

Testing GR with the Double Pulsar: Recent Results

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With:

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PPARC

Texas Symposium – 16 December 2004



Outline

Introduction

- The system
- Interaction between A&B

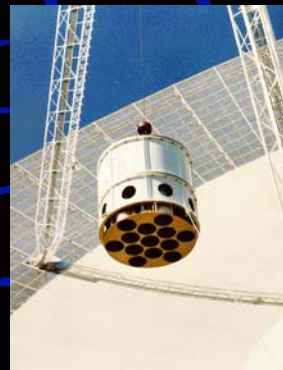
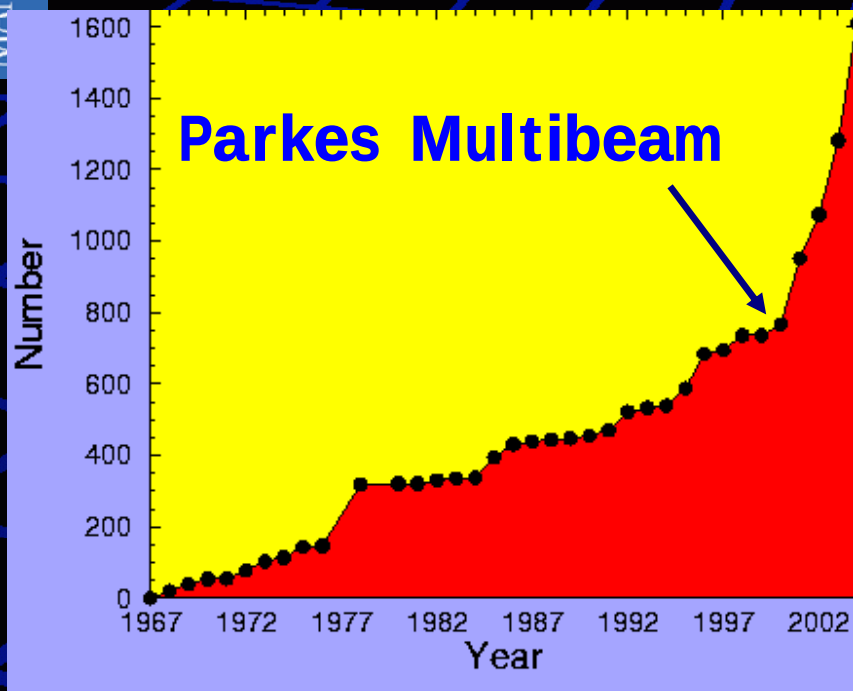
Tests of General Relativity

- Improved parameters
- New measurements & tests

The Future

Parkes Multibeam Survey

lead by Jodrell Bank & ATNF in
collaboration with many partners

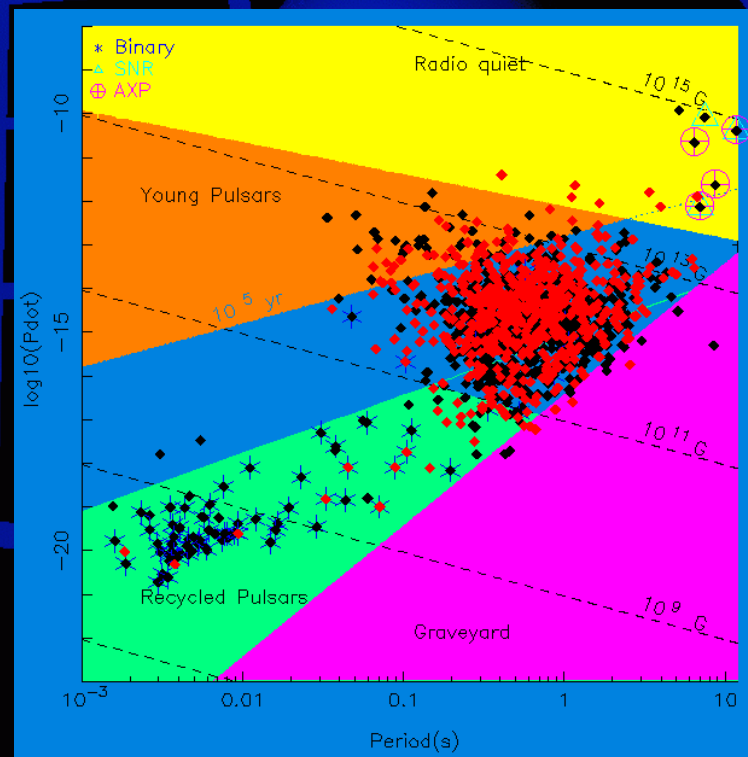


- Most sensitive & most successful
- More than 700 discoveries
- Still counting...
- Lots of exciting systems...

Manchester et al. 2001, Morris et al. 2002

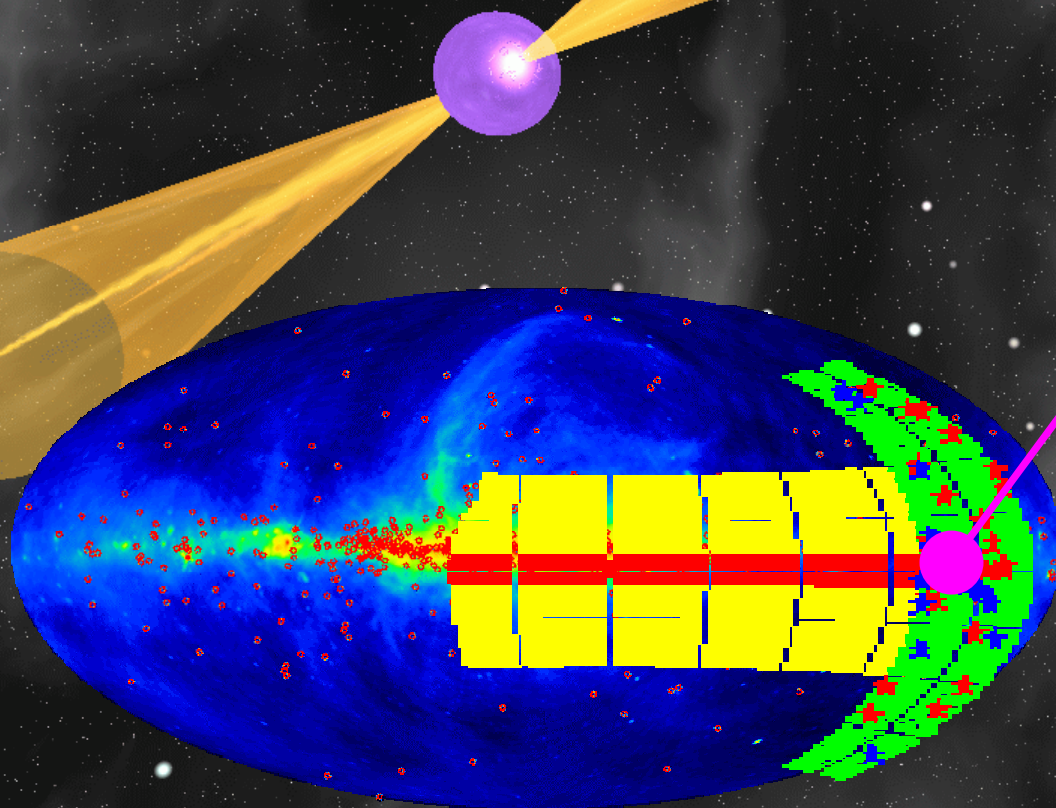
Kramer et al. 2003, Hobbs et al. 2004,

Faulkner et al. 2004

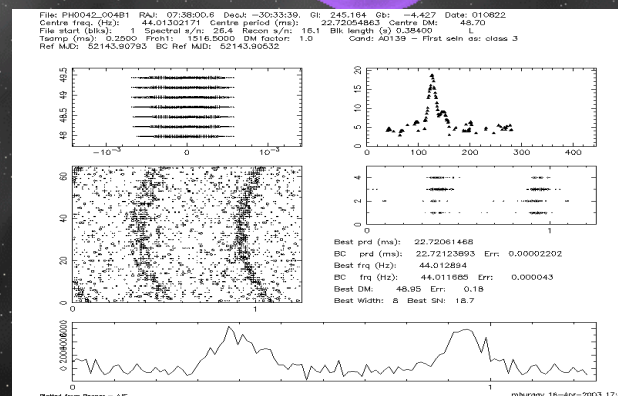


Discovery of "A"

PSR J0737-3039 discovered in April 2003 in an PKSMB extension: the Parkes High-Latitude Pulsar Survey (Burgay et al., Nature, 2003)

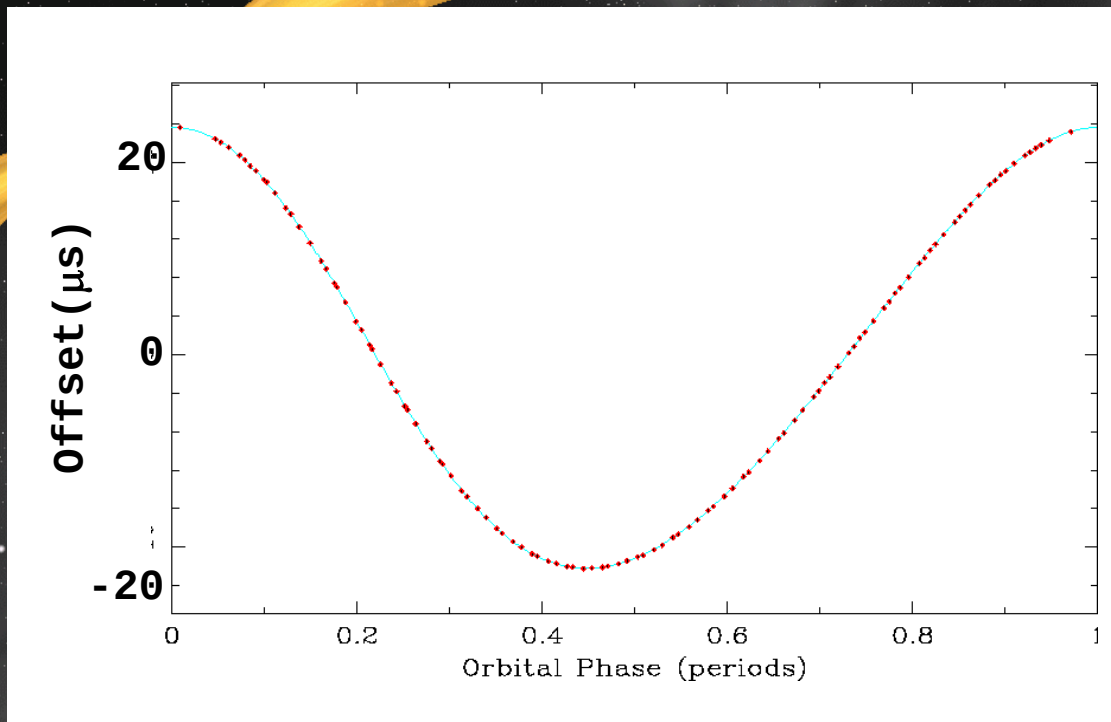


J0737-3039



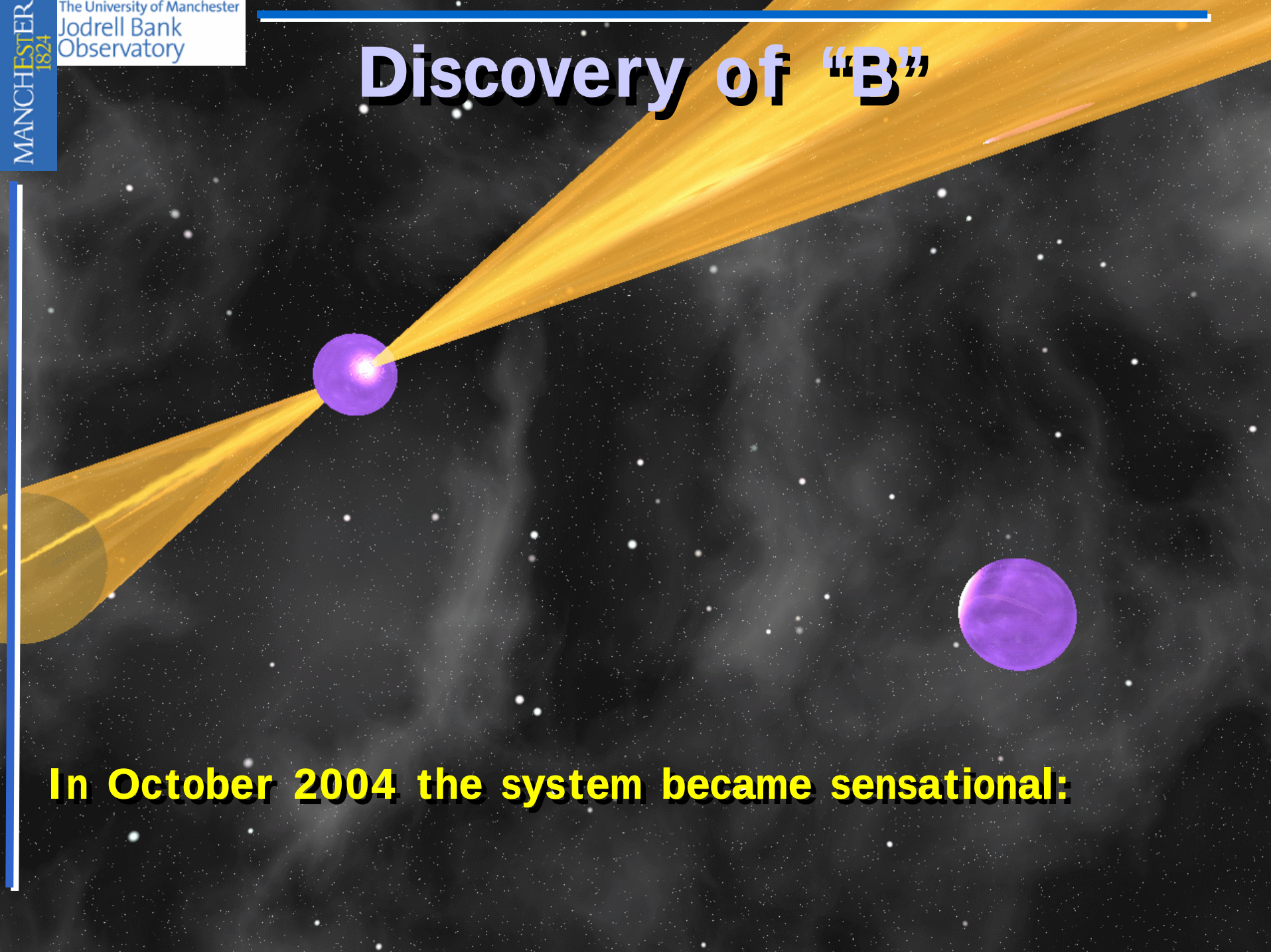
Discovery of “A”

- Observations showed that the orbit is very tight ($P_p = 2.4$ hrs) and eccentric ($e = 0.088$) with orbital velocities of ~ 300 km/s!



- Orbital parameters suggested that the companion to 22-ms pulsar is probably another neutron star

Discovery of "B"



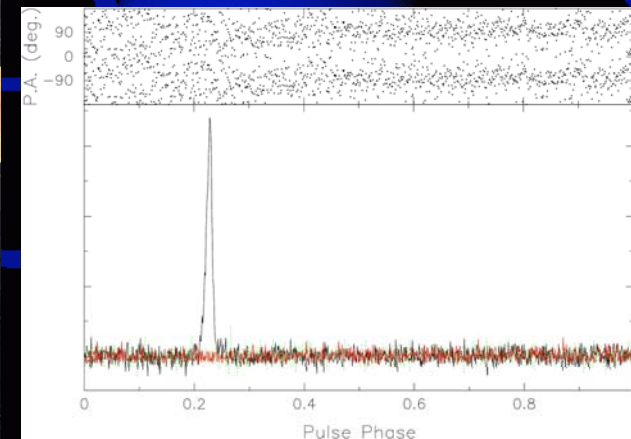
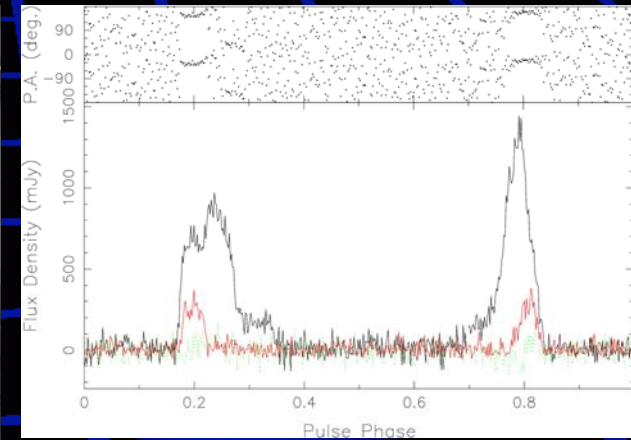
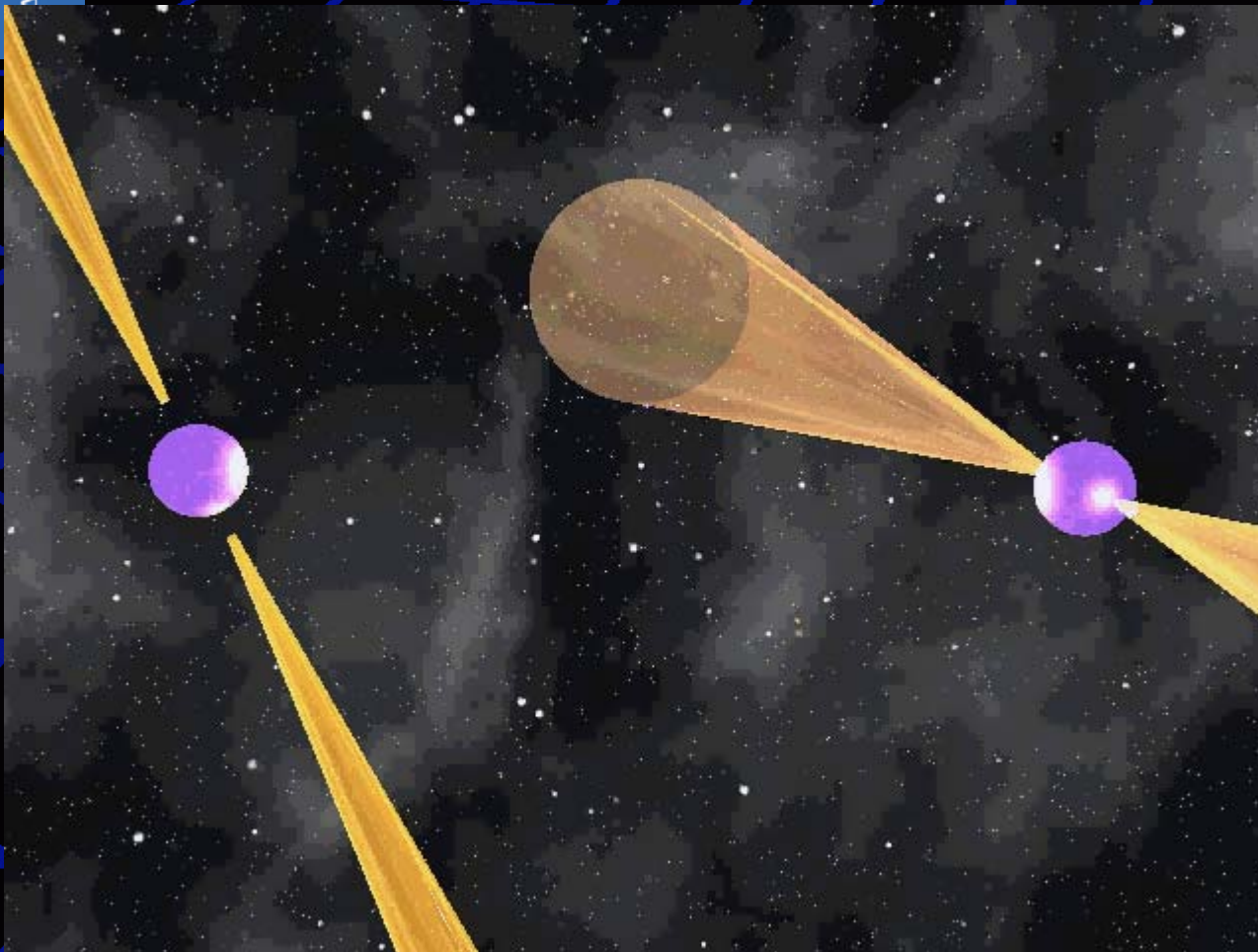
In October 2004 the system became sensational:

Discovery of “B”

In October 2004 the system became sensational:

A “holy grail” was discovered - the first double pulsar!

A double pulsar system



Discovery of an additional 2.77-sec periodicity!
(Lyne et al., Science, 2004)



Basic parameters

A:

B:

P

22.7 ms

2.77 s

$\dot{P}$

1.7×10^{-18}

0.82×10^{-15}

Char.age

200 Myr

50 Myr

B_{surf}

$6 \times 10^9 \text{ G}$

$1.6 \times 10^{12} \text{ G}$

R_{LC}

1,080 km

$1.32 \times 10^5 \text{ km}$

B_{LC}

$5 \times 10^3 \text{ G}$

0.7 G

dE/dt

$6 \times 10^{33} \text{ erg s}^{-1}$

$1.6 \times 10^{30} \text{ erg s}^{-1}$

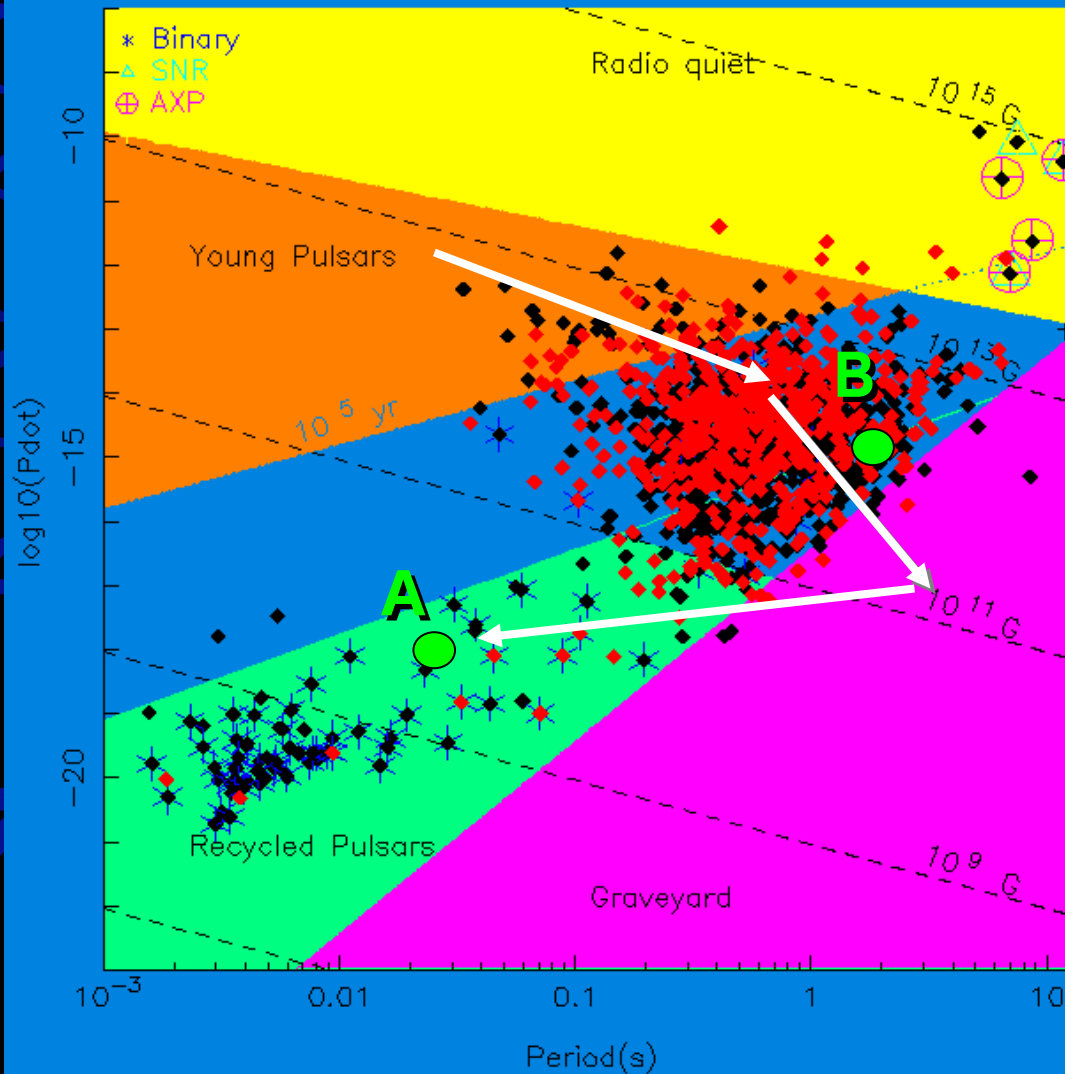
Mean V_{orb}

301 km s⁻¹

323 km s⁻¹

Evolution of the Double Pulsar

“P-Pdot diagram:”



A is old & recycled

B is young

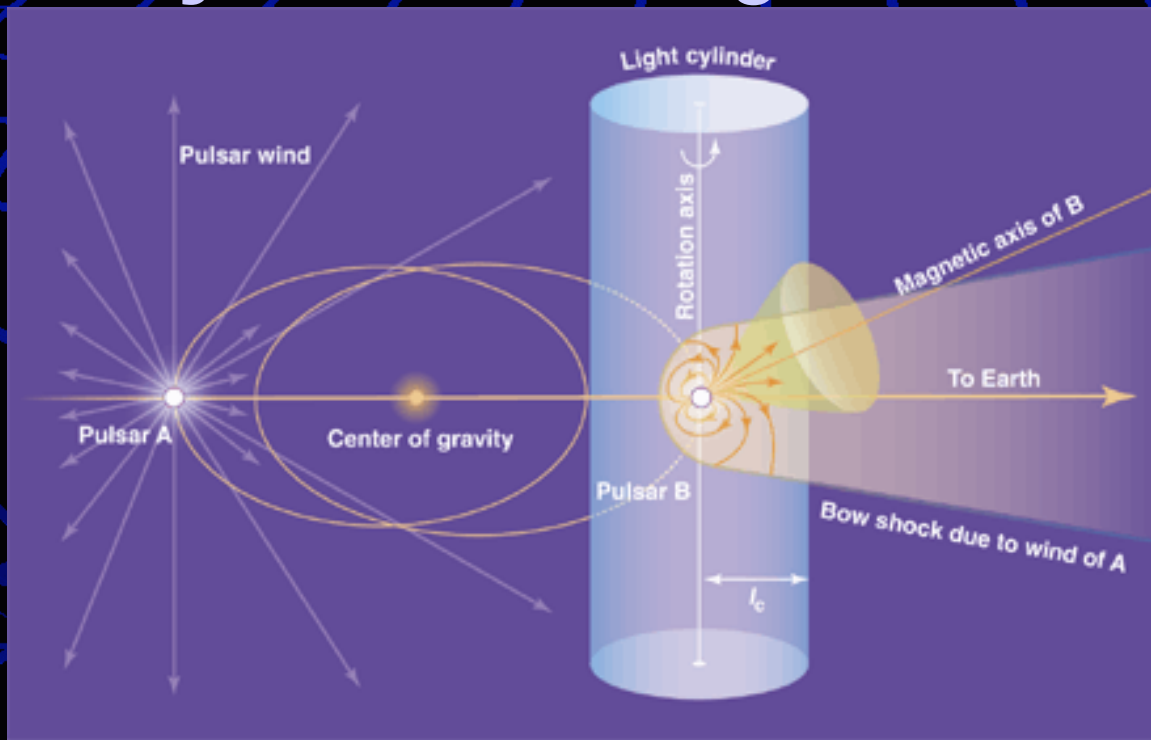
Their life in short:



Basic parameters

A:**B:****P****22.7 ms****2.77 s** **$\dot{P}$** **1.7×10^{-18}** **0.82×10^{-15}** **Char. age****200 Myr****50 Myr** **B_{surf}** **$6 \times 10^9 \text{ G}$** **$1.6 \times 10^{12} \text{ G}$** **$R_{\text{LC}}$** **1,080 km** **$1.32 \times 10^5 \text{ km}$** **$B_{\text{LC}}$** **$5 \times 10^3 \text{ G}$** **0.7 G****dE/dt** **$6 \times 10^{33} \text{ erg s}^{-1}$** **$1.6 \times 10^{30} \text{ erg s}^{-1}$** **Mean V_{orb}** **301 km s^{-1}** **323 km s^{-1}**

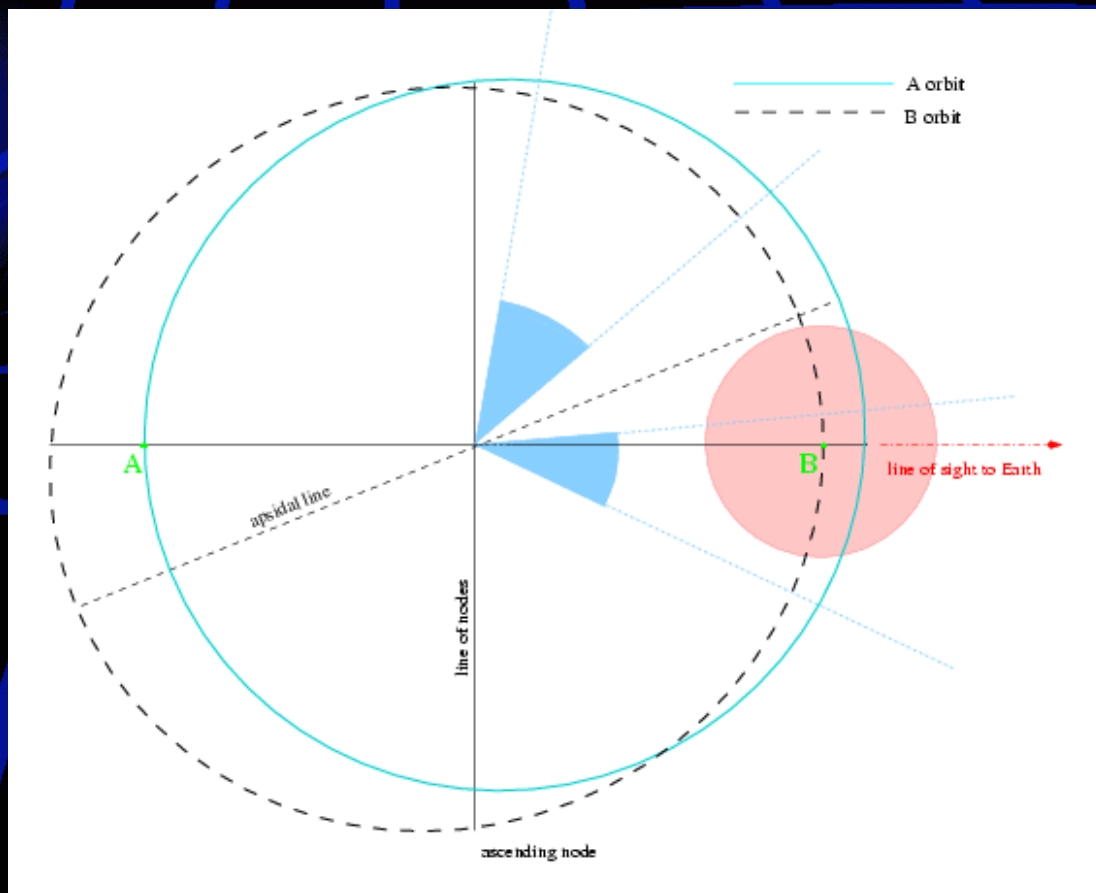
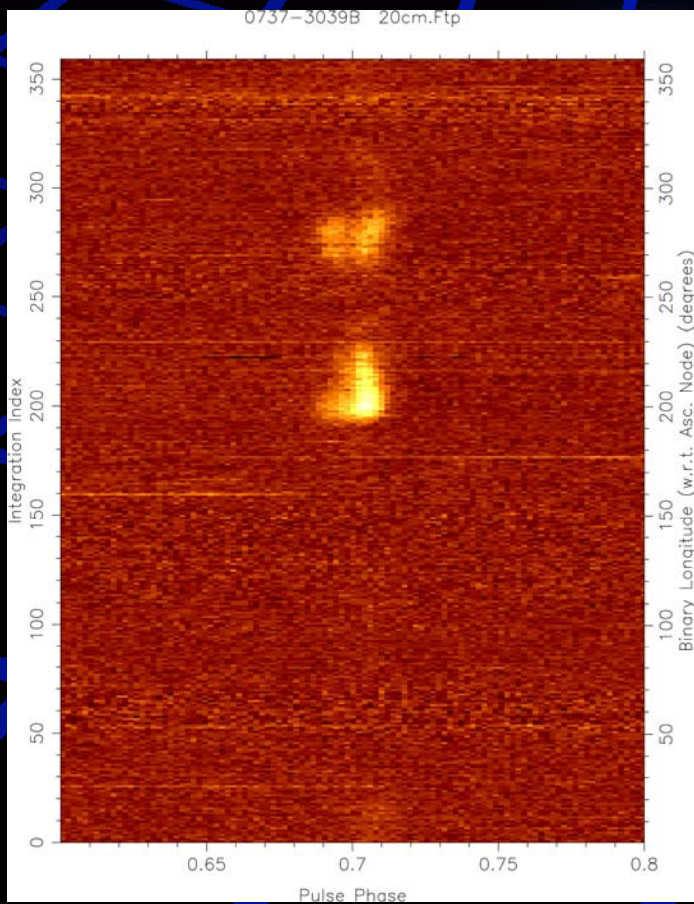
System Configuration



- Wind energy density at B light cylinder:
A: $\sim 2.1 \text{ erg cm}^{-3}$ B: $\sim 0.024 \text{ erg cm}^{-3}$
- Therefore, A wind will penetrate B magnetosphere.
- **Approximate pressure balance with B's magnetic field at $r \sim 0.5 R_{LC}$. Will vary with spin and orbital phase.**

Orbital modulation of “B” emission

Two bright intervals near inferior conjunction:



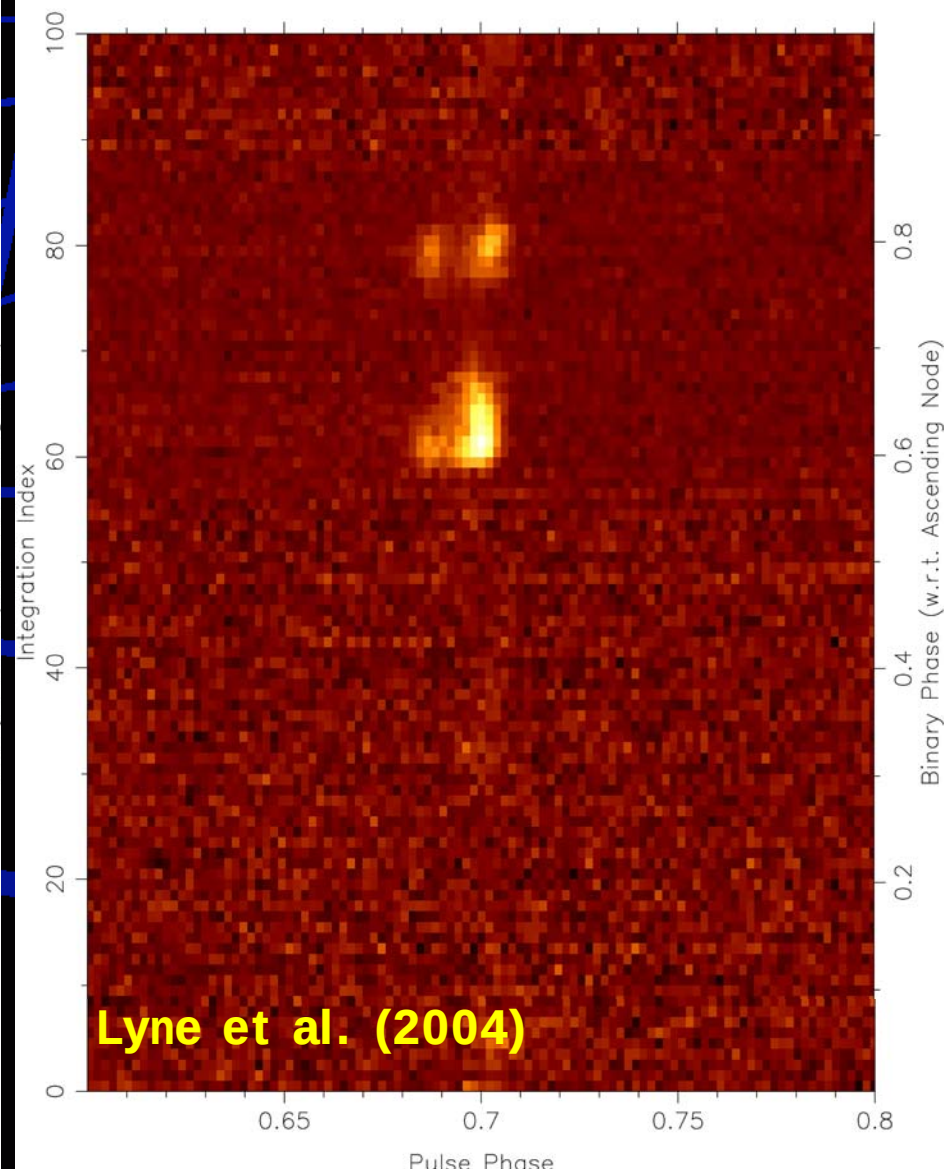
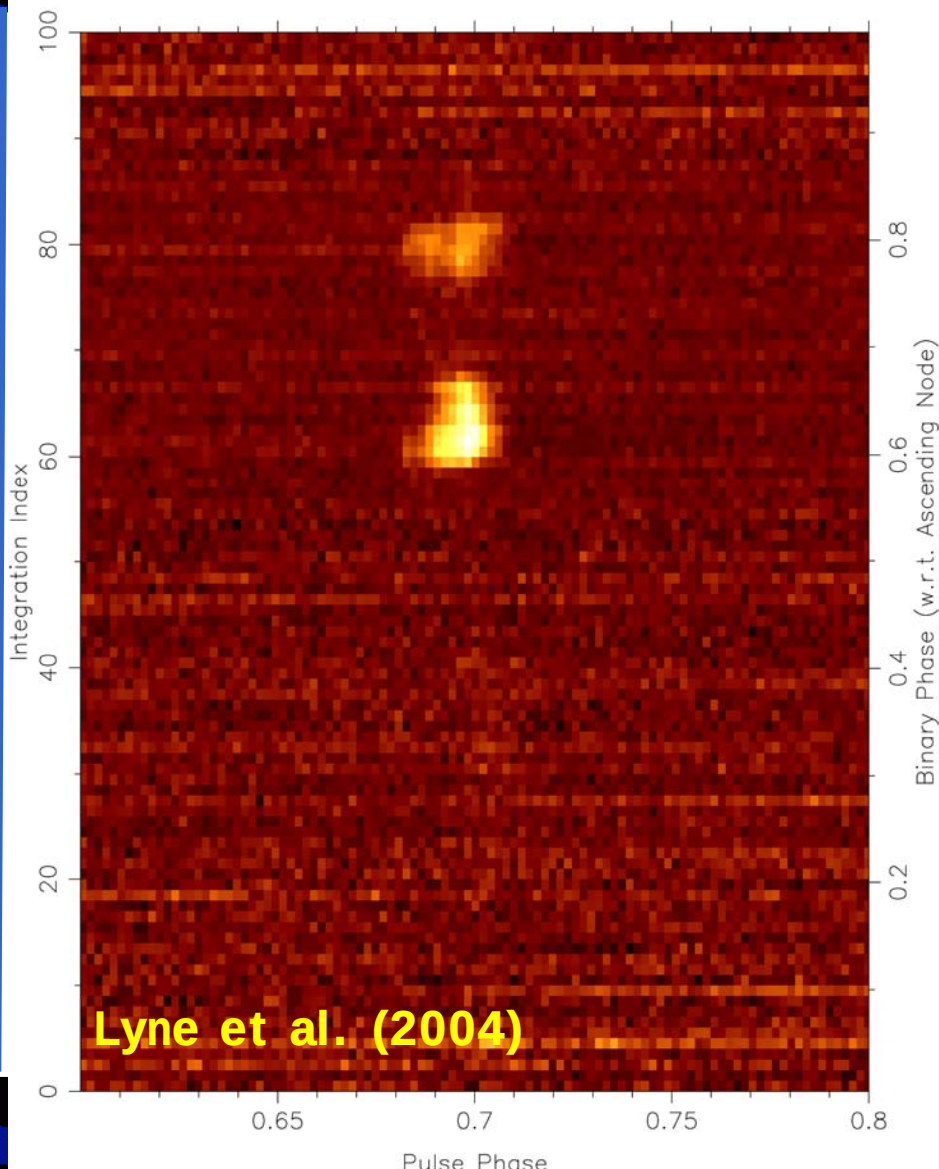
Orbital modulation of “B” emission

50cm (680 MHz)

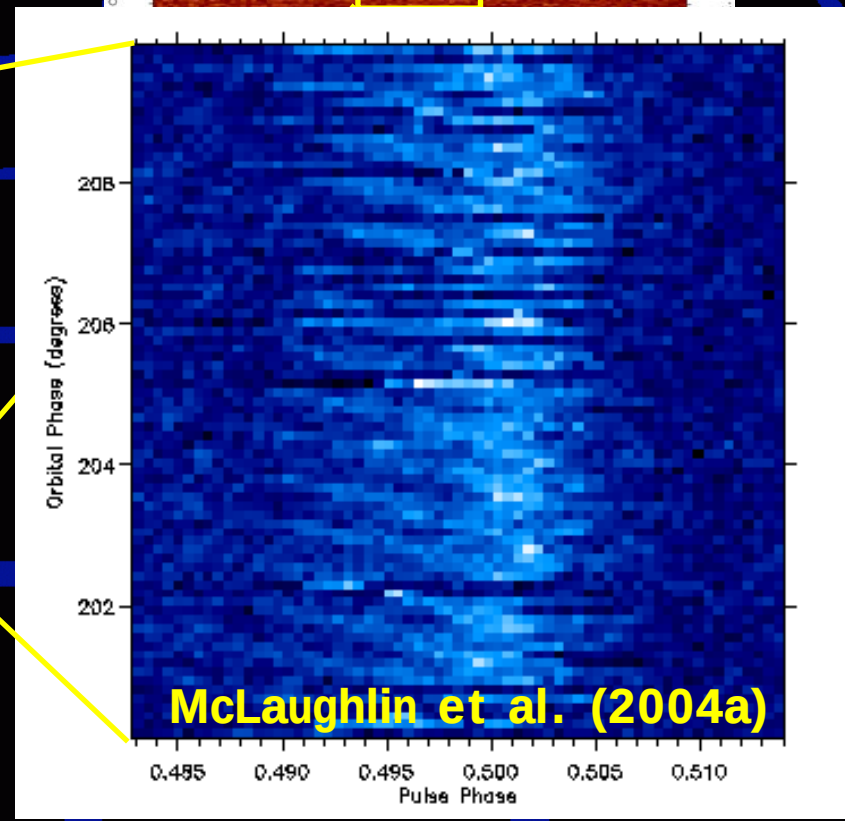
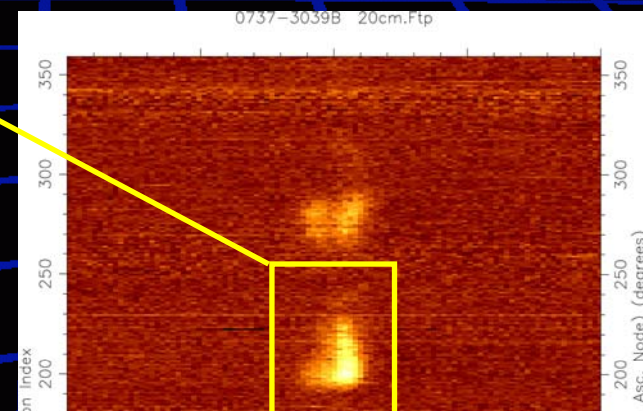
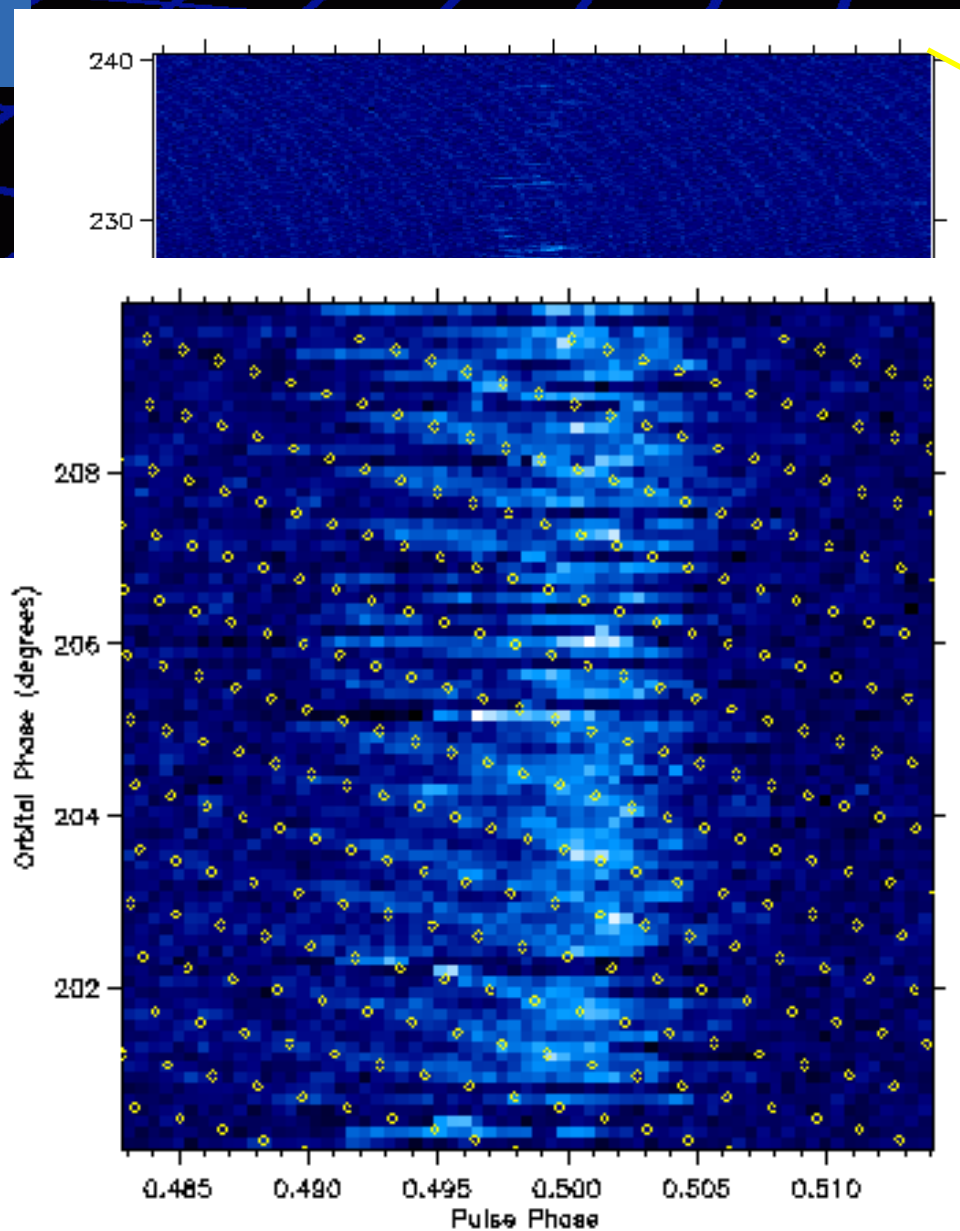
10cm (3 GHz)

0737-3039B 50cm.arb

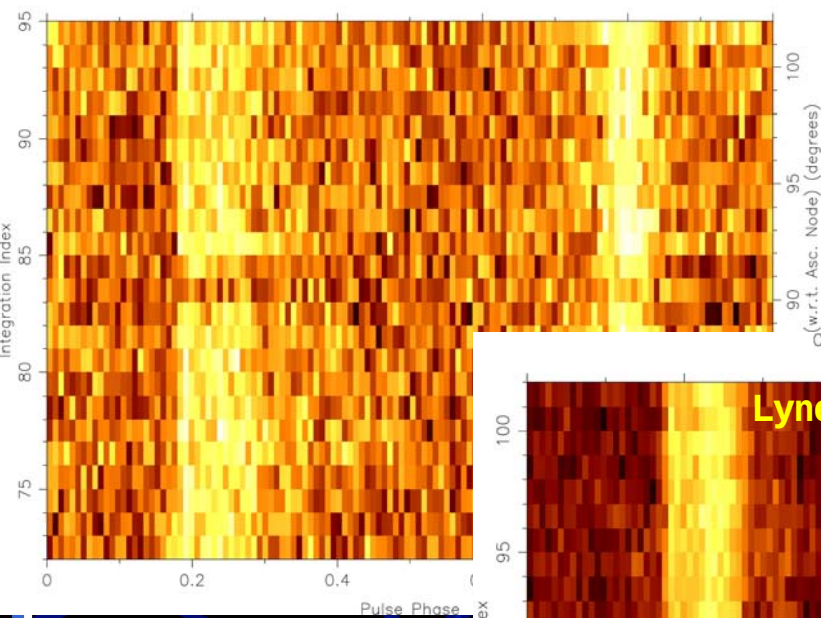
0737-3039B 10cm.arb



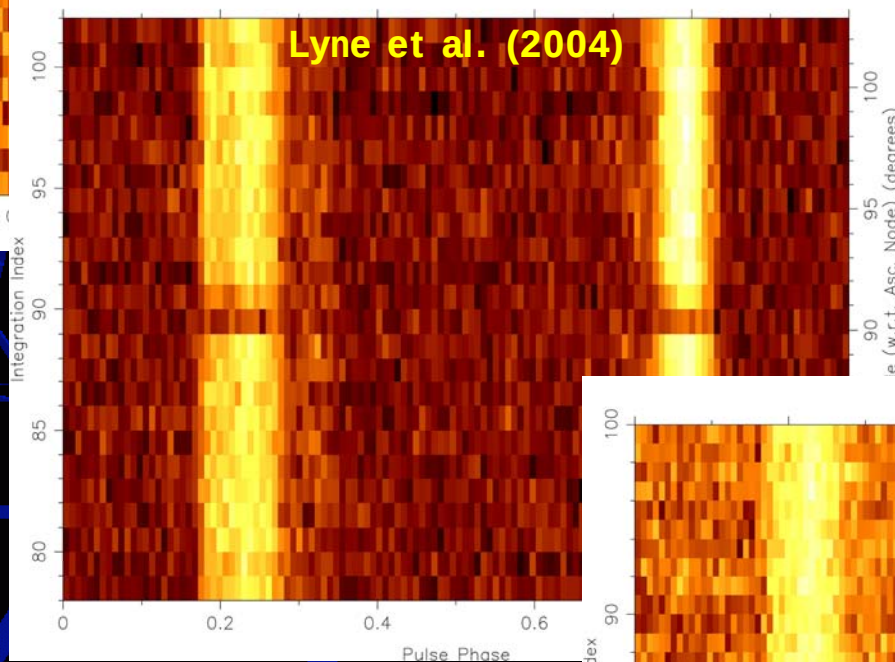
Direct modulation of B's emission by A



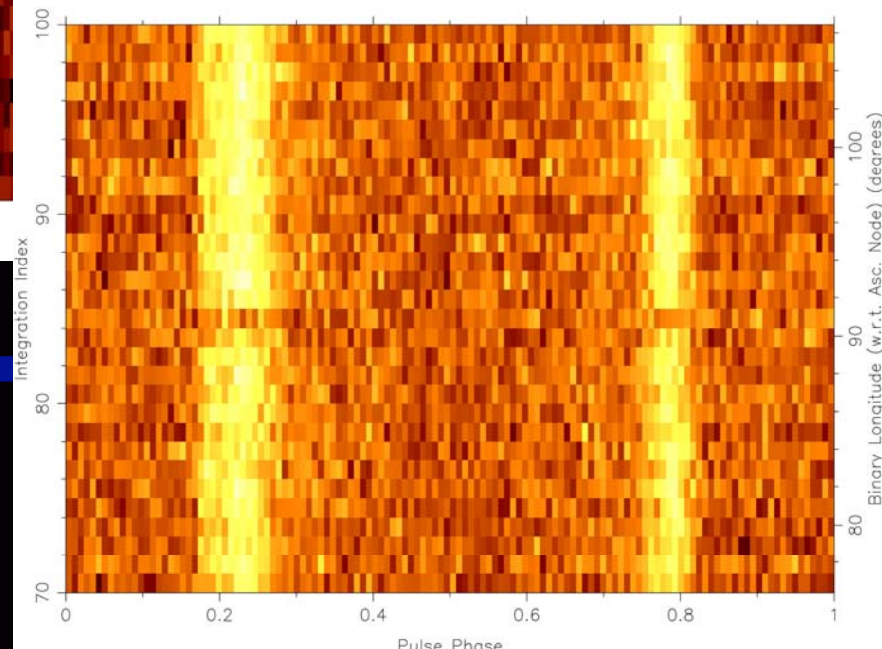
Eclipses of A



0737-3039A 20cm.Ftp



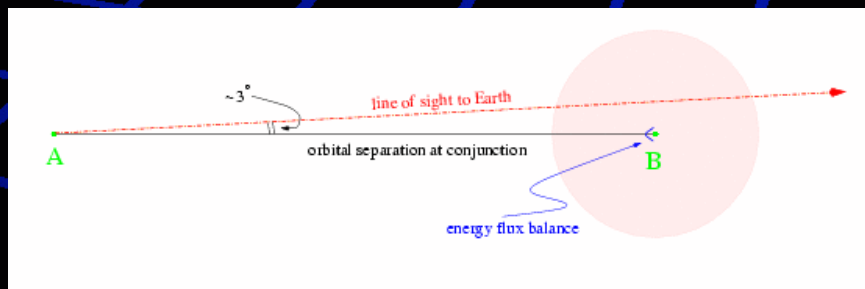
0737-3039A 50cm.Ftp



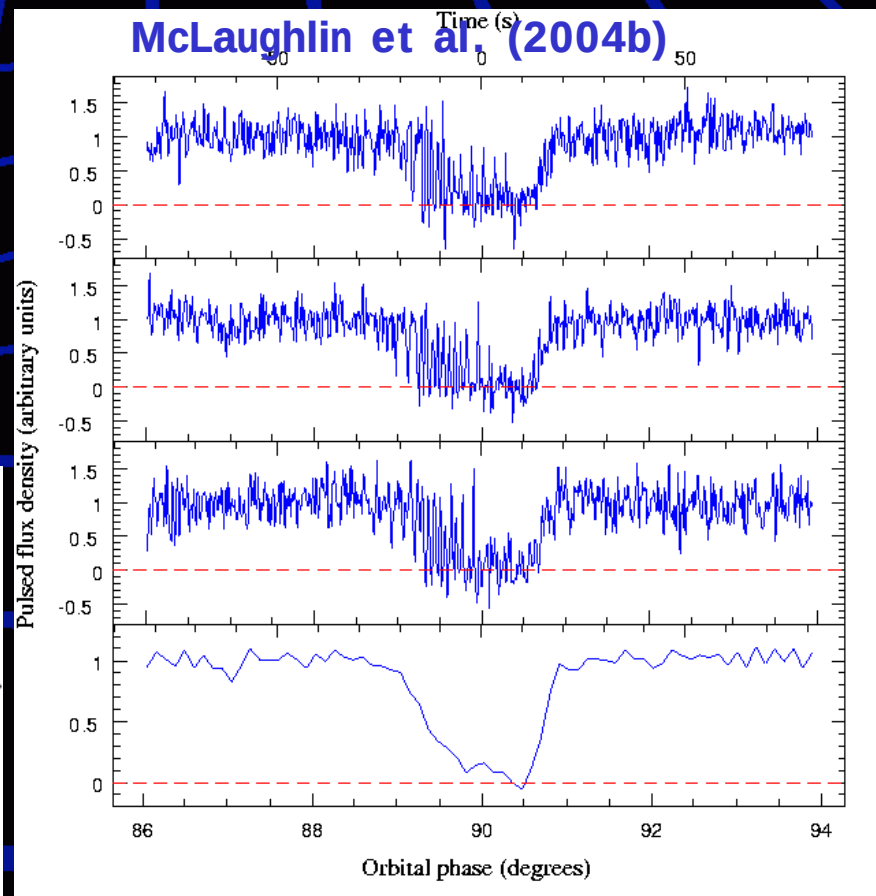
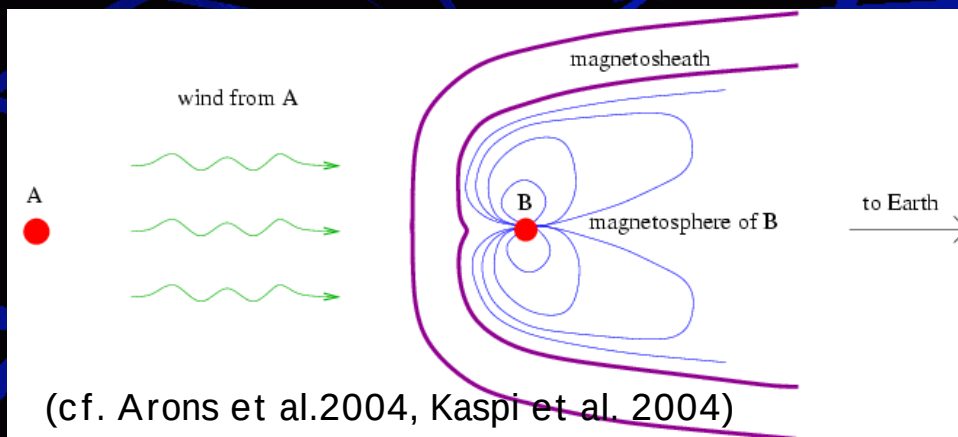
10cm

- At superior conjunction **20cm**
- Lasting for ~27 sec
- Deepest just AFTER superior conjunction **50cm**

Eclipses of A



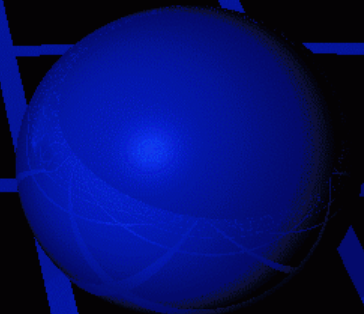
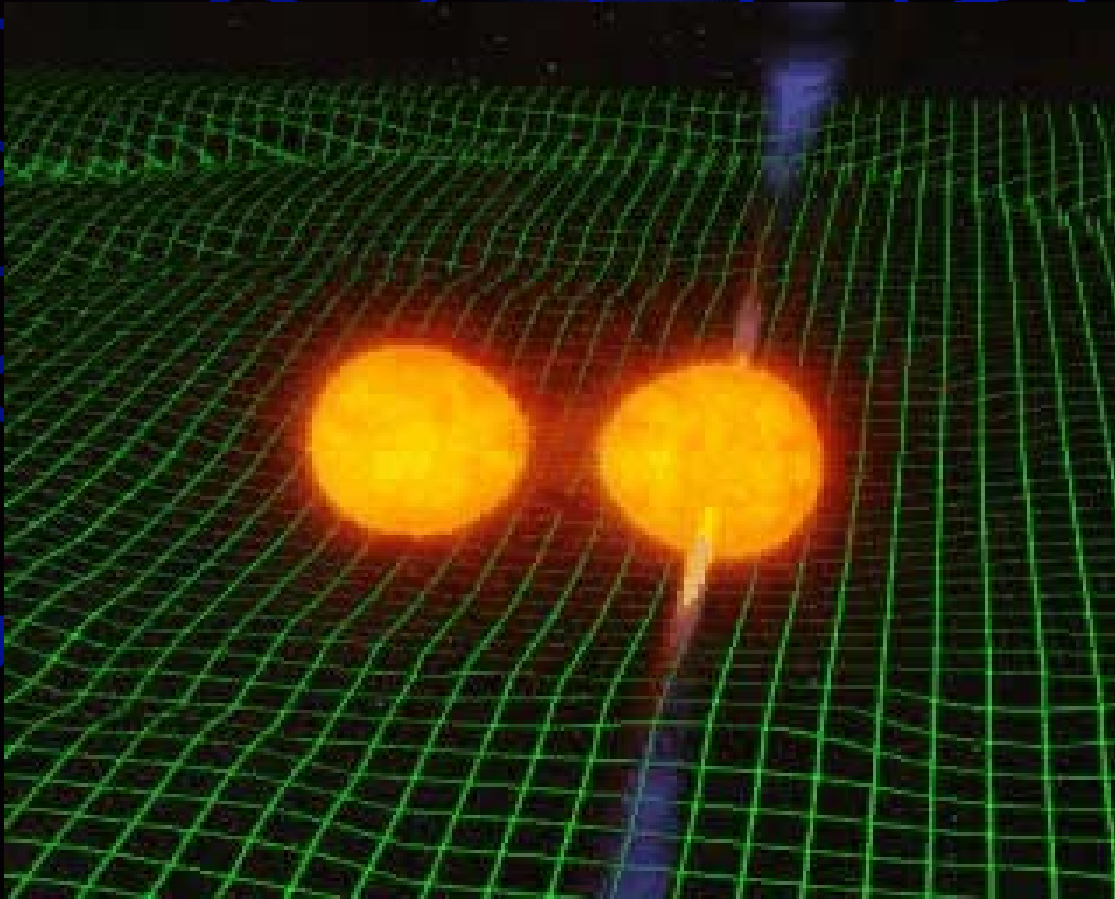
**At 88° inclination, LOS to A passes
30,000 km from B**



We can see the rotation of B!

Boost for gravitational wave hunters

- Neutronstars merge after only 85 Myr due to gravitational wave emission!



Since system...

...is accelerated

...merges “soon”

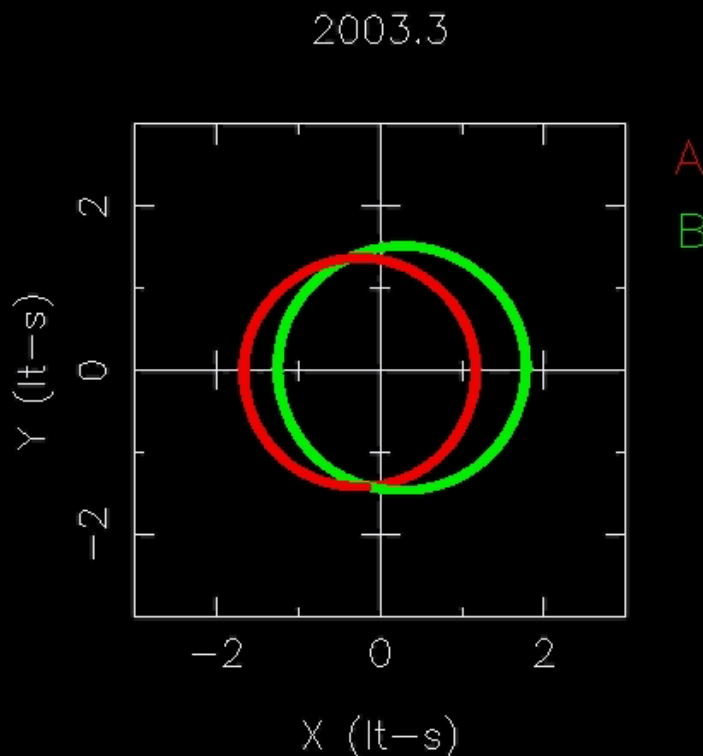
...is close

...not very luminous

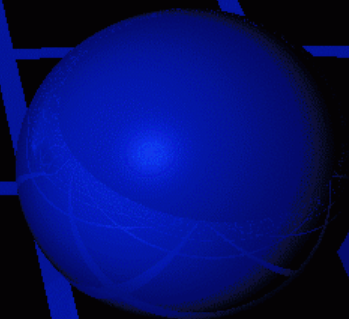
Most relativistic system ever!

Huge relativistic precession of the orbit:
periastron advance of **17 deg/yr!**

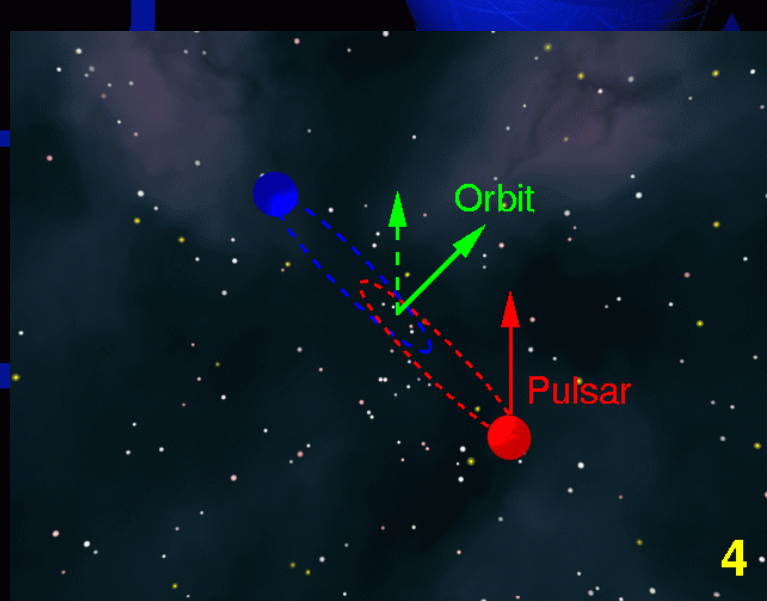
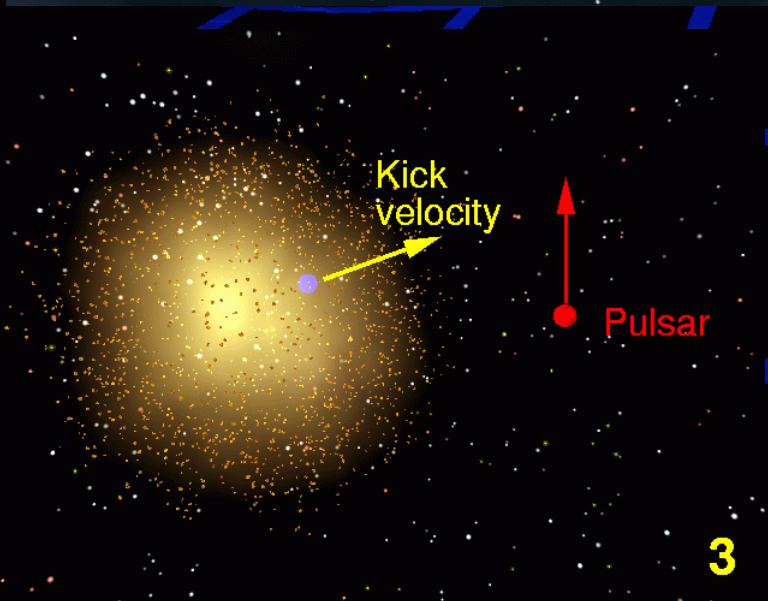
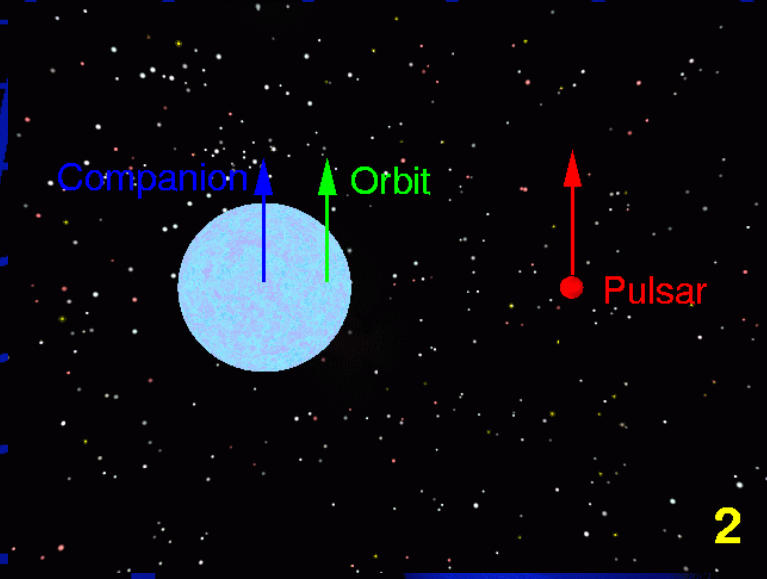
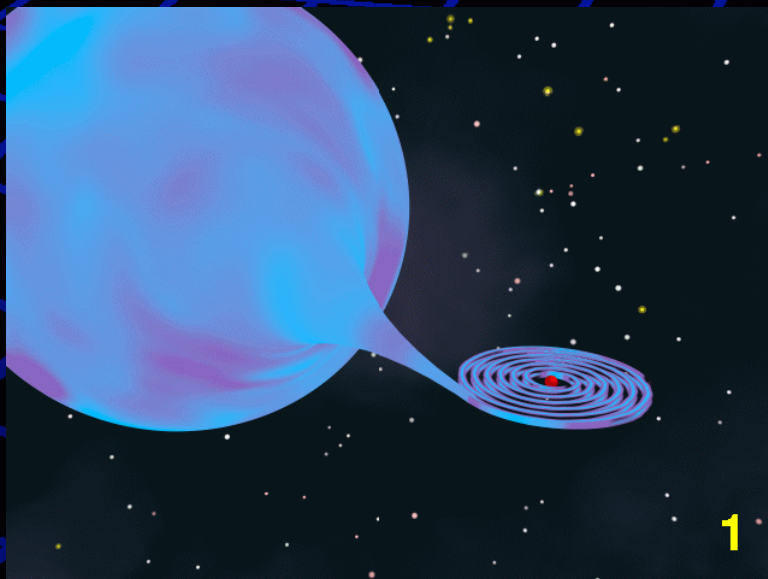
Remember B1913+16:
 $\dot{\omega} = 4.23 \text{ deg/yr}$



- **Also, orbital decay and huge rel.spin-orbit coupling!**

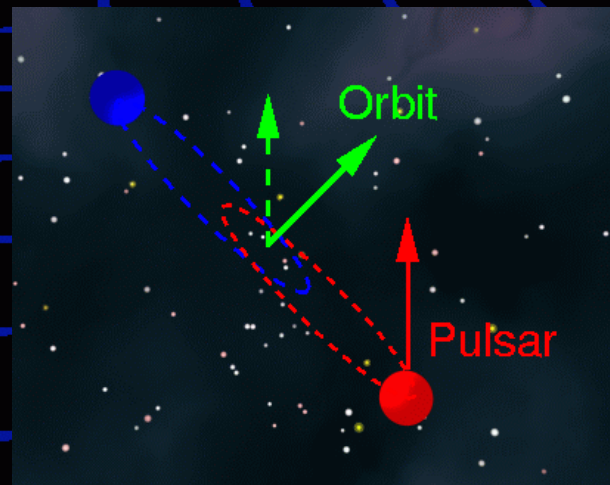


Spin-Orbit Coupling due to misaligned spins



Geodetic Precession

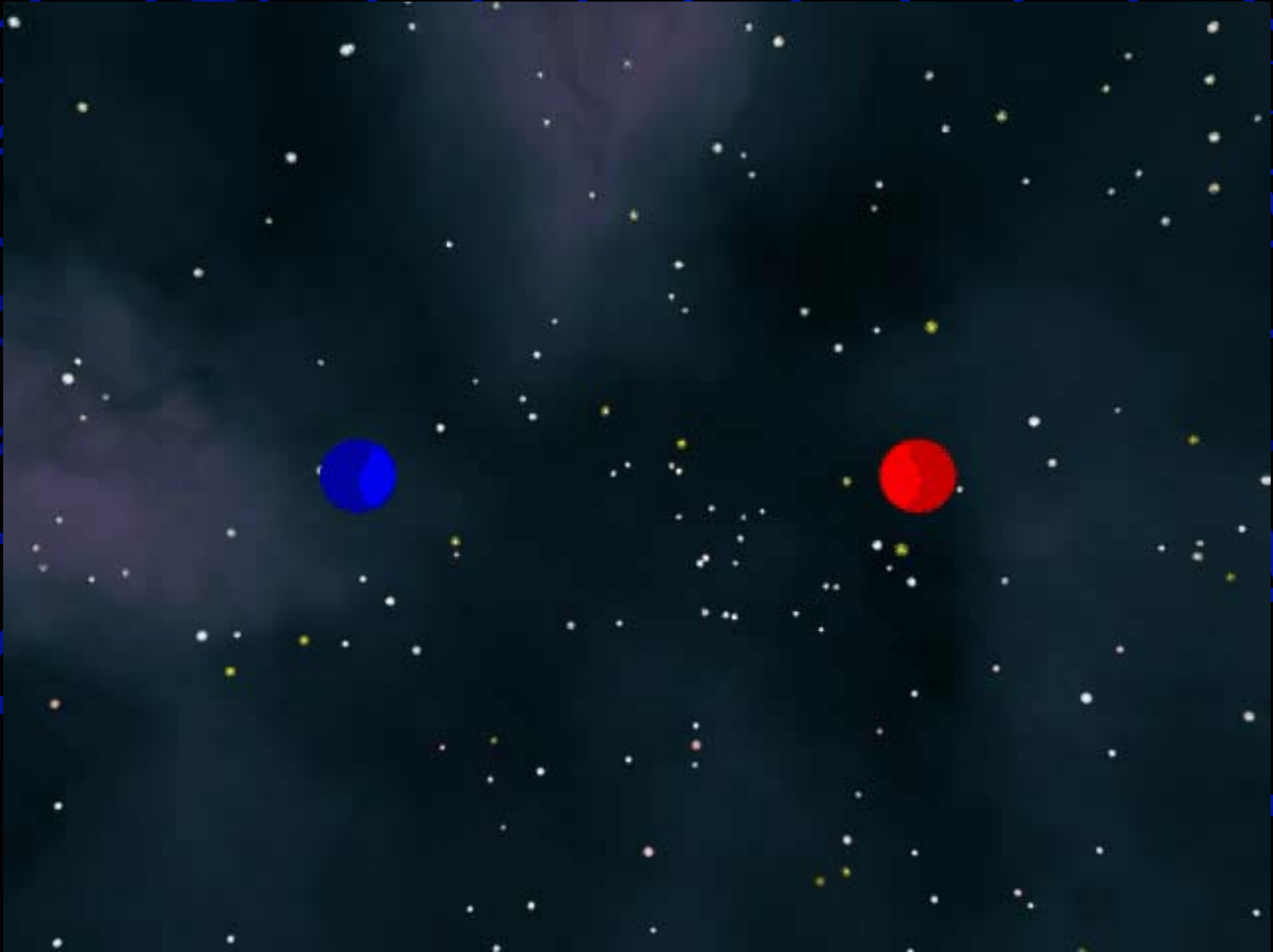
- Relativistic Spin-Orbit Coupling
- First prediction for binary pulsar by Damour & Ruffini (1974)
- Precession rate expected in GR:
(e.g. Barker & O'Connell 1975, Börner et al. 1975)



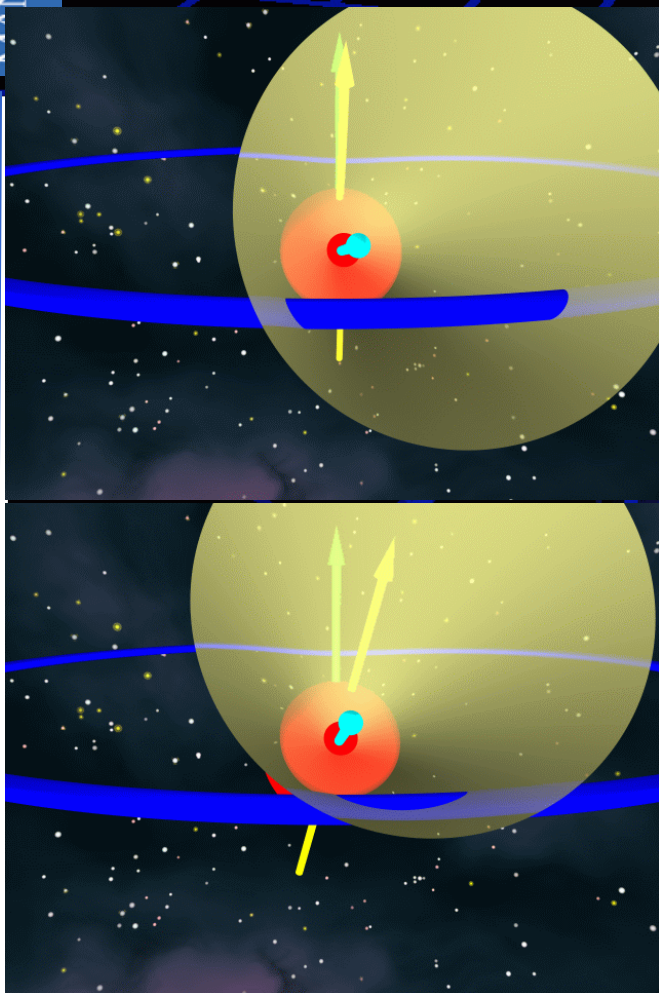
$$\Omega^p = \left(\frac{2\pi}{P_b} \right)^{5/3} T_{\odot}^{2/3} \frac{m_c (4m_p + 3m_c)}{2(m_p + m_c)^{4/3}} \frac{1}{1 - e^2}, \quad T_{\odot} = GM_{\odot} c^{-3}$$

What effects do we expect to observe?

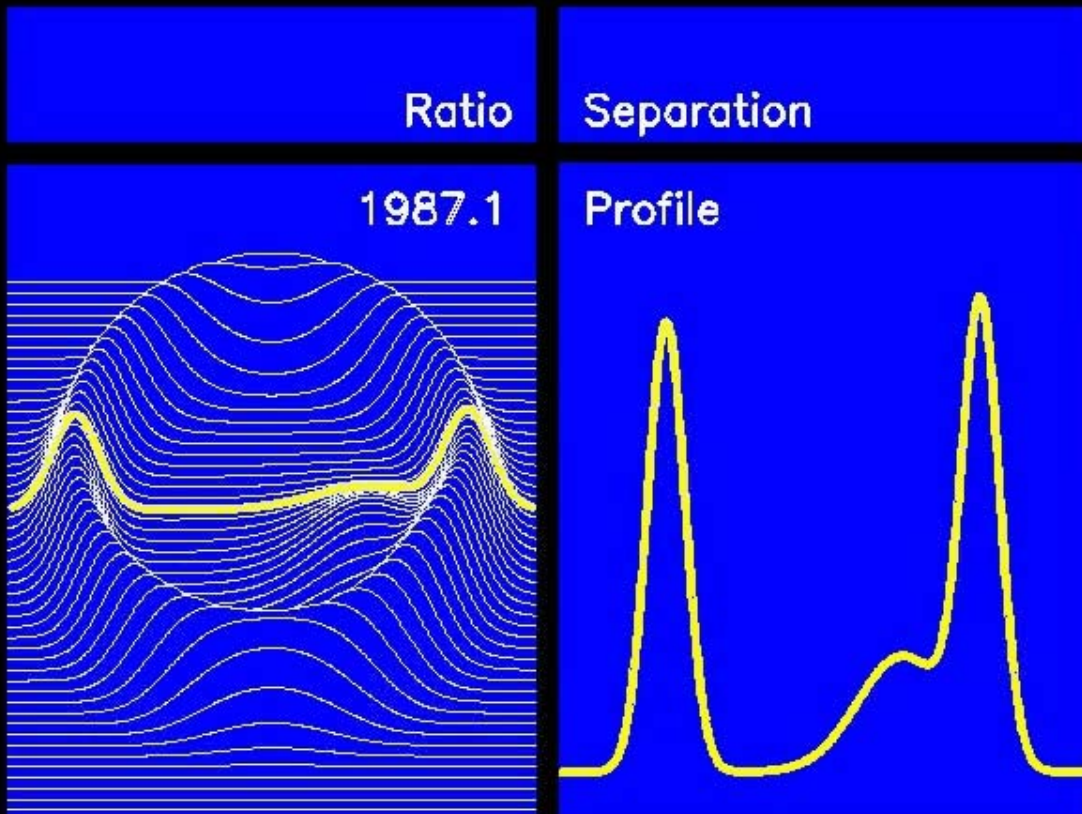
Effects of Geodetic Precession



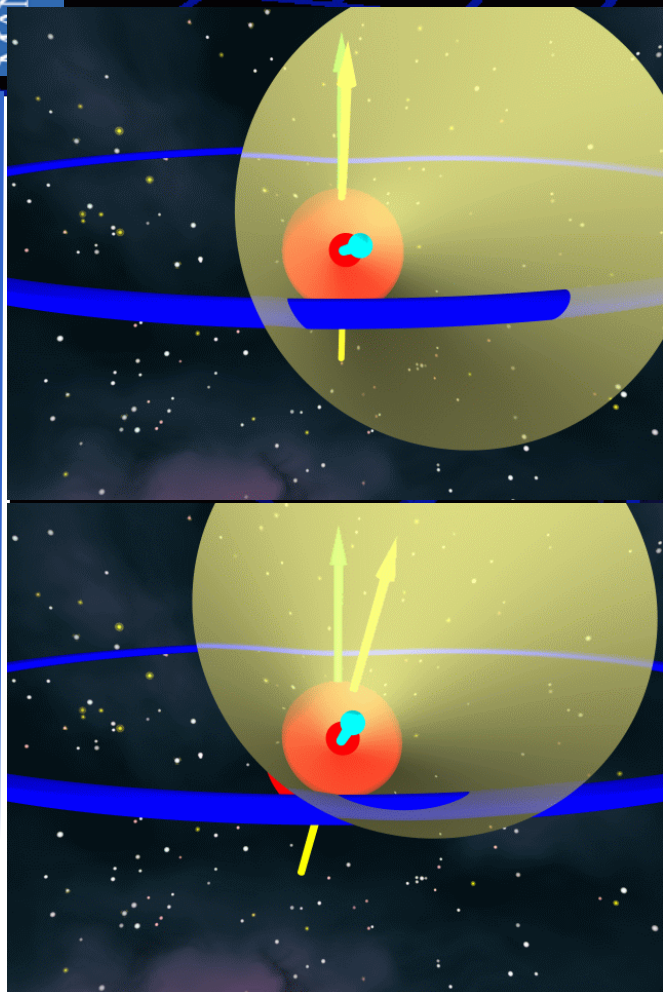
Effects of Geodetic Precession



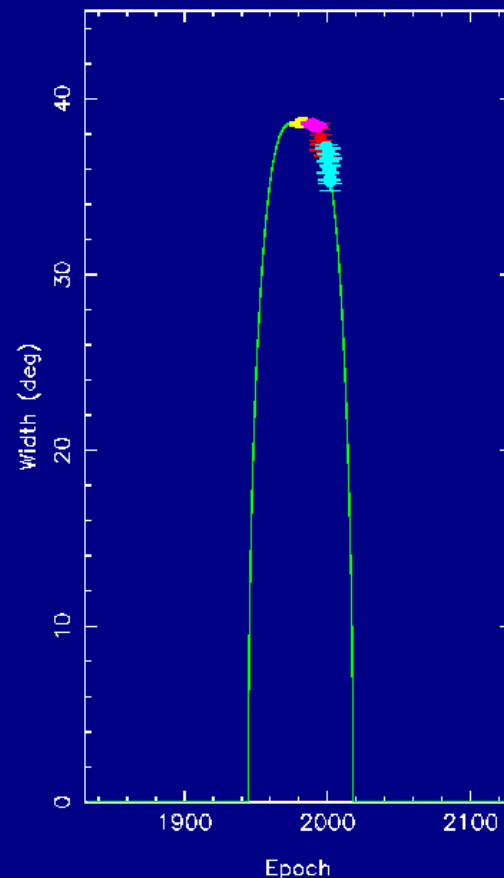
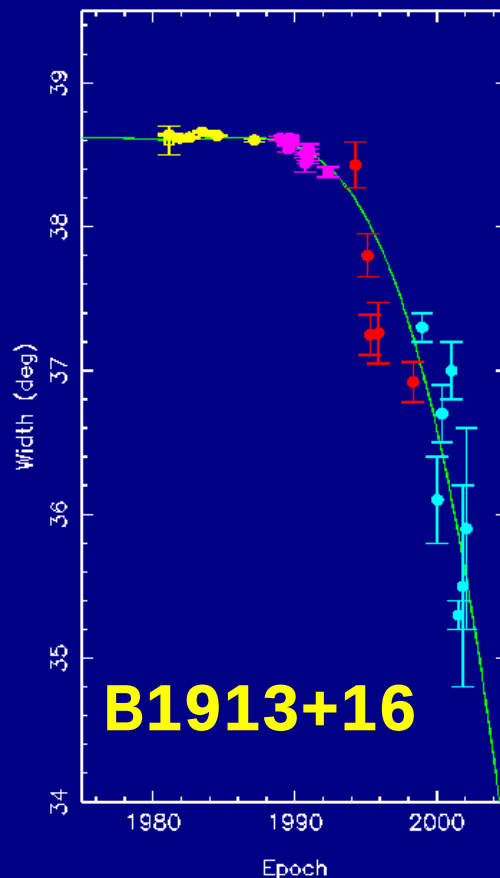
- Pulse shape changes!



Effects of Geodetic Precession



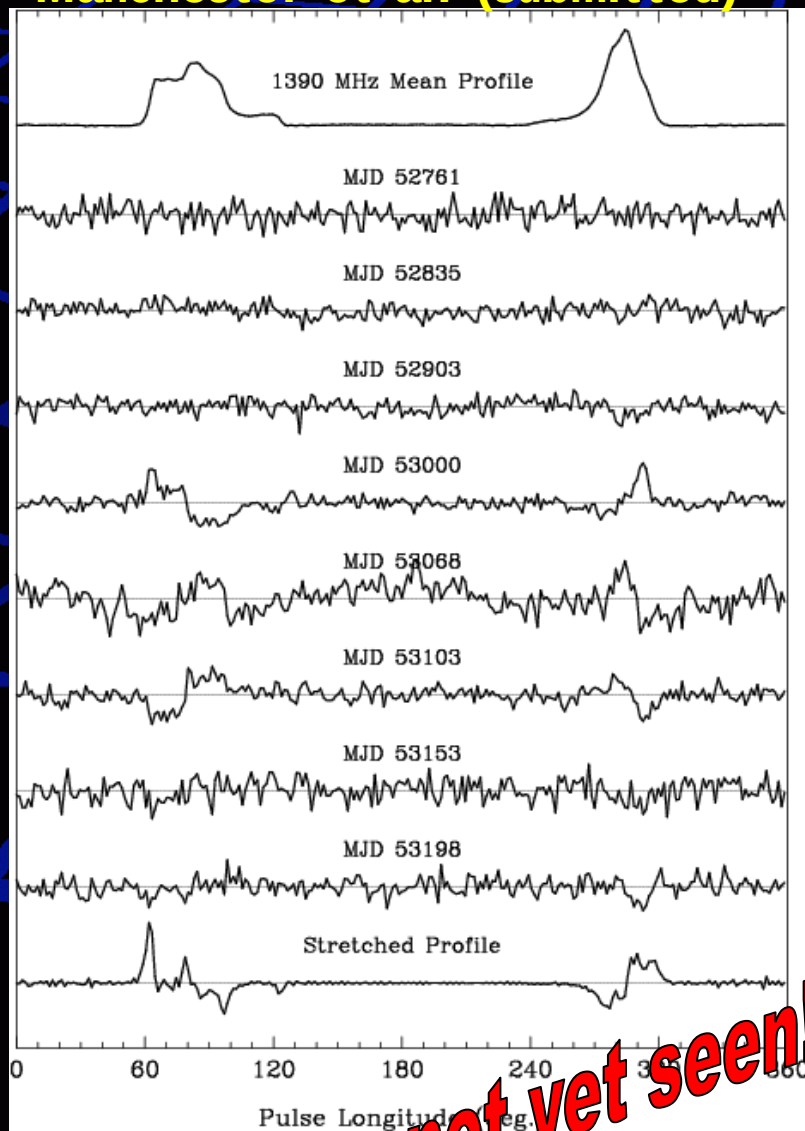
Kramer (1998, 2002, 2003; Weisberg & Taylor 2002)



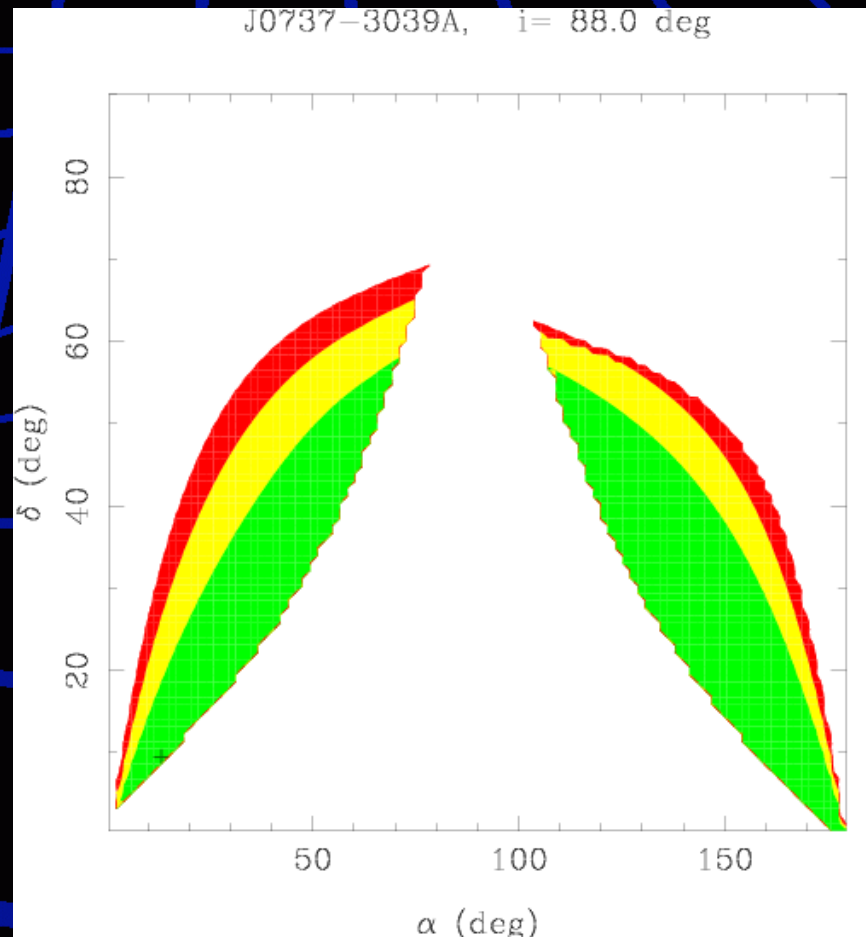
- **Pulse shape changes** (seen in B1913+16, B1534+12, J1141-6545!)
- **B1913+16** (Period 300 yr) will disappear ~2025! (Kramer 1998)
- **Total precession period of J0737-3039 only 75 years!!**

Geodetic Precession in J0737-3039

Manchester et al. (submitted)



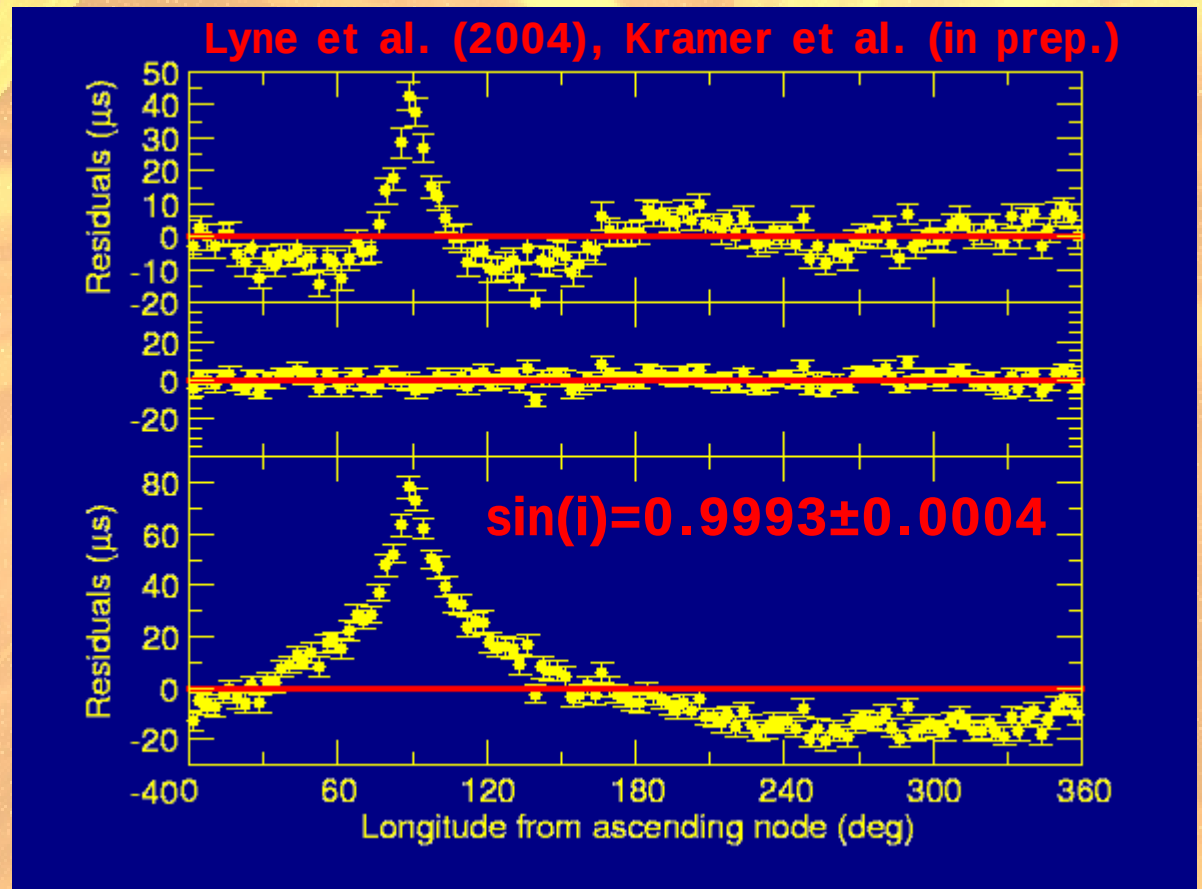
not yet seen!



- Geometry still unconstrained
- Jenet & Ransom (2004) model ruled out

Detection of Shapiro delay

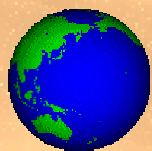
Pulses of A are delayed when propagating through curved space-time near B:



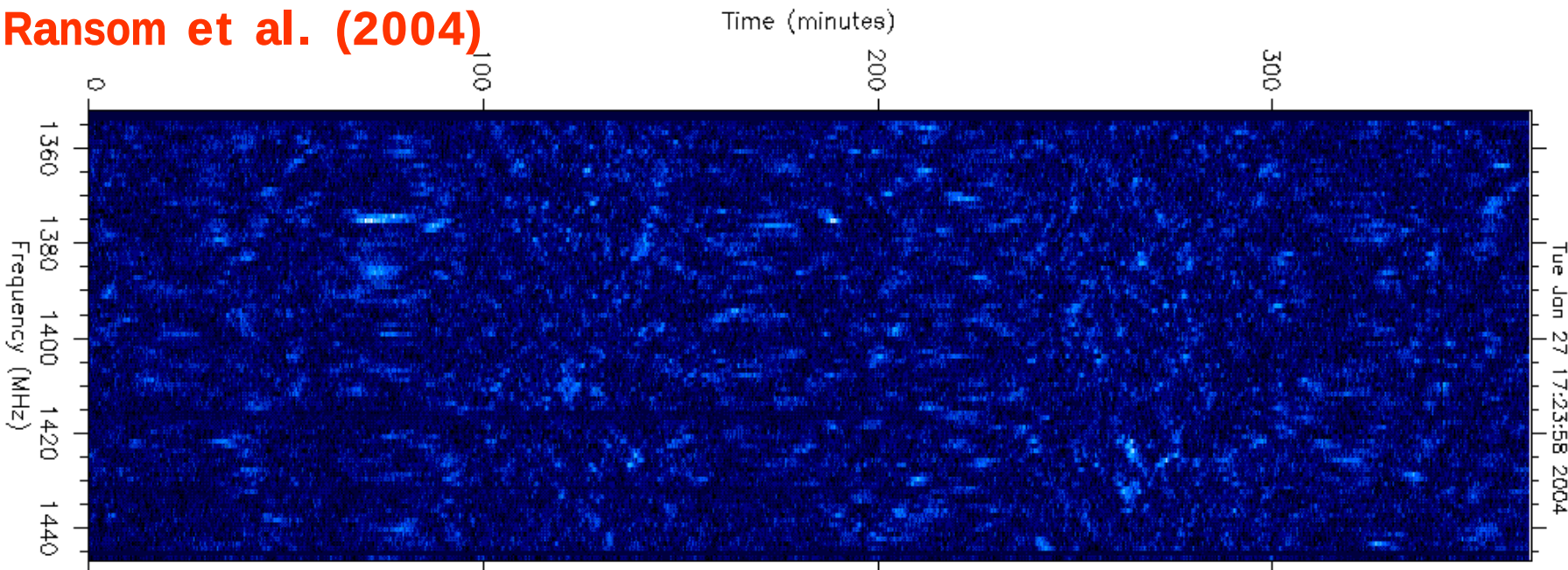
Compare to scintillation measurements...

Scintillation measurements

Intensity variation due to ISM depending on relative vel.:



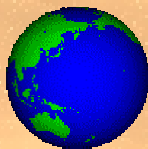
Ransom et al. (2004)



Scintillation measurements

Even better: at conjunction they see the same ISM

⇒ correlation of scintillation properties:

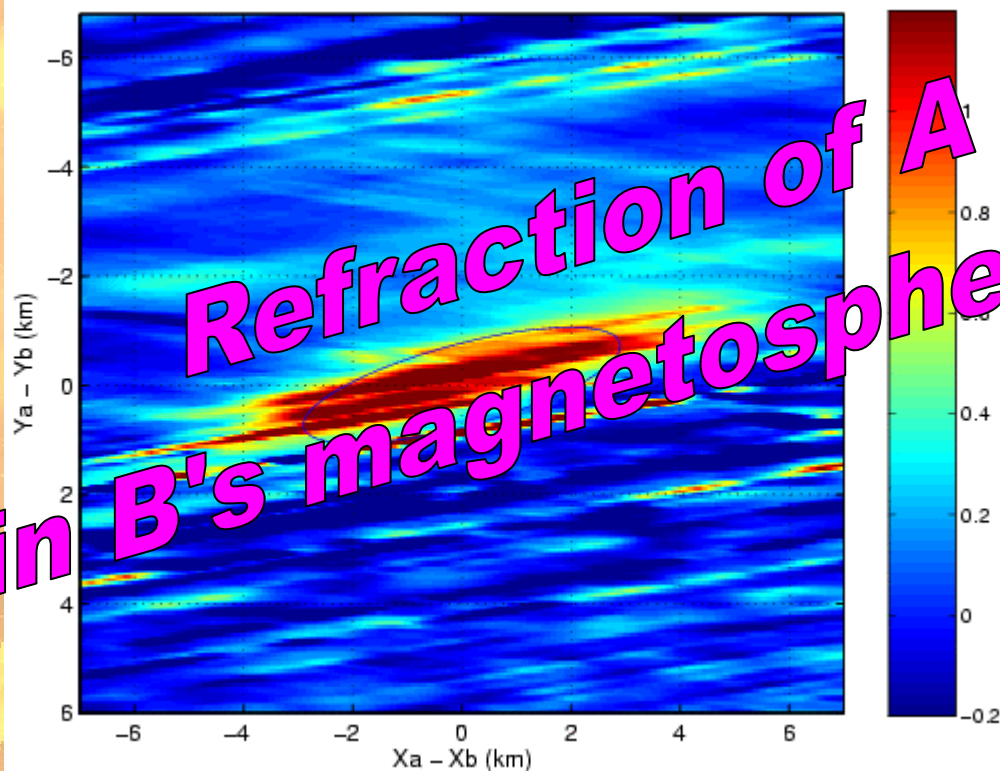


ISM

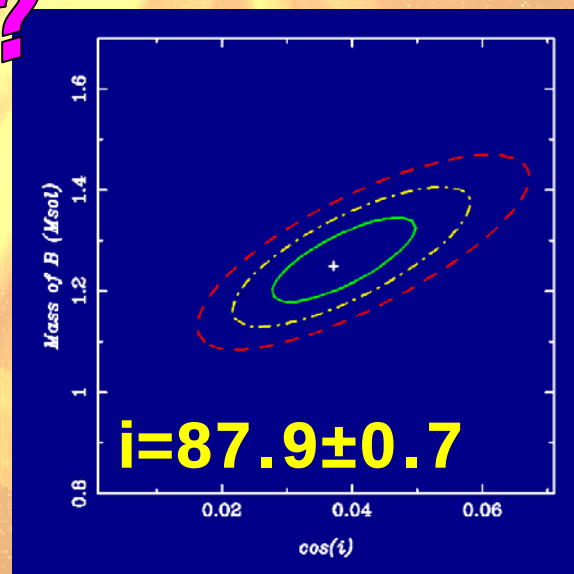


However, ISS result of $i=90.26 \pm 0.13$ inconsistent with Shapiro result:

Refraction of A
in B's magnetosphere?



Coles et al.(in press)



Kramer et al.(in prep.)

Binary pulsars as gravity labs: mass-mass plot

Elegant method to test any theory of gravity

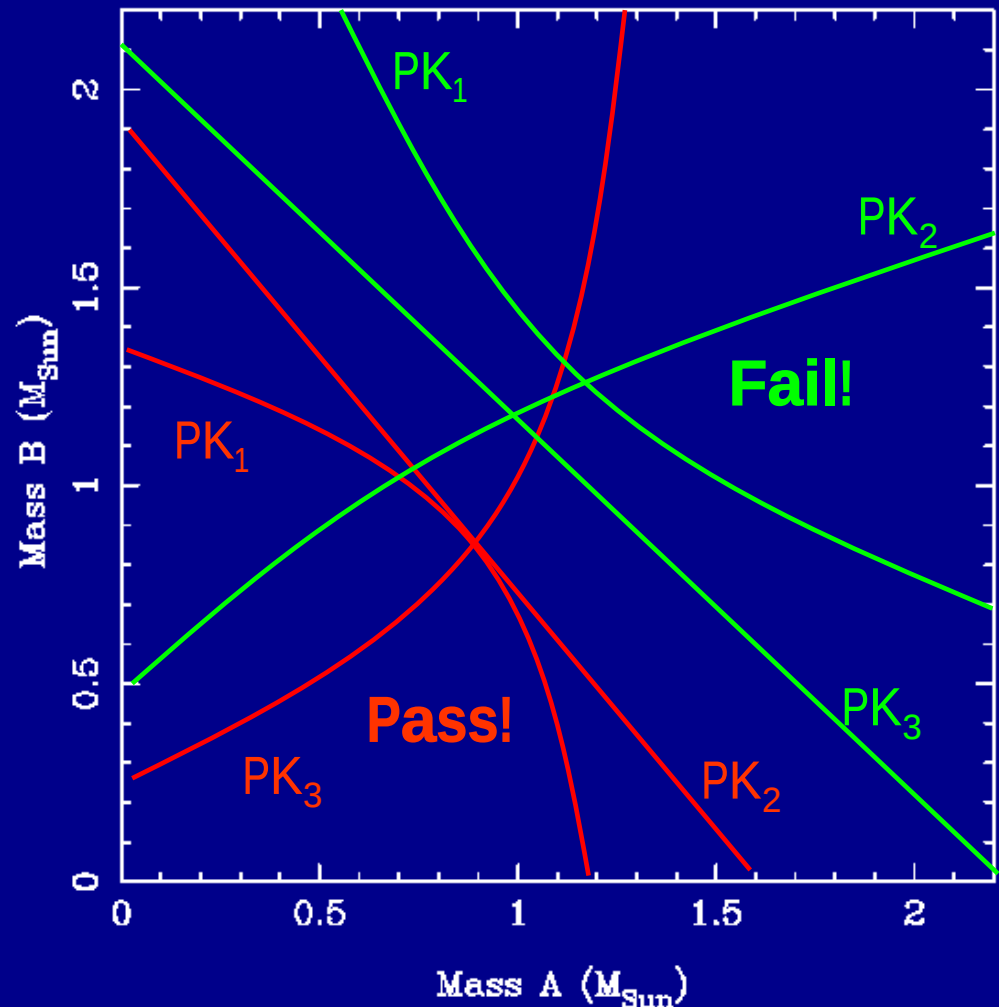
(see Damour & Deruelle 1986,
Damour & Taylor '92)

All PK parameter can
be written as function of
only observed Keplerian
and the masses of pulsar
and companion

$$PK = f(K, m_p, m_c)$$

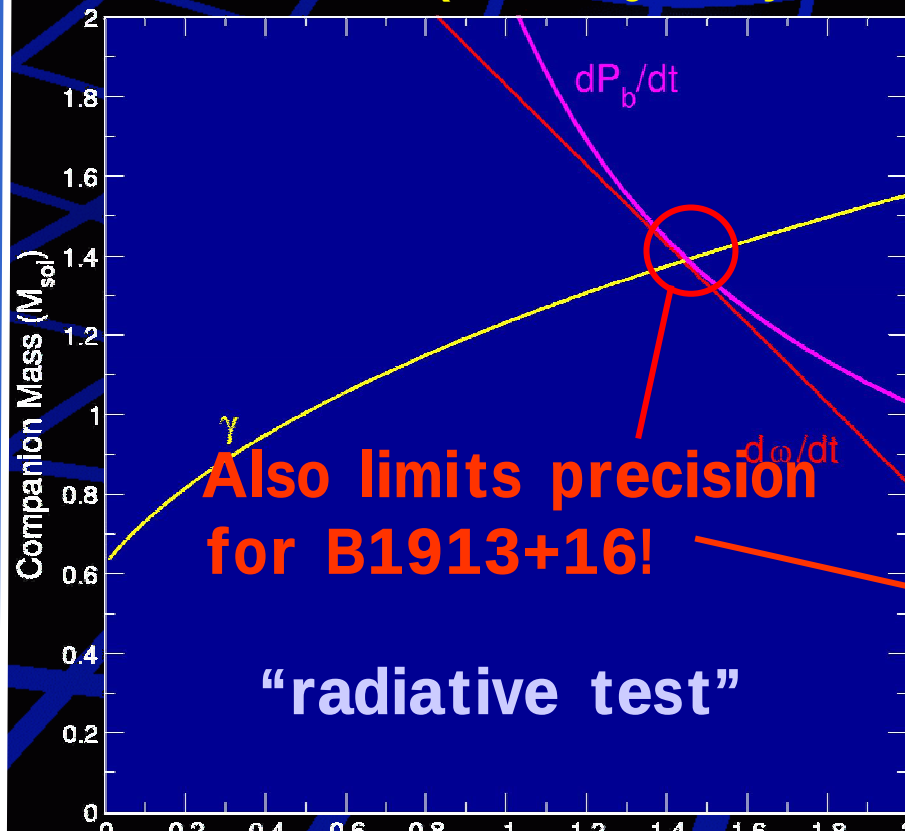
↓ f, g depend
on theory!

$$m_c = g(K, PK, m_p)$$

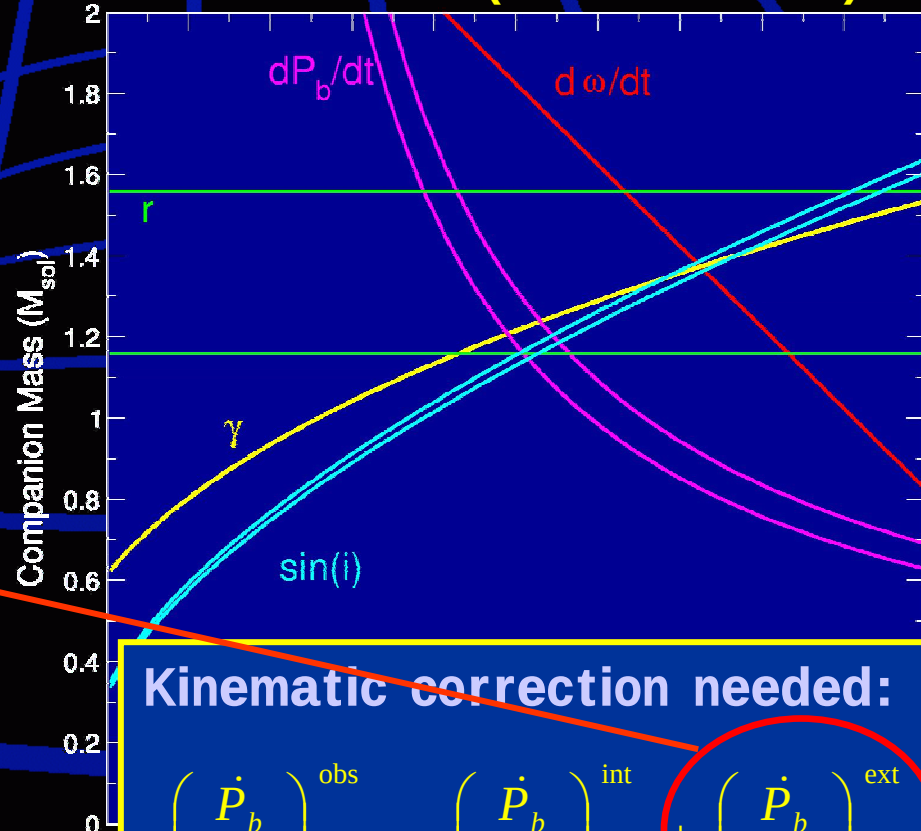


Binary pulsars as gravity labs: mass-mass plot

B1913+16 (Weisberg & Taylor '03)



B1534+12 (Stairs et al. '02)

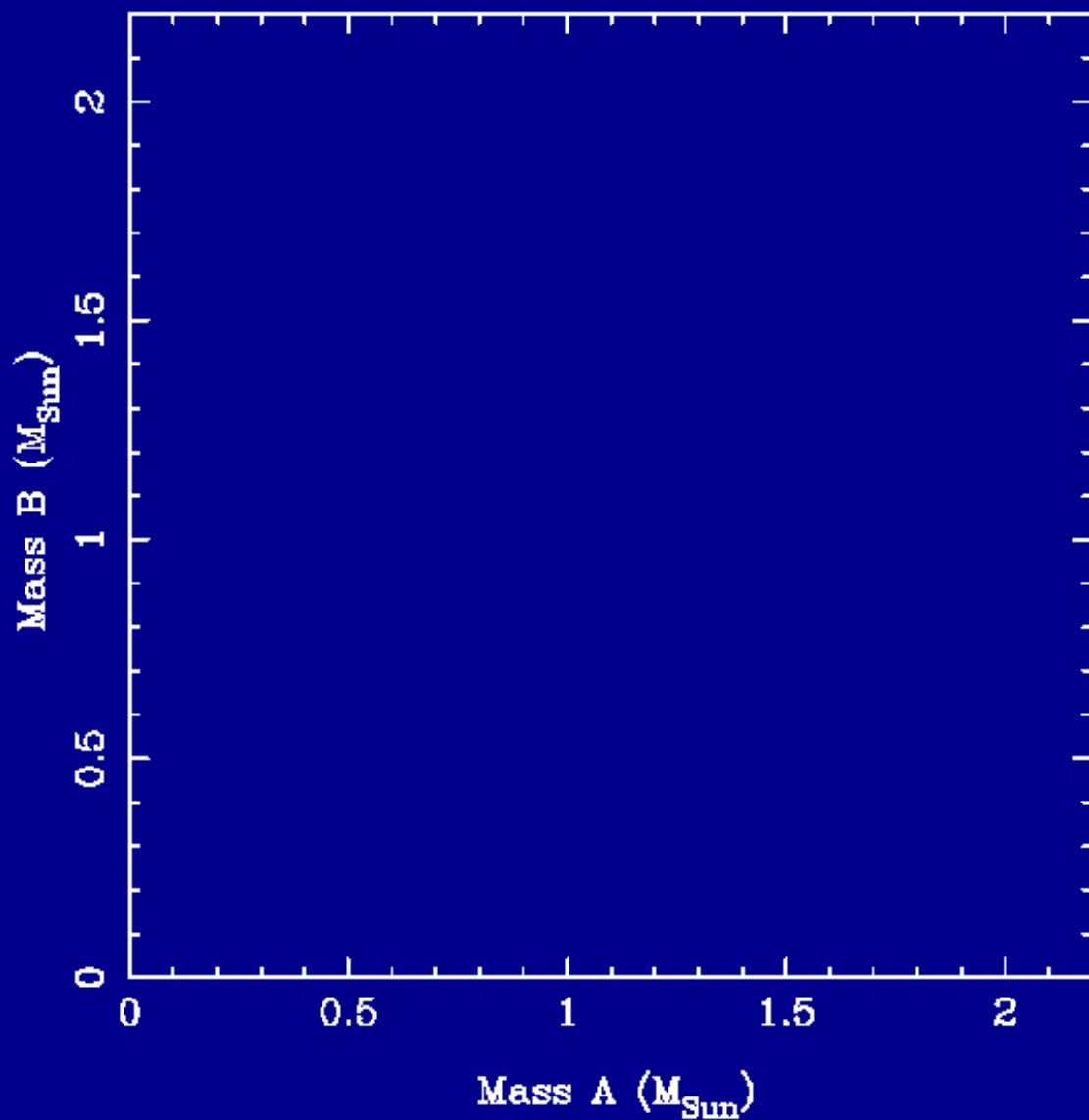


Kinematic correction needed:

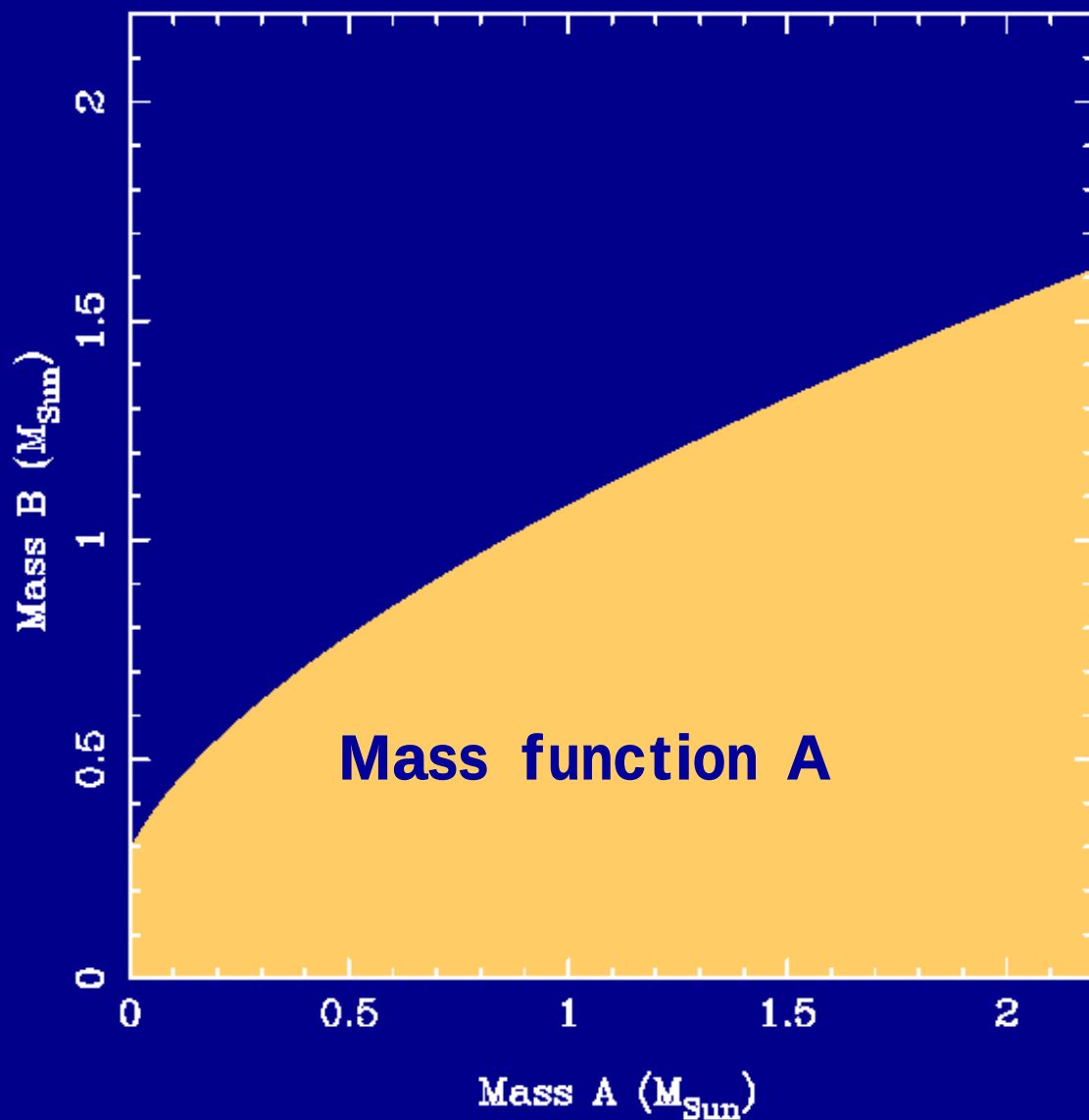
$$\left(\frac{\dot{P}_b}{P_b} \right)^{\text{ext}} = -\frac{a_z \sin b}{c} - \frac{v_0^2}{cR_0} \left(\cos l + \frac{d/R_0 - \cos l}{\sin^2 l + (d/R_0 - \cos l)^2} \right) + \frac{v^2}{cd}$$

$$\left(\frac{\dot{P}_b}{P_b} \right)^{\text{obs}} = \left(\frac{\dot{P}_b}{P_b} \right)^{\text{int}} + \left(\frac{\dot{P}_b}{P_b} \right)^{\text{ext}}$$

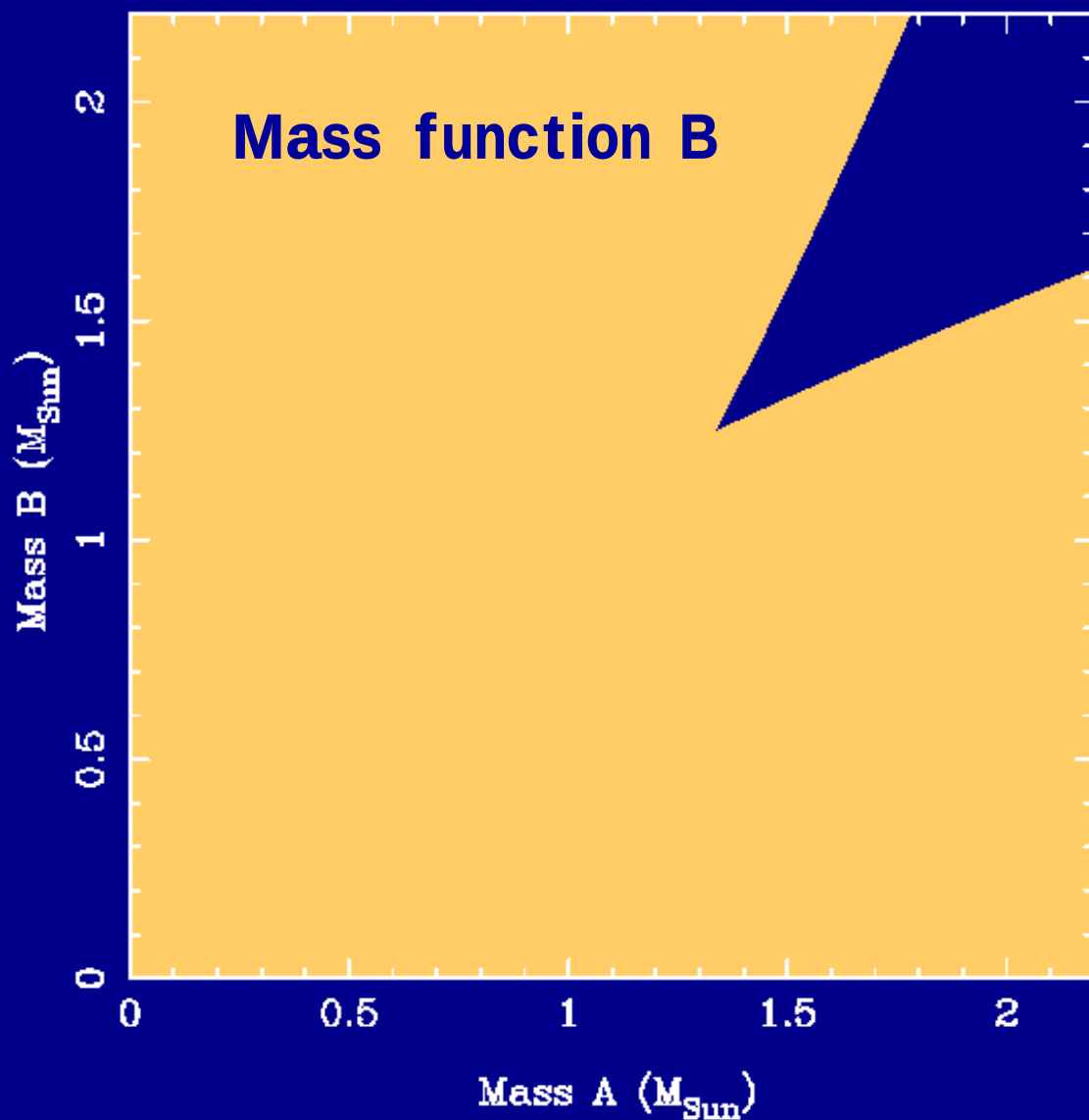
Tests of GR



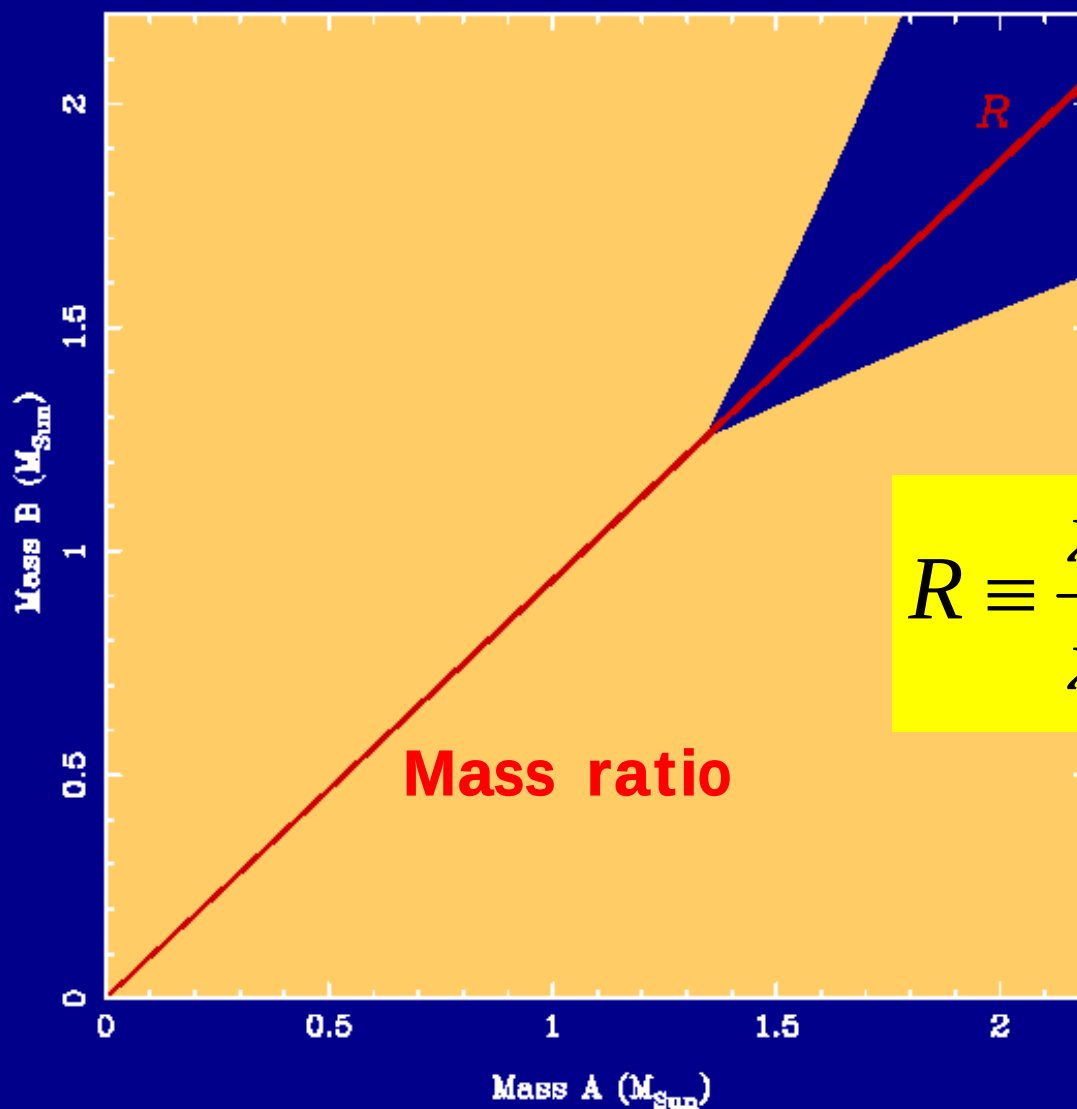
Tests of GR



Tests of GR

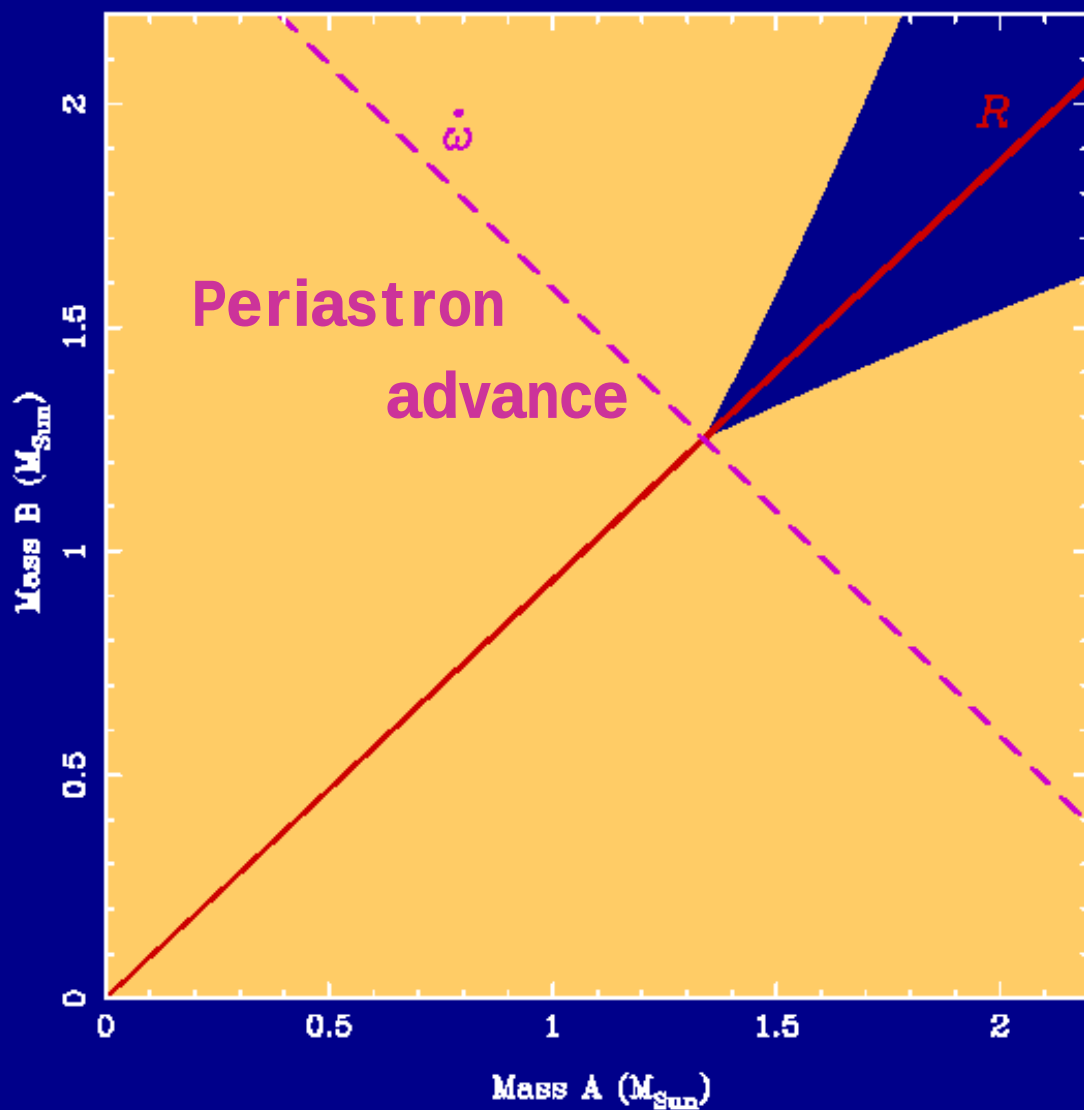


Tests of GR

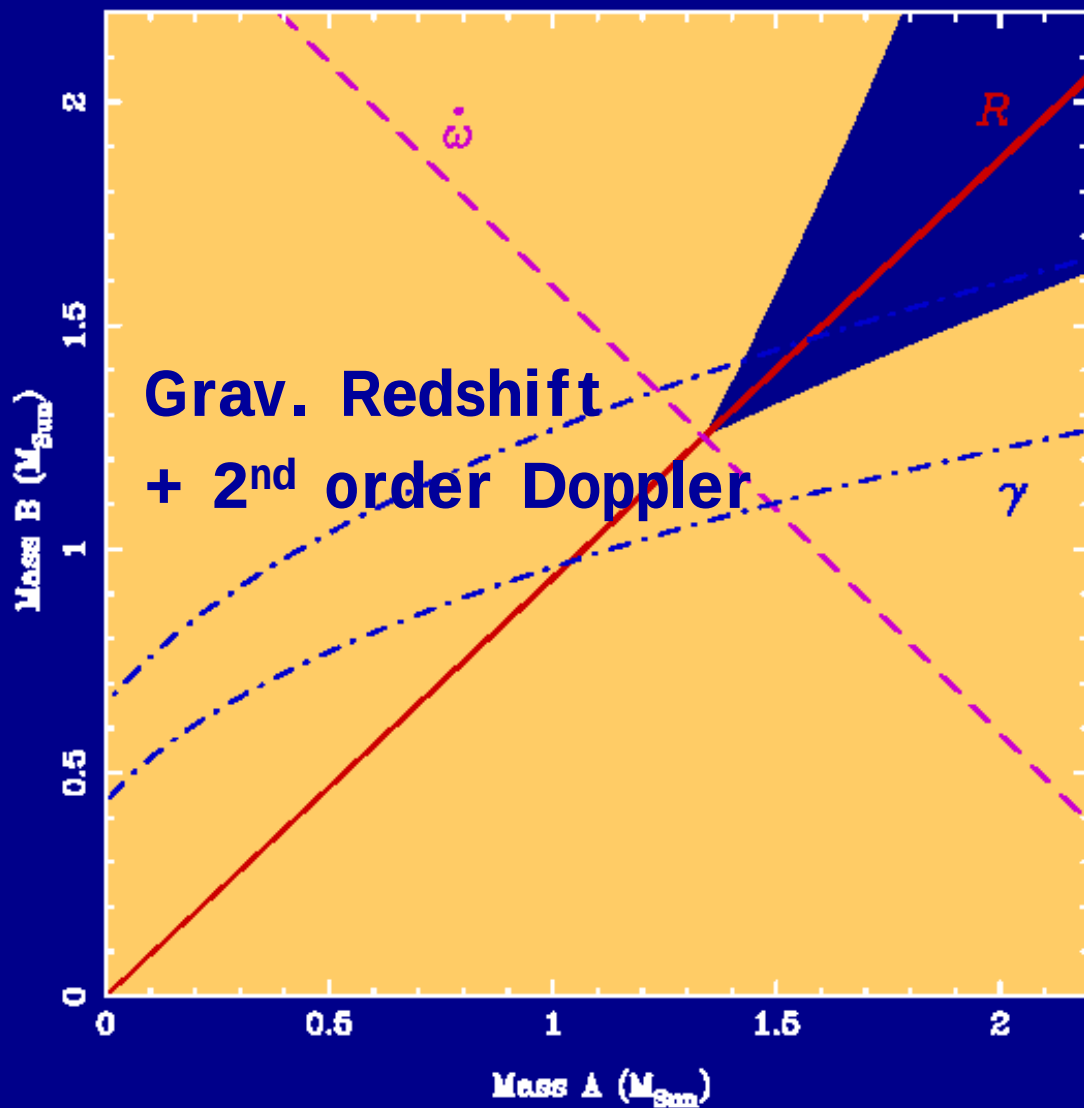


$$R \equiv \frac{x_B}{x_A} = \frac{m_A}{m_B}$$

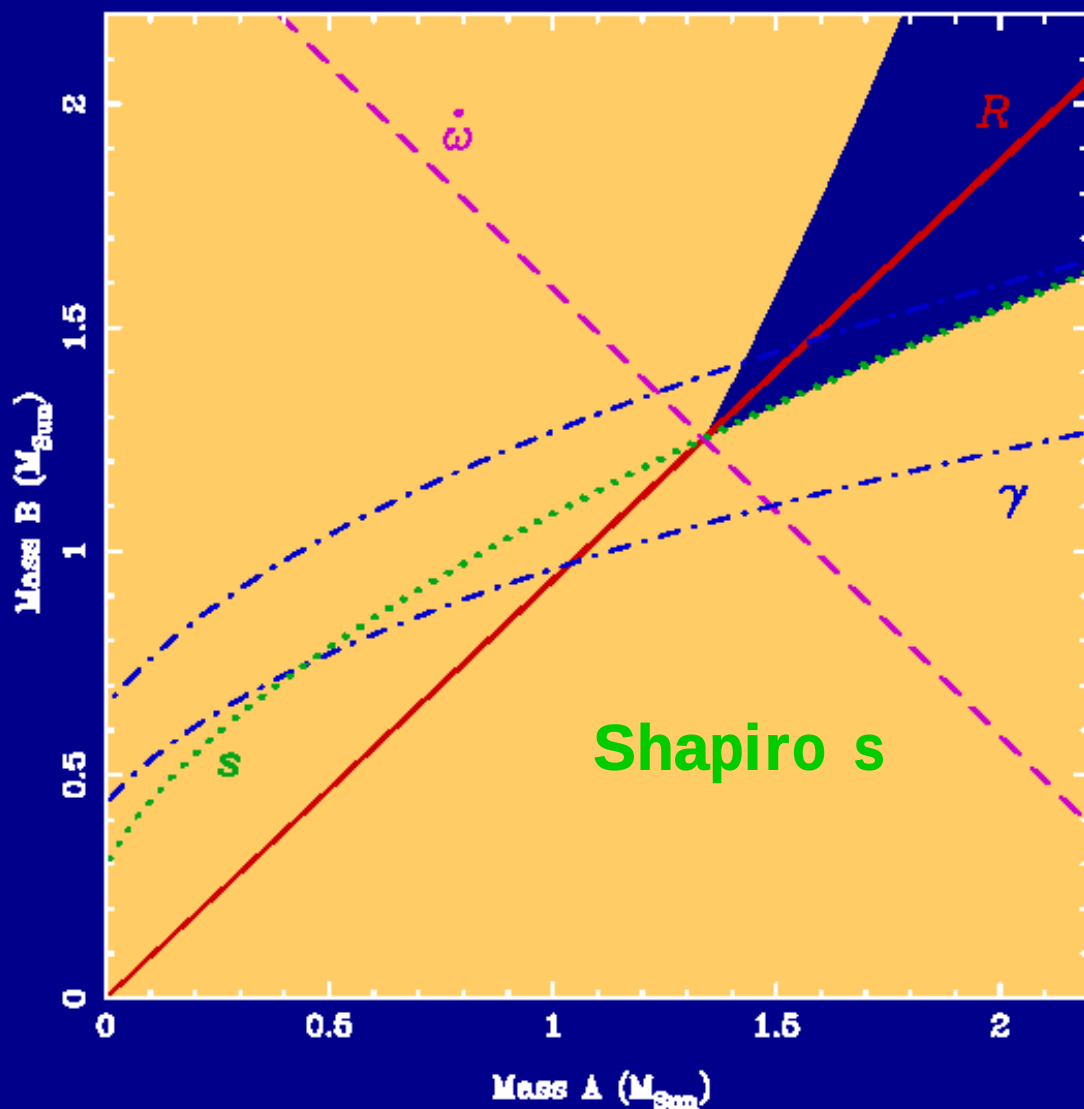
Tests of GR



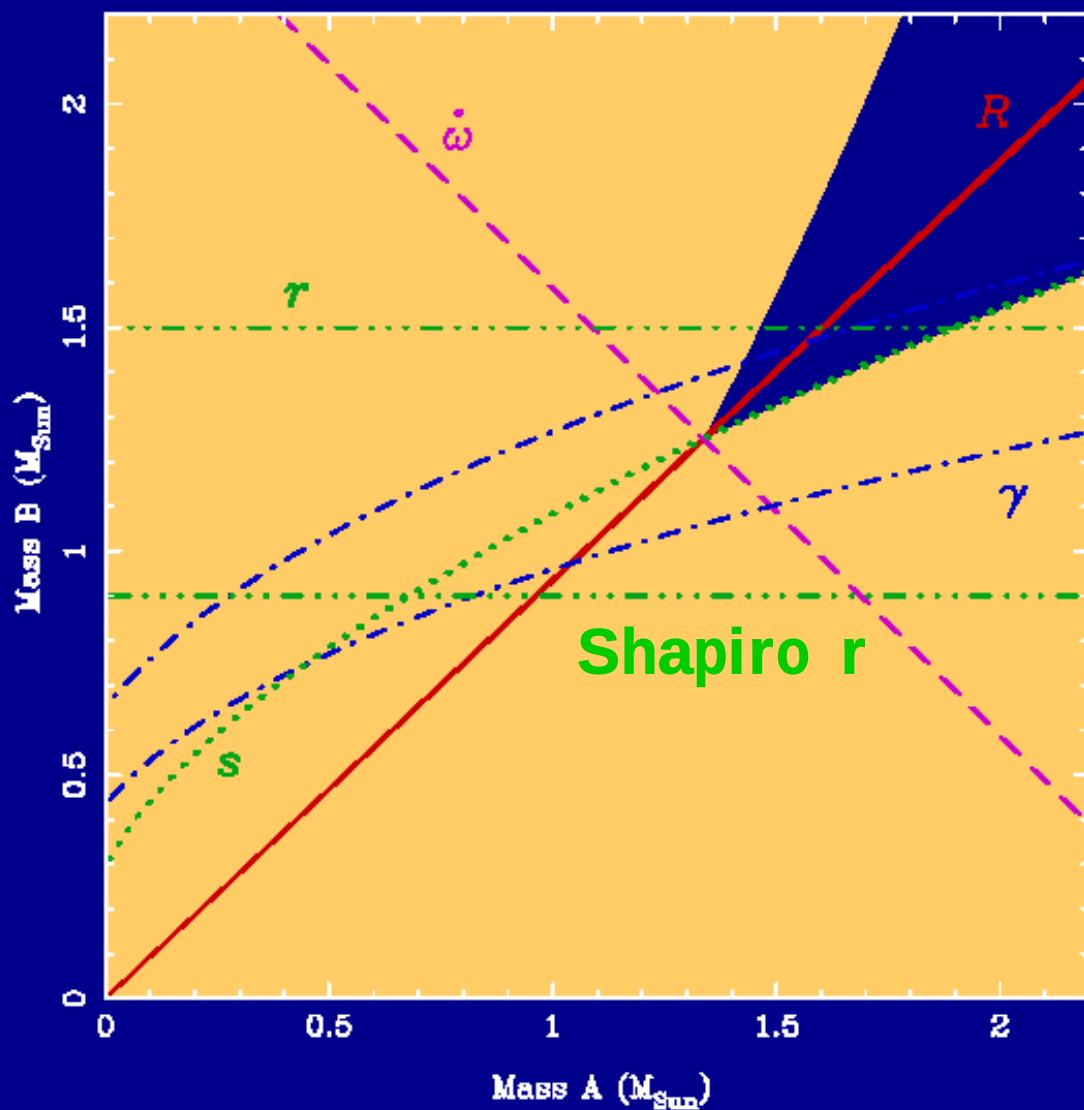
Tests of GR



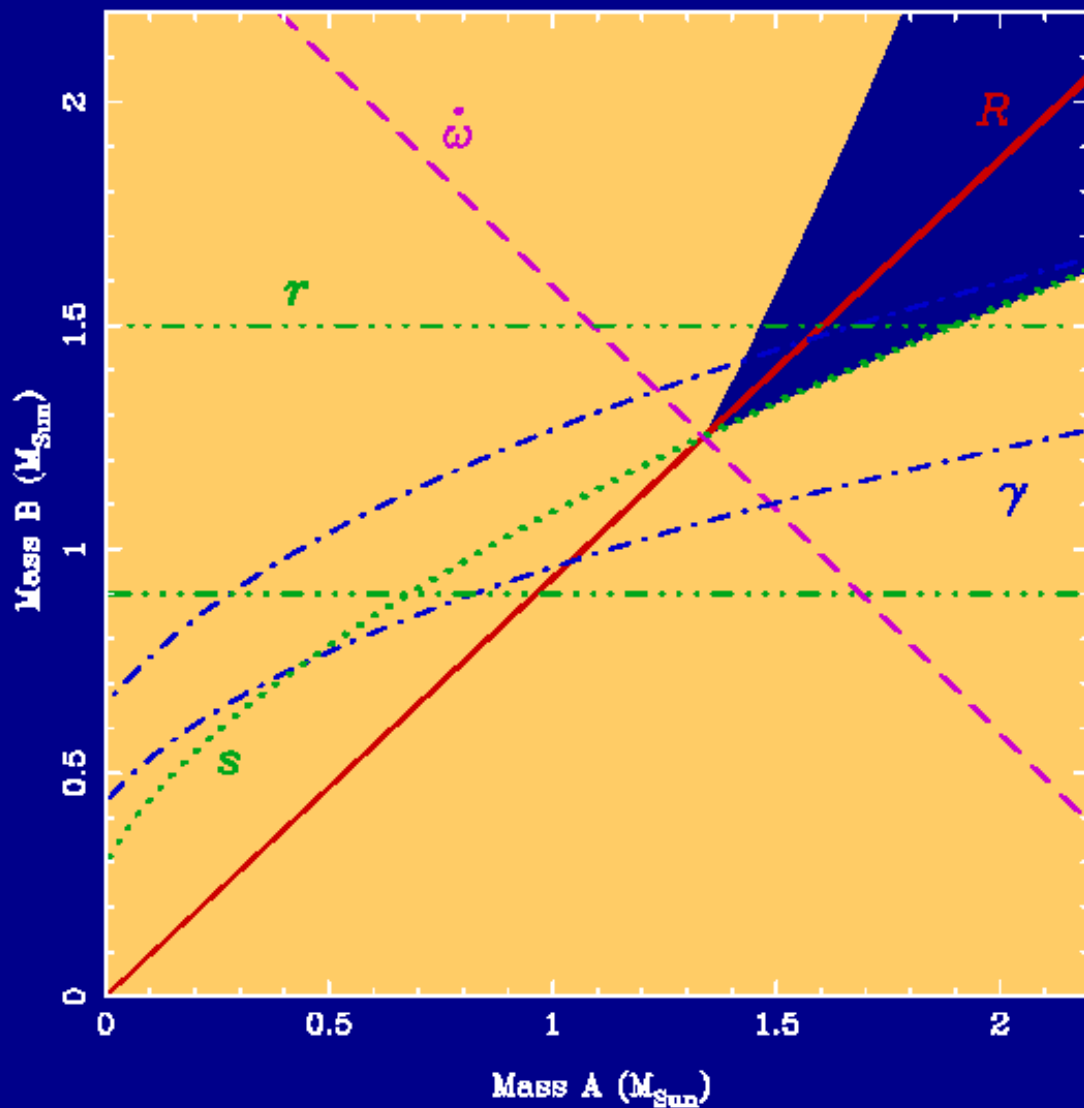
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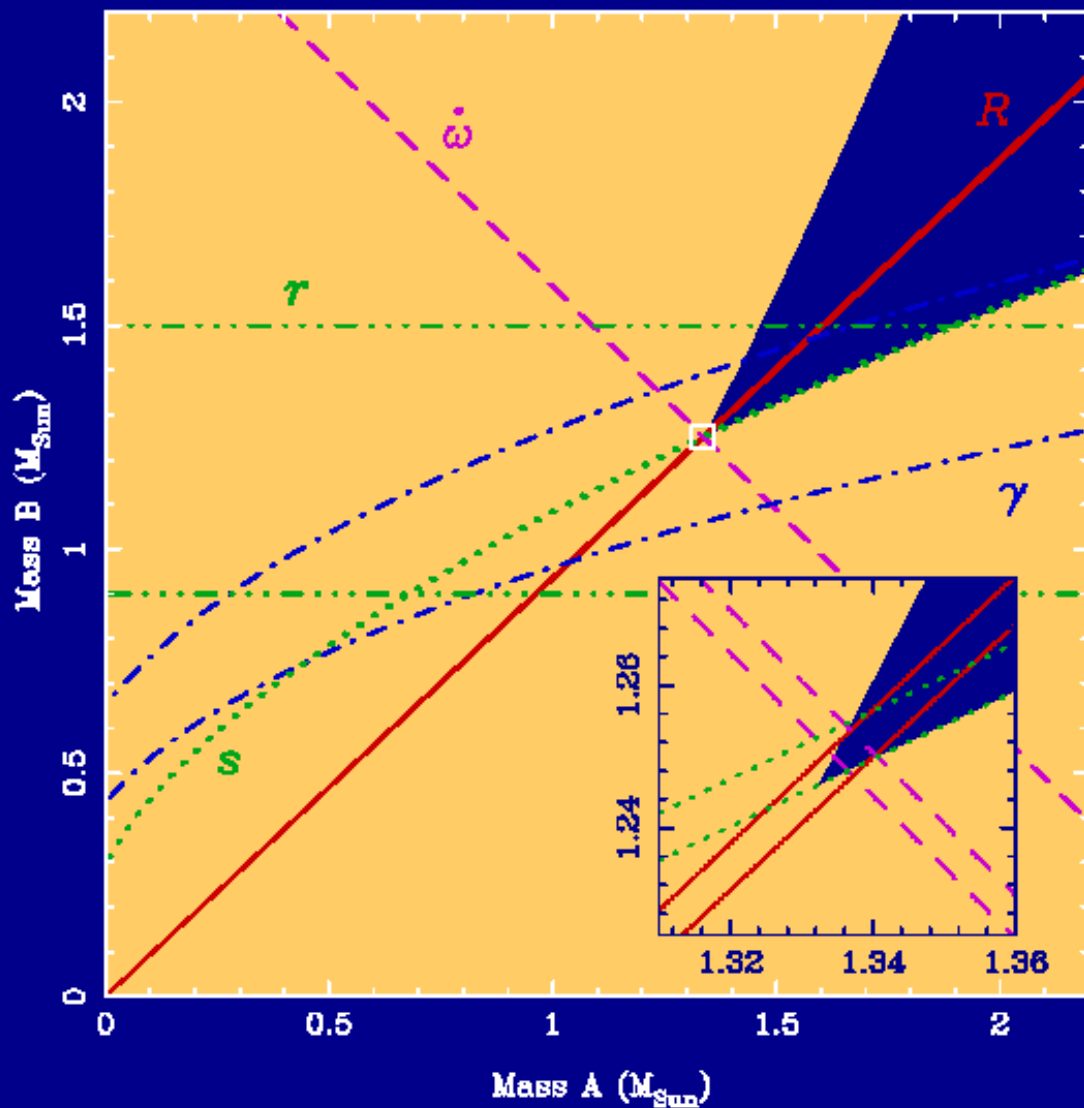
Tests of GR



Tests of GR

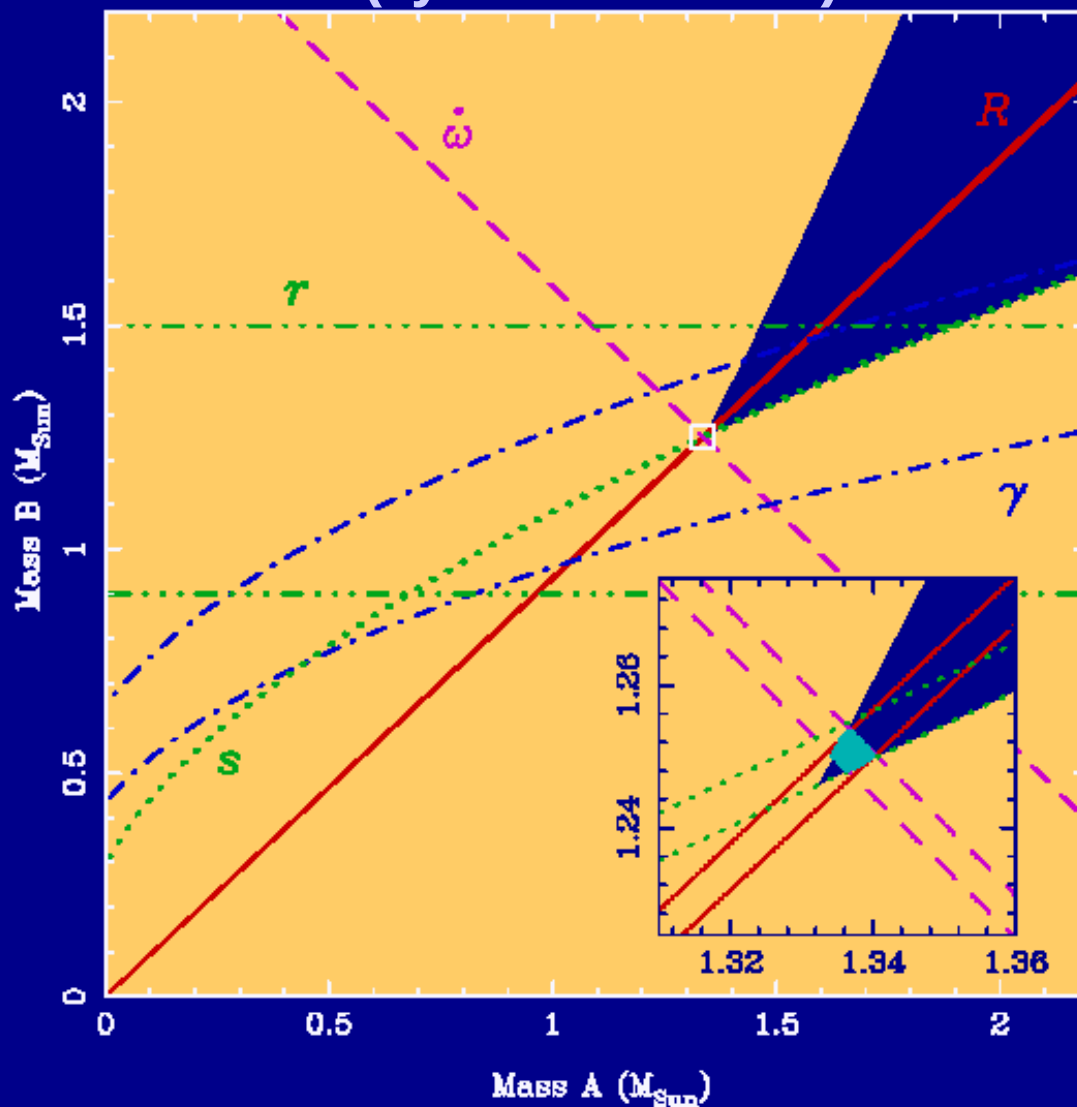


Tests of GR



Tests of GR

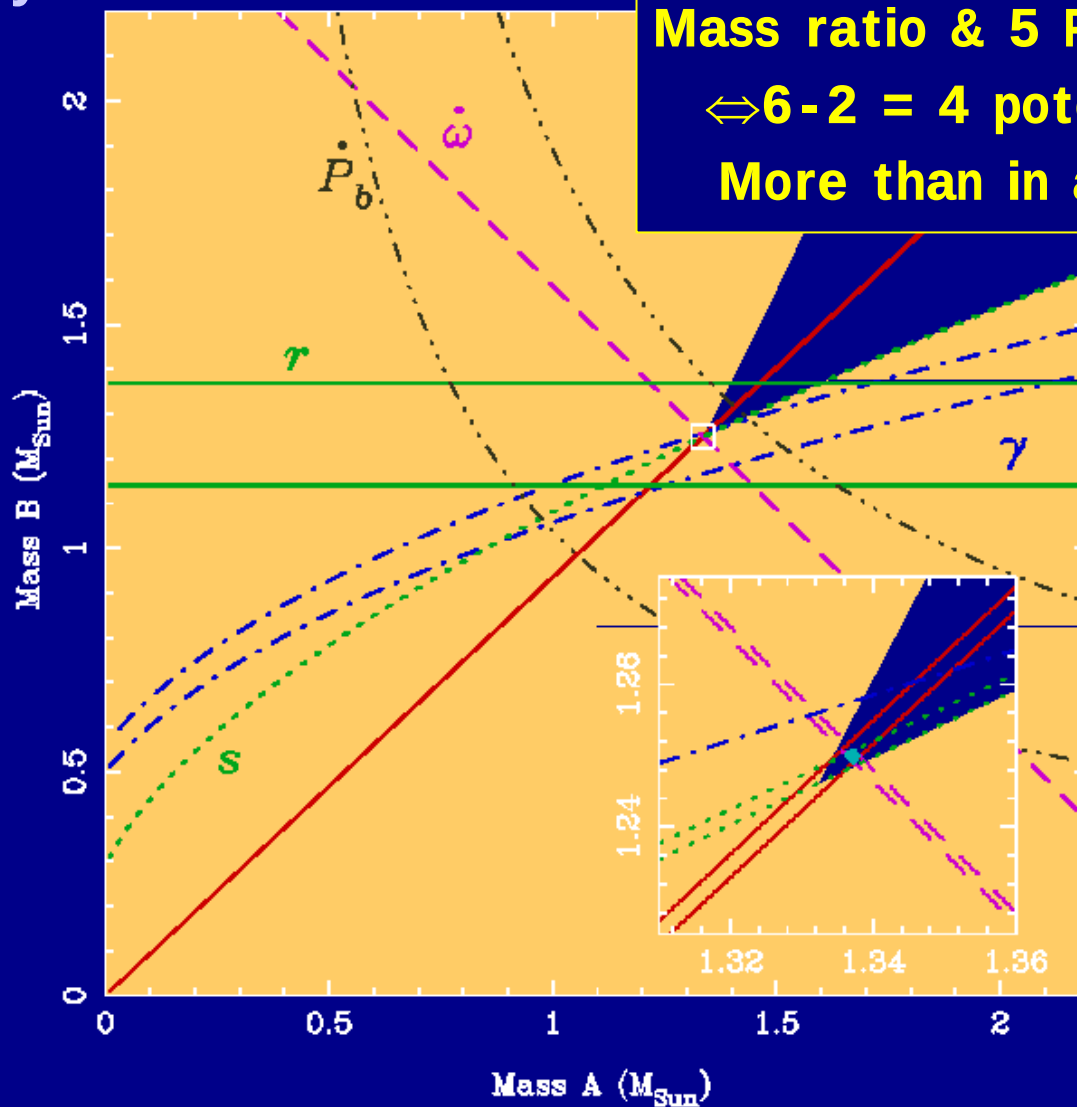
December 2003 (Lyne et al. 2004)



Tests of GR

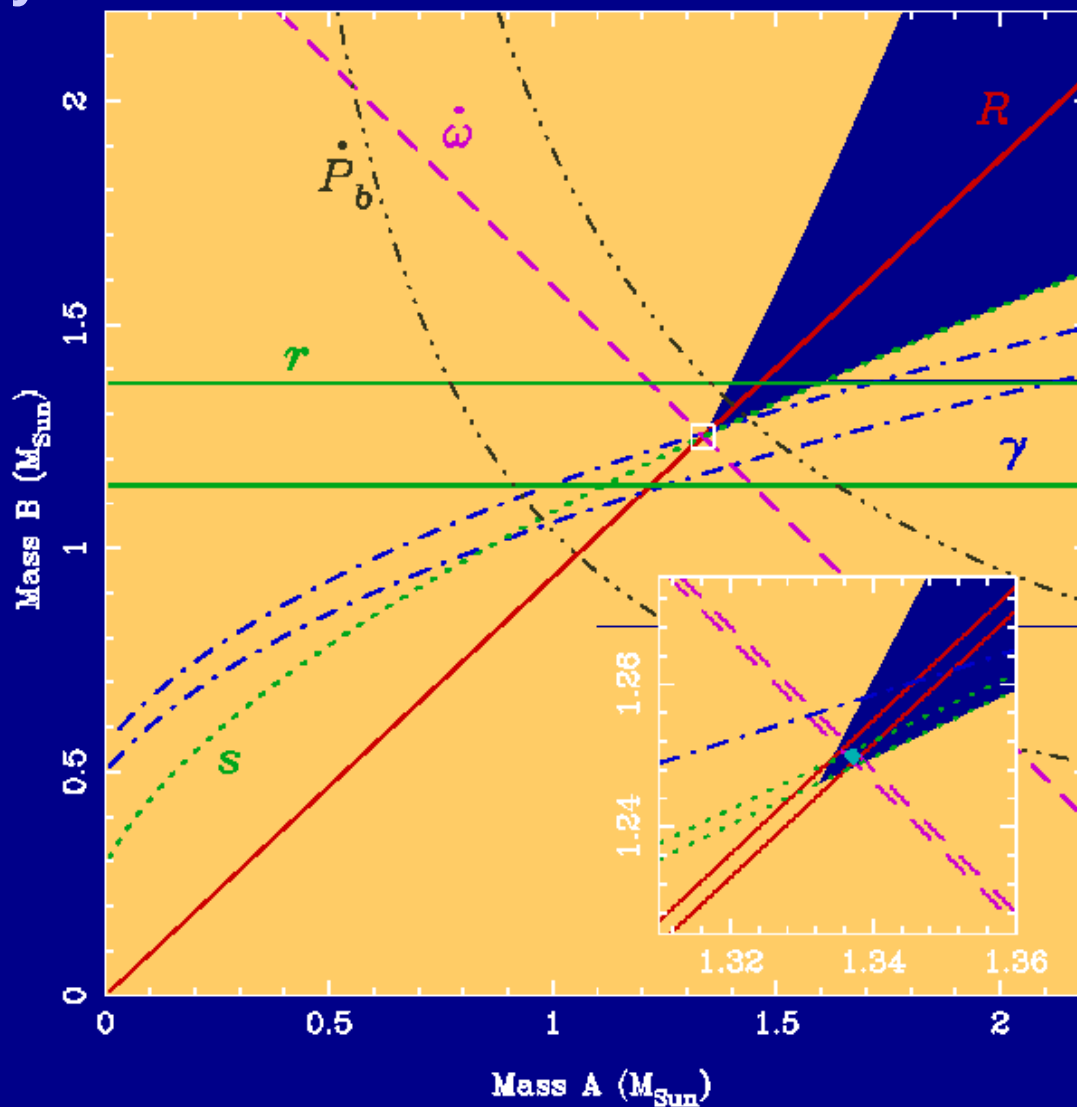
July 2004

Mass ratio & 5 PK parameters
 $\Leftrightarrow 6 - 2 = 4$ potential tests!
More than in any system!

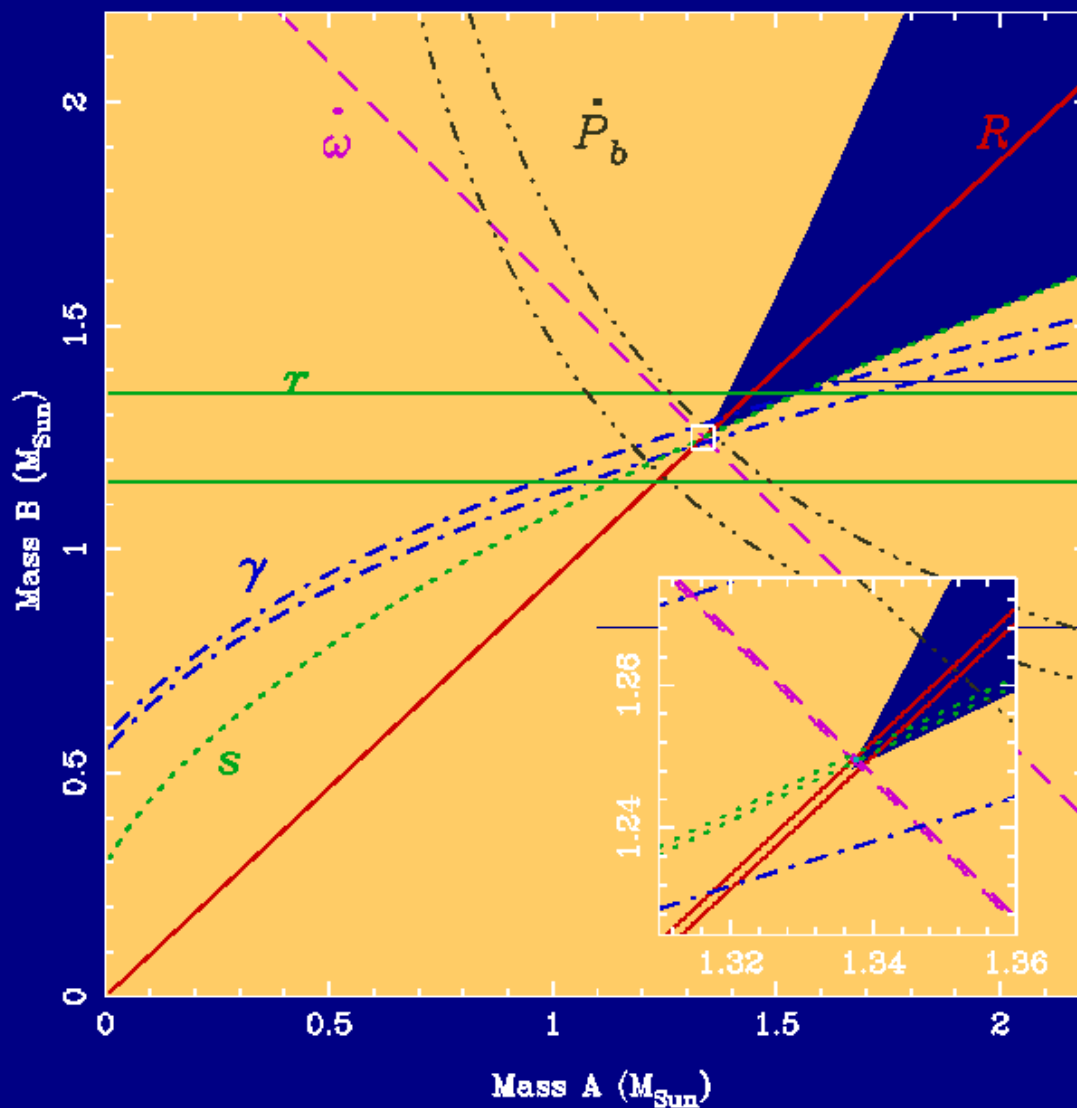


Tests of GR

July 2004

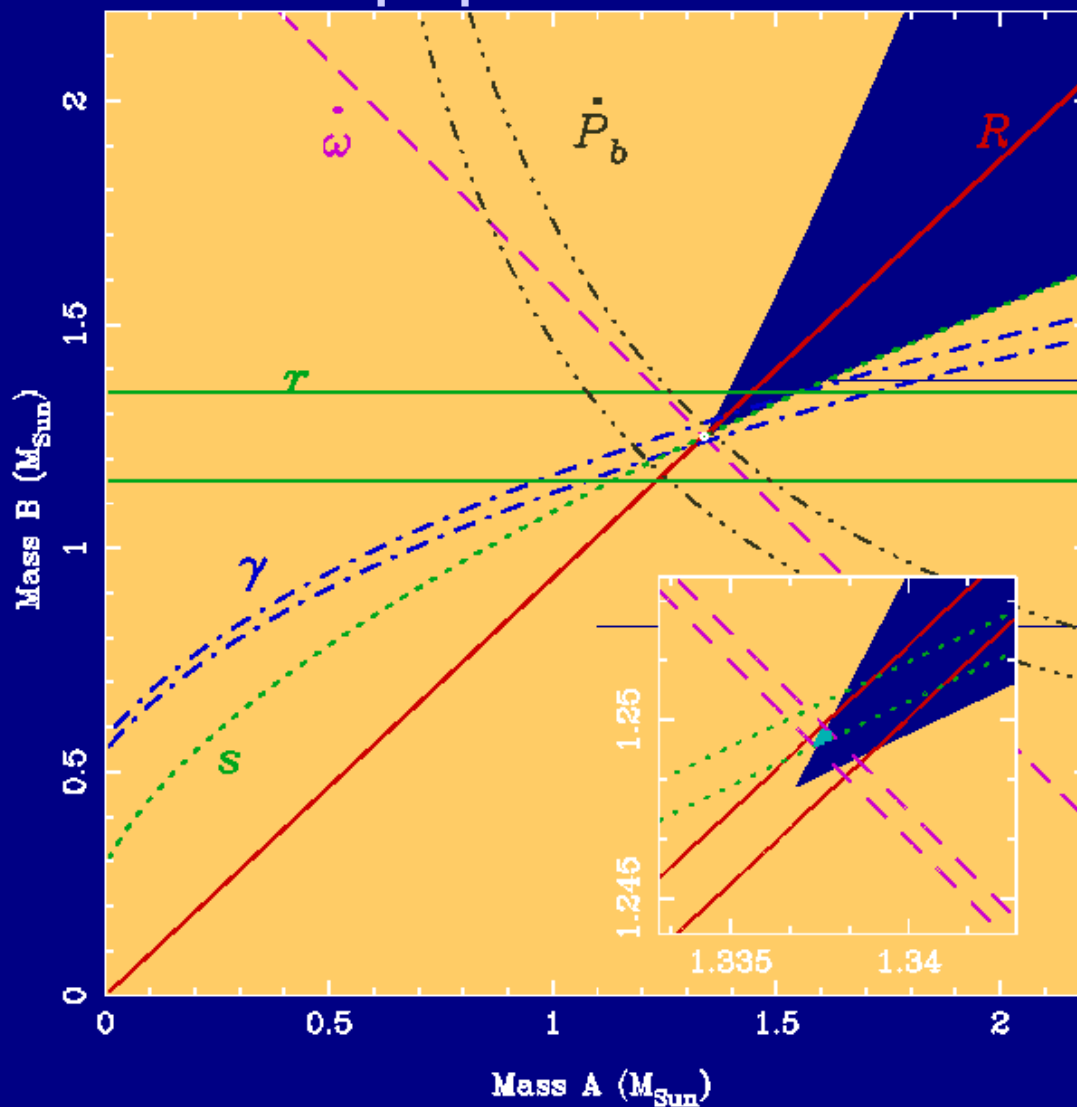


Tests of GR



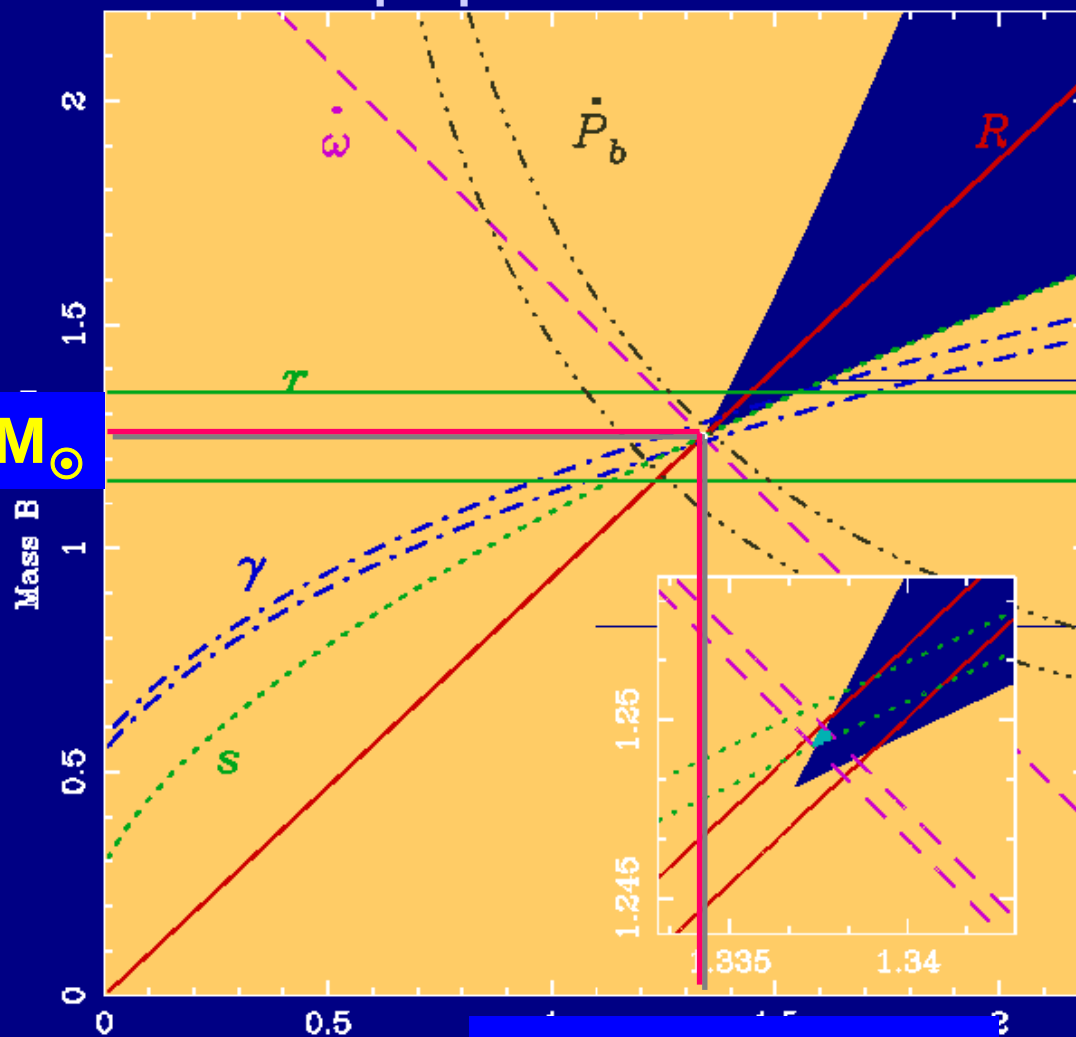
Tests of GR

Kramer et al. in prep.



Tests of GR

Kramer et al. in prep.



$$M_B = 1.249(1)M_{\odot}$$

$$M_A = 1.338(1)M_{\odot}$$

Precision of 0.08%

Tests of GR

Based on:

$$R = 1.071 \pm 0.001 \text{ \& } \dot{\omega} = 16.899 \pm 0.001 \text{ deg/yr } (6 \times 10^{-5})$$

Expected in GR:

$$\gamma = 0.384 \text{ ms}$$

$$dP_b/dt = -1.24 \times 10^{-12}$$

$$r = 6.2 \text{ } \mu\text{s}$$

$$s = 0.9997$$

Observed:

$$\gamma = 0.387 \pm 0.006 \text{ ms } (10^{-2})$$

$$dP_b/dt = (-1.19 \pm 0.08) \times 10^{-12} (7 \times 10^{-2})$$

$$r = 6.2 \pm 0.5 \text{ } \mu\text{s } (10^{-1})$$

$$s = 0.9993 \pm 0.0004 (4 \times 10^{-4})$$

$$\frac{S^{\text{exp}}}{S^{\text{obs}}} = 1.0004^{+0.0011}_{-0.0006}$$

precision of 0.1%!!

- Best test in strong-field
- Purely non-radiative with fundamentally different constraint!

Significance of “R”

To 1PN order, Kepler’s 3rd law given in generic form as:

$$a_R = \left(\frac{G_{AB} M_{tot}}{n^2} \right)^{1/3} \left[1 - \frac{1}{6} (5\varepsilon + 3 - 2\nu) \left(\frac{G_{AB} M_{tot} n}{c^3} \right)^{2/3} \right] \quad \text{e.g. Daumour \& Taylor '92}$$

$$n = (2\pi / P_b), \quad \nu = m_A m_B / M_{tot}^2, \quad \varepsilon = 2\hat{\gamma} + 1, \quad G_{AB} = G_{AB}(\text{strong field})$$

...so that for “any” theory of gravity to 1PN order:

$$R \equiv \frac{x_B}{x_A} = \frac{m_A}{m_B}$$

**Qualitatively
different
constraint!**

**independent of
field effects!**

Different to other PK parameters, which all depend on strong-field modified “constants” like G_{AB} which differs from G^{Newton} depending on strong-field effects in theory!

Significance of “R”

- Beyond 1PN approximation, used coordinate system and mass definition important:

$$R \equiv \frac{x_B}{x_A} = \frac{m_A}{m_B} + O(c^{-4})$$

may deviate from straight line

- In >1PN, probably with precision much below that of PK parameters.

Future: Predicted precision

- Difficult to predict behaviour of mass ratio, R
- For PK parms, precision increases due to more but also more precise data:
(also depends on orbital orientation!)

$\Delta\dot{\omega}/\dot{\omega} \propto T^{-1.5}$: expected since Science paper factor 4
actual improvement a factor of 100!

$\Delta\sin i/\sin i \propto T^{-0.5}$: expected since Science paper factor 1.6
actual improvement a factor of 10!

$\Delta\gamma/\gamma \propto T^{-1.5}$: expected since Science paper factor 4
actual improvement a factor of 10!

Further expected scaling: $\Delta(dP_b/dt)/(dP_b/dt) \propto T^{-2.5}$

$$\Delta\delta_{\theta}/\delta_{\theta} \propto T^{-2.5}$$

Will we be able to use dP_b/dt ?

- Orbit shrinkage
- Observed velocity

$$\left(\frac{\dot{P}_b}{P_b}\right)^{\text{ext}} = -\frac{a_z \sin b}{c} - \frac{v_0^2}{cR_0} \left(\cos l + \frac{d/R_0 - \cos l}{\sin^2 l + (d/R_0 - \cos l)^2} \right) + \frac{v^2}{cd} \frac{P_b}{P_b}$$

Observed: -1.36×10^{-16}

Vertical: -1.26×10^{-20}
Plane: -3.10×10^{-20} } **negligible**

Upper limit on velocity from timing: 17 km/s
Velocity from scintillation: 66 km/s?!?

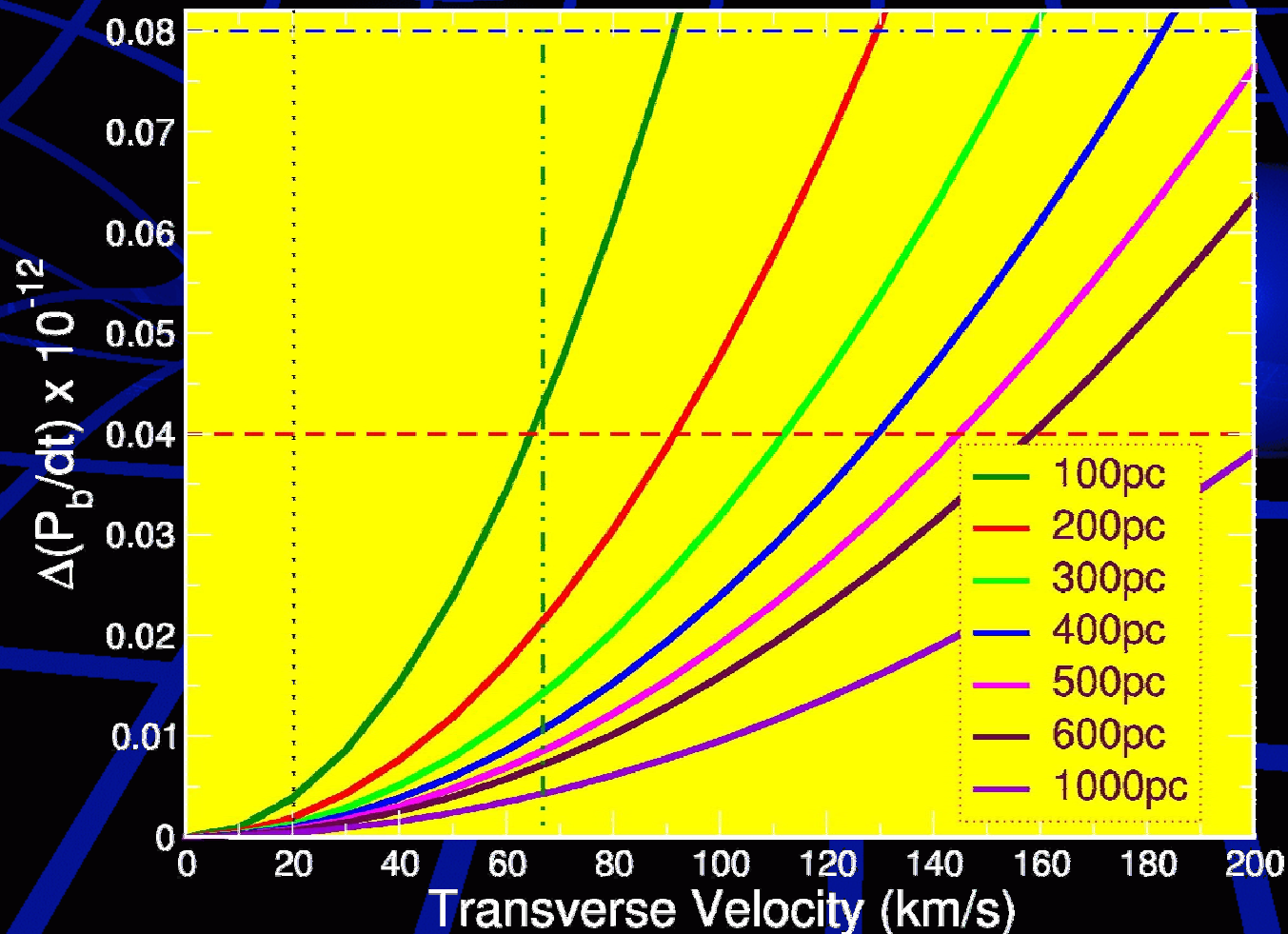
Transverse motion (17km/s): 5.25×10^{-20}
Transverse motion (66km/s): 7.91×10^{-19}
 $\Rightarrow$ Needed correction: $< 1\%$

Dominated by transverse speed: VLBI obs. underway

Will we be able to use dP_b/dt ?

yes!

- Summary of transverse motion:



Newly measurable PK parameters

- Relativistic orbit is deformed
- Two, rather than a single eccentricity needed (DD86):

$$e_r \equiv e(1 + \delta_r)$$

$$e_\theta \equiv e(1 + \delta_\theta)$$

while the PK parameter

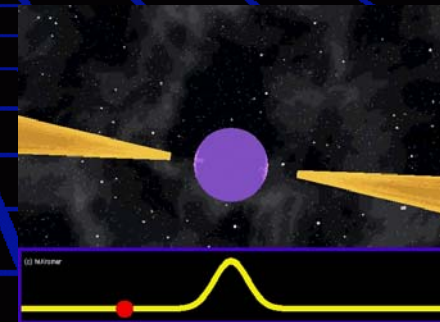
$$\delta_\theta = T_{sol}^{2/3} \left(\frac{2\pi}{P_b} \right)^{2/3} \frac{7m_p^2 / 2 + 6m_p m_c + 2m_c^2}{(m_p + m_c)^{4/3}}$$

may be measurable in a few years:

$$\delta\theta = 12.6 \times 10^{-6} \text{ expected}$$

Aberration

- Pulsar rotates rather than pulses
- Aberration contributes to timing & profile
- ToAs are modified by “aberration delay” (DD86)



$$\Delta_A = A\{\sin[\omega + A_e(u)] + e \sin \omega\} \\ + B\{\cos[\omega + A_e(u)] + e \cos \omega\}$$

with PK parameters A and B which are usually absorbed in Roemer delay as:

$$x_{\text{obs}} = (1 + \varepsilon_A) x_{\text{int}}$$

$$e_{\text{obs}} = (1 + \varepsilon_A) e_{\text{int}}$$

$$\delta_{\theta}^{\text{obs}} = \delta_{\theta}^{\text{int}} - \varepsilon_A$$

$$\delta_r^{\text{obs}} = \delta_r^{\text{int}} - 3\varepsilon_A, \quad \varepsilon_A \equiv \frac{A}{\chi}$$

However...

Damour & Taylor (1992)

Aberration & Geodetic Precession

- Aberration parameters will change due to geodetic precession:

$$\frac{d\varepsilon_A}{dt} = -\frac{P_p}{P_b} \frac{1}{\sin i (1-e^2)^{1/2}} \frac{d}{dt} \left(\frac{\sin \eta}{\sin \lambda} \right)$$

Damour & Taylor (1992)

leading to different geometries,
so that A & geometry may be
determined! Expected:

$$A = -0.365 \mu\text{s} \times \text{geometry!!}$$



But spin-orbit coupling is likely to be visible in other ways too...

Spin contributions

We have seen that spin-coupling is large:

- **PK parameters are only expected to meet in a single point of mass-mass diagram IF spin contributions are negligible**
- **For instance, periastron advance is usually only used in 1PN approximation ignoring spin**
- **Formally, spin-orbit coupling enters at 1PN level!**
- **For binary pulsars however, numerically they are of size as 2PN effects (Wex 1995)**

Spin contributions

Total periastron advance at 2PN level: Damour & Schaefer (1988)

$$k^{tot} = \frac{3\beta_0^2}{1-e_T} \left[1 + f_0\beta_0^2 - g_s^A \beta_0 \beta_s^A - g_s^B \beta_0 \beta_s^B \right]$$

1PN

2PN

Spin A

Spin B

Geometry dependent

Neutron star dependent

Assuming 'canonical' values: **1PN = 16.9 deg/yr**

2PN = 0.0004 deg/yr

14 x 1913+16's value!

SpinA = 0.0002 deg/yr

already at 0.001 deg/yr!

Not easy! Need two other parms with similar precision... Worth trying...

Neutronstar structure

Total periastron advance to 2PN level: Damour & Schaefer (1988)

$$k^{tot} = \frac{3\beta_0^2}{1-e_T} \left[1 + f_0\beta_0^2 - g_s^A \beta_0 \beta_s^A - g_s^B \beta_0 \beta_s^B \right]$$

1PN

2PN

Spin A

Spin B

Neutron star dependent

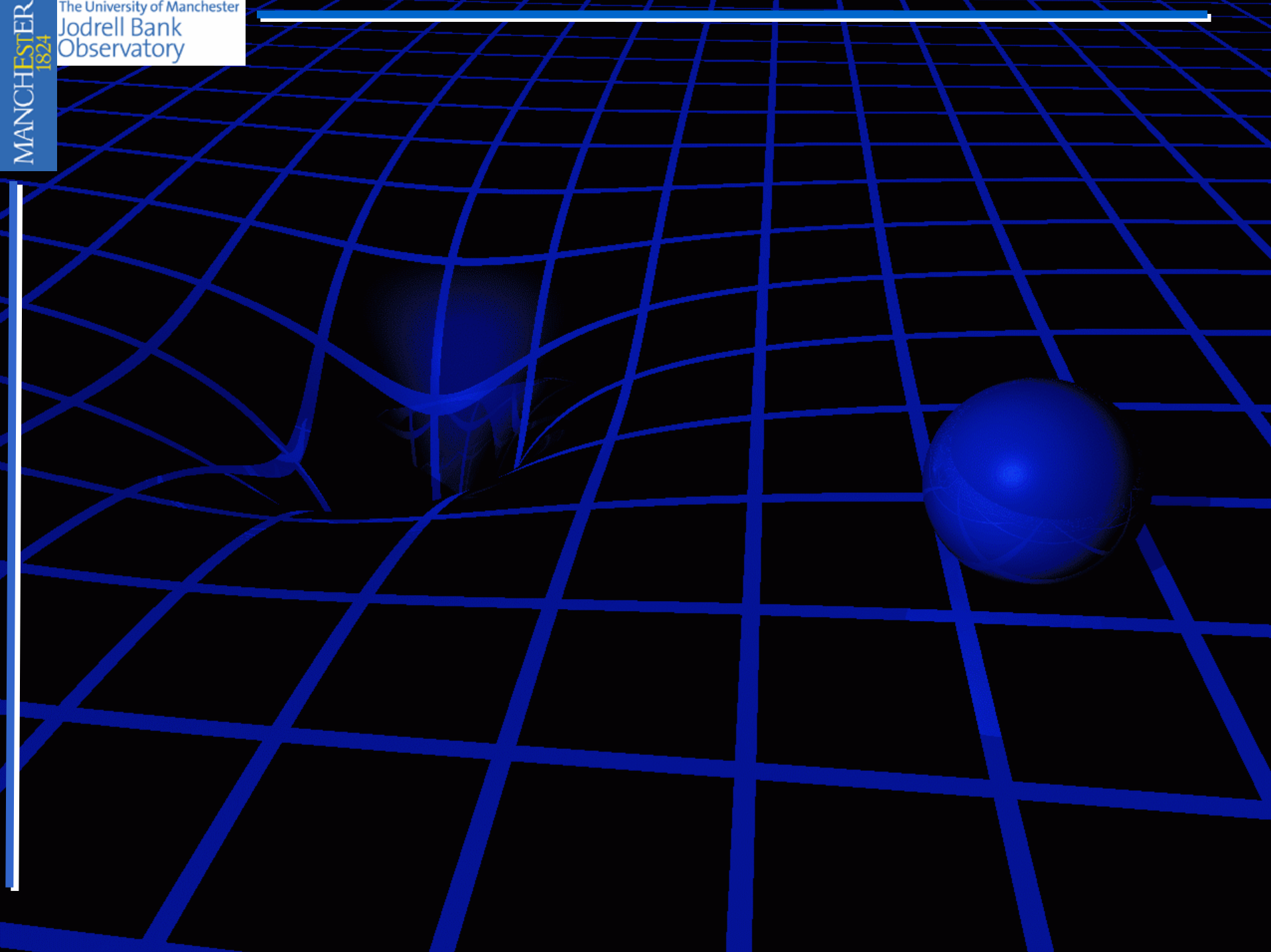
Equation-of-State!

Measure NS moment of inertia!!!

$$\beta_s = \frac{2\pi c}{G} \frac{1}{P_p} \frac{I}{m^2}$$

Summary

- Beautiful laboratory for plasma physics
- Invaluable for studying pulsar magnetospheres
- **Unique test-bed for relativistic gravity**
- **Most over-constrained system already**
- Only system with constraint independent of self-field
- **Most precise tests already (0.1%)**
- More PK parameter/effects potentially measurable:
 - **Measurement of orbital deformation**
 - **Measurement of aberration**
- Measurement of 2nd order PN effects
(Lightbending, How do Kepler's laws look like??)
- **Moment of inertia & Equation of State**



Finally...

Hopefully, next time that you type
“double pulsar” into Google, you get something
different than this:

