

Study of Incoherent Pair Generation in the Beam-beam Interaction Simulation Program GUINEA-PIG

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This paper deals with two topics: the generation of incoherent pairs in two beam-beam simulation programs, GUINEA-PIG and CAIN, and the influence of the ILC beam parameter choices on the background in the micro-vertex detector (VD) induced by direct hits. One of the processes involved in incoherent pair creation (IPC) is equivalent to a four fermions interaction and its cross section can be calculated exactly with a dedicated generator, BDK. A comparison of GUINEA-PIG and CAIN results with BDK allows to identify and quantify the uncertainties on IPC background predictions and to benchmark the GUINEA-PIG calculation. Based on this simulation and different VD designs, the five currently suggested ILC beam parameter sets have been compared regarding IPC background induced in the VD by direct IPC hits. We emphasize that the *high luminosity* set, as it is currently defined, would constrain both the choices of magnetic field and VD inner layer radius.

1. INTRODUCTION

GUINEA-PIG¹ [1] and CAIN [2] are programs dedicated to simulating the beam-beam interaction in high-energy e^+e^- linear colliders such as ILC² and CLIC³. Reliable and efficient computing tools are important to predict the luminosity and to study the backgrounds from secondary particles produced in the collisions, in order to optimize the design of both the machine and detectors. In the framework of the EuroTeV Design Study⁴, a complete study, benchmarking and improvement of GUINEA-PIG is under way, in collaboration with the team working on CAIN.

In this note, a study of the production of secondary e^+e^- pairs created through the incoherent scattering of synchrotron radiation induced in the beam-beam interaction, so called beamstrahlung, is presented. An important objective is to probe the realism of the predictions for the small fraction of such pairs which can reach the micro-vertex detector (VD). For large enough rates, the induced backgrounds can significantly confuse the pattern recognition for associating hits in the VD, and hence lead to reduced impact parameter resolution for the tracks involved. The aims of the study are to identify and assess:

- the intrinsic theory uncertainty in the prediction; for this, the three physical processes which contribute to e^+e^- pair production are investigated and compared for the different settings available in GUINEA-PIG and CAIN. An additional dedicated four-fermion event generator, BDK [3], based on a different theoretical approach, has also been used for one of the physical processes,
- the changes in rates reaching the VD for the different ILC beam parameter sets [4] proposed as alternatives

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¹Generator of Unwanted Interactions for Numerical Experiment Analysis-Program Interfaced to GEANT

²International Linear Collider

³Compact Linear Collider

⁴European Design Study Towards a Global TeV Linear Collider

to the nominal reference, and for the most relevant design parameters of the three detector concepts presently under study [5–7].

2. INCOHERENT PAIR CREATION PROCESSES

Following the emission of beamstrahlung photons, e^+e^- pairs are produced both by coherent (CPC) and incoherent pair creation (IPC) processes. The CPC process consists of the interaction of the beamstrahlung photons with the collective electromagnetic field of the opposite beam, while the IPC pairs arise from the interaction of both real or virtual photons from each beam with individual particles of the other beam. For ILC running energies up to 1 TeV in the center of mass, the coherent production process is negligible compared to the incoherent one.

Three main physical processes are responsible for IPC, referred to respectively as Breit-Wheeler (BW), Bethe-Heitler (BH) and Landau-Lifshitz (LL). Two real photons interact in the BW process, a real and a virtual in the BH process and two virtual ones in the LL process. The real photons are from the beamstrahlung and virtual ones can be pictured as an off-shell photon cloud accompanying each high-energy beam electron or positron. While both GUINEA-PIG and CAIN use the explicit leading-order cross-section calculation for the BW process, an approximation is used for the processes involving virtual photons, called the Equivalent Photon Approximation (EPA). This approximation treats virtual photons as real ones by convoluting an equivalent spectrum for the virtual photons with the cross section for the real-real case. These photons are treated as being real as long as their virtuality remains below an upper limit, above which they are ignored. This upper limit, Q_{max}^2 , is fixed to the electron mass squared, m_e^2 , in CAIN whereas GUINEA-PIG offers the choice between m_e^2 , $m_e^2 + p_\perp^2$, the transverse mass squared of the final state and $s/4$, half of the invariant mass squared. The latest choice is recommended and used by default in GUINEA-PIG. More details can be found in [1, 8].

Two important phenomena must be taken into account in the production of secondary pairs from the beam-beam interaction: deflections due to the electromagnetic field of the opposite beam and the so-called “beam-size effect”.

- Electromagnetic deflections: Most pairs are produced with very small angles along the beam axis. Half of them are emitted in the direction opposite to the beam of same charge and are consequently defocused while those following the direction of the beam of same charge are focused. The resulting effect is shown both in figures 1 and 2. A clear accumulation at large transverse momenta can be seen. Electromagnetic deflections however don’t affect the energy spectrum or the overall production cross section. An additional effect which arises from electromagnetic deflections is a suppression of virtual photon emissions at small angles.
- Suppression from finite beam size: The virtuality of the quasi-real photons involved in two of the IPC processes implies some spatial indeterminacy. For the smallest virtual photon transverse momenta, this quantum uncertainty on their localization can exceed the physical sizes of the tightly focused colliding beams. A suppression of the cross section for small transverse momentum virtual photons is expected from this and consequently a reduction in pair production rates [9].

2.1. Comparison of GUINEA-PIG and CAIN

Input parameters and options

Table I gives the values of the beam parameters for several ILC design optimisations under consideration[4]. The American version of the cold accelerator design (USSC) has been used to compare GUINEA-PIG and CAIN. A cut of 5 MeV is applied on the energy of the produced IPC electron or positron. The default settings of GUINEA-PIG and CAIN are firstly used:

- the suppression effect from the finite beam size is activated in both programs.
- The virtual-photon suppression effect due to the field of the opposite beam is turned off.

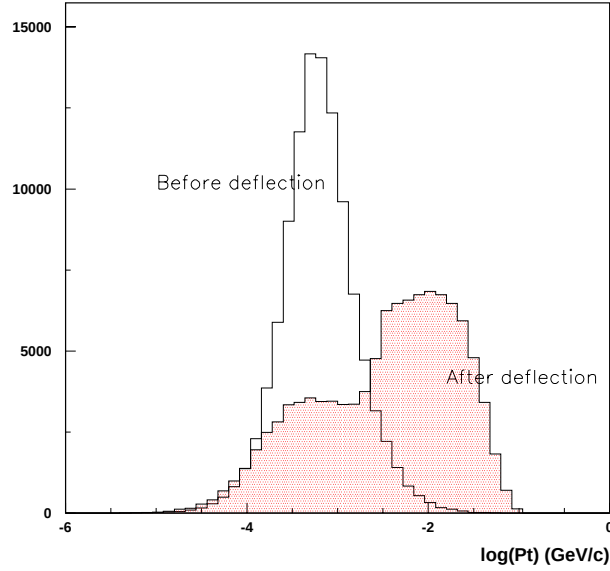


Figure 1: P_t distribution of the pairs before (empty histogram) and after (solid histogram) electromagnetic deflections from the opposite beam.

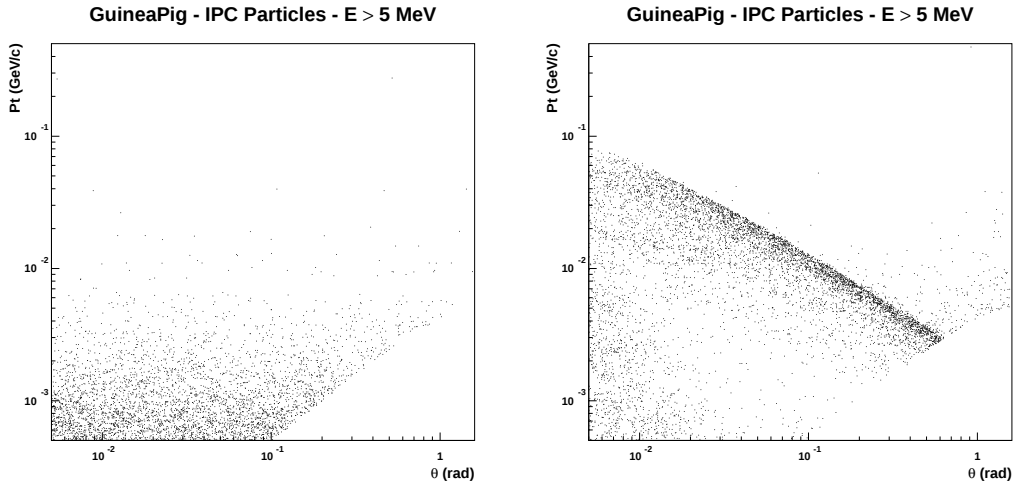


Figure 2: P_t versus θ distributions for IPC particles before (left-hand plot) and after (right-hand plot) electromagnetic deflections from the opposite beam.

- The maximum virtuality scale allowed in pair production processes is set to the electron mass and to half the center of mass energy of the scattering, respectively in CAIN and GUINEA-PIG.

All the results are given for one bunch crossing.

Qualitatively speaking, CAIN and GUINEA-PIG give very similar results. Energy spectra are shown in figure 3 for BW, BH and LL processes, and show a very good agreement between the two simulations. One notes that the mixed process is largely dominant whereas the real-real process represents only a few percent of the total production.

	TESLA	USSC	Nominal	Low Q	Large Y	Low P	High Lum
E_{cm} [GeV]	500	500	500	500	500	500	500
N [10^{10}]	2	2	2	1	2	2	2
Nb	2820	2820	2820	5640	2820	1330	2820
β_x [mm]	15.0	15.0	21.0	12.0	10.0	10.0	10.0
β_y [mm]	0.4	0.4	0.4	0.2	0.4	0.2	0.2
$\gamma\epsilon_x$ [10^{-6} mrad]	10.0	9.6	10.0	10.0	12.0	10.0	10.0
$\gamma\epsilon_y$ [10^{-6} mrad]	0.030	0.040	0.040	0.030	0.080	0.035	0.030
σ_x [nm]	554	543	655	495	495	452	452
σ_y [nm]	5.0	5.7	5.7	3.5	8.1	3.8	3.5
σ_z [μ m]	300	300	300	150	500	200	150

Table I: Beam parameters for different ILC design optimisations under consideration.

Similar conclusions hold for the (P_t, θ) spectra obtained with both programs (see figure 4 and the plot on the left-hand side of figure 2).

The cross sections⁵ and the corresponding numbers of secondary electrons produced per bunch crossing for each IPC process are given in table II in the case of the USSC parameters. CAIN predicts about 12% less particles than GUINEA-PIG. This comes entirely from the processes which involve virtual photons, especially the virtual-virtual one for which one finds a 20% difference.

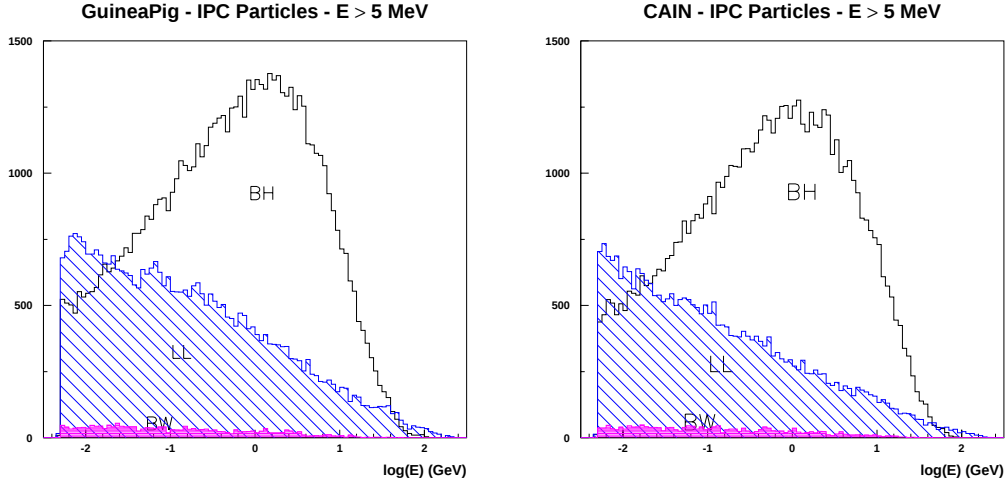


Figure 3: Log-energy spectra for the three incoherent pair creation processes modeled in GUINEA-PIG (left plot) and CAIN (right plot).

2.2. Comparison with BDK for the Landau-Lifshitz process

BDK is a Monte-Carlo event generator for four fermion processes in e^+e^- interactions which is based on complete calculations with leading-order massive matrix elements for all relevant electroweak diagrams involved. The results

⁵For the two processes involving real photons, BW and BH, the quoted cross sections should be understood as effective ones.

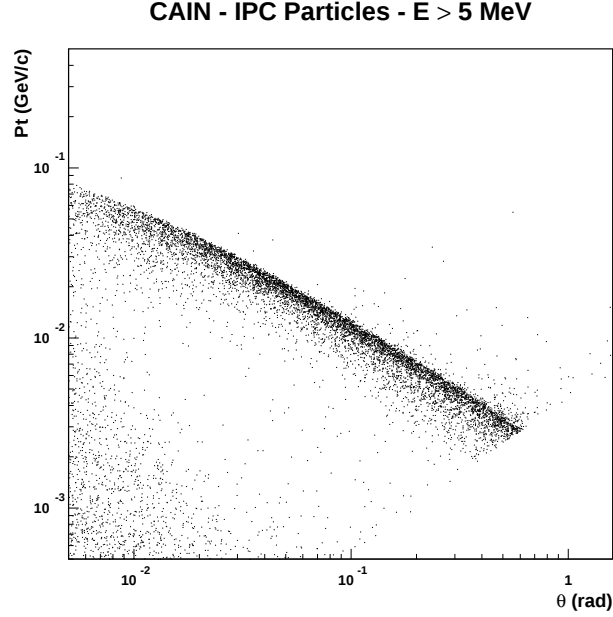


Figure 4: Transverse momentum, P_t , versus polar angle, θ , for $e^\pm$ from IPC processes modeled in CAIN.

	GUINEA-PIG	CAIN
Cross Section (mb)		
All processes	58.0	50.7
Breit-Wheeler	1.05	1.04
Bethe-Heitler	37.7	34.5
Landau-Lifshitz	19.2	15.2
Total number of electrons and positrons per bunch crossing with $L = 1.82 \mu b^{-1}$		
All processes	105500	92300
Breit-Wheeler	1900	1900
Bethe-Heitler	68600	62800
Landau-Lifshitz	35000	27700

Table II: Number of particles and (effective) cross sections for each IPC process in GUINEA-PIG and CAIN.

for the $e^+e^- \rightarrow e^+e^-e^+e^-$ process obtained in GUINEA-PIG and CAIN can be compared with BDK as a test of the Equivalent Photon Approximation used in the two beam-beam simulations.

To perform this test, one has to turn off the cross section suppression from the finite beam size, used by default in GUINEA-PIG and CAIN and look at the distributions of pair space variables before their deflection. In BDK, in order to generate the same phase space as in GUINEA-PIG and CAIN, the square of the invariant mass of the produced pairs is lowered down to $10^{-6} GeV^2$, corresponding to the threshold for electron-pair production.

The log-energy, transverse momentum and polar angle distributions of the IPC particles produced through the Landau-Lifshitz process are shown in figures 5 and 6, respectively. Table III gives the cross sections for the pairs produced through all processes, without the suppression from the finite beam size. Comparing with the results in table II, for which this effect was included, one can see that the reduction induced amounts to about 40% and that it of course only is present for processes involving virtual photons. Both GUINEA-PIG and CAIN predict Landau-Lifshitz cross sections in broad agreement with BDK, with GUINEA-PIG being the closest.

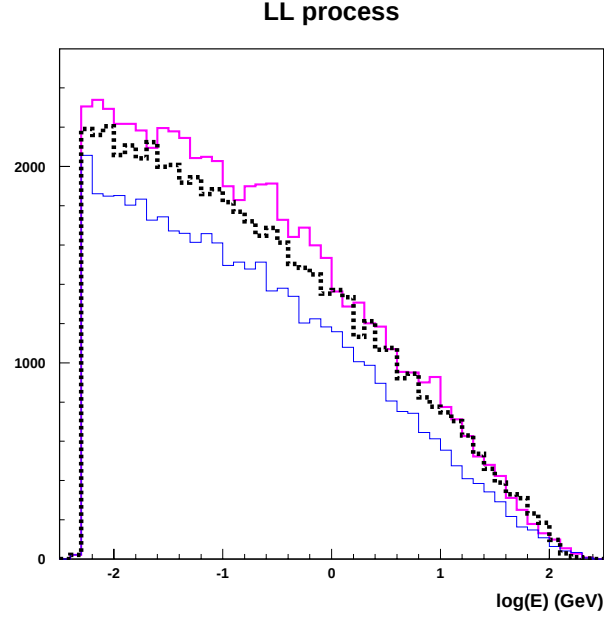


Figure 5: Log-energy spectrum for the Landau-Lifshitz process in GUINEA-PIG (upper line), CAIN (lower thin line) and BDK (dashed line).

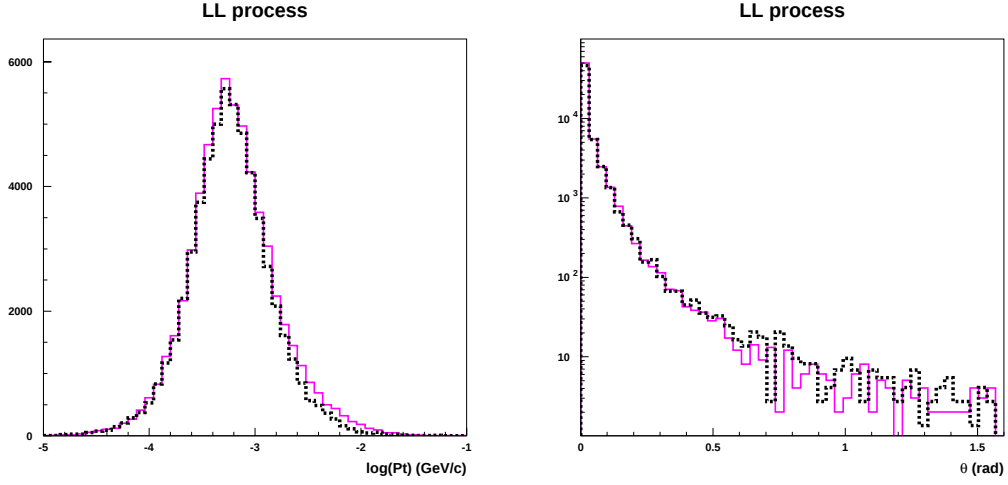


Figure 6: Log-Pt (left plot) and polar angle (right plot) distributions for the Landau-Lifshitz process in GUINEA-PIG and BDK (dashed line).

σ (mb)	GUINEA-PIG	CAIN	BDK
All processes	101	89.5	-
Breit-Wheeler	1.01	1.11	-
Bethe-Heitler	66.3	61.7	-
Landau-Lifshitz	33.9	26.7	31.8

Table III: Cross sections for incoherent pair production without finite beam-size suppression effects in GUINEA-PIG, CAIN and BDK

2.3. Event rates in the Micro-Vertex Detector

A small fraction of the electrons and positrons produced through IPC processes can reach the micro-vertex detector (VD). The corresponding rates are computed for a detector consisting of five cylindrical layers [5], L_i , $i = 1 - 5$, with the following lengths, ℓ and radii, r :

$$\ell_1 = 100 \text{ mm}, \quad \ell_{2-5} = 250 \text{ mm},$$

$$r_1 = 15 \text{ mm}, \quad r_2 = 26 \text{ mm}, \quad r_3 = 37 \text{ mm}, \quad r_4 = 48 \text{ mm}, \quad r_5 = 60 \text{ mm}.$$

To determine if a particle with transverse momentum P_t and production angle θ_0 travelling in a magnetic field B reaches the VD, the helix equation is used:

$$r(z) = r_0 \sqrt{2(1 - \cos\phi(z))}, \quad \phi(z) = \frac{z}{r_0} \tan\theta_0,$$

with

$$r_0[m] = 3.33 P_t [GeV/c] / B[T],$$

where $r(z)$ is the distance in meters to the beam axis at the abscissa z . The magnetic field is set to 4 T and the USSC parameters are still used.

Figure 7 highlights the region in the two-dimensional (P_t, θ) distribution corresponding to pairs which can reach the VD. The minimum transverse momentum and polar angle involved is found to be $P_t > 5 \text{ MeV}$ and $\theta > 10^\circ$.

This region is fortunately outside of the beam-beam deflection induced accumulation zone, for the beam parameters considered. The corresponding P_t and θ are not a consequence of the electromagnetic deflections, but arise intrinsically in the IPC process, as shown in figure 8.

It is important to note that the ranges in P_t and θ shown in figure 7, corresponding to pairs which can reach the VD, depend both on the VD geometrical design (for θ) and on the detector magnetic field (for P_t). On the other hand, the exact location of the beam-beam deflection induced accumulation zone depends on the chosen ILC beam parameters. These considerations will be developed further in section 3.

σ (μb)	GUINEA-PIG	CAIN	BDK
All processes	64.1 ± 5.9	37.4 ± 4.5	-
	60.5 ± 6.0	36.5 ± 4.5	-
Breit-Wheeler	8.2 ± 2.1	6.4 ± 1.9	-
	10.3 ± 2.4	7.0 ± 2.0	-
Bethe-Heitler	26.6 ± 3.8	20.9 ± 3.3	-
	20.5 ± 3.3	16.6 ± 3.0	-
Landau-Lifshitz	29.3 ± 4.0	10.2 ± 2.3	-
	29.7 ± 4.0	13.4 ± 2.7	37.5 ± 5.3

Table IV: Cross sections for the pair background reaching the VD predicted by GUINEA-PIG, CAIN and BDK, with (upper lines) and without (lower lines) the “beam size effect”.

Table IV gives the cross section of the pair background reaching the VD predicted by GUINEA-PIG and CAIN, with (upper lines) and without (lower lines) the expected suppression from the finite beam size. It can be seen that the beam size effect has little influence on the background rates in the VD (within statistical fluctuations). Activating the virtual-photon suppression effect due to the opposite beam field has also been tried (instead of the beam size effect, to avoid potential double counting) and leads to a VD background reduction of the order of 10%.

There is at least a 40% difference between CAIN and GUINEA-PIG for the total number of IPC particles reaching the VD. A comparison with BDK for the Landau-Lifshitz process indicates that CAIN seems to underestimate the corresponding rate by a factor 3, whereas GUINEA-PIG is in good agreement.

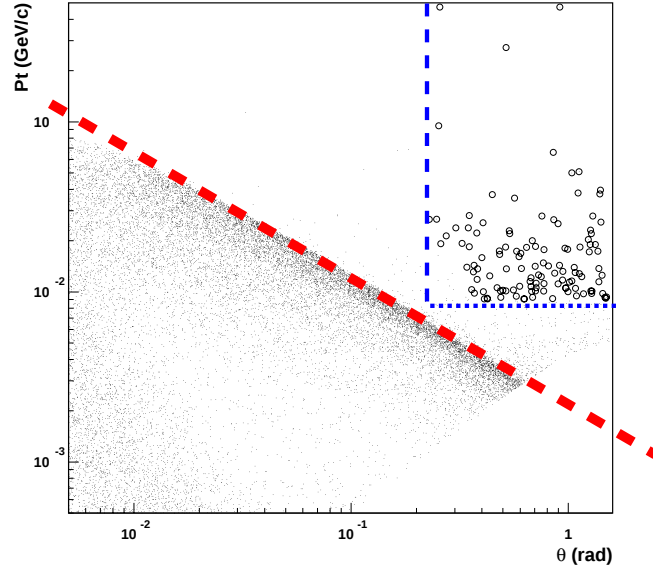


Figure 7: Distribution of P_t versus θ for electrons from IPC processes. The region corresponding to particles reaching the VD (circles) is indicated with the two dashed lines for the detector configuration described in the text. A thick dotted line highlights the edge of the beam-beam deflection induced accumulation zone.

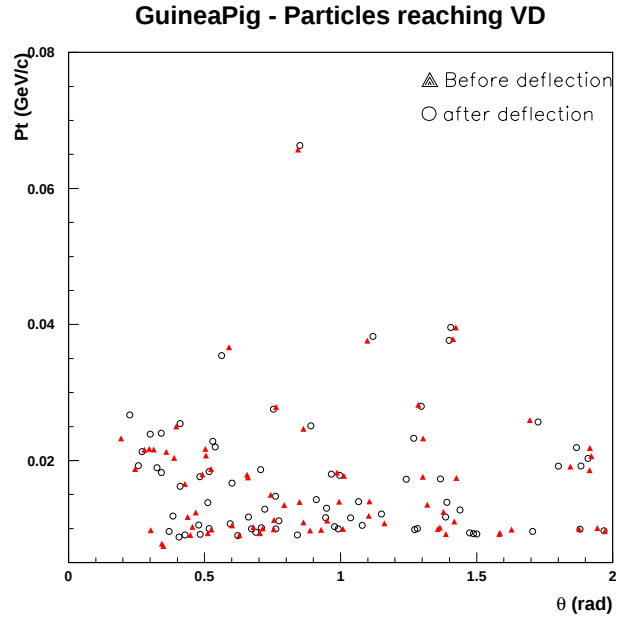


Figure 8: Distribution of P_t versus θ for electrons from IPC processes reaching the VD, before electromagnetic deflections (triangles) and after (circles).

2.4. Origin of the difference between CAIN and GUINEA-PIG

This difference between CAIN and GUINEA-PIG can be traced to the different choices made in the two programs for the maximum virtuality, Q_{max} , used in the equivalent photon spectrum (see section 2). Table V shows this: if Q_{max} is set to m_e in GUINEA-PIG instead of the default value, one obtains $\sigma_{all} = 32.0 \mu b$ and $\sigma_{LL} = 9.7 \mu b$ for the background reaching the VD, which is indeed consistent with the results from CAIN (see tables II and IV).

GUINEA-PIG	$\sigma_{e^+e^-}$ (mb)	σ_{VD} (μb)
All processes	51.8	32.0 ± 4.3
Breit-Wheeler	1.09	5.7 ± 1.8
Bethe-Heitler	35.2	16.5 ± 3.1
Landau-Lifshitz	15.6	9.7 ± 2.4

Table V: Cross sections for incoherent pair production, $\sigma_{e^+e^-}$, and for the pair background reaching the VD, σ_{VD} , predicted by GUINEA-PIG, with the “beam size effect” activated and using $Q_{max} = m_e$ for the maximum virtuality in the equivalent photon spectrum instead of the default value.

In order to assess the importance of cutting events with photon virtualities beyond a certain value as part of the equivalent photon approximation, the virtuality spectrum generated in GUINEA-PIG, using the default running option $Q_{max}^2 = s/4$ and no beam size effect, was extracted and compared with that which can be reconstructed from BDK events using the following equation:

$$Q^2 = (P_i - P_s)^2 \simeq m_e^2(2 - (E_i/E_s + E_s/E_i)\cos\theta) - 2E_iE_s(1 - \cos\theta), \text{ with } \theta \ll 1,$$

where $P_{i,s} = (E_{i,s}, \vec{p}_{i,s})$ are the four-momenta of the incident and scattered electrons and θ the scattering angle. The comparison is shown in figure 9, where the position of the electron mass is also indicated.

A much better agreement between the spectra in GUINEA-PIG and BDK can be seen with the GUINEA-PIG default choice for the maximum photon virtuality cut, at half the invariant mass of the process, than when setting it to m_e as in CAIN.

Figure 10 shows the virtualities of the two photons involved in the LL process, reconstructed from the BDK events. The highlighted squares correspond to the events for which a pair particle reaches the VD. The dashed lines correspond to the electron mass. 24% of the produced pairs arise through an interaction where at least one of the quasi-real photons involved has a virtuality larger than m_e . Removing these events reduces the cross section by about $24 mb$, which corresponds to the CAIN result (see table III). Moreover, only 33% of the VD background comes from two low virtuality photons, which corresponds to a cross section of $12 \mu b$, again in accordance with CAIN (see table IV).

BDK being a genuine matrix element calculation, it should give the more reliable prediction at large virtuality. On the other hand, the equivalent photon approximation should be best in the quasi-real limit. Since the two spectra have very similar shapes and since the additional cross section predicted by BDK, as compared with the equivalent photon approximation using a cut on photon virtualities at m_e , is in the large virtuality part of the spectrum, it can be argued that the GUINEA-PIG prediction, with the cut set at its default value of half the invariant mass of the produced final state, is the better one. How much this prediction can be trusted is however limited by the fact that this default cut, although it seems a rather natural choice, is ad hoc, while the matrix elements used in BDK are only leading order ones. Nonetheless, what does seem clear is that the cross section predicted by the equivalent photon approximation with a cut on photon virtualities at m_e is too small.

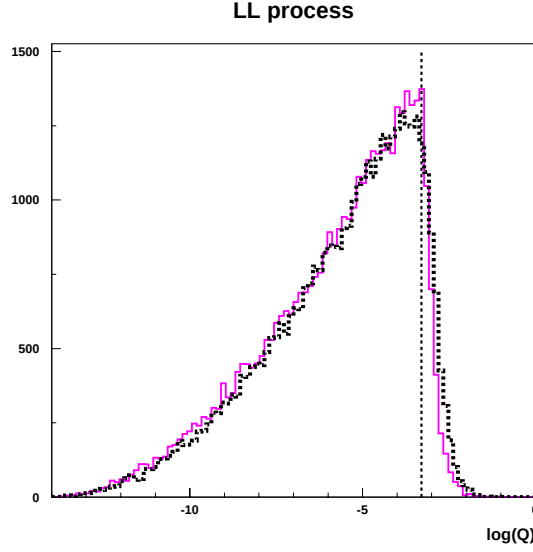


Figure 9: Comparison of GUINEA-PIG and BDK (dashed thick line) photon virtuality spectra. The vertical dashed line indicates the position of the electron mass.

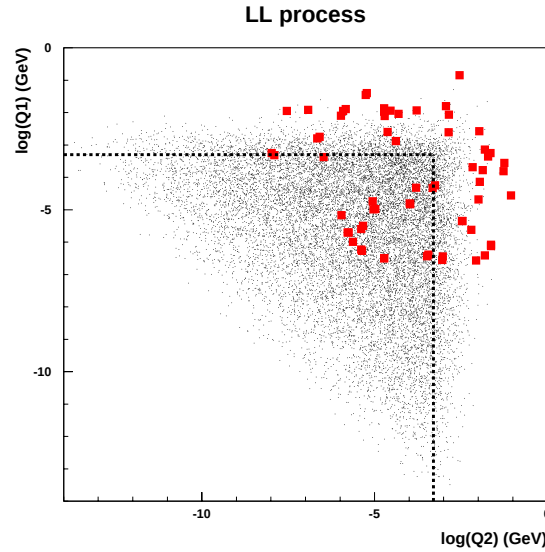


Figure 10: Q_{γ_1} versus Q_{γ_2} in BDK simulation. The highlighted points correspond to events with pair particles reaching the VD. The dashed lines indicate the position of the electron mass.

3. IMPACT OF ILC BEAM PARAMETER SETS ON PAIR BACKGROUND RATES IN THE VERTEX DETECTOR

Looking at figure 7, two regions are interesting to highlight: that corresponding to events which can reach the VD, represented by the rectangle, and the stripe where most events accumulate after being deflected by the electromagnetic field of the opposite beam. The edge of this stripe is represented by the thick dashed line.

The acceptance rectangle depends on the characteristics of the VD (length and radius) and on the magnetic field, B , while the accumulation stripe depends on the beam parameters (σ_x , σ_z , N). One has to be sure that the chosen

beam parameters and VD design allows the VD acceptance rectangle to stay clear off the pair accumulation stripe, called in the following “inflationary case”.

We have tested the five official sets of beam parameters: *nominal*, *low Q*, *large Y*, *low P* and *high luminosity*, for three values of the magnetic field, 3T [7], 4T [5] and 5T [6], and four different inner VD layer radii, 10mm, 15mm, 20mm and 25mm. Results using the TESLA TDR configuration are also given for reference and comparison, since it corresponds to a case which was studied in detail with full GEANT-based detector simulations. GUINEA-PIG was used with its default settings as previously described.

Table VI gives the cross sections for the IPC particles reaching the VD for all the studied cases. The underlined numbers correspond to inflationary cases. For all such cases, the smallest VD inner layer radii are probably excluded.

Increasing the magnetic field by 1T for a given VD design (15 or 20 mm) suppresses on average 38% of the considered background. One can also notice an approximate equivalence between the cases:

- $(r_1 = 20 \text{ mm}, B = 4 \text{ T})$ and $(r_1 = 15 \text{ mm}, B = 5 \text{ T})$,
- $(r_1 = 20 \text{ mm}, B = 3 \text{ T})$ and $(r_1 = 15 \text{ mm}, B = 4 \text{ T})$,
- $(r_1 = 15 \text{ mm}, B = 3 \text{ T})$ and $(r_1 = 10 \text{ mm}, B = 5 \text{ T})$ except for inflationary cases.

Figure 11 shows the (P_t, θ) plane for IPC electrons reaching the VD for $r_1 = 15 \text{ mm}$ and $B = 3, 4, 5 \text{ T}$ and the evolution of the accumulation limit compared to the case with nominal parameters (illustrated by the thick line). One can see that the *nominal* and *low Q* designs lead to the same results, both for the cross section and for the distance between the VD acceptance and the pair accumulation region. The *large Y* design offers the safest distance to the accumulation region while for the *low P* and *high lum* designs, the acceptance of the VD at 3 and 4 T is too close to the accumulation zone, not to say inside, as it is clearly shown in the last picture of figure 11. For this last design, the choice of $B=3 \text{ T}$ is probably excluded if an innermost VD layer of 15 mm is desired.

Finally, table VII summarises the main results concerning the IPC and the background in the VD. The integrated luminosities, $\mathcal{L}$, are extrapolated from the luminosities per bunch crossing, $\mathcal{L}_{bc}$, given by GUINEA-PIG. $N_{IPCe/bc}$ is the number of particles generated by the IPC processes and it depends both on the luminosity per bunch crossing, $\mathcal{L}_{bc}$, and the beamstrahlung radiation, quantified in table VII by N_γ , the average number of emitted photons per beam particle. One sees that the virtual-virtual process is independant of the choice of beam parameters. The last part of table VII gives an estimation of the number of IPC background particles reaching the VD for different inner layer radii and magnetic fields. Considering for example the TESLA VD design, i.e. $r_1 = 15 \text{ mm}$ and $B = 4 \text{ T}$, with the *nominal*, *low Q* and *large Y* beam parameter sets, $\simeq 1.2$ million/s IPC particles are estimated to reach the VD, while for the *low P* and *high luminosity* designs the rates increase to 1.5 and 3.3 million/s, respectively.

4. CONCLUSIONS

The goals of this study were on the one hand to evaluate the uncertainty in the background from incoherent pair creation reaching the VD directly, predicted by the beam-beam interaction simulation programs, GUINEA-PIG and CAIN, and on the other hand to evaluate the impact of the choice of beam parameters on this background.

The incoherent pair creation cross section predicted in CAIN is 12% less than the one in GUINEA-PIG. This comes from the processes involving virtual photons, Breit-Wheeler and Landau-Lifshitz processes, and is explained by the different choices in the two programs for the maximal value of the photon virtuality (set to the electron mass in CAIN and to half of the invariant mass of the produced final state in GUINEA-PIG). These differences are enhanced for the fraction of the events which produce particles reaching the VD directly, with CAIN predicting a 40% lower rate than GUINEA-PIG. A comparison with an $e^+e^- \rightarrow 4f$ dedicated generator, BDK, was made for the Landau-Lifshitz process and showed a very good agreement between its results and those of GUINEA-PIG. For the VD background arising from this process, CAIN predicts a three times lower rate than BDK. This difference comes indeed from the choice of virtuality limit since the three simulations leads to almost exactly the same results at low virtualities.

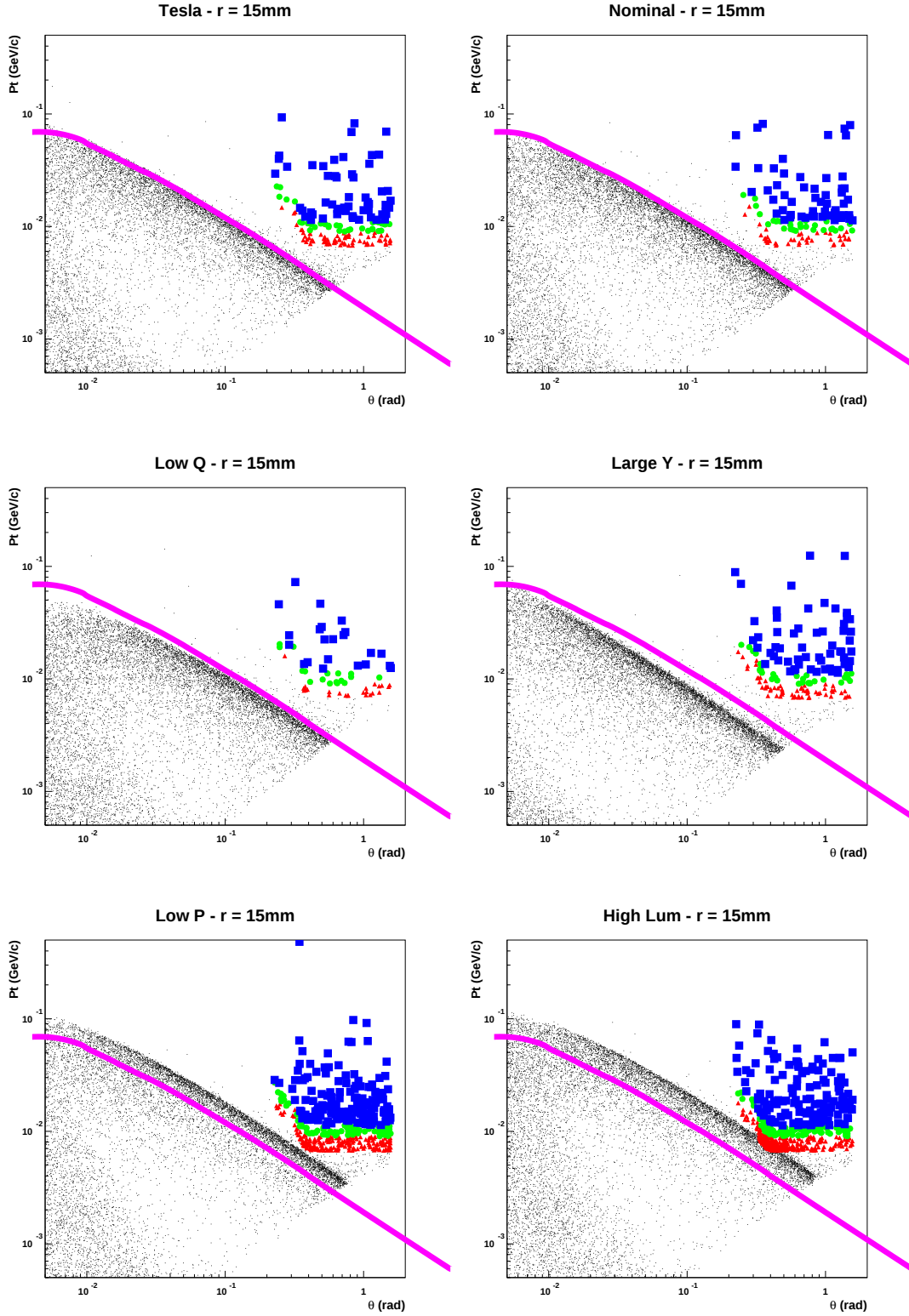


Figure 11: P_t versus θ plane for the background electrons reaching the VD for $r_1 = 15\text{ mm}$. The black points are all the IPC particles, generated including the beam size effect (see section 2). Blue square-shaped points correspond to the background in the VD for a magnetic field of 5T. Adding the green circle-shaped (red triangle-shaped) ones, it corresponds to the background for 4T (3T). The thick line indicates the edge of accumulation limit for the *nominal* design.

$\sigma[\mu b]$	3T	4T	5T	3T	4T	5T
	TESLA TDR			Nominal		
$r_1 = 10 \text{ mm}$	<u>1320</u>	171 ± 9	90 ± 7	<u>1067</u>	166 ± 11	92 ± 8
$r_1 = 15 \text{ mm}$	85 ± 7	49 ± 5	30 ± 4	88 ± 8	59 ± 6	39 ± 5
$r_1 = 20 \text{ mm}$	46 ± 5	27 ± 4	17 ± 3	58 ± 6	36 ± 5	21 ± 4
$r_1 = 25 \text{ mm}$	34 ± 4	19 ± 3	11 ± 2	42 ± 5	23 ± 4	16 ± 3
	Low Q			Large Y		
$r_1 = 10 \text{ mm}$	<u>600</u>	143 ± 14	90 ± 11	351 ± 18	189 ± 13	129 ± 11
$r_1 = 15 \text{ mm}$	90 ± 11	55 ± 9	31 ± 7	132 ± 11	79 ± 8	54 ± 7
$r_1 = 20 \text{ mm}$	53 ± 9	31 ± 7	20 ± 5	79 ± 8	51 ± 7	32 ± 5
$r_1 = 25 \text{ mm}$	38 ± 7	24 ± 6	17 ± 5	65 ± 8	38 ± 6	24 ± 5
	Low P			High Lum		
$r_1 = 10 \text{ mm}$	<u>3527</u>	<u>1731</u>	<u>410</u>	<u>4460</u>	<u>2807</u>	<u>1523</u>
$r_1 = 15 \text{ mm}$	145 ± 7	77 ± 5	50 ± 4	<u>490</u>	70 ± 5	40 ± 3
$r_1 = 20 \text{ mm}$	77 ± 5	46 ± 4	29 ± 3	67 ± 4	35 ± 3	24 ± 3
$r_1 = 25 \text{ mm}$	59 ± 5	33 ± 3	20 ± 3	48 ± 4	28 ± 3	18 ± 2

Table VI: Cross sections in μb for the pair background reaching the VD per bunch crossing for different beam parameters sets. The *TESLA TDR* case is shown for reference.

The similarity of the GUINEA-PIG and BDK virtuality spectra found, added to the almost equal cross section predictions, seem to justify a choice of virtuality limit larger than the electron mass, as has been done in GUINEA-PIG. This gives some confidence in the results from that program, even if the particular value chosen does not have a first principle explanation and the BDK calculation does not include any radiative corrections.

Other potential uncertainties in the IPC rates predicted may arise from the two different sources of virtual photon suppression, which are modeled with effective methods in GUINEA-PIG and CAIN, because neither corresponds to a fully well-defined parameter region where standard methods can be applied. However, for what concerns the background in the VD, these two effects do not produce changes in rates larger than about 10%, which is small in the present context.

The design of the accelerator can on the other hand significantly change the rates of direct pair backgrounds in the VD, for a given magnetic field and inner layer radius. Contrary to the *nominal*, *low Q* and *large Y* beam parameter sets, which leave the choices of magnetic field and VD innermost layer radius rather open, the *low P* and *high lum* designs would be more constraining. For instance, for the case of the *high lum* design, to have similar background rates as with the other designs, a magnetic field of 5T and a larger inner layer radius would have to be used.

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TESLA TDR Nominal Low Q Large Y Low P High Lum						
Luminosities						
$\mathcal{L}_{bc} [\mu b^{-1}]$	1.92	1.46	0.71	1.14	2.84	3.44
$\mathcal{L} [nb^{-1}.s^{-1}]$	27.0	20.6	20.0	16.1	18.9	48.5
IPC particles						
N_γ	1.66	1.35	0.86	2.00	1.97	1.89
N_{IPCe}/bc	135200	96600	38100	96800	219000	258600
$\sigma_{BW}/bc [mb]$	1.5	1.3	0.5	2.5	1.5	1.3
$\sigma_{BH}/bc [mb]$	41	36	26	51	48	47
$\sigma_{LL}/bc [mb]$	29	29	28	31	28	27
IPC particles reaching the VD						
$r_1 = 15 \text{ mm } B = 3 \text{ T}$						
N_{IPCe}/bc	163 ± 13	128 ± 11	64 ± 8	150 ± 12	412 ± 20	<u>1700</u>
$N_{IPCe}/train[10^3]$	460	362	360	424	548	<u>4753</u>
$r_1 = 15 \text{ mm } B = 4 \text{ T}$						
N_{IPCe}/bc	94 ± 10	86 ± 9	39 ± 6	90 ± 9	220 ± 15	240 ± 15
$N_{IPCe}/train[10^3]$	265	243	220	254	291	679
$r_1 = 15 \text{ mm } B = 5 \text{ T}$						
N_{IPCe}/bc	58 ± 8	57 ± 8	22 ± 5	62 ± 8	142 ± 12	138 ± 12
$N_{IPCe}/train[10^3]$	162	161	124	174	189	388
$r_1 = 20 \text{ mm } B = 3 \text{ T}$						
N_{IPCe}/bc	88 ± 9	85 ± 9	38 ± 6	90 ± 9	219 ± 15	230 ± 15
$N_{IPCe}/train[10^3]$	249	239	212	254	291	650
$r_1 = 20 \text{ mm } B = 4 \text{ T}$						
N_{IPCe}/bc	52 ± 7	53 ± 7	22 ± 5	58 ± 7	131 ± 11	120 ± 11
$N_{IPCe}/train[10^3]$	146	148	124	164	174	340
$r_1 = 20 \text{ mm } B = 5 \text{ T}$						
N_{IPCe}/bc	33 ± 6	31 ± 6	14 ± 4	36 ± 6	82 ± 9	83 ± 9
$N_{IPCe}/train[10^3]$	92	86	80	103	110	233

Table VII: GUINEA-PIG simulation results of background production for different ILC design optimisations. The *TESLA TDR* case is shown for reference.

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