

Probing Electroweak Top Quark Couplings at Hadron and Lepton Colliders

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1 – Introduction

- Although we have discovered the top quark almost 10 years ago, we know little about its couplings to photons and Z bosons
- The most general ttV ($V = \gamma, Z$) vertex function (for on-shell V) can be written in terms of 8 form factors
- ☞ for on-shell top quarks 4 form factors remain:

$$\Gamma_{\mu}^{ttV}(s, q, \bar{q}) = -ie \left\{ \gamma_{\mu} \left(F_{1V}^V(s) + \gamma_5 F_{1A}^V(s) \right) + \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} \left(iF_{2V}^V(s) + \gamma_5 F_{2A}^V(s) \right) \right\}$$

m_t : top quark mass; q (\bar{q}): t (\bar{t}) four momenta

$$\sigma_{\mu\nu} = (i/2)[\gamma_{\mu}, \gamma_{\nu}]$$

☞ physics interpretation of form factors:

→ F_{1V}^V (F_{1A}^V) are the vector (axial vector) form factors

→ F_{2V}^γ is related to the anomalous magnetic moment:

$$F_{2V}^\gamma(0) = Q_t (g - 2)/2, \quad Q_t = 2/3$$

→ F_{2A}^V violates CP and is related to electric (weak) dipole moment:

$$d_t^V = (e/2m_t) F_{2A}^V(0)$$

☞ concentrate on these 4 form factors here

☞ assuming a dipole form factor, S -matrix unitarity restricts the low energy form factors to

$$\left| F_{iV,A}^V(0) \right| \leq \left(c_i^V / \Lambda \right)^{i+1}$$

where Λ = scale of new physics, and

$$c_1^\gamma = 6.8 \text{ TeV}, \quad c_1^Z = 5.1 \text{ TeV}, \quad c_2^\gamma = 3.4 \text{ TeV}, \quad c_2^Z = 2.8 \text{ TeV}$$

- $b \rightarrow s\gamma$ weakly constrains $F_{2V,A}^\gamma$: $-0.2 < F_{2V}^\gamma < 0.5, |F_{2A}^\gamma| < 4.5$

- LEP data indirectly constrain $F_{1V,A}^Z$ but **not** $F_{1V,A}^\gamma$ (Larios et al.).
LEP data also constrain a linear combination of F_{2V}^Z and F_{2V}^γ (Eboli et al.).

Disadvantages:

- ☞ constraints are (mildly) cutoff dependent
- ☞ constraints assume no other new physics is present
- A linear e^+e^- collider promises to determine $F_{iV,A}^V$ with a precision of **a few percent** in $e^+e^- \rightarrow t\bar{t}$ for $\sqrt{s} = 500$ GeV and 200 fb^{-1} (Snowmass 2001)
disadvantage: difficult to disentangle $tt\gamma$ and ttZ couplings
deficiency: only one coupling at a time is varied in existing studies:
how do correlations between couplings affect the limits?

- is it possible to determine the $t\bar{t}V$ couplings at the Tevatron and/or the LHC?
 - ➡ consider $t\bar{t}\gamma$ and $t\bar{t}Z$ production
 - ➡ can separate $t\bar{t}\gamma$ and $t\bar{t}Z$ couplings
 - ➡ $F_{1V,A}^V$ ($F_{2V,A}^V$) are dimension 4 (5) couplings
 - ➡ p_T distribution of photon/ Z is harder for $F_{2V,A}^V$
 - ➡ and may help to discriminate F_1 and F_2 type couplings

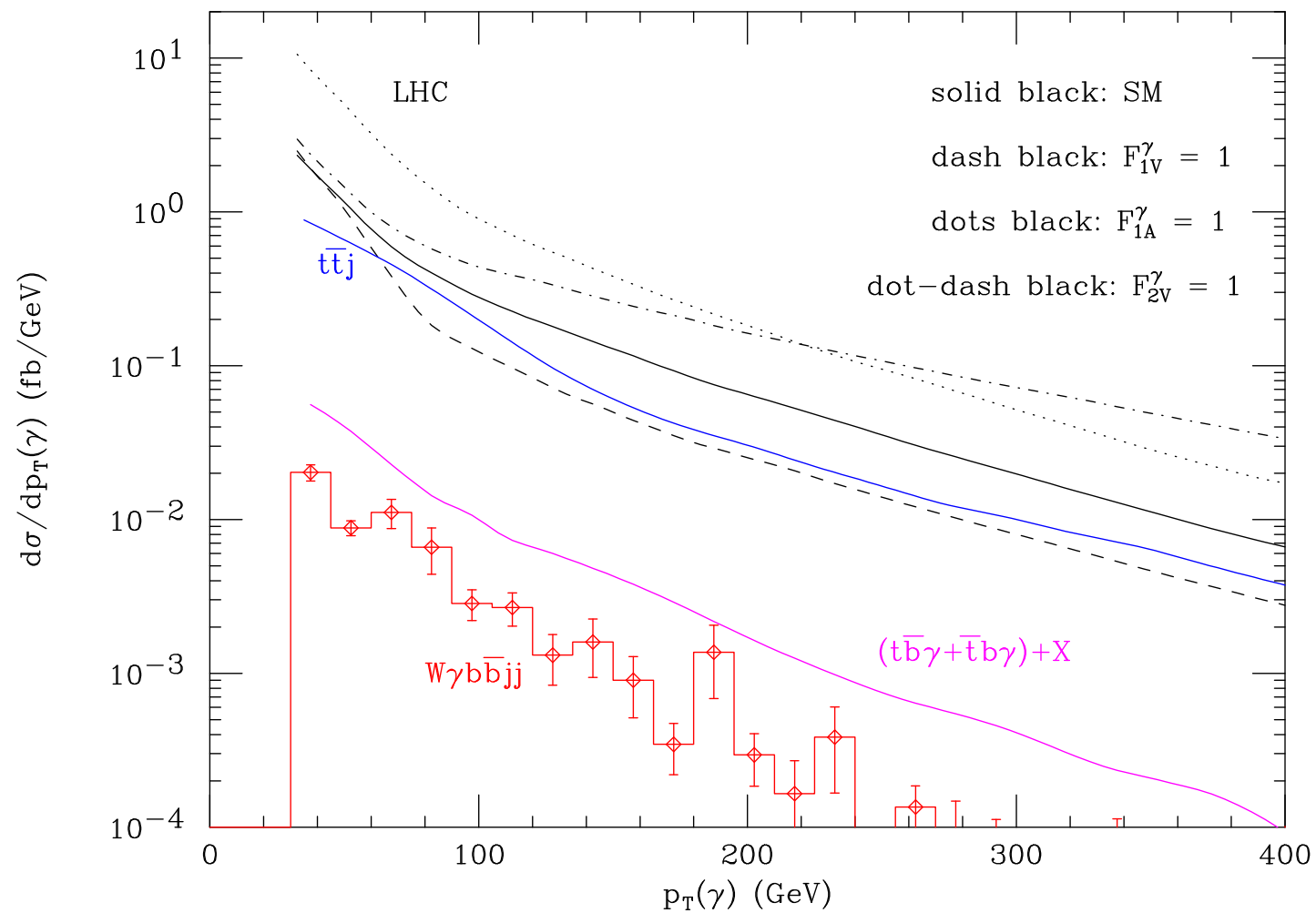
2 – $t\bar{t}\gamma$ Production

- concentrate on $\ell^\pm \nu jj b \bar{b} \gamma$ final state and require 2 tagged b 's
- signal:
 - ☞ include photon radiation off b 's, W 's and W decay products
 - ☞ require $\Delta R(b, \gamma) > 1$ to suppress radiation off b 's
 - ☞ require $m(jj\gamma) > 90$ GeV and $(e\gamma) \cancel{p}_T$ cluster transverse mass $m_T(e\gamma; \cancel{p}_T) > 90$ GeV to suppress radiation off W decay products
 - ☞ impose invariant mass and m_T cuts on bjj , $bjj\gamma$, $\ell\nu b\gamma$ and $\ell\nu b$ requiring them to be consistent with coming from top decay
 - ☞ photon transverse momenta of interest are < 500 GeV
 - ➔ form factor effects can be neglected if $\Lambda \geq 1$ TeV is assumed
 - ☞ gg fusion ($q\bar{q}$ annihilation) dominates at LHC (Tevatron)

- backgrounds:

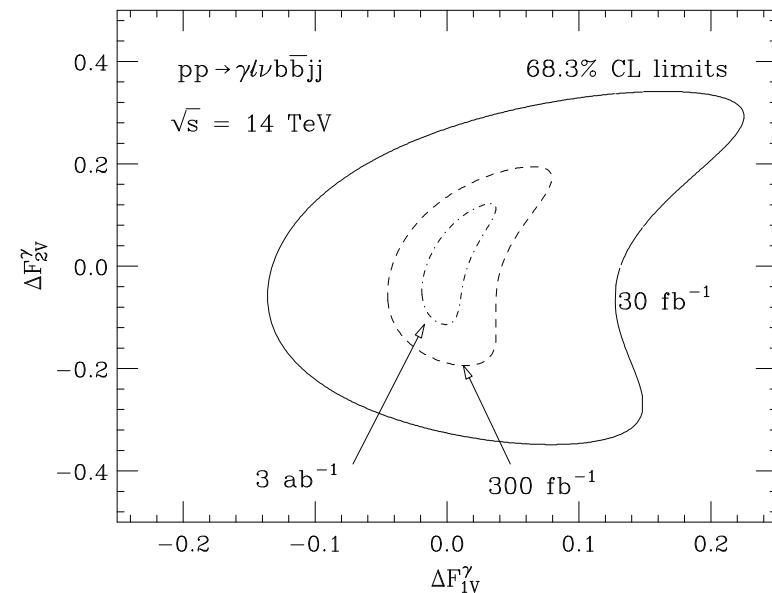
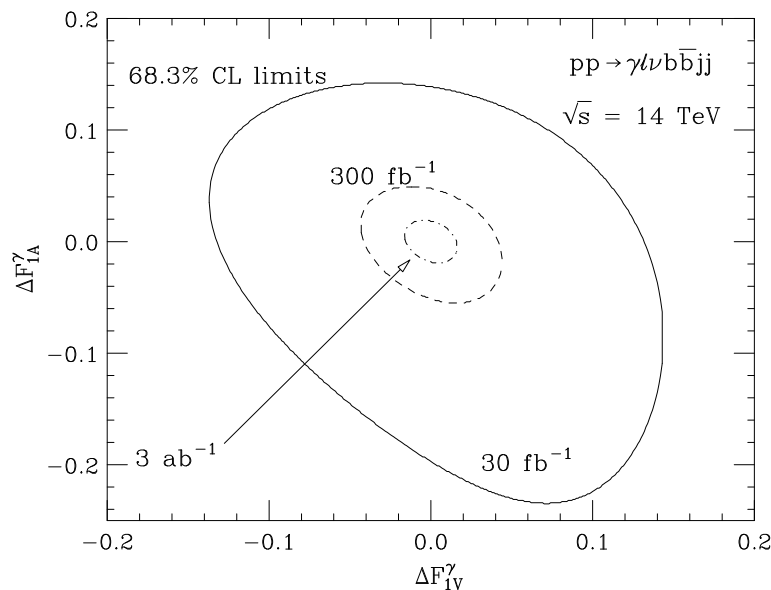
- ☞ $W^{\pm}\gamma b\bar{b}jj$ production (non-resonant diagrams contributing to final state)
- ☞ $t\bar{b}\gamma jj$, $\bar{t}b\gamma jj$, $t\bar{b}\gamma\ell^{-}\bar{\nu}$ and $\bar{t}b\gamma\ell^{+}\nu$ production (single resonant diagrams contributing to final state)
- ☞ $t\bar{t}j$ production, where one jet fakes a photon
 - largest background if jet misidentification probabilities of CDF, DØ, ATLAS or CMS are used

☞ $p_T(\gamma)$ distribution at LHC

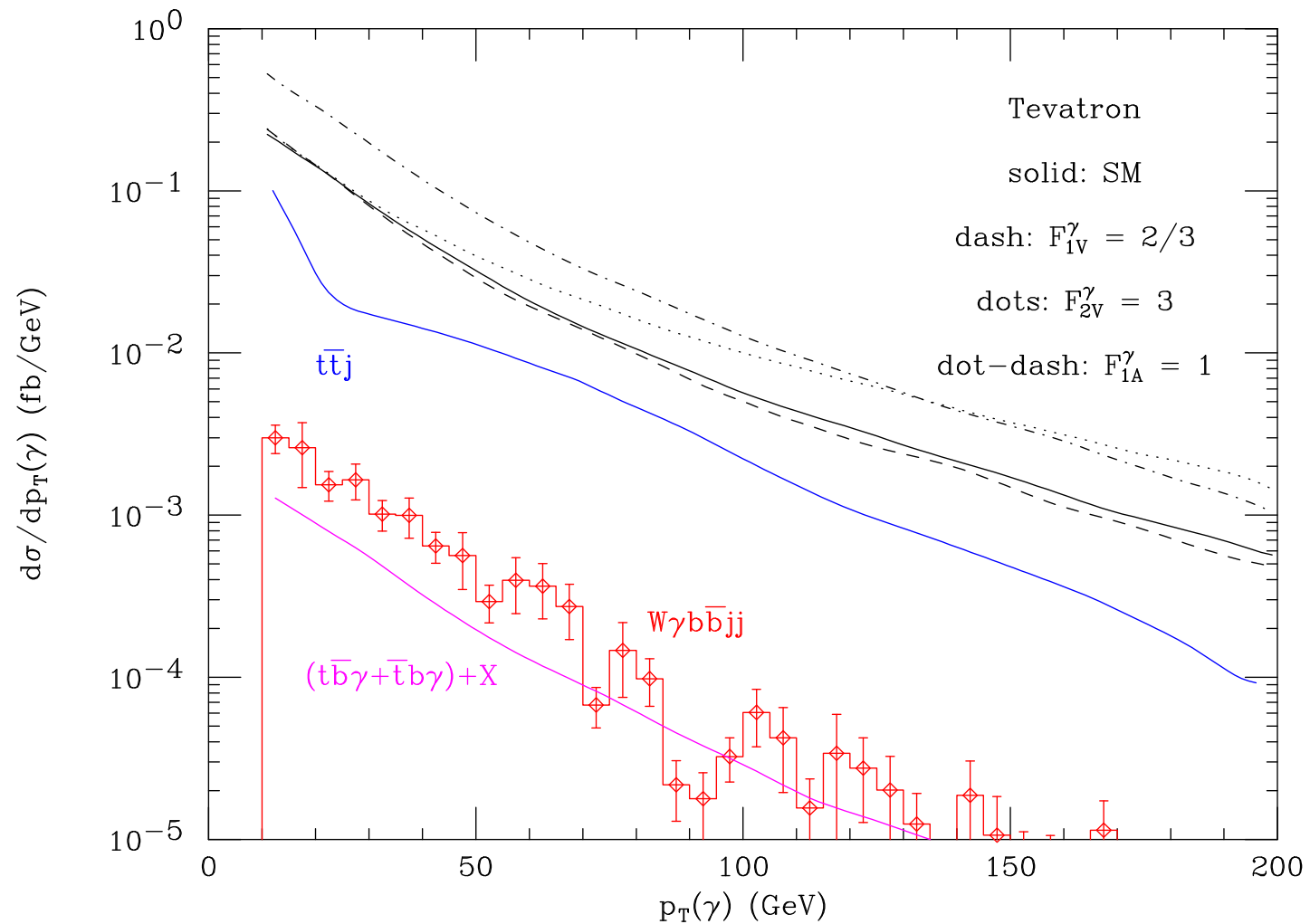


☞ background manageable

- determine sensitivity limits from χ^2 fit to $p_T(\gamma)$ distribution, assuming a 30% normalization uncertainty of the SM cross section
- ☞ can constrain $tt\gamma$ vector and axial vector couplings to **O(10%)** with **30 fb^{-1}** , and to **a few %** with **300 fb^{-1}**
- ☞ can constrain F_2^γ type couplings to **O(30%)** with **30 fb^{-1}** , and to **O(15%)** with **300 fb^{-1}**



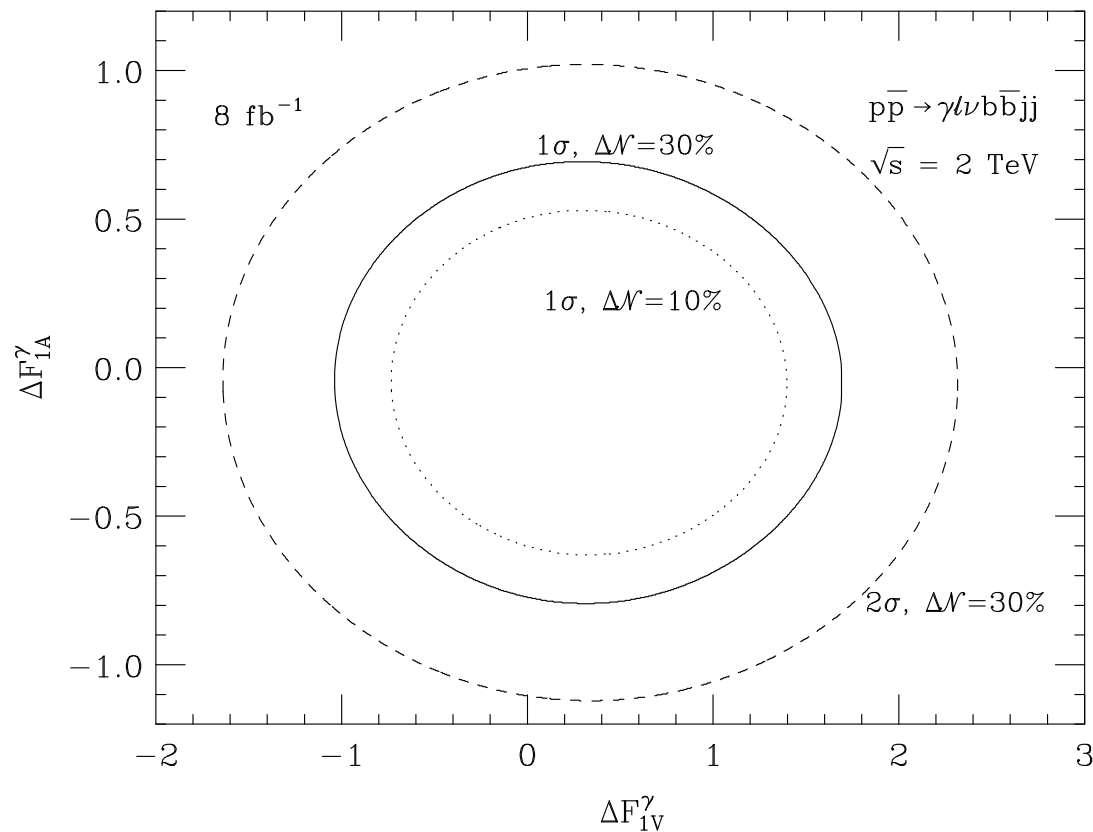
- Tevatron: reduced sensitivity due to “bgd.” from initial state radiation ($q\bar{q}$ annihilation dominates)



- As a result:

- ☞ no sensitivity to F_2 type couplings

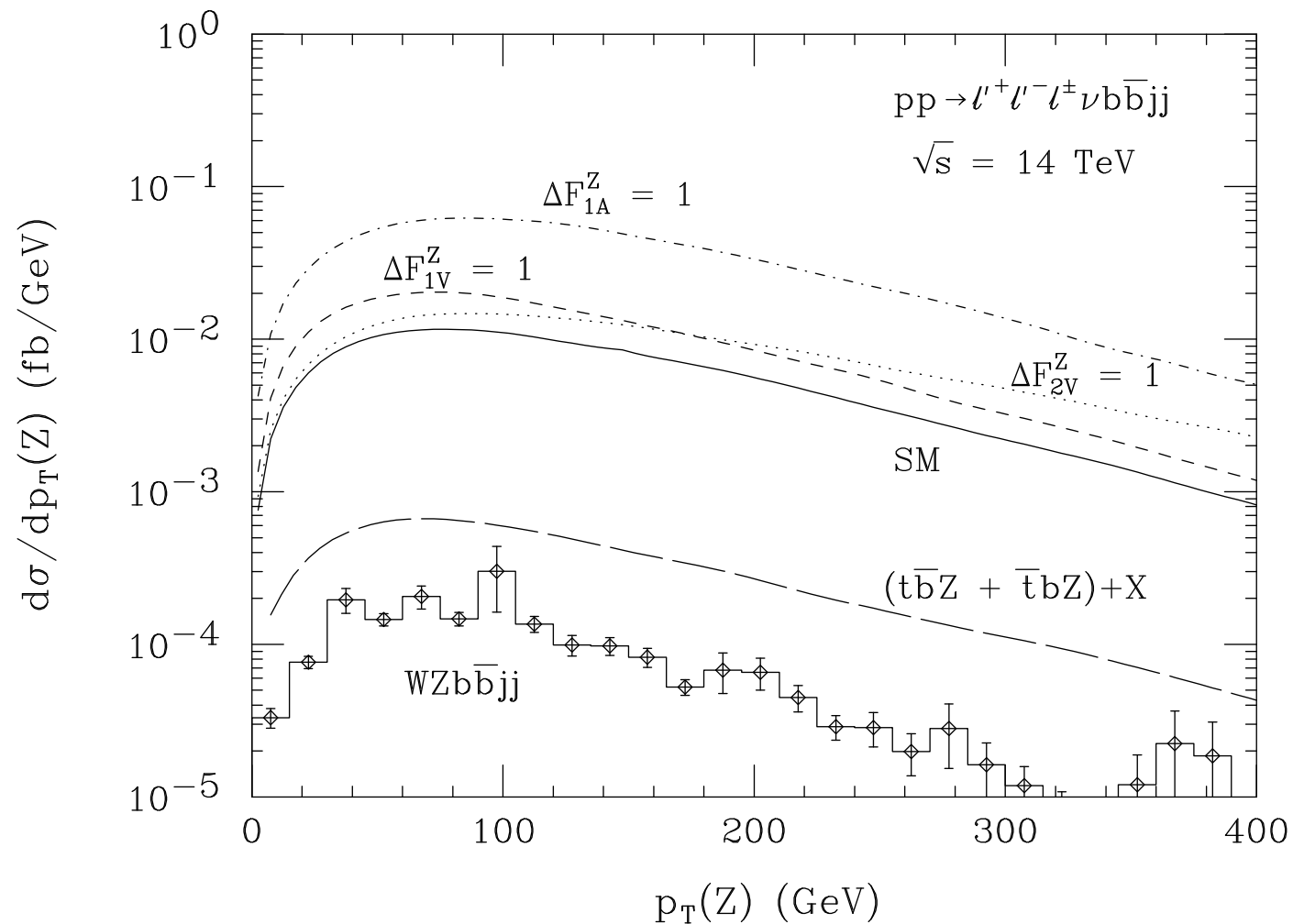
- ☞ for $\geq 8 \text{ fb}^{-1}$ can perform a first rough test of $tt\gamma$ vector and axial vector couplings



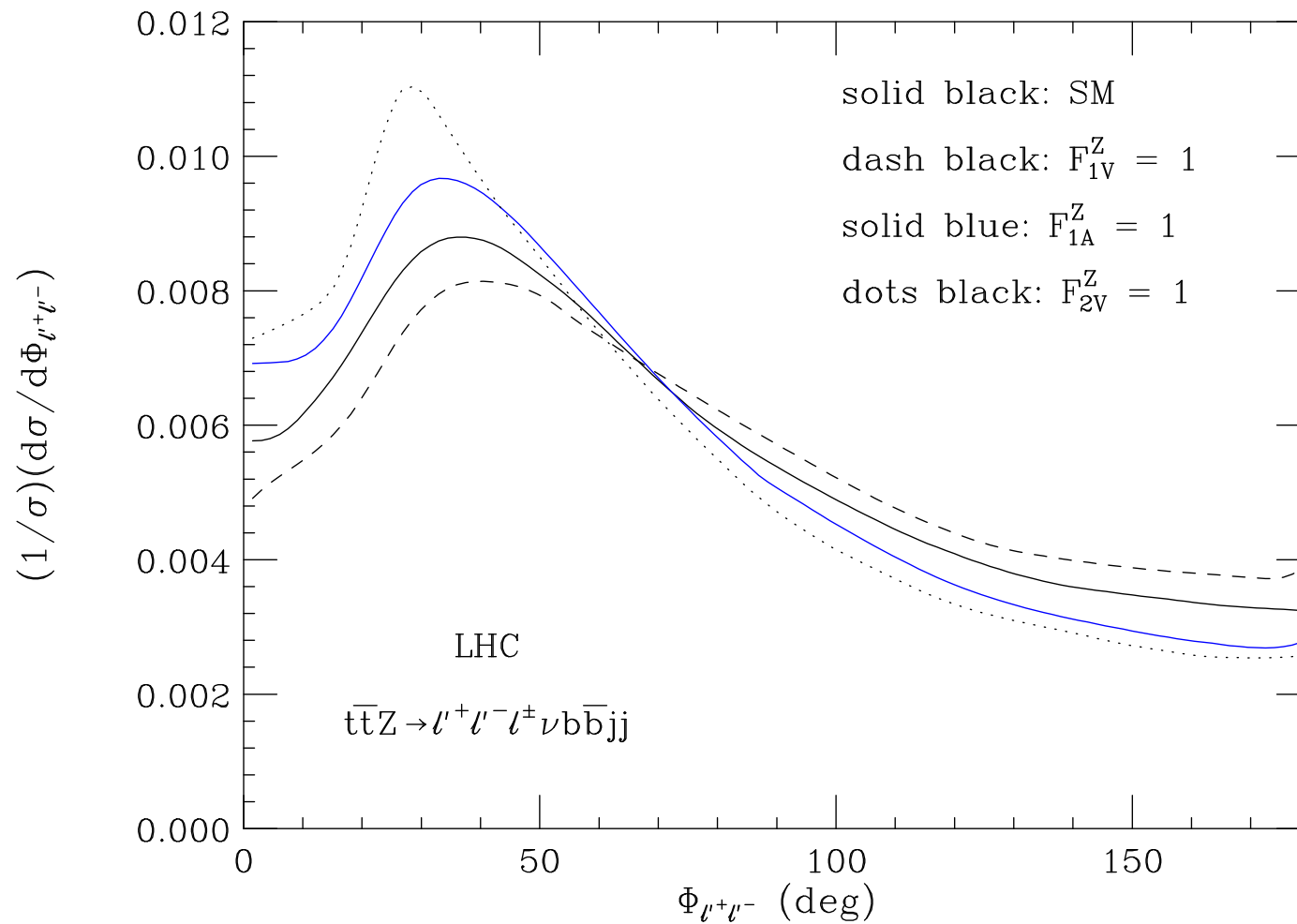
3 – $t\bar{t}Z$ Production

- first consider events with leptonic Z decays
 ☞ $t\bar{t}Z$ production not observable at Tevatron
- consider semi-leptonic and all-hadronic $t\bar{t}$ decays
- again, require 2 b -tags
- signal: include Z emission from top decay products
- (almost) no phase space for $t \rightarrow WZb$ decays: impose invariant mass and m_T cuts such that $\ell'^+ \ell'^-$ pair is consistent with Z , and $\ell\nu b$ and $j j b$ are consistent with top
- $\ell'^+ \ell'^- \ell^\pm \nu b \bar{b} j j$ final state:
 ☞ backgrounds: $W^\pm Z b \bar{b} j j$, $t \bar{b} Z j j$, $\bar{t} b Z j j$, $t \bar{b} Z \ell^- \bar{\nu}$ and $\bar{t} b Z \ell^+ \nu$ production

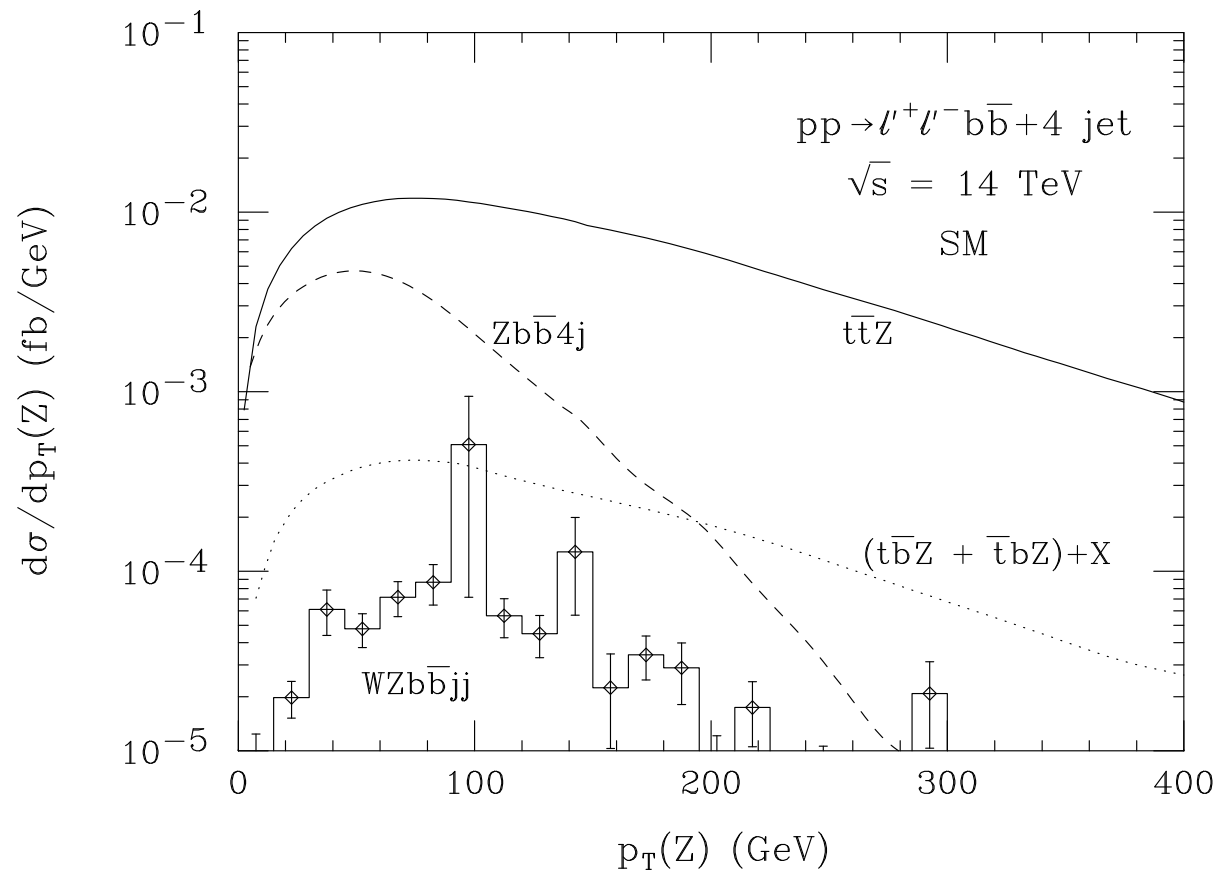
👉 $p_T(Z)$ distribution: effect of anomalous couplings similar to $t\bar{t}\gamma$ case



👉 distribution of opening angle of Z decay leptons also sensitive to F_1 and F_2



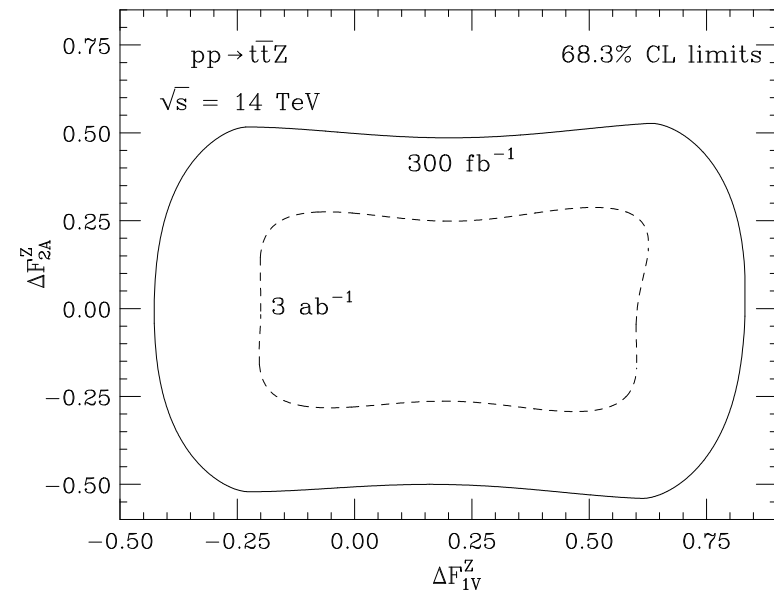
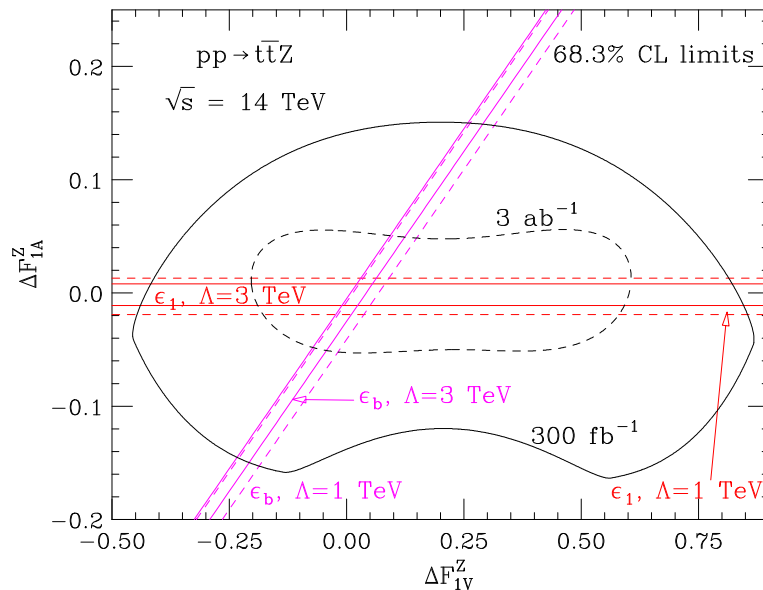
- ☞ all-hadronic top decays: additional background from $Zb\bar{b}4j$ production (calculated using Alpgen)
- ☞ manageable if bjj (jj) systems are required to be consistent with top (W)



- obtain sensitivity limits from $p_T(Z)$ and $\Phi_{\ell'\ell'}$ distributions, assuming 30% normalization uncertainty of SM cross section and two tagged b 's

☞ can test $F_{1V,A}^Z$ at the 15 – 85% (6 – 60%) level for 300 fb⁻¹ (3000 fb⁻¹, SuperLHC)

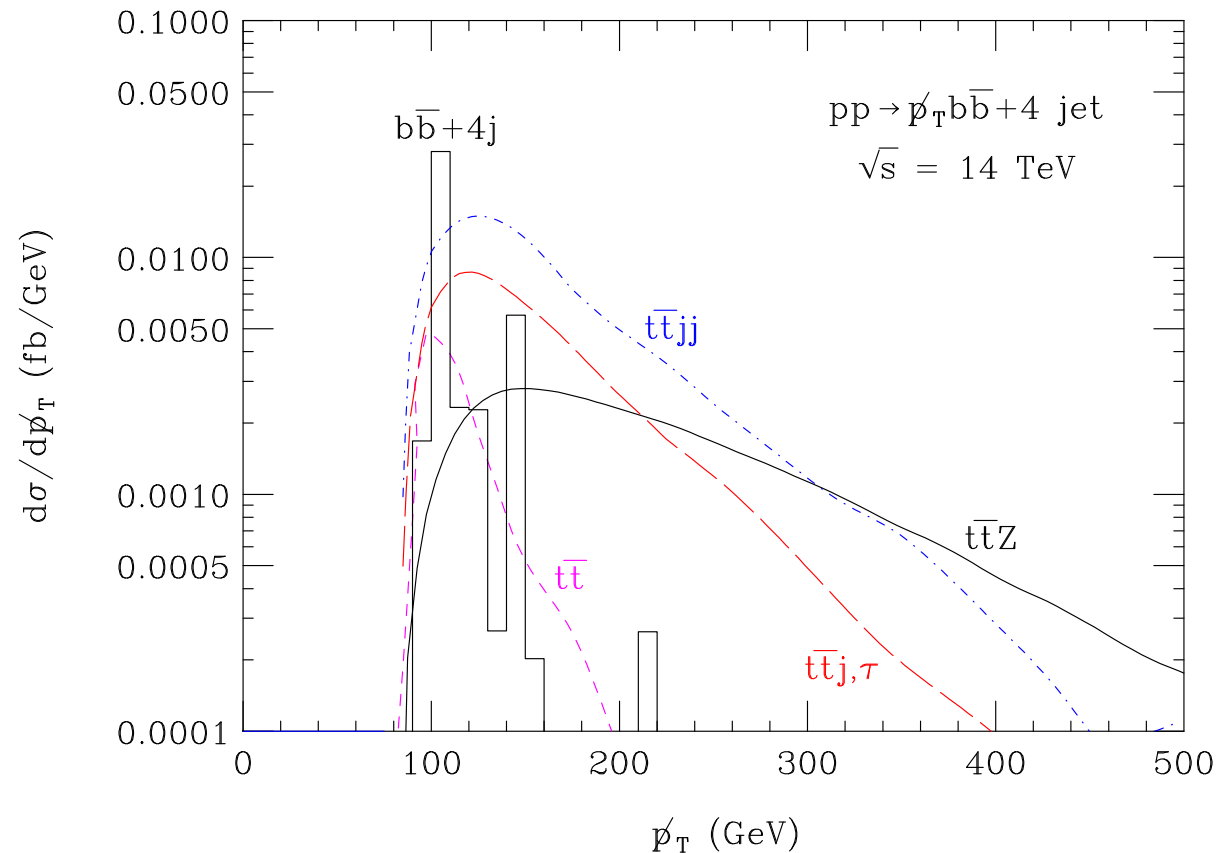
☞ can test $F_{2V,A}^Z$ at the 50% (30%) level for 300 fb⁻¹ (3000 fb⁻¹)



$$t\bar{t}Z \rightarrow \cancel{p}_T b\bar{b} + 4j$$

- now consider $pp \rightarrow t\bar{t}Z$ with $Z \rightarrow \bar{\nu}\nu$ and $t\bar{t} \rightarrow b\bar{b} + 4j$
- advantage: the cross section is about a **factor 5 larger** than for $\ell'^+ \ell'^- \ell^\pm \nu b\bar{b} jj$ final state
- require ≥ 3 jets with $p_T(j) > 50 \text{ GeV}$, $\cancel{p}_T > 5 \text{ GeV}^{1/2} \sqrt{\sum E_T}$ and 2 b tags
- main backgrounds:
 - ☞ $pp \rightarrow t\bar{t}$ and $b\bar{b} + 4j$ production with badly mismeasured jets
 - ☞ $pp \rightarrow t\bar{t}jj$ with $t\bar{t} \rightarrow \ell\nu b\bar{b} + 2j$ where charged lepton is lost
 - ☞ $pp \rightarrow t\bar{t}j$ with $t\bar{t} \rightarrow \tau\nu b\bar{b} + 2j$ and $\tau \rightarrow \text{hadrons}$

- signal dominates at sufficiently high values of p_T



➡ the $p_T b \bar{b} + 4j$ final state improves the limits on anomalous ttZ couplings by 20 – 40%

4 – LHC - ILC Comparison

- $e^+e^- \rightarrow t\bar{t}$ studies (**Snowmass resource book**) use a different parameterization of the $t\bar{t}V$ vertex:

$$\Gamma_{\mu}^{t\bar{t}V}(s, q, \bar{q}) = ie \left\{ \gamma_{\mu} \left(\tilde{F}_{1V}^V(s) + \gamma_5 \tilde{F}_{1A}^V(s) \right) + \frac{(q - \bar{q})_{\mu}}{2m_t} \left(\tilde{F}_{2V}^V(s) + \gamma_5 \tilde{F}_{2A}^V(s) \right) \right\}$$

- $\tilde{F}_{iV,A}^V$ and $F_{iV,A}^V$ are related by

$$\begin{aligned} \tilde{F}_{1V}^V &= - (F_{1V}^V + F_{2V}^V) , & \tilde{F}_{1A}^V &= -F_{1A}^V , \\ \tilde{F}_{2V}^V &= F_{2V}^V , & \tilde{F}_{2A}^V &= -iF_{2A}^V . \end{aligned}$$

- ILC parameters used in Snowmass study: $\sqrt{s} = 500$ GeV, linear polarization $\mathcal{P}(e^-) = \mathcal{P}(e^+) = 0.8$,
only one coupling is varied at a time

coupling	LHC, 300 fb ⁻¹	e ⁺ e ⁻
$\Delta\tilde{F}_{1V}^\gamma$	+0.043 -0.041	+0.047 -0.047, 200 fb ⁻¹
$\Delta\tilde{F}_{1A}^\gamma$	+0.051 -0.048	+0.011 -0.011, 100 fb ⁻¹
$\Delta\tilde{F}_{2V}^\gamma$	+0.038 -0.035	+0.038 -0.038, 200 fb ⁻¹
$\Delta\tilde{F}_{2A}^\gamma$	+0.16 -0.17	+0.014 -0.014, 100 fb ⁻¹
$\Delta\tilde{F}_{1V}^Z$	+0.34 -0.72	+0.012 -0.012, 200 fb ⁻¹
$\Delta\tilde{F}_{1A}^Z$	+0.079 -0.091	+0.013 -0.013, 100 fb ⁻¹
$\Delta\tilde{F}_{2V}^Z$	+0.26 -0.34	+0.009 -0.009, 200 fb ⁻¹
$\Delta\tilde{F}_{2A}^Z$	+0.35 -0.35	+0.052 -0.052, 100 fb ⁻¹

- The ILC is able to achieve better limits for the ttZ couplings
 - The LHC is competitive for some $tt\gamma$ couplings
 - it appears likely that the LHC will accumulate 300 fb^{-1} before the ILC achieves $100 - 200 \text{ fb}^{-1}$
 - ☞ it is worthwhile measuring the ttV couplings at the LHC
 - LHC and Tevatron limits can potentially be improved by including single b -tagged final states (at the cost of an increased background)
 - biggest drawback of current ILC study of ttV couplings: no correlations between different ttV couplings are taken into account
- It is worthwhile launching a new study of $e^+e^- \rightarrow t\bar{t}$

5 – Conclusions

- the Tevatron may be able to perform a very rough first test of the $tt\gamma$ vector and axial vector couplings, if $\geq 8 \text{ fb}^{-1}$ can be achieved
- the LHC will be able to perform the first precision measurement of the $tt\gamma$ couplings (3 – 10%)
- the determination of the ttZ couplings at the LHC is limited to the 10 – 80% level.
- The ILC will be able to measure both $tt\gamma$ and ttZ couplings at the few percent level.