

# Chiral Quark Approach for $\Theta^+$ and its production

Feb. 17-19 (2004) Kyoto, Atsushi Hosaka (RCNP, Osaka Univ)

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Manifestly the first **EXOTIC** state of  $qqqq\bar{q}$

Toward multi-quark matter

Relatively small mass  
Unexpectedly narrow width  
Parity unknown

# Contents

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## ■ Theories

Quark model, Chiral soliton, Diquark

**Chiral bag**, Lattice, Sum rule, . . .

Parity, decay width

## ■ Productions

To know parity

# Theoretical papers

About 100 have appeared

## Theory prediction

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D. Diakonov <i>et al.</i> (chiral quark soliton)	: $1/2^+$ , I=0
Naive quark model	: $1/2^-$
S. Capstick <i>et al.</i> (isotensor formulation)	: $1/2^-$ , $3/2^-$ , $5/2^-$ , I=2
Fl. Stancu, D.O. Riska (qq with $\pi$ int.)	: $1/2^+$
A. Hosaka (chiral potential)	: $1/2^+$ ( <b>strong <math>\pi</math></b> )
R. L. Jaffe <i>et al.</i> (qq-qq-q : 10 + 8)	: $1/2^+$ , I=0
J. Sugiyama <i>et al.</i> (QCD sum rule)	: $1/2^-$ , I=0
F. Csikor <i>et al.</i> (Lattice QCD)	: $1/2^+ \rightarrow 1/2^-$
S. Sasaki (Lattice QCD)	: $1/2^-$

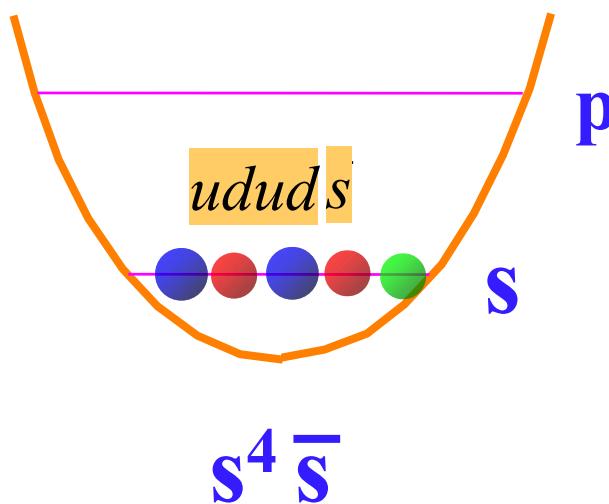
**Naïve quark model**

**Diquark vs. Chiral~strong  $\pi$**

Negative  
Positive

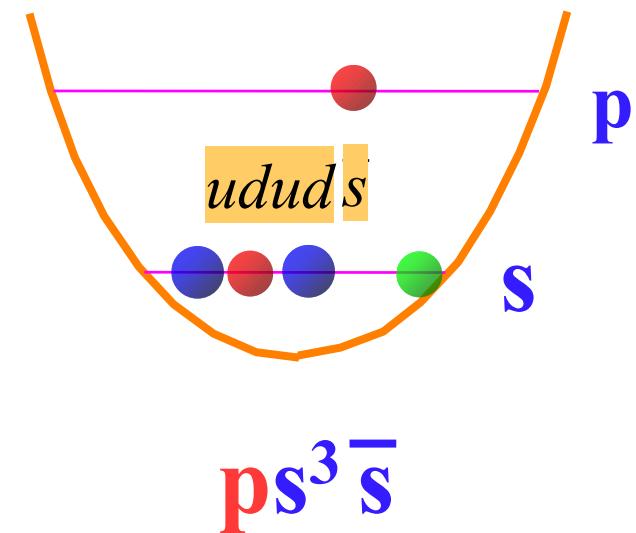
# Parity in theoretical models

## Naïve quark model



Negative

<<  
(mass)



Positive

What makes the **p** state lower?

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**Diquark correlations**

Jaffe-Wilczek

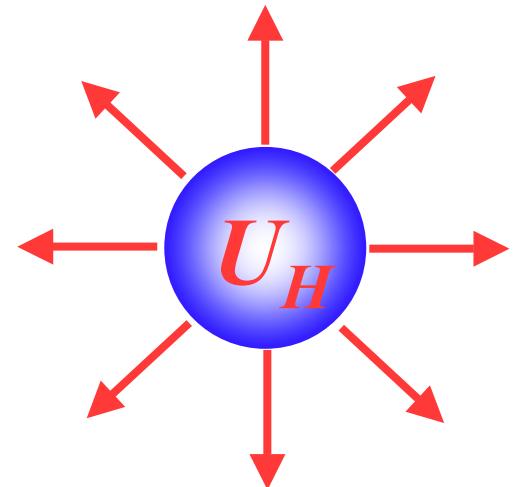
**Chiral interaction, especially  
hedgehog structure?**

# Chiral soliton

Large- $N_c$  QCD

Diakonov et al,  
Z. Phys. A359 (1997) 305

**Baryons  $\sim$  solitons** (Hartree qq...q)  
 **$\Theta \sim$  SU(3) rotational band** of  
the hedgehog Skyrmion



$$\pi_{\text{isospin}} \sim r_{\text{radial}}$$

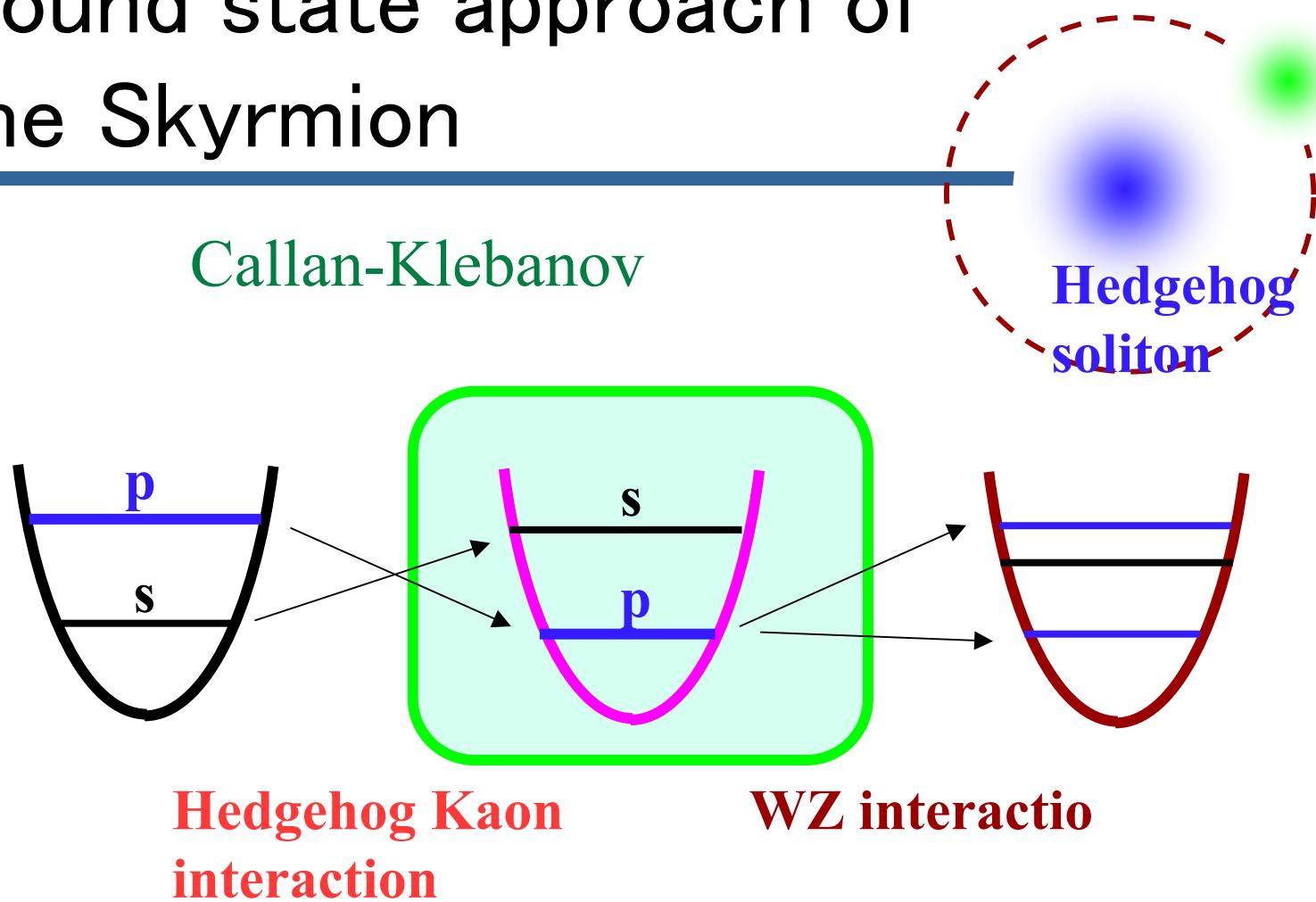
$$A(t)U_HA(t)^\dagger$$



$$J^P = 1/2^+$$

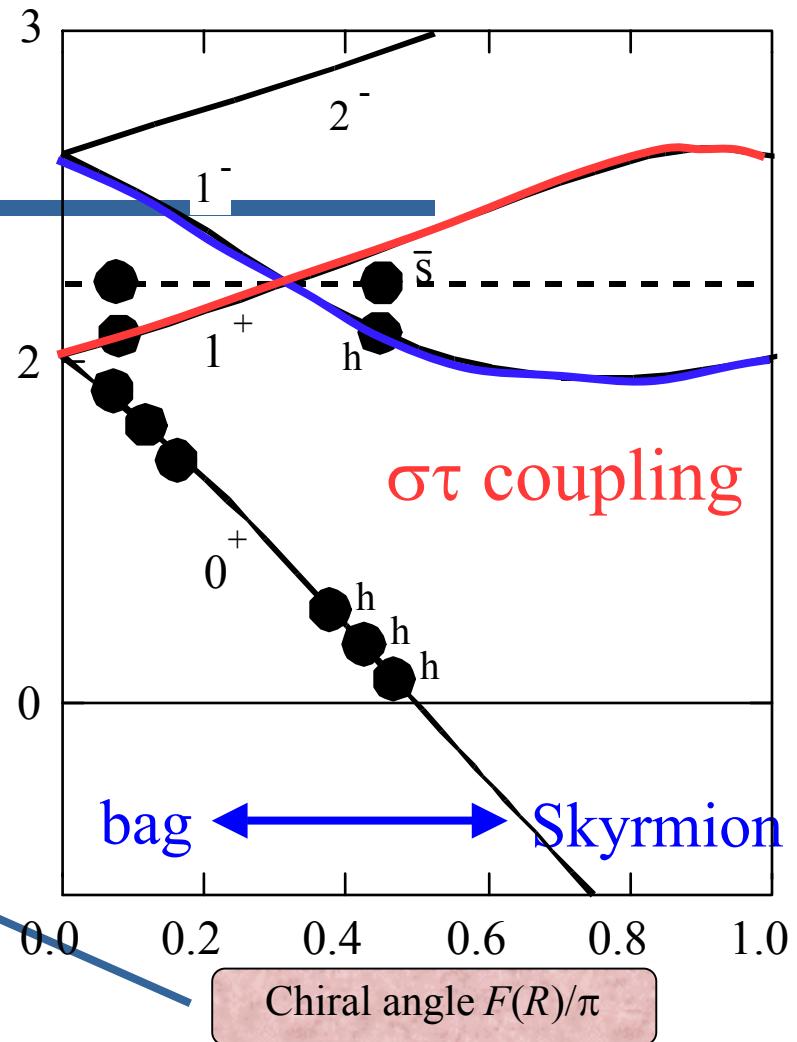
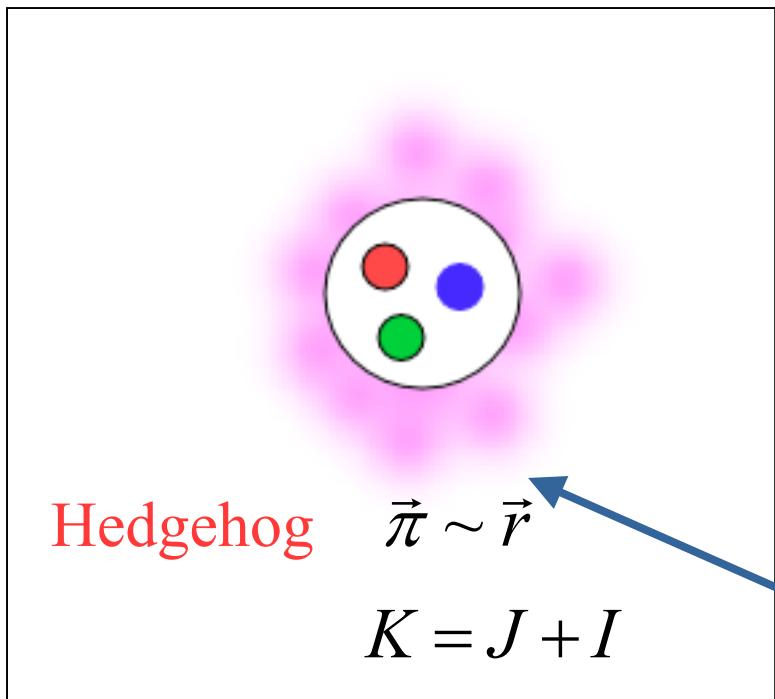
Cranking  $\sim$  rigid rotation

# Bound state approach of the Skyrmion



# Chiral potential

A. Hosaka hep-ph/0307323  
Phys. Lett. B571, 55 (2003)



$$(i\partial - g(\sigma(\vec{x}) + i\vec{\tau} \cdot \vec{\pi}(\vec{x})\gamma_5)) \psi = 0 .$$

# $\sigma\tau$ interaction $\sim$ strong pion field

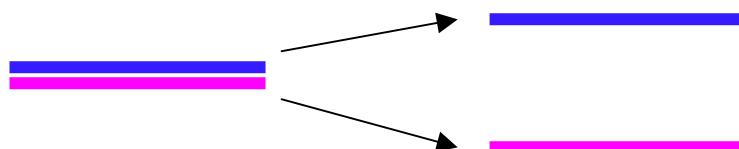
Spin-isospin splitting

$$\vec{\pi} \sim \hat{r}F(r)$$

$$H = c_1 + c_2 \langle \chi | \vec{\sigma} \cdot \vec{\tau} | \chi \rangle$$

$$(J=I=1/2)$$

$$K = J + I = 0, 1$$

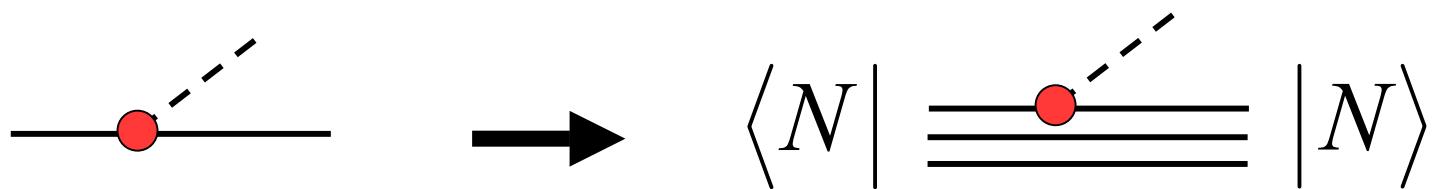


# Decay width

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A simple estimate in the quark model

mqq coupling



$$g \frac{\sigma_q q}{2m_q} \rightarrow 5g \frac{\sigma_B q}{2M_B} \rightarrow g \sim 2.6$$

# Matrix elements

Carlson et al, hep-ph/0312325

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$$\langle \Theta | \begin{array}{c} K \\ \diagdown \quad \diagup \\ \text{---} \end{array} | N \rangle$$
$$|N\rangle = |(qqq)_N\rangle$$
$$|\Theta\rangle = \underbrace{a |(q\bar{q})_K (qqq)_N\rangle}_{\text{---}} + \text{others}$$

**1/2<sup>-</sup>, KN in s-wave**  $\rightarrow a = 1/2 \rightarrow \Gamma \sim 360 \text{ MeV}$

**1/2<sup>+</sup>, KN in p-wave**  $\rightarrow a = \dots \rightarrow \Gamma \sim \text{** MeV}$   
small about factor 10 smaller

# Theta productions

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To obtain more information of  $\Theta -- J^P$

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(1)  $\gamma + n \rightarrow K^- + \Theta^+$  **Nam-Hosaka-Kim, PLB579, 43 (04)**

(2)  $K^*$  production

(3)  $K$ -induced **Hyodo-Hosaka-Oset, PLB579, 290 (04)**

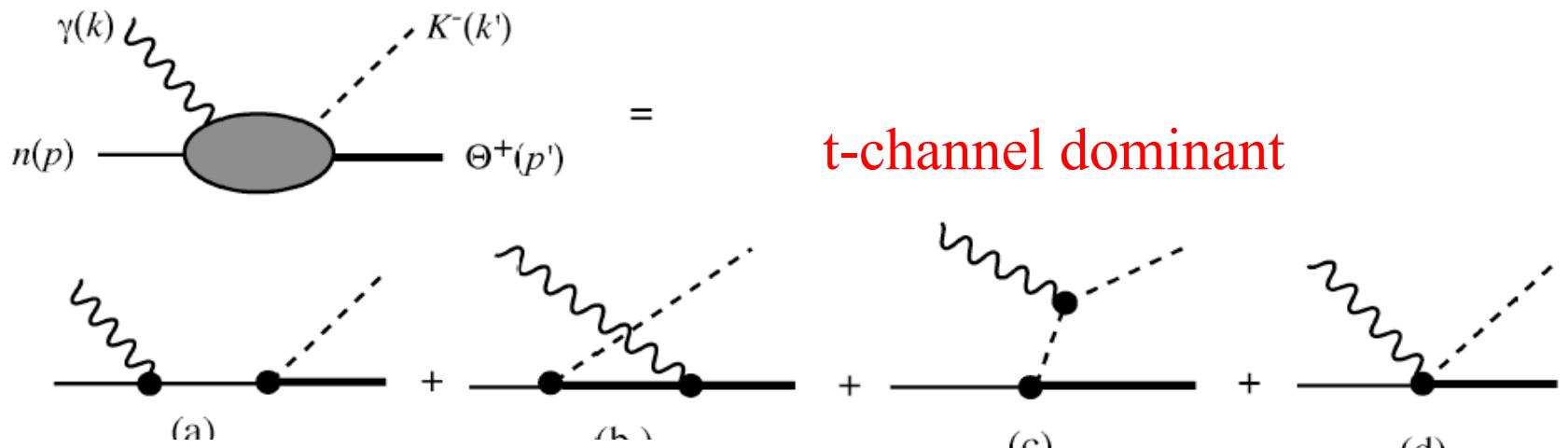
(4) Model-independent method

$$\overset{\rightarrow}{p} + \overset{\rightarrow}{p} \rightarrow \Theta^+ + \Sigma^+$$

**Thomas-Hicks-Hosaka, to appear in PTP**  
**Nam-Hosaka-Kim, hep-ph/0401074**  
**hep-ph/0402\*\*\***

$$(1) \gamma + n \rightarrow K^- + \Theta^+ \quad \text{Nam-Hosaka-Kim, PLB579, 43 (04)}$$

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Suppressed at  
High momentum transfer

# Cross sections

$\gamma n \rightarrow K^-\Theta$

t-channel  
dominance



Positive parity

Negative parity

150

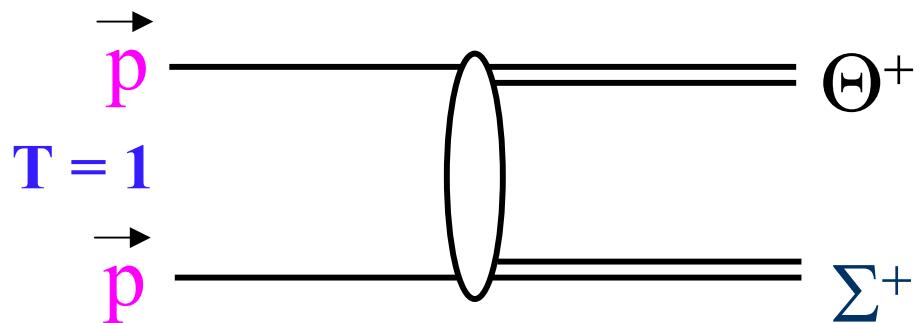
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# (4) Model-independent method

Thomas-Hicks-Hosaka, to appear in PTP



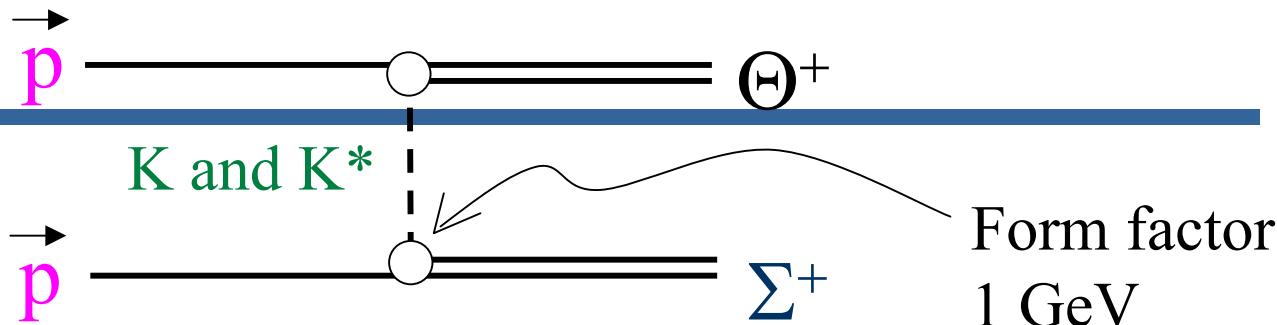
At threshold  
**S-wave dominant**

If  $S = 0$ , then  $L_i = \text{even}$ ,  $P = \text{even} \implies P(\Theta) = +$

If  $S = 1$ , then  $L_i = \text{odd}$ ,  $P = \text{odd} \implies P(\Theta) = -$

# Cross sections

Nam-Hosaka-Kim, hep-ph/0401074



Positive parity

Negative parity

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S=0

2729

S=1

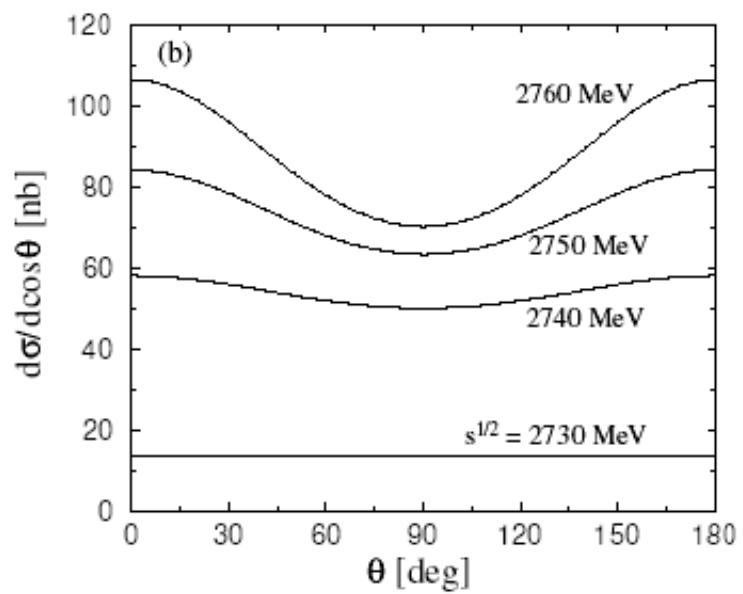
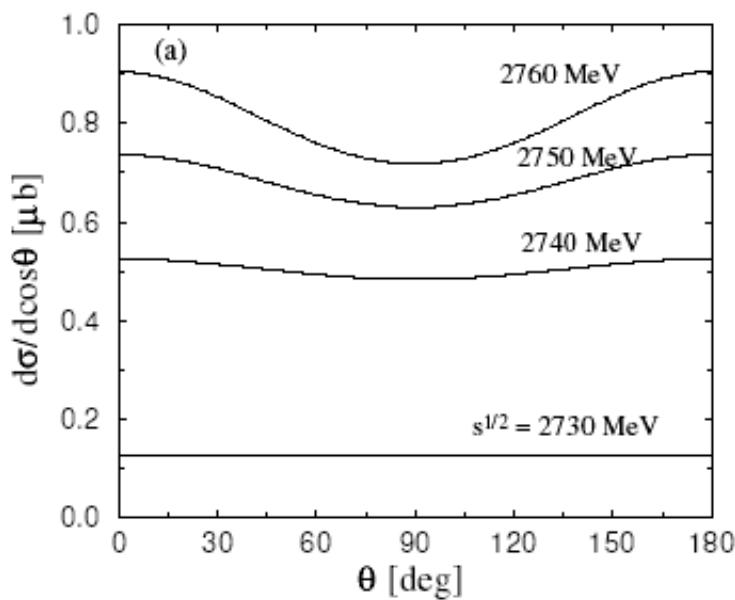
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S=1

S=0

# Angular dependence

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# Summary

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## ■ Positive parity

Diquark correlation

Spin-isospin force due to the hedgehog

## ■ Width

Too wide for  $1/2^-$ , several tens MeV for  $1/2^+$

## ■ Role of chiral symmetry, strangeness