

# Trilinear $\gamma WW$ Couplings at a $\gamma\gamma$ - collider at ILC

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# Introduction

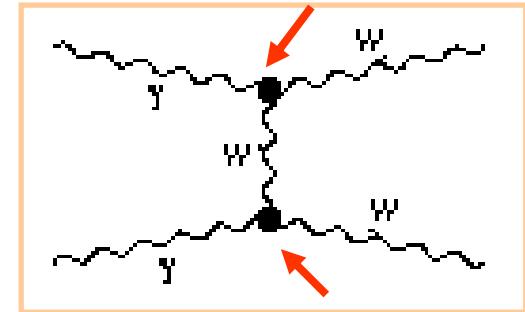
$$\gamma\gamma \rightarrow W^+W^- \rightarrow q\bar{q}q\bar{q} \quad \sqrt{S_{ee}} = 500 \text{ GeV}$$

Dominating diagram for  $\gamma\gamma \rightarrow W^+W^-$

Two initial states

$$J_Z = 0, \left( h_\gamma, h_\gamma = \pm 1, \pm 1 \right)$$

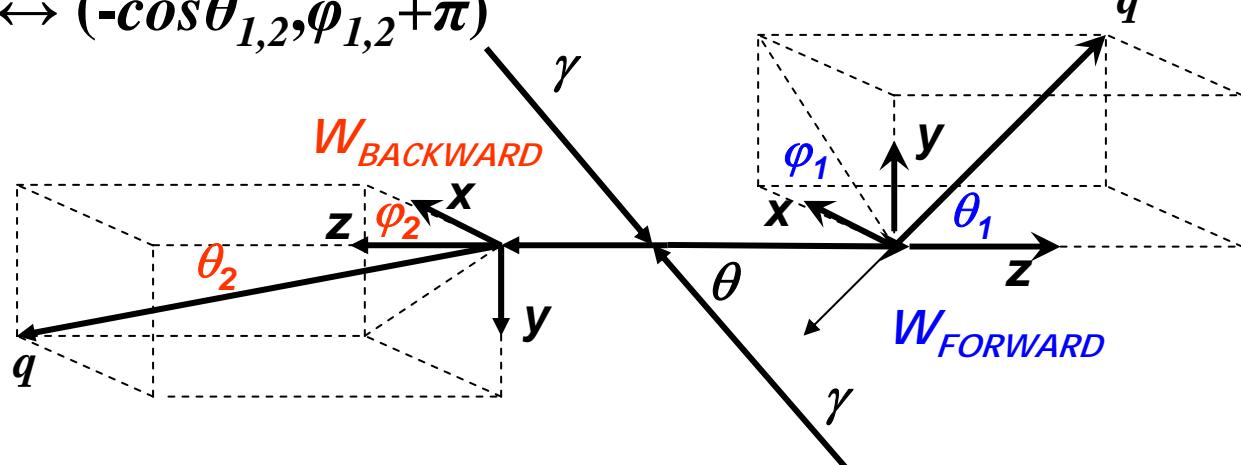
$$J_Z = 2, \left( h_\gamma, h_\gamma = \pm 1, \mp 1 \right)$$



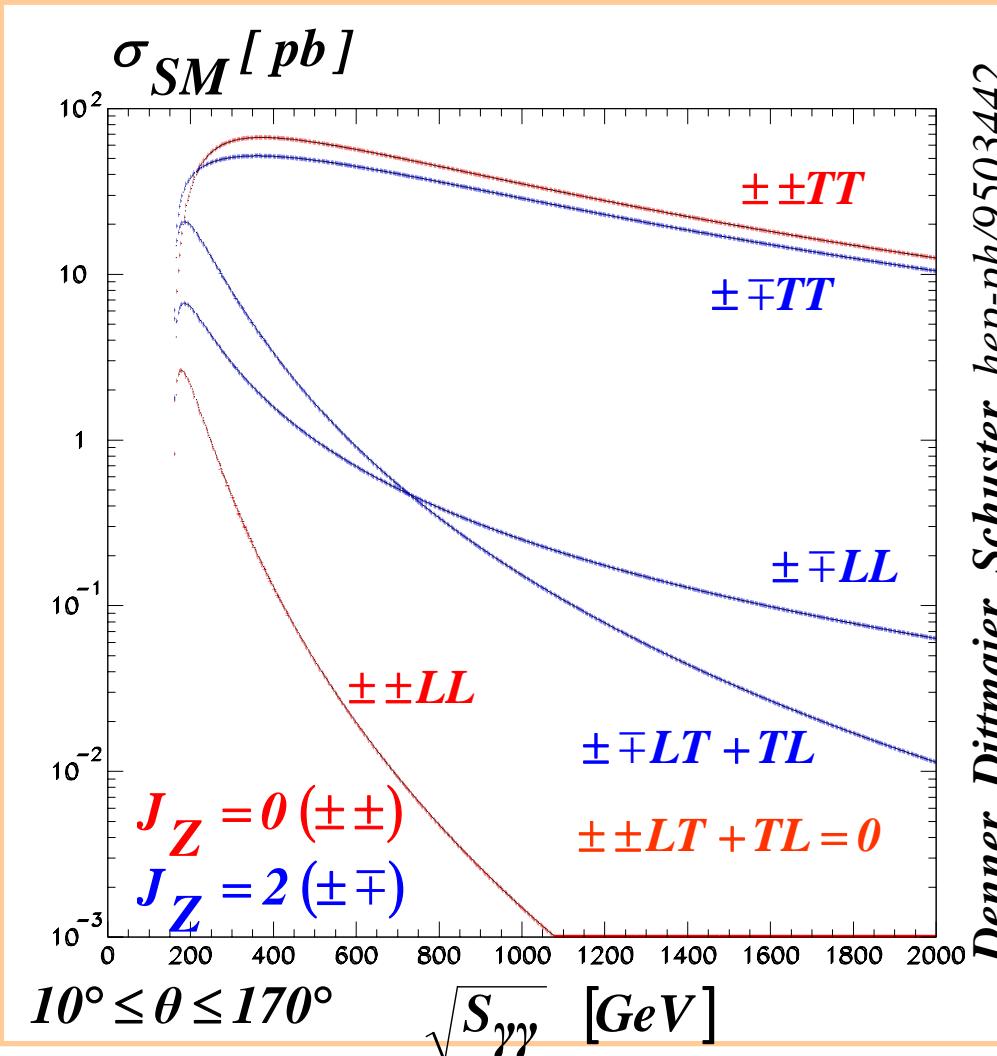
TGCs :  $\kappa_\gamma, \lambda_\gamma$  (in SM 1,0)

Ambiguities in 4-jet events:

$$(\cos\theta_{1,2}, \phi_{1,2}) \leftrightarrow (-\cos\theta_{1,2}, \phi_{1,2} + \pi)$$



# Total Cross-Section vs. CMS



notation

$$(TT) \rightarrow W_T W_T$$

$$(TL) \rightarrow W_L W_T$$

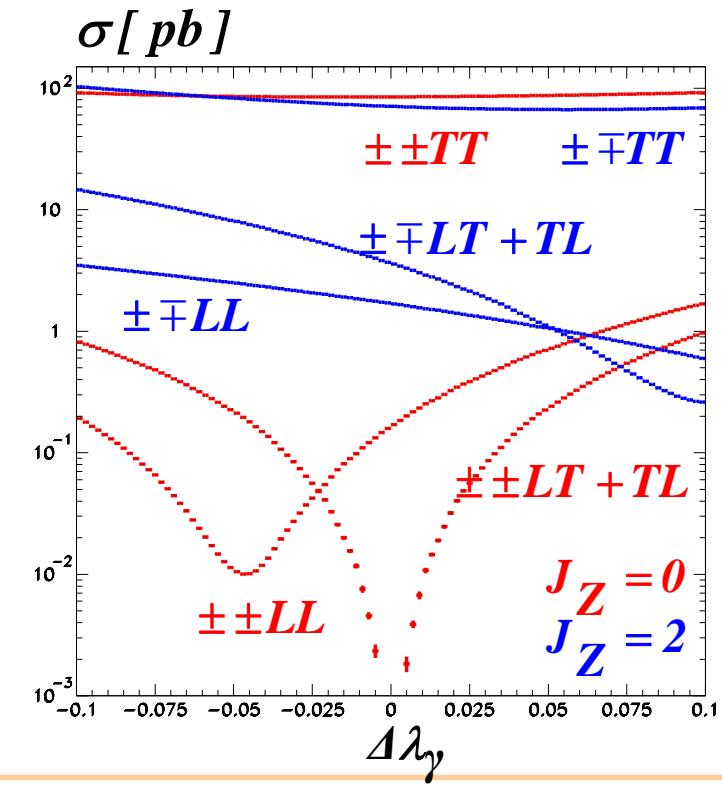
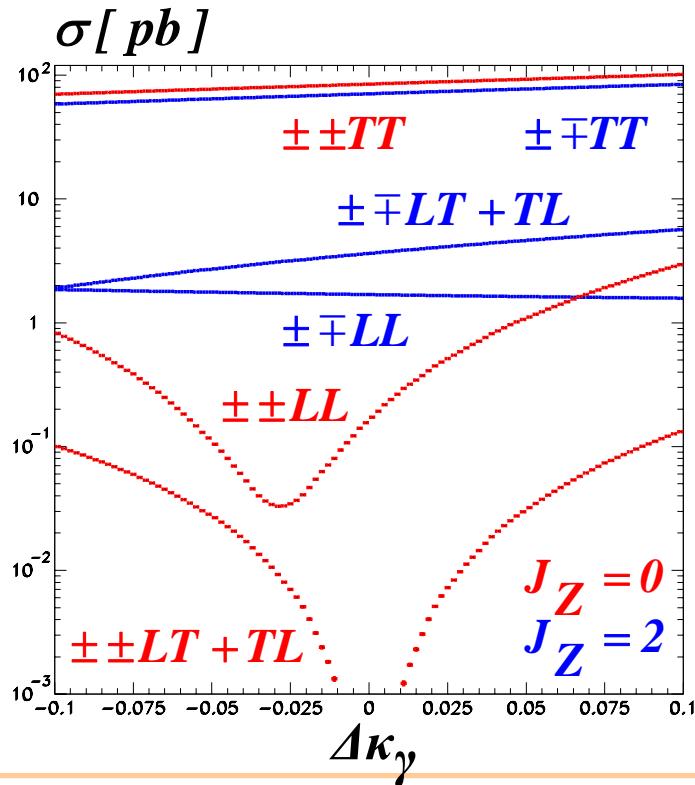
$$(LL) \rightarrow W_L W_L$$

$L$  = longitudinal  $W$

$T$  = transversal  $W$

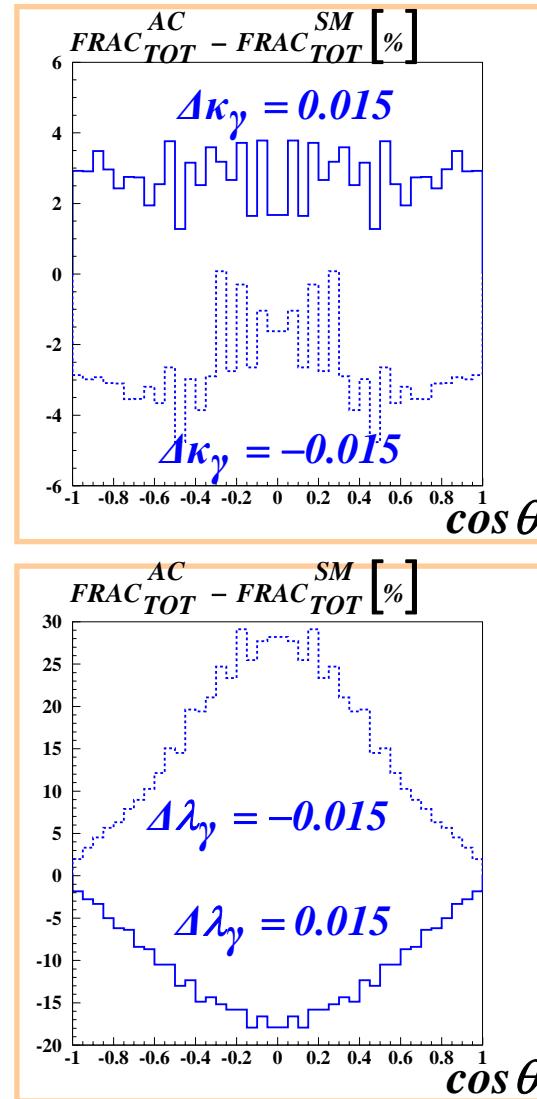
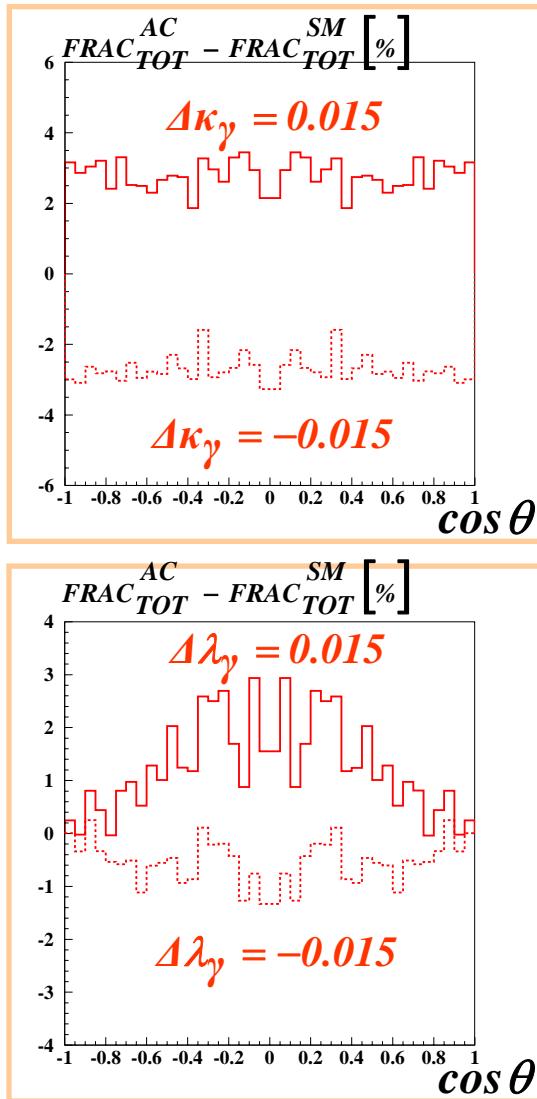
# Total Cross-Section ( $\kappa_\gamma, \lambda_\gamma$ ) - Whizard

On-shell Ws at cme = 400 GeV, 100% polarized beams



# Diff. Cross-Section ( $\kappa_\gamma, \lambda_\gamma$ ) - Whizard

Relative deviations of diff. cross-section from the SM in presence of anomalous couplings



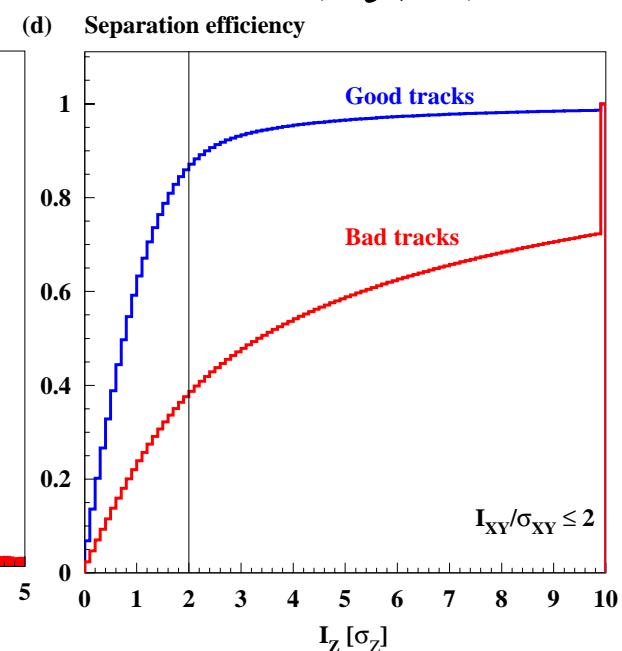
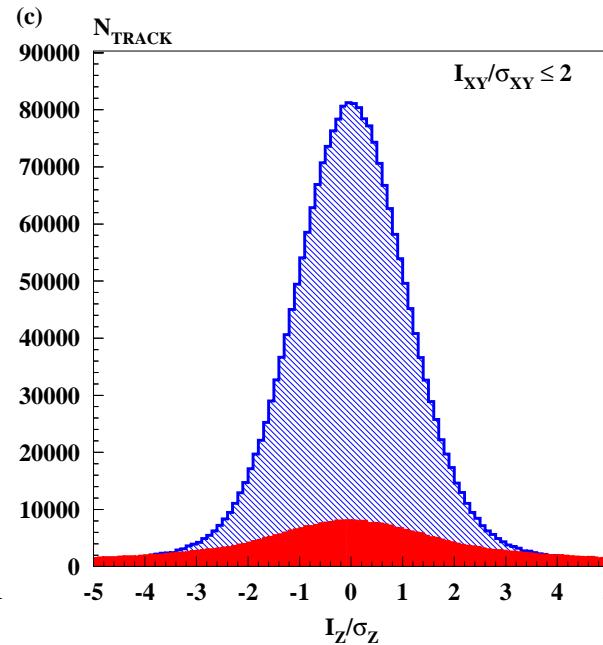
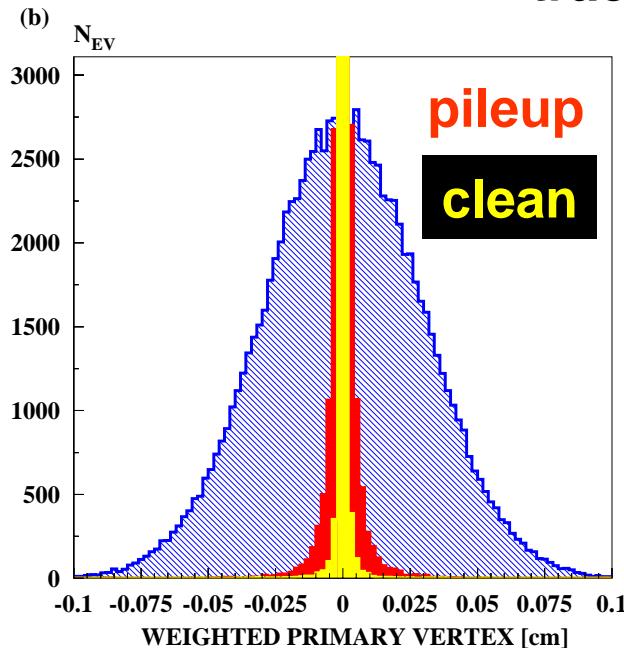
$W_L W_L$  masked by dominating  $W_T W_T$  fraction

# Analysis

- Signal ( $\gamma\gamma \rightarrow WW$ ) and (background, pile-up) samples at detector level WHIZARD – W. Kilian & CIRCE2 – T. Ohl (Telnov's spectra) (variable energy spectra, 85% polarized  $e^-$  and 100%  $\gamma$  beams)
  - pileup : low-energy  $\gamma\gamma \rightarrow qq$  (1.8 ev/BX)
  - background :  $\gamma\gamma \rightarrow qq \rightarrow 4 \text{ jets}$  (O'Mega)  
 $J_z=2 \rightarrow \sigma(\text{QCD}) \sim (1 + i\alpha_s/\pi)$ ,  $J_z=0 \rightarrow \sigma(\text{QCD}) \sim (1 + j\alpha_s/\pi)$   $i[\mathcal{O}(1)] < j$   
(for  $J_z=0$  + QCD contribution  $\mathcal{O}(\alpha^2)$  via  $\gamma\gamma \rightarrow qqgg$  and  $\gamma\gamma \rightarrow qq(g \rightarrow)qq$ ) (MadGraph)
- Response of a detector simulated with **SIMDET V4**
- Ws are reconstructed from **hadronic final states**
- Estimated errors of measurement of  $\kappa_\gamma$  and  $\lambda_\gamma$  parameters, obtained by fit (binned Likelihood )

# Pileup rejection

track selection via impact parameter  $I$  ( $xy, z$ )



Reconstructed PV of an event as the momentum weighted average impact parameter  $I_z$  of all tracks, using the information from

VTX

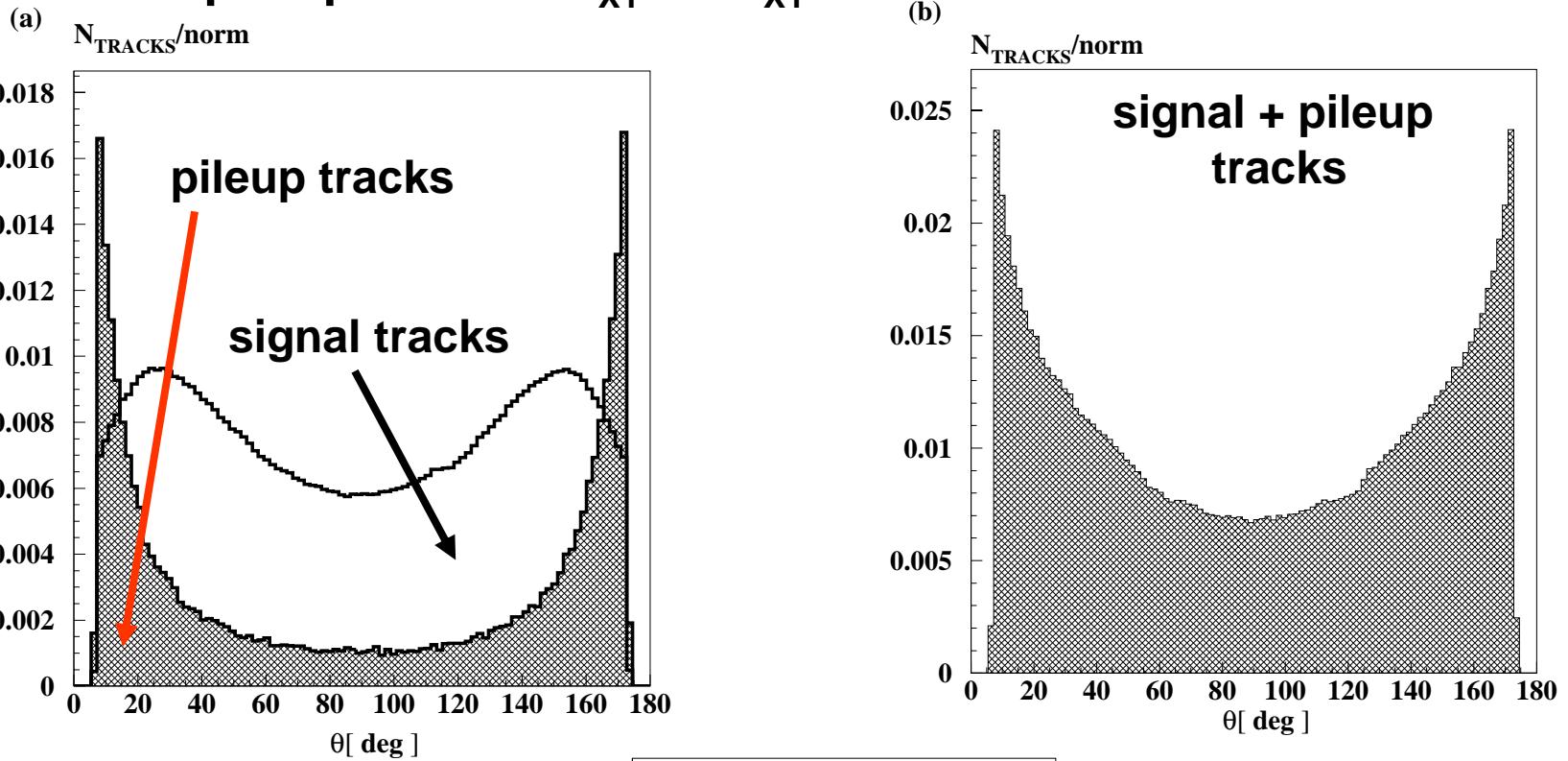
LCWS05 - SLAC

March 2005

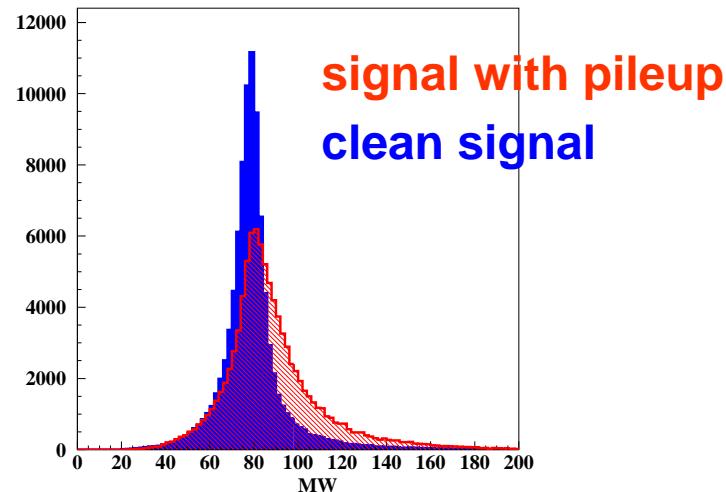
Reconstructed  $I_z$  of each good/bad track normalized to its error

- All neutral accepted
- neutral + tracks with  $\theta > 7^\circ$

# After impact parameter $|I_{XY}| < 2\sigma_{XY}$ condition

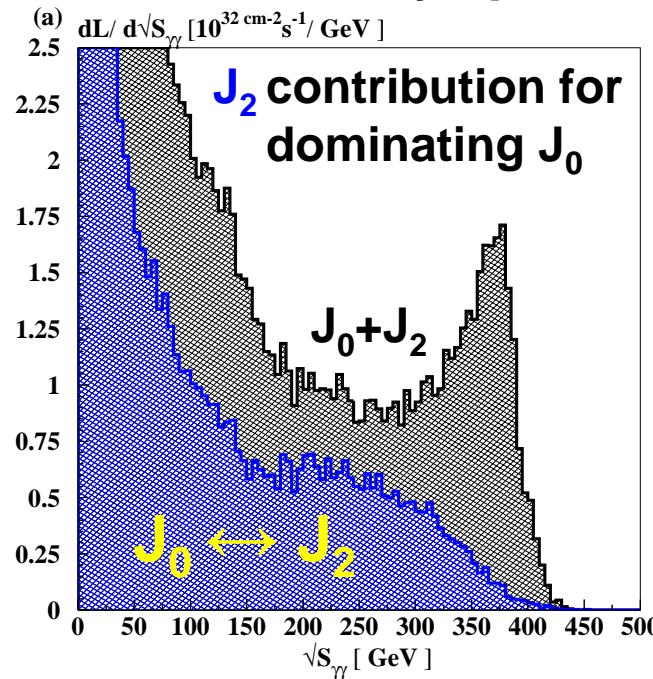


- All neutral accepted
- neutral + tracks with  $\theta > 7^\circ$



# $\gamma\gamma \rightarrow qq \rightarrow 4\text{jets}$ Background

- used luminosity spectra (with mixed  $J_z=0$  and  $J_z=2$  states  $\rightarrow \sigma^{mix}$ )



Born Level       $\sigma_2 \gg \sigma_0$

$J_z=2$ :  $\sigma_2$

$J_z=0$ :  $\sigma_0 \sim \sigma_2 \cdot (m^2/s)$   $\rightarrow$  suppression

NLO corrections       $k_2^{\text{QCD}} < k_0^{\text{QCD}}$

$J_z=2$ :  $k_2^{\text{QCD}} \sim (1+i\alpha_s/\pi)$

$J_z=0$ :  $k_0^{\text{QCD}} \sim (1+j\alpha_s/\pi)$        $i < j$

$$j \sim 1 + aF + \dots + bF^4$$

$$F \sim \frac{\alpha_s}{\pi} \log^2 \frac{s}{m_q^2}$$

1-loop  
non-Sudakov  
form factor

## Corrections to the Born Level $\sigma$

$J_z=2$ :  $\gamma\gamma \rightarrow qq$  (O'Mega) + QCD (4-5%) parton shower well described by Lund model ( $q \rightarrow qg$  soft gluons);  
 $J_0 (\rightarrow 0)$  and  $J_2 \rightarrow$  dominates in  $\sigma^{mix}$

$J_z=0$ :  $\gamma\gamma \rightarrow qq$  (O'Mega)  $\sigma_0^{\text{Born}} \ll \sigma_2^{\text{Born}} \rightarrow J_2$  dominates in  $\sigma^{mix}$  but...

# Correction to $\sigma_{\gamma\gamma \rightarrow qq}$ in the $J_z = 0$ state

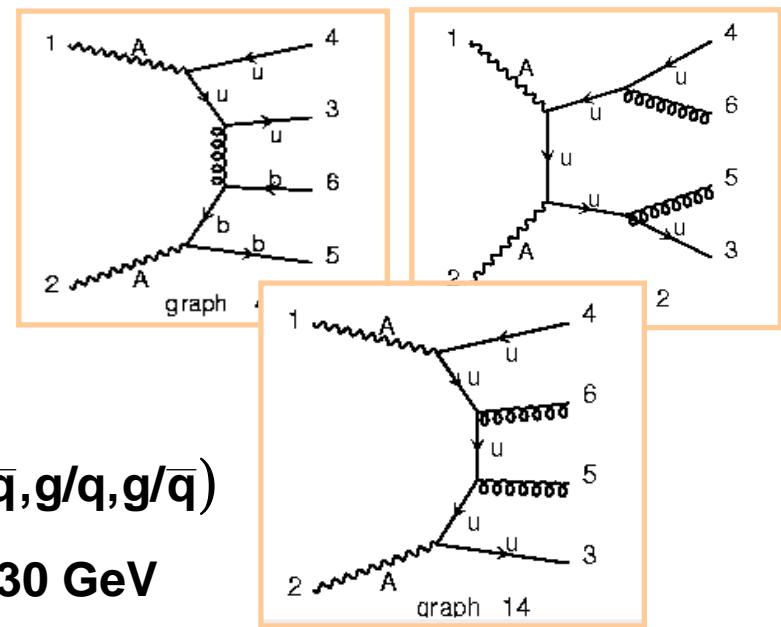
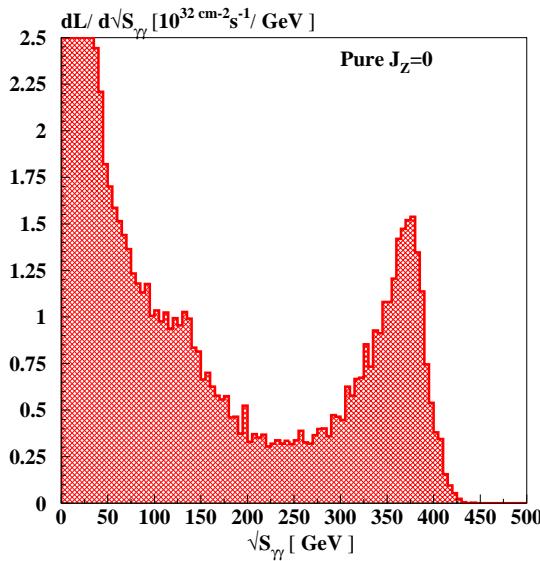
$\sigma_0^{\text{QCD}} \rightarrow 0$  (m<sup>2</sup>/s) suppression canceled by double-logarithms (two-loop)

QCD corrections to the Born Level  $\sigma$  in  $J_z = 0 > \sigma_0^{\text{QCD}}$

Pure  $J_z=0$  (whole spectrum):

MadGraph  $\rightarrow \gamma\gamma \rightarrow qqqg + qq(g \rightarrow qq)$

(O'Mega does not calc. QCD)  $\rightarrow$



$$(p_i + p_j)^2 > ys, (i, j = q, \bar{q}, g/q, g/\bar{q})$$

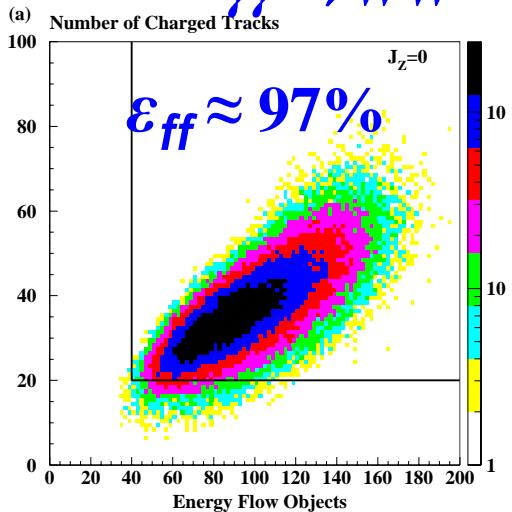
$$M_{\text{INV}}(3, 5, 6, 9, 10, 12) > 30 \text{ GeV}$$

$$M_{\text{INV}}(3, 5, 6, 9, 10, 12) > 30 \text{ GeV}$$

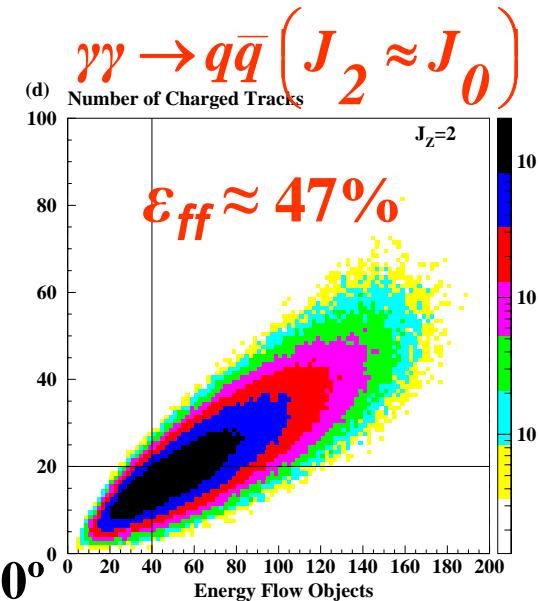
... and added to  $\gamma\gamma \rightarrow qq$  (O'Mega) with  $J_z=0$

# Selection

$\gamma\gamma \rightarrow WW$



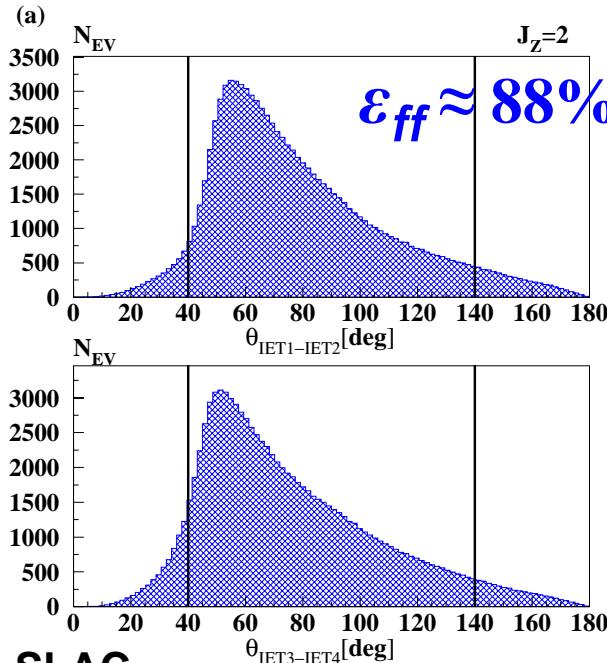
Accepted events:  
NENFLO > 40,  
NCT > 20



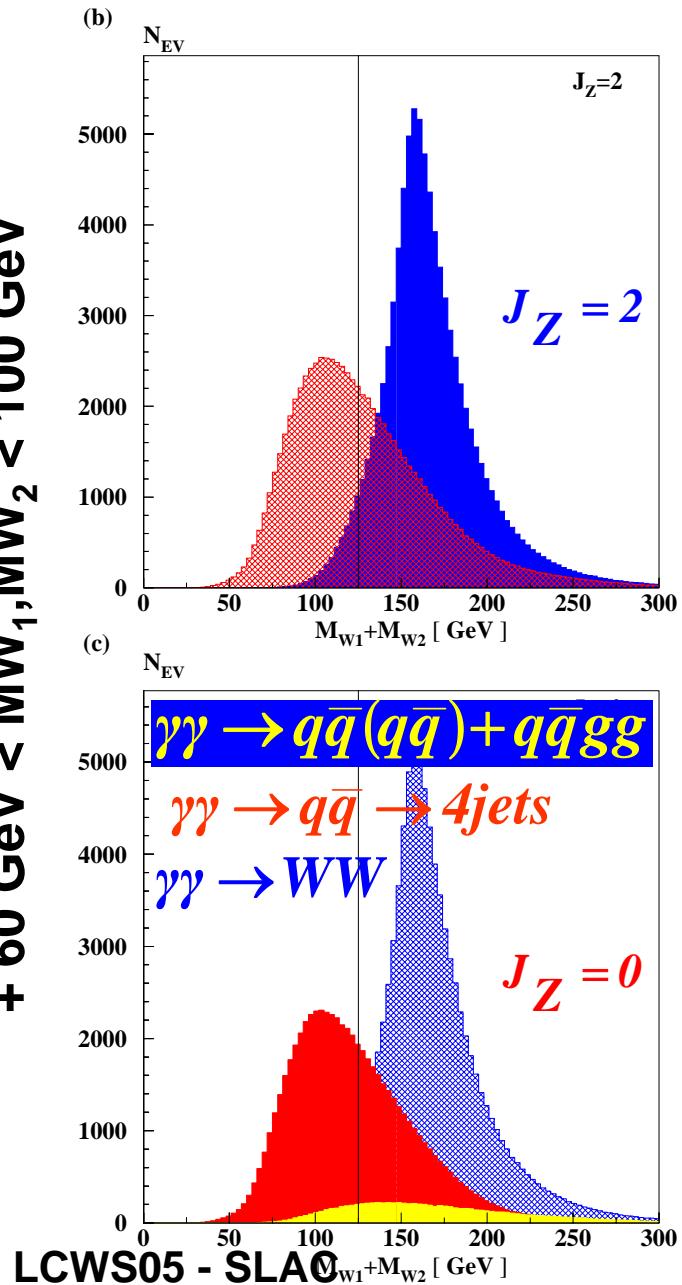
$40^\circ < \text{accepted events} < 140^\circ$

$W_F \cos\theta > 0$   
 $W_B \cos\theta < 0$

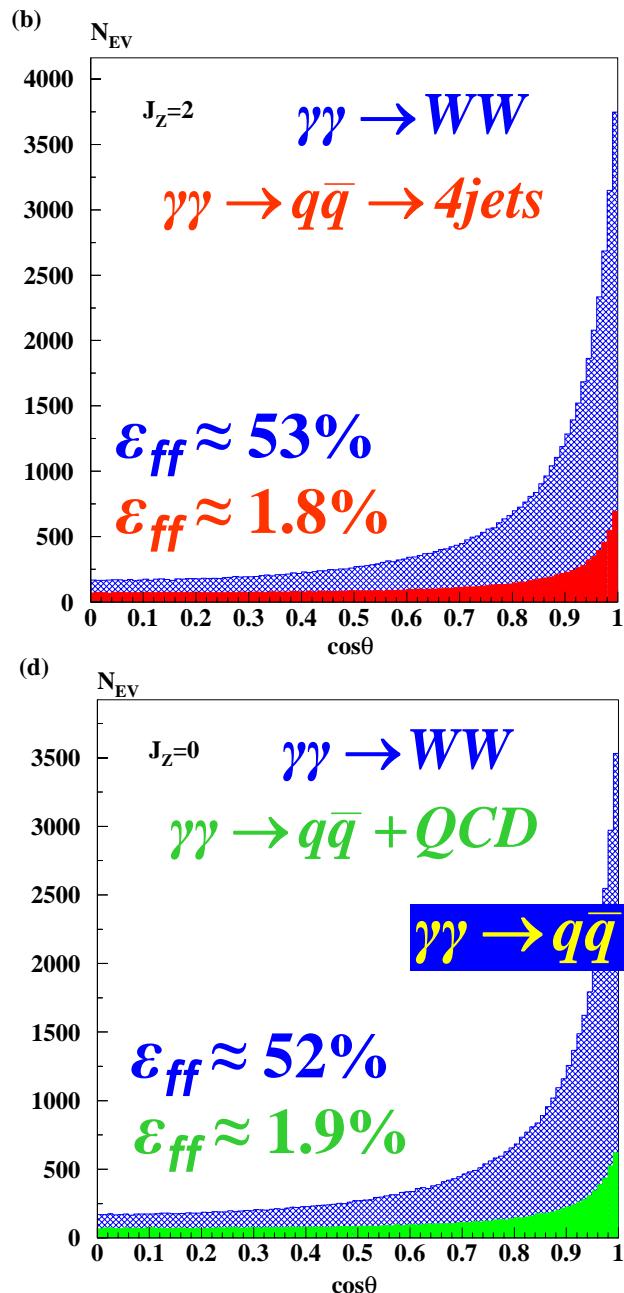
$J1, J2 \rightarrow W_F$   
 $J3, J4 \rightarrow W_B$



$(MW_1 + MW_2) > 125 \text{ GeV}$   
 $+ 60 \text{ GeV} < MW_1, MW_2 < 100 \text{ GeV}$



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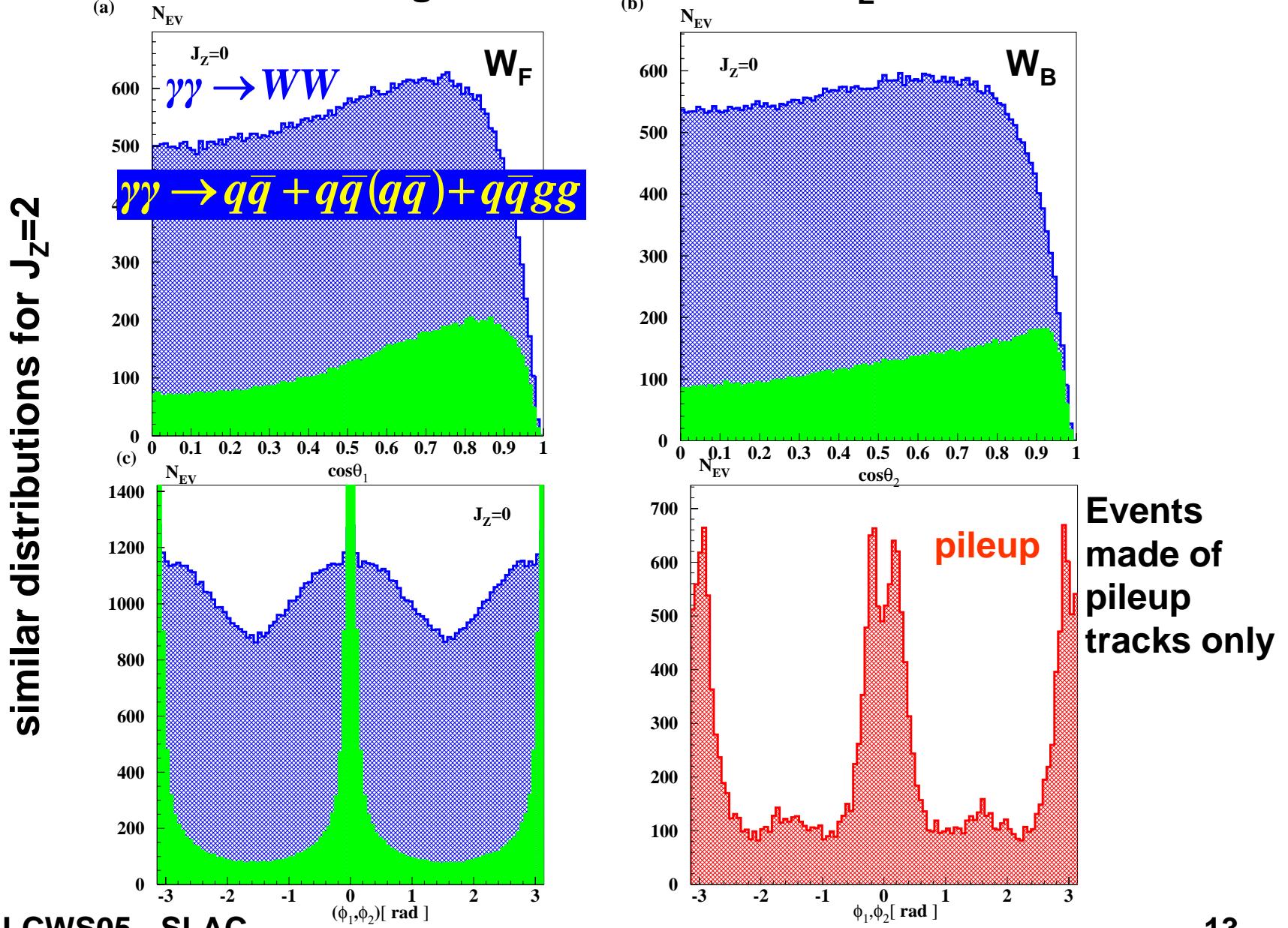
$$\frac{N_s}{N_b} \approx 4.3 \text{ in } J_z = 2$$

Purity = 81%

$$\frac{N_s}{N_b} \approx 4.3 \text{ in } J_z = 0$$

Purity = 81%

# Final angular distributions for $J_z=0$



# Monte Carlo Fit

**Each event described with 5 kinematical variables (sensitive to TGC) :**

- W production angle,  $\cos\theta$  of W boson
- W polar decay angles,  $\cos\theta_{1,2}$  (sensitive to the different W helicity states)
- azimuthal decay angles,  $\varphi_{1,2}$  (sensitive to the interference between different W helicity states)

**Matrix element calculations (O'Mega) → weights to reweight SM events  
 $(\Delta\kappa_\gamma=0, \Delta\lambda_\gamma=0)$  as functions of anomalous TGC by**

**Weight/event:**

$$R(\Delta\kappa_\gamma, \Delta\lambda_\gamma) = 1 + A \cdot \Delta\kappa_\gamma + B \cdot (\Delta\kappa_\gamma)^2 + C \cdot \Delta\lambda_\gamma + D \cdot (\Delta\lambda_\gamma)^2 + E \cdot \Delta\kappa_\gamma \Delta\lambda_\gamma$$

**+ 6-th dimension → cme**

$$L = \left\{ - \sum_{ijklmn} N_{ijklmn}^{DATA} \log \left( N_{ijklmn}^{MC} \right) + \sum_{ijklmn} N_{ijklmn}^{MC} \right\} + \frac{(n-1)^2}{\Delta L^2}$$

$N^D = N^{SM}$  - data sample (SM),  $N^{MC}$  - Monte Carlo sample [ $N^{SM} \cdot R(\Delta\kappa_\gamma, \Delta\lambda_\gamma)$ ],  
 $\Delta L$  – error on luminosity measurement

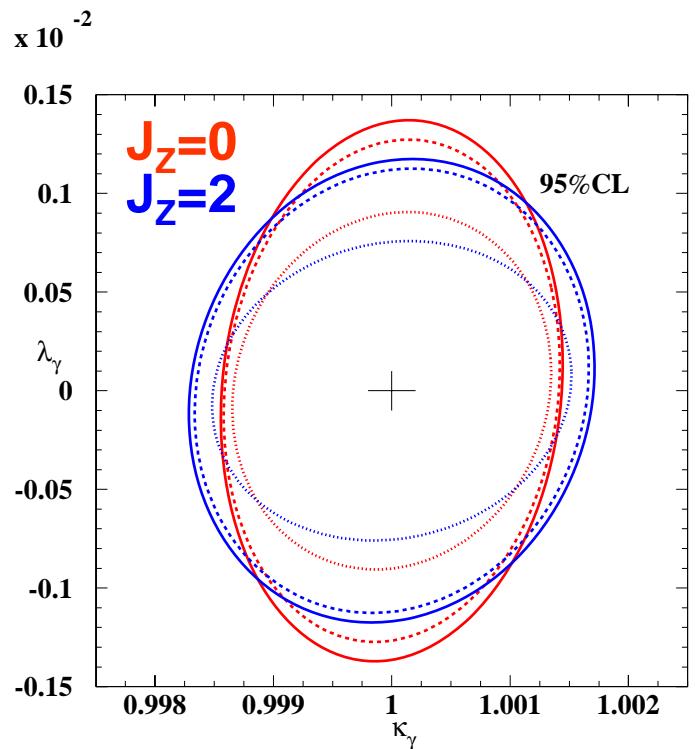
# Error Estimations

Estimated errors for  $\kappa_\gamma$  and  $\lambda_\gamma$  - two-parameter +  $n$  6D fit

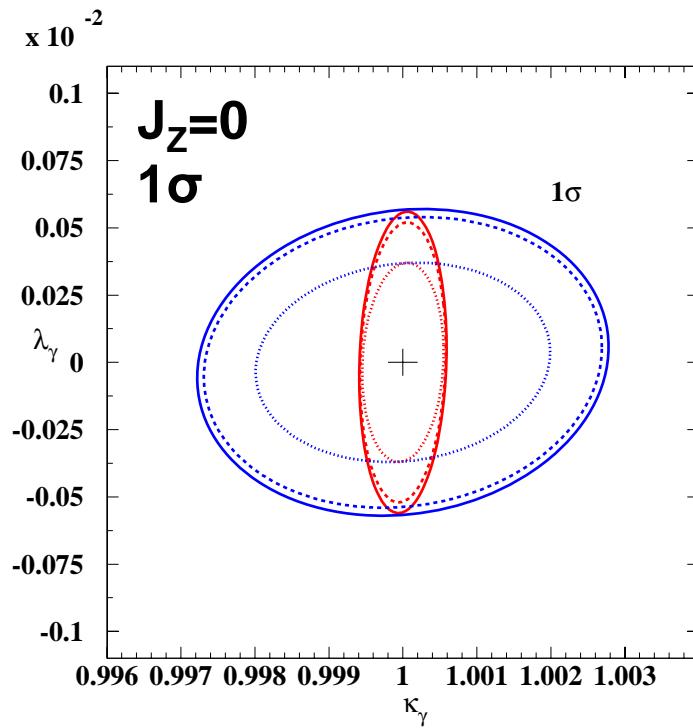
6D FIT	$J_z = 0$		
	without pileup / with pileup / + background		
$\Delta L$	1%	0.1%	accurate
$\Delta \kappa_\gamma \cdot 10^{-4}$	19.9 / 26.9 / 27.8	5.5 / 5.8 / 5.9	2.6 / 3.0 / 3.1
$\Delta \lambda_\gamma \cdot 10^{-4}$	3.7 / 5.4 / 5.7	3.7 / 5.2 / 5.6	3.7 / 5.2 / 5.6

6D FIT	$J_z = 2$		
	without pileup / with pileup / + background		
$\Delta L$	1%	0.1%	accurate
$\Delta \kappa_\gamma \cdot 10^{-4}$	29.9 / 37.4 / 37.8	6.2 / 6.8 / 7.0	3.7 / 4.6 / 4.8
$\Delta \lambda_\gamma \cdot 10^{-4}$	3.1 / 4.6 / 4.8	3.1 / 4.6 / 4.8	3.1 / 4.6 / 4.8

## 2-dimensional contour plots



$\Delta L = 0.1\%$   
95% CL



$\Delta L = 0.1\%$   
 $\Delta L = 1\%$

# 400 GeV % 800 GeV

Estimated errors for  $\kappa_\gamma$  and  $\lambda_\gamma$  - two-parameter +  $n$  (5D fit)  
 (generator level, fixed beam energy)

5D FIT	$J_z = 0$			$J_z = 2$		
	400 GeV / 800 GeV (110 fb $^{-1}$ )	400 GeV / 800 GeV (110 fb $^{-1}$ )	400 GeV / 800 GeV (110 fb $^{-1}$ )	400 GeV / 800 GeV (110 fb $^{-1}$ )	400 GeV / 800 GeV (110 fb $^{-1}$ )	400 GeV / 800 GeV (110 fb $^{-1}$ )
$\Delta L$	1%	0.1%	accurate	1%	0.1%	accurate
$\Delta \kappa_\gamma \cdot 10^{-4}$	14.4/7.2	5.4 / 4.5	2.6 / 2.4	20.1/8.1	6.2/4.6	3.8/2.6
$\Delta \lambda_\gamma \cdot 10^{-4}$	3.0 / 1.3	3.0 / 1.3	3.0 / 1.3	1.6/0.63	1.6/0.58	1.6/0.56

# $\gamma e$ - $\gamma\gamma$ - $e^+e^-$ comparison

	$\gamma e$ $\int L \Delta t \approx 160/230 \text{ fb}^{-1}$	$\gamma\gamma$ $\int L \Delta t \approx 1000 \text{ fb}^{-1}$	$e^+e^-$ $\int L \Delta t = 500 \text{ fb}^{-1}$
<b>500 GeV</b>			
$\Delta L$	0.1%	0.1% (1%)	-
$\Delta \kappa_\gamma \cdot 10^{-4}$	<b>10.0 / 11.0</b>	<b>7.0 / 5.9 (28)</b>	<b>3.6<sup>1</sup></b>
$\Delta \lambda_\gamma \cdot 10^{-4}$	<b>4.9 / 6.7</b>	<b>4.8 / 5.6 (5.7)</b>	<b>11.0<sup>1</sup></b>

	$e^+e^- (800)$ $\int L \Delta t = 1000 \text{ fb}^{-1}$	$\gamma\gamma$ $\int L \Delta t \approx 1000 \text{ fb}^{-1}$
<b>1000GeV</b>		
$\Delta L$	-	(0.1%) / (1%)
$\Delta \kappa_\gamma \cdot 10^{-4}$	<b>2.1<sup>1</sup></b>	<b>5.2 / 13.9</b>
$\Delta \lambda_\gamma \cdot 10^{-4}$	<b>3.3<sup>1</sup></b>	<b>1.7 / 2.5</b>

$\gamma e$ : Real / Paras.  
 $\gamma\gamma$ : JZ=2 / JZ=0  
<sup>1</sup> generator level  
 e- & e+ pol.  
 Scaled for bkg.,  
 spectrum, pileup

# Systematic Errors



## Polarization influence on $\kappa_\gamma$ and $\lambda_\gamma$

Data sample - 1% changed polarization  $J_z=2/J_z=0$  in the sample with  $P_{0,2} = + 0.90$   $J_z=0/J_z=2$

(realized increasing  $N_{ev}$  with  $J_z=2,0$  for 10% → increase of  $N_{ev}$  corresponds to the  $P_{0,2} = + 0.89$ )

fit (with MC):  $J_z=0$  ( $\Delta L = 1\%$ ) →  $\kappa_\gamma, \lambda_\gamma$  shifted  $< 1\sigma$

$J_z=2$  ( $\Delta L = 0.1\%$ ) →  $\kappa_\gamma$  shifted  $< 3\sigma$ ,  $\lambda_\gamma$  shifted  $< 1\sigma$



## Effect of the background

### Data sample

Estimated background per bin is changed for both modes, fit (with MC):  
( $\Delta L = 0.1\%$ )

$J_z=2$  → for  $\kappa_\gamma$  shifted by  $1\sigma$  → bck. at level of  $< 0.8\%$ , for  $\lambda_\gamma < 4\%$

$J_z=0$  → for  $\kappa_\gamma$  shifted by  $1\sigma$  → bck. at level of  $< 1.1\%$ , for  $\lambda_\gamma < 0.6\%$

( $\Delta L = 1\%$ ) for  $\kappa_\gamma$  shifted by  $1\sigma$  → bck. at level of  $\sim 15\%$ , for  $\lambda_\gamma < 0.6\%$

## Conclusions

- Pileup rejection is difficult (still has a large contribution – decrease: to enlarge ‘b’)
- Good signal / background separation
- Information on  $\Delta\kappa_\gamma$  in the cross-section (via n)
- Information on  $\Delta\lambda_\gamma$  in the shape of the distributions
- Statistical error estimations  $\Delta\kappa_\gamma, \Delta\lambda_\gamma \sim 10^{-4}$
- Systematic errors → background