal and background with CIRCE for the Beamstrahlung.
- Signature: 2 soft charm jets + missing energy
- Luminosity=500 Fb⁻¹ ; $\sqrt{s}$ =500 GeV
- A short list of the sequential cuts applied as a preselection first, allowed larger samples to be produced and the cut refined at selection stage.

Pre-selection:

- 4 < Number of Charged tracks < 50
- Pt > 5 GeV
- $\cos\theta_{\text{Thrust}} < 0.8$
- $|P_{l,\text{tot}}|/P < 0.9$
- $E_{\text{vis}} < 380$ GeV
- M(inv) < 200 GeV

Selection:

- Njets = 2
- Cos ($\Phi_{\text{A-coplanarity}}$) > -0.9
- $\cos\theta_{\text{Thrust}} < 0.7$, $P_t > 12$ revisited.
- $E_{\text{vis}} < 0.4 \sqrt{s}$
- $60 \text{ GeV}^2 < \text{Minv}_{\text{jets}} < 90 \text{ GeV}^2$
- c-tagging- From T. Khul

5a-Pre-selection: Efficiency Each Cut

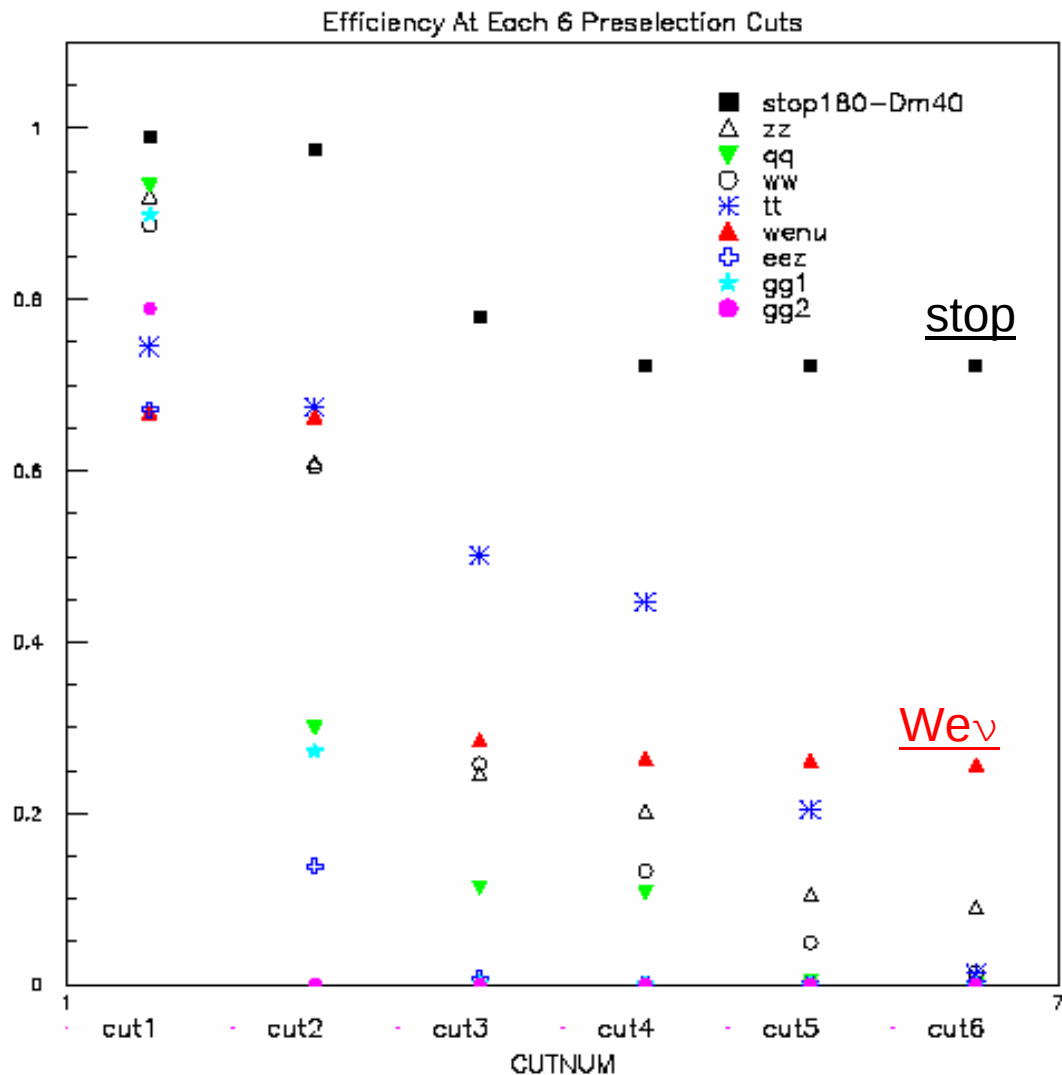


Fig 1

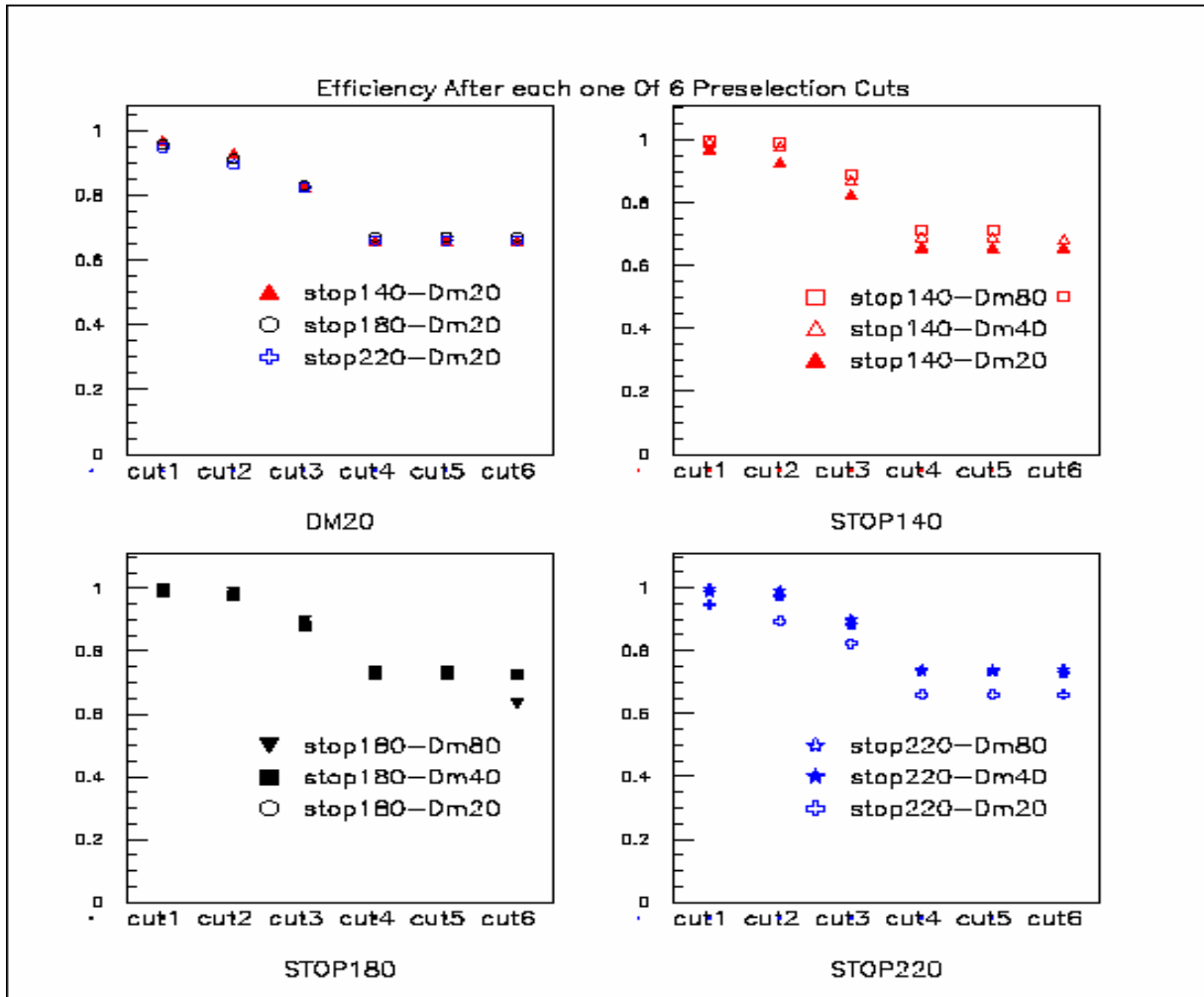
Colour point:

% of Background left after each cut,
Reduced < 30%

Black Points:

% of signal left after each cut, Ends up to a
~70% signal left

5b-Pre-selection Efficiency: Stop



Upper Left:

$\Delta M(\tilde{t}_1 - X_0) = 20 \text{ GeV}$

$M_{\tilde{t}_1} = 140 \text{ GeV}$

$M_{\tilde{t}_1} = 180 \text{ GeV}$

$M_{\tilde{t}_1} = 220 \text{ GeV}$

Independent of $M_{\tilde{t}_1}$

Others:

$\Delta M(\tilde{t}_1 - X_0) =$

20, 40, 80 GeV

Separately for $\neq M_{\tilde{t}_1}$

~Independent of

$\Delta M(\tilde{t}_1 - X_0)$

Fig. 2

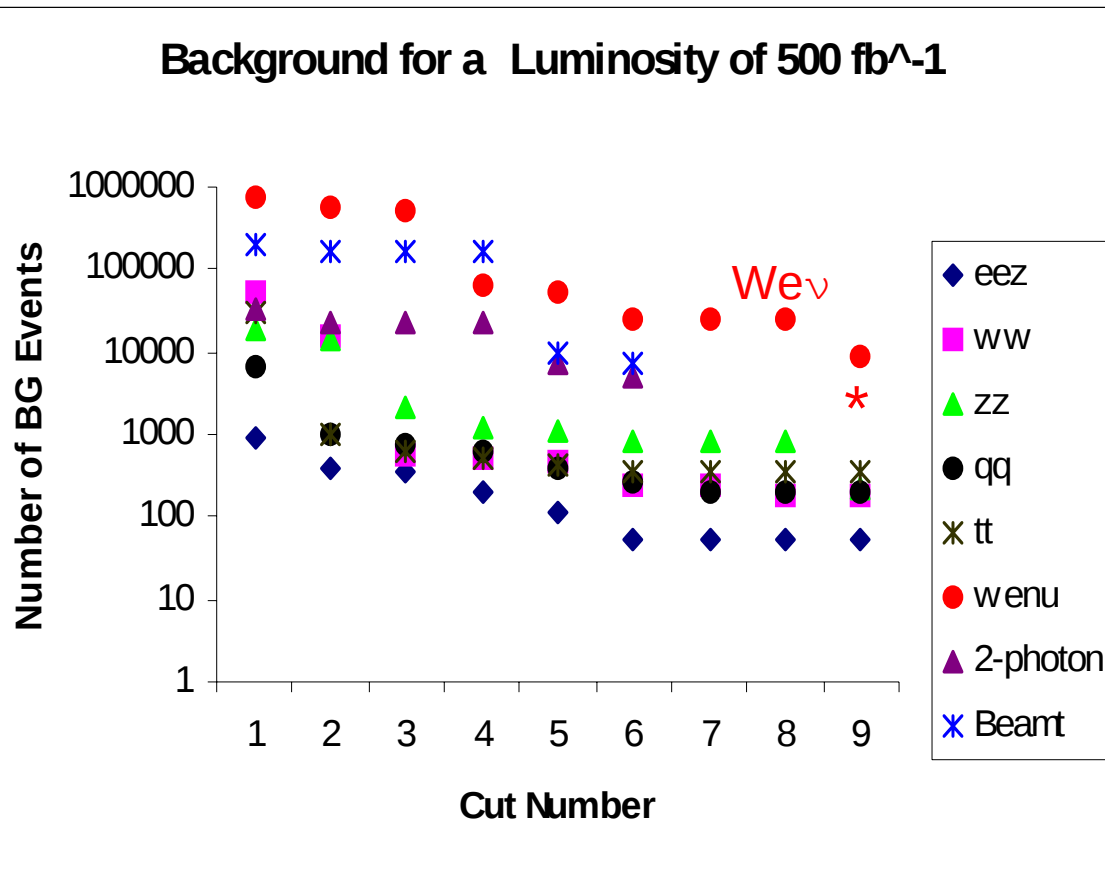
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6a-Selection: The Background Rejection

Background	% Left - End Presel	Number Gen. Selection	Num Events Left after End Sel. – For 500 fb ⁻¹	
YY	0.06%	8.00 Millions	0.	< 164.
ZZ	9%	0.03 M	35.	257.
qq, q≠t	0.09%	0.35 M	8.	160.
ww	1.45%	0.21 M	8.	145.
tt	1.36%	0.18 M	25.	38.
wev	25.70%	0.21 M	345	5044.
eez	0.06%	0.21 M	2	36.

Table 2-The cut efficiency- And the number of background particles left normalized to 500fb⁻¹ are shown in the next figure for each BG channel separately. Largest remaining Background :**Wev** , already **reduced by a factor 2 by c-tagging**

6b-Selection: The Background Rejection



For a Luminosity of 500 fb^{-1} , the number of BG events left are reported after each of the 9 selection cuts

The **c-tagging reduces the $W e \nu$ background to half** its previous value, the **red Star** in the plot. It is the leading background

Fig. 3

7a-Selection: The Signal Efficiency

Background	% Left - End Presel	Number Gen. Selection	% Left - Num. Left End Sel. – For 500 fb ⁻¹	
Mstop=140				
Dm=20	68.5	50000	20.9	9720
Dm=40	71.8	50000	10.1	4700
Dm=80	51.8	50000	10.4	4840
Mstop=180				
Dm=20	68 .0	25000	28.4	6960
Dm=40	72.7	25000	20.1	4925
Dm=60	63.3	25000	15.0	3675
Mstop=220				
Dm =20	66.2	10000	34.6	2600
Dm=40	72.5	10000	24.2	1815
Dm=60	73.1	10000	18.8	1410

Table 3

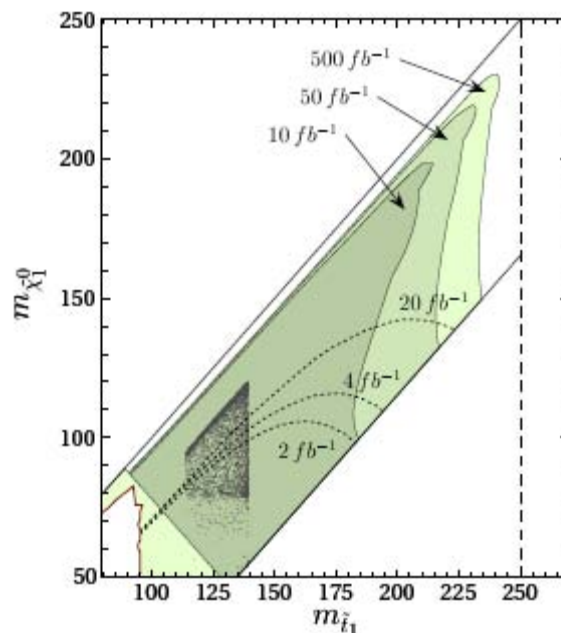
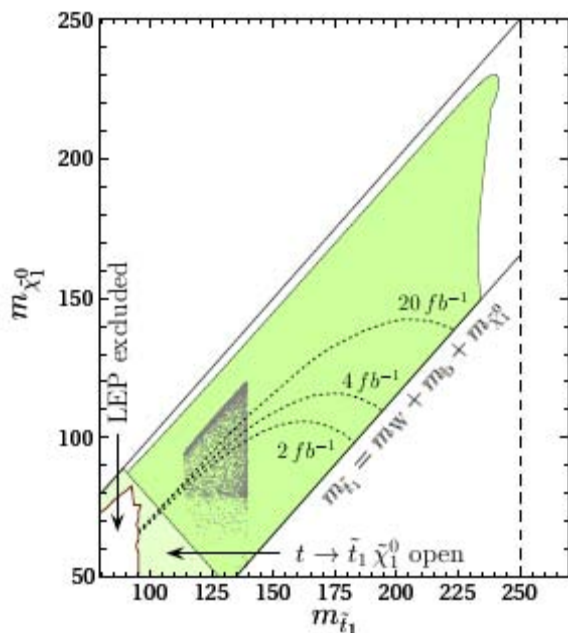
7b-Signal Efficiency

Δm (GeV)	$\tilde{M}_{t_1}=120\text{GeV}$	$\tilde{M}_{t_1}=140\text{GeV}$	$\tilde{M}_{t_1}=180\text{GeV}$	$\tilde{M}_{t_1}=220\text{GeV}$
80		10%	15%	19%
40		10%	20%	24%
20	17%	21%	28%	35%
10	19%	20%	19%	35%
5	2.5%	1.1%	0.3%	0.1%

Table 4

- Highest Signal efficiencies are reached for $\Delta m=10\text{-}20$ GeV and the efficiency increases for higher $\tilde{m}_{t_1}$.
- Overall Signal for 500fb^{-1} , after selection cuts $\sim O(10^3)\text{-}O(10^4)$, remaining background $O(10^3)$
- $\Delta m=5$ GeV were not included in the cuts optimization(besides c-tagging)

8-Stop Discovery Reach



From Simulations:
strong green region:

$$e^+e^- \rightarrow \tilde{t}_1 \tilde{t}_1^* \rightarrow c \tilde{\chi}_0^1 \bar{c} \tilde{\chi}_1^0$$

And Significance:

$$(S/\sqrt{S+B}) > 5$$

Background B

Signal $S = \epsilon \sigma L$

For ϵ , Signal efficiency

For σ , Theoretical
cross-section

dark gray region:

Consistent with DM

And Baryogenesis

Fig 4a-Luminosity: 500 fb⁻¹

$E_{\text{cm}} = 500 \text{ GeV}$

Fig 4b-Lumi. 500 fb⁻¹, 50 fb⁻¹, 10 fb⁻¹

*Simulations with: Pythia + Simdet +CIRCE

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9a-Sample Parameter Point

- $m_{\tilde{U}_3}^2 = -99^2 \text{ GeV}^2$
- $m_{\tilde{Q}_3} = -4200 \text{ GeV}$
- $A_t = -1050 \text{ GeV}$
- $M_1 = 112.6 \text{ GeV}$
- $M_2 = 225 \text{ GeV}$
- $|\mu| = 320 \text{ GeV}$
- $\Phi_\mu = 0.2$
- $\tan \beta = 5$
- $m_{\tilde{L}_{123}} = 2000 \text{ GeV}$
- $m_{\tilde{R}_{123}} = 200 \text{ GeV} \rightarrow \text{Rsleptmass reachable@ILC}$
- $A_{e,\mu,\tau} = 5 \text{ TeV} \cdot e^{i\pi/2}$
- $m_{\tilde{Q},\tilde{U},\tilde{D}_{12}} = 4000 \text{ GeV}$

Constrained by the electric dipole moment of e, n

(Important 1loop contrib. of $\tilde{f}-X^0$; $\tilde{f}-X^\pm \rightarrow \tilde{q}, \tilde{l}$ of first 2 gener. heavy)

$\rightarrow \tilde{q}$ soft super symmetry breaking param. 2 first gener.

are heavy $\sim 4\text{TeV}$ and left-chiral sleptons too

Which gives:

$m_{\tilde{t}_1} = 122.5 \text{ GeV}$; $m_{\tilde{t}_2} = 4203 \text{ GeV}$;

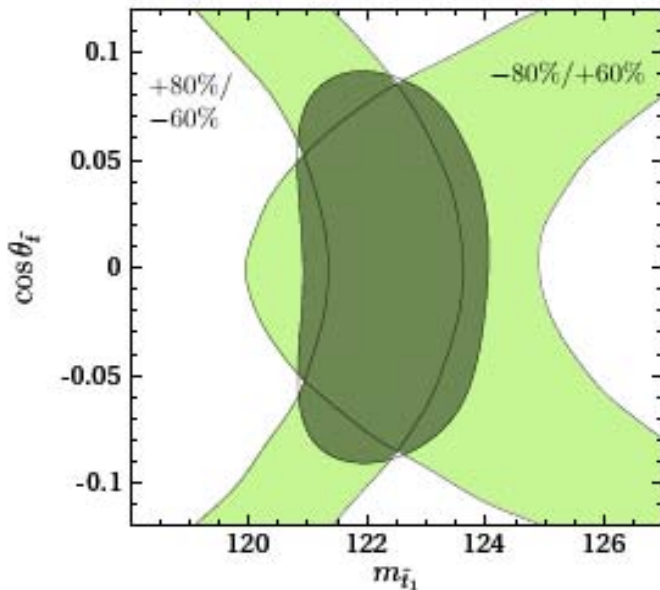
$m_{\tilde{X}_1^0} = 107.2 \text{ GeV}$; $m_{\tilde{X}_1^\pm} = 194.3 \text{ GeV}$; $m_{\tilde{X}_2^0} = 196.1 \text{ GeV}$

$m_{\tilde{X}_3^0} = 325.0 \text{ GeV}$; $m_{\tilde{X}_2^\pm} = 359.3 \text{ GeV}$

$\cos\theta_{\tilde{t}} = 0.0105 \sim \tilde{t}$ right handed

$\rightarrow \Delta m = 15.2 \text{ GeV}$

9b-Light Stop Mass and Mixing Angle



From: $\sigma(e^+ e^- \rightarrow \tilde{t}_1 \tilde{t}_1^*)$ and $\sigma(Bq)$ measured for 2 beam Polarizations:

$P(e^-)/P(e^+) = -80\%/+60\%$; $+80\%/-60\%$

$L=250 \text{ fb}^{-1}$ each

The green errors bands :

$\sim 1\sigma$ errors of the cross-sections combined into 1σ two-parameters allowed region: dark green

With statistical and systematical errors

No Radiative Corrections included but should be available at ILC time .

$M_{\text{stop}1} = 122.5 \pm 1.0 \text{ GeV}$, $\cos \theta_{t_1} < 0.074$ $\sim$ Right Chiral state

9c-Systematic Errors

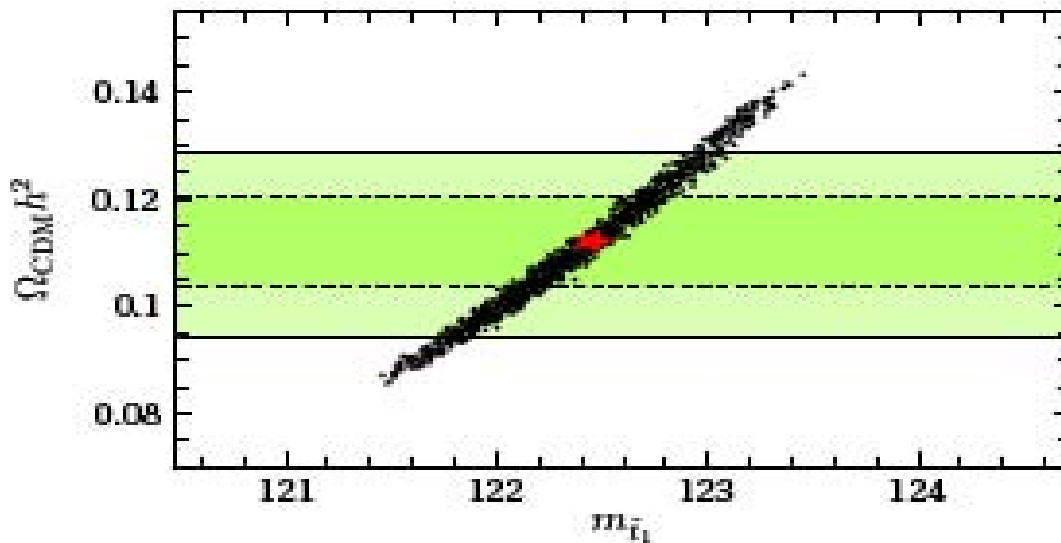
Stop Parameters Evaluation

The systematic errors include

- $\Delta m(x_1^0) = 0.11 \text{ GeV} (0.1\%)$; Beam Polar. $\Delta p/p = 0.5\%$ (0.01%);
- Theoretical (Bg simul) $= \Delta(BG)/BG = 0.3\% (< 0.5\%)$
- Stop_Hadronization_Fragmentation (experimental data from ILC stop discovery) (1%)
- Charm tagging (Charm.Frag. Func.) samples charm jets from SM processes e.g. $Z \rightarrow c\bar{c}$ ($< 0.5\%$)
- Realistic simulation of the detector effects $\rightarrow$ limited by (1) simulation stat. & (2) Det. Calib., nowadays (2) only $\sim < 0.5\%$ (LEP2)
- Beamstrahlung spectrum (from Bhabha scattering) (0.02%)
 $\rightarrow 1.3\%$ for $(-80\%/+60\%)$ polarization and 1.2% for $(+80\%/-60\%)$

10-Dark Matter Prediction

D. Morissey's program was used to calculate $\Omega_{\text{CDM}} h^2$
(Balazs, Carena, Menon, Morissey, Wagner 04)



So the overall precision is comparable to the direct WMAP determination. The uncertainty in the theoretical determination is dominated by the uncertainty in the stop mass, while the precision on the determination of the Neutralino, and ϕ_μ and $\theta_{\tilde{t}}$ are also important.

Using the stop parameters Detailed above and combining estimated errors for Chargino and Neutralino, the collider measurements of the stop and Chargino/Neutralino parameters Constrain, the relic density at the 1- σ level (dark points) to:

$$0.086 < \Omega_{\text{CDM}} h^2 < 0.143$$

WMAP measurements (in green)

$$0.095 < \Omega_{\text{CDM}} h^2 < 0.129$$

Dark Matter Determination

- Mass Measurements:

- Light $m(X_1^0)$ from selectron decay at ILC $\tilde{e} \rightarrow e X_1^0$ (Ee spectrum),
Threshold scan of $m = f(\sqrt{s}) \rightarrow M_{X_1^0}, M_{X_2^0}, M_{X_3^0}, M_{X^{\pm 1}}$
- Other neutralino/chargino masses from ILC threshold scans

Mass Systematic errors estimated from LHC/ILC report 04

Remark: Heavy 1st/2nd generation of squarks, very little $\sigma \rightarrow$ difficult to measure neutralino Masses from squark cascades at LHC

- σ Measurements

For $P(e^-)/P(e^+) = -80\%/+60\%$; $+80\%/-60\%$ for $\sqrt{s} = 500, 600$ GeV

Assuming $dP/P = 0.5\%$ (Tesla Tech. report)

$\sigma(e^+ e^- \rightarrow X_1^+ X_1^-)$; $\sigma(e^+ e^- \rightarrow X_1^0 X_2^0)$; $\sigma(e^+ e^- \rightarrow X_2^0 X_2^0)$;

Analytical Estimate (S.Y. Choi et al), assuming systematic errors

And stat. errors, use a Chi2 to extract fundamental SUSY Parameters

- $M_W, M_Z, \sin\theta_W, \cos\theta_W$ from SM
- And from the parameters obtained at the parameter point $m_{\tilde{t}_1}$; $\cos\tilde{\theta}_t$,
 M_1 ; M_2 ; $|\mu|$; Φ_μ ; $\tan\beta$; $\sin\alpha$; m_{h^0} and assuming $m_{\tilde{t}_2} > 1000 \text{ GeV}$

Outlook

The sensitivity to small mass differences is particularly important for the co-annihilation mechanism

We have shown that with the linear collider we can cover the region of co-annihilation down to mass differences $\sim O(5\text{GeV})$.

We can determine the parameters accurately enough to reach comparable precisions for the dark matter predictions than the direct WMAP measurements

Next to be done

- a) Further refinement of the analysis.
- b) Inclusion of radiative corrections
- c) Optimization of the cuts for $\Delta m \sim 5 \text{ GeV}$ and below
- e) Scalar tops: possible benchmark reaction for vertex detector projects (e.g. Sopczak LCWS'04).

International Collaboration involving Fermilab (USA), Lancaster (UK) within the LCFI (Linear Collider Flavor Identification) Collaboration and DESY (Germany).

C-tagging-The Principle

A Vertex Identification followed by a Neural Network application
Developed by T. Khul for LEP.

- Vertex Identification:

As a maximum in track overlapping (product of probability density tubes defined using the track parameters)

3 cases:

Case 1) Only a primary Vertex

Case 2) 1 secondary vertex

Case 3) >1 secondary vertex

- Neural Network (NN):

data used: 255000 stops, $M_{\text{stop}}=120-220$; $D_m=5, 10, 20$ GeV
240000 W_{ev} , the most resilient background

C-tagging-Neural Network Input

- Vertex Case 1: NN Input variables

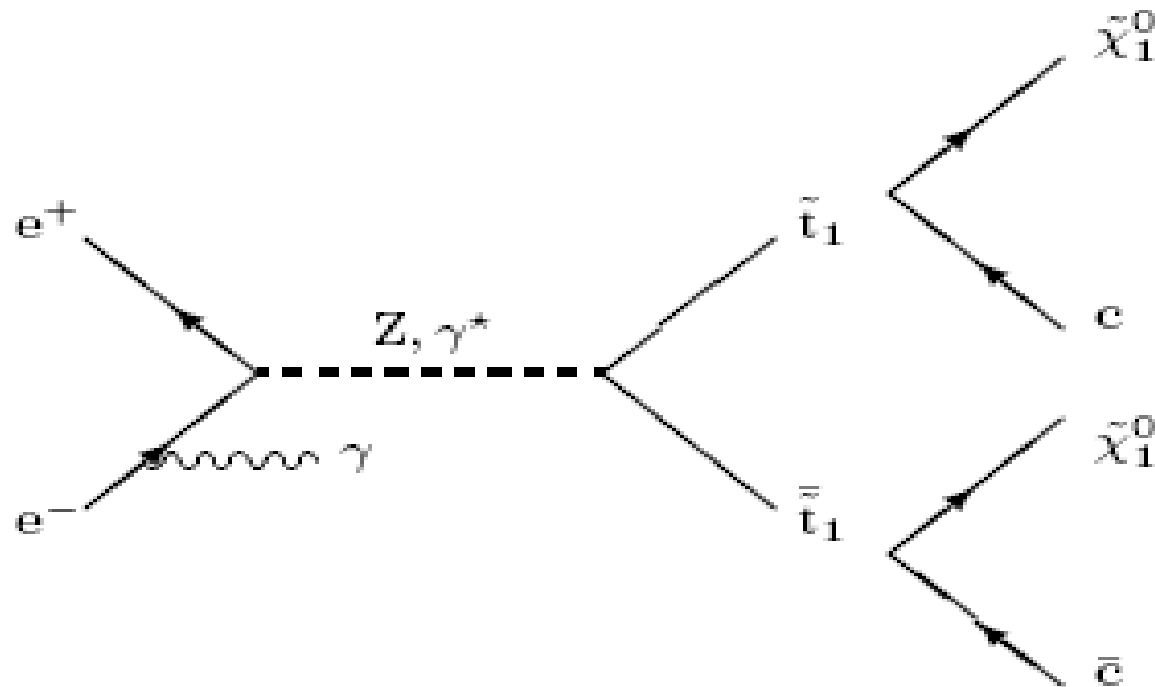
- *Impact parameter* significance (impact parameter/error) of the 2 most significant tracks in the r - Φ plane (tracks with the biggest separation) && their Impact parameters.
- The impact parameter significance & Impact parameters of the 2 tracks in z
- Their momenta
- The joint probability in r - Φ (tiny beam spot size in that plane)& z

- Vertex Case 2: NN Input variables (all of Case 1+below)

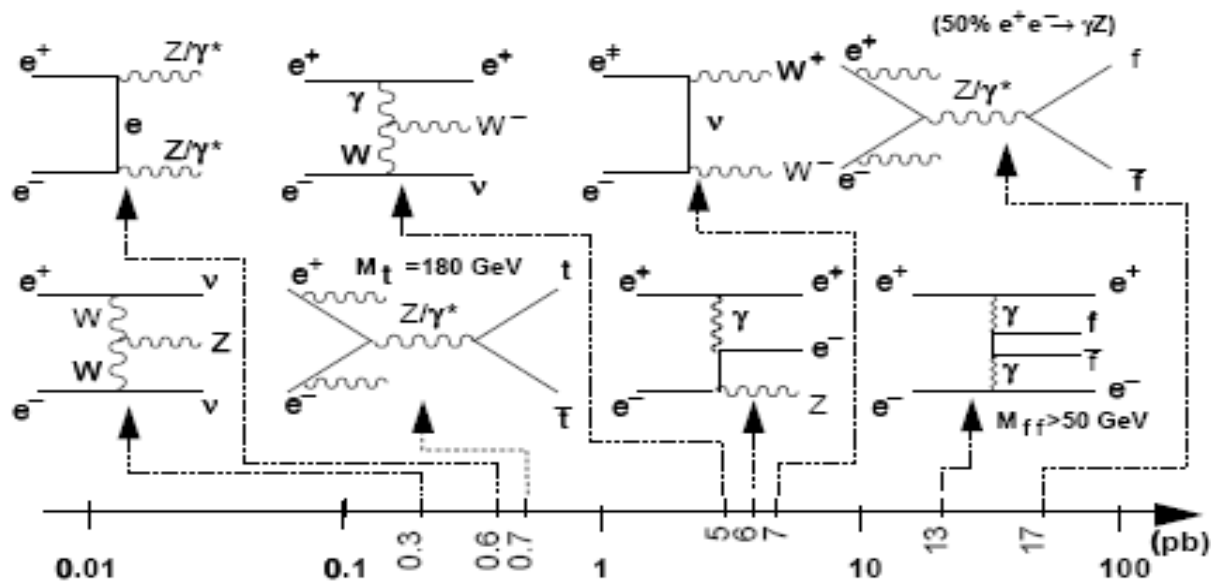
- *Decay Length* significance of the secondary vertex && Decay Length
- Momentum of all tracks associated to the secondary vertex && Multiplicity
- Pt corrected mass of secondary vertex (corrected for neutral hadrons & v 's), the pt of the decay products perpendicular to the flight direction (between primary && secondary Vertex) && joint probability in r - Φ and z

- Vertex Case 3: 2 secondary vertices, the tracks are assigned to the vertex closest to the primary vertex and the NN input variables are those of case 2

Two-Soft Charm Jets and Missing Energy



Background- Channels



hep-ph9701336-A.Bartl,H. Eberl,S. Kraml, W.Majerotto,W.Porod,A. Sopczak