

# Neutrino oscillation tomography

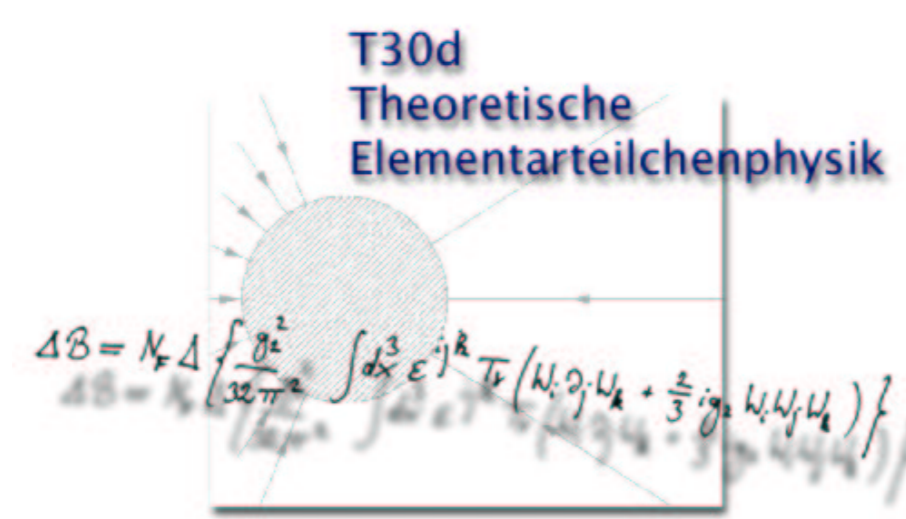
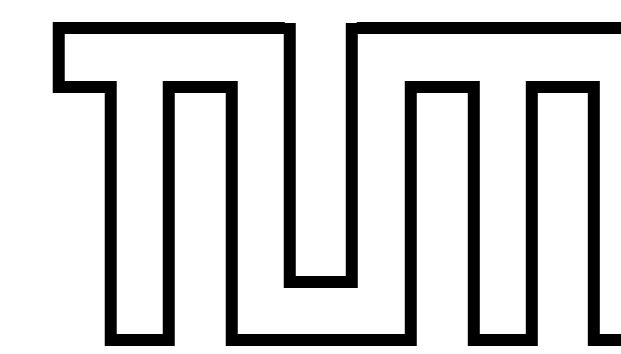
OR

What could be learned about the Earth's interior from neutrino oscillations in matter?

Tommy Ohlsson and Walter Winter

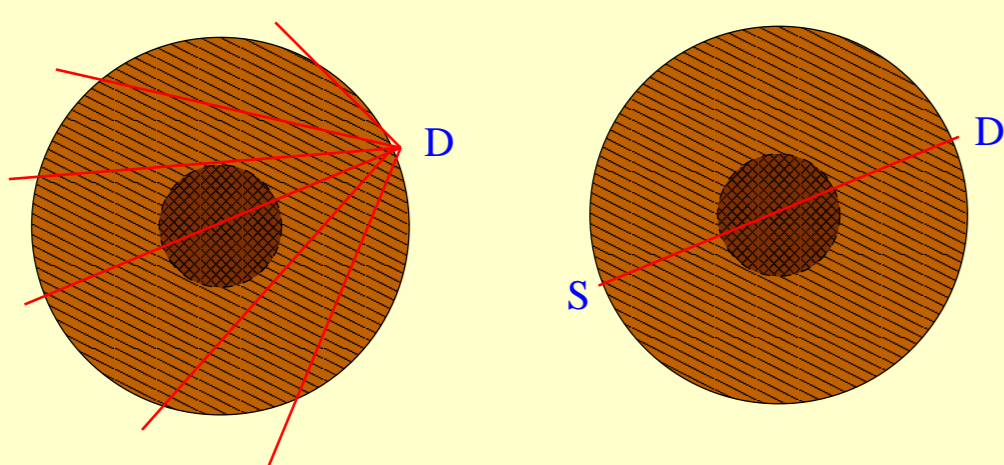
Technische Universität München

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## Neutrino tomography

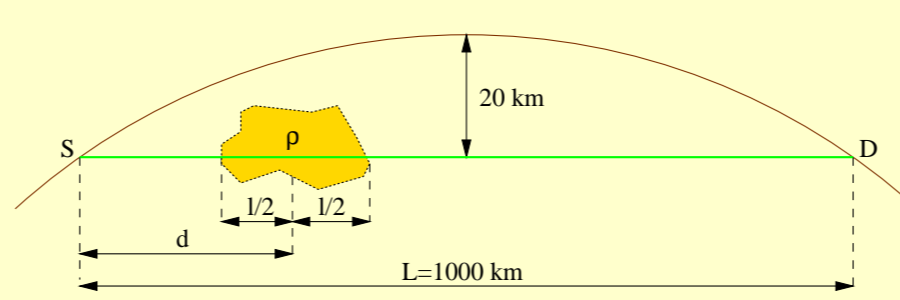
Neutrino absorption tomography      Neutrino oscillation tomography



Principle	Neutrino absorption in matter	MSW effect
Baselines	Many	One
Energies	$\geq$ TeV	$\sim 0.1 - 50$ GeV
Sources	Cosmic	Superbeams, Neutrino Factories
Analogy	X-ray tomography	Interference experiments
	De Rújula et al. (1983) and others	Ermilova et al. (1988) and others

## The search for large cavities in the Earth's mantle

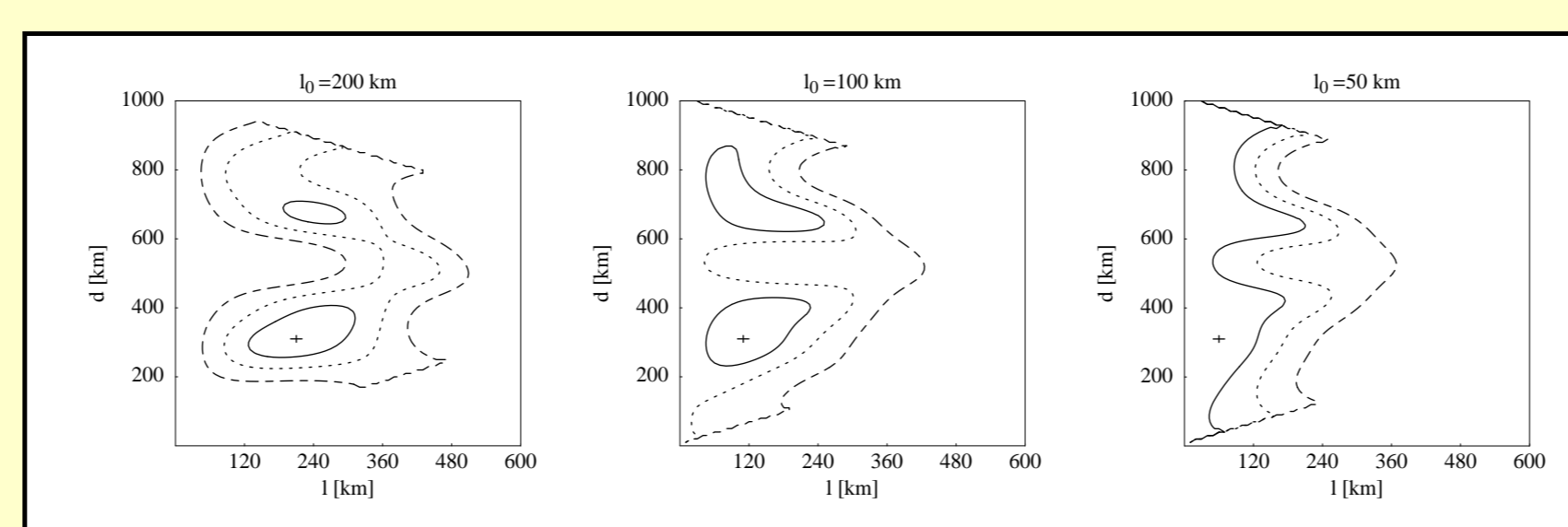
Experimental setup: Low energy superbeam 500 MeV,  $\nu_\mu \rightarrow \nu_e$



In this scenario:

- Cavity centered at  $d_0$  with length  $l_0$
- Maximum depth 20 km
- Average depth 13 km
- Average matter density:  $2.9 \text{ g/cm}^3$
- Matter density in the cavity:  $\rho = 1.0 \text{ g/cm}^3$

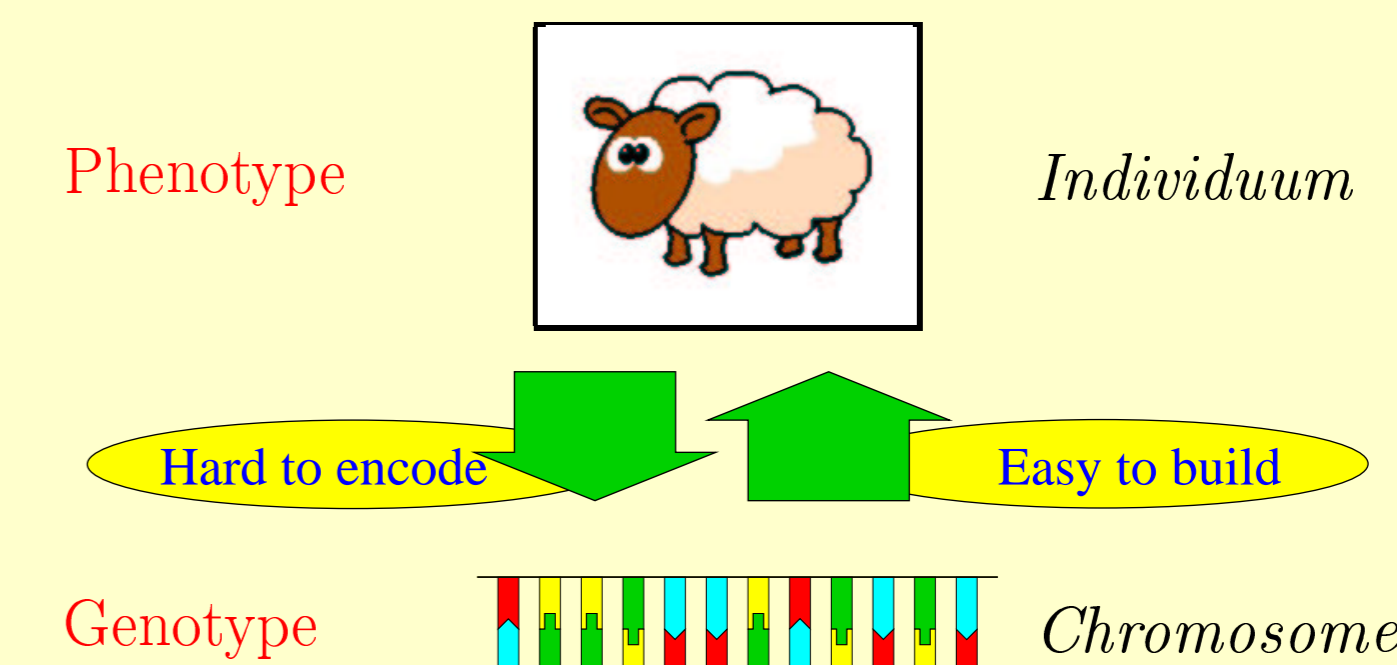
For a cavity centered at  $d_0 = 300$  km:



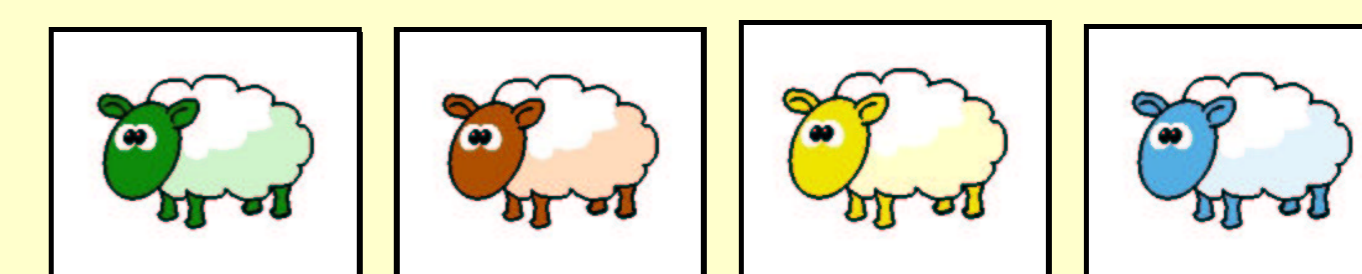
The cavity can be seen on the  $3\sigma$ -level for  $l_0 = 200$  km,  $1\sigma$ -level for  $l_0 = 100$  km and not at all for  $l_0 = 50$  km.

## Genetic algorithms ...

... for searching the high-dimensional parameter space



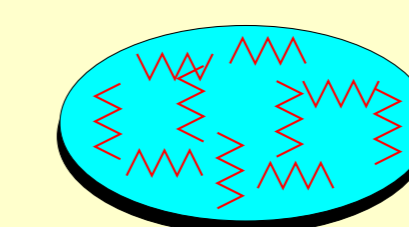
**Fitness function:** Survival probability of an individual in its environment



Sample fitness      0.5      0.9      0.3      0.8

Can be easily calculated for phenotype, but not for genotype  
→ Build individual from chromosome first, then calculate the survival probability

The genetic algorithm



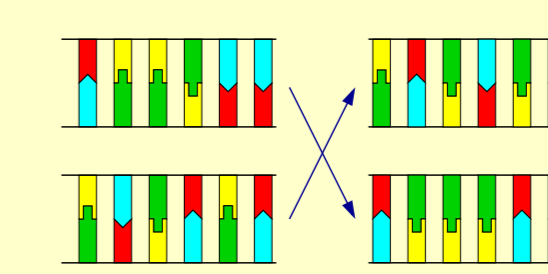
Generate initial generation of chromosomes by random

**Reproductive plan for the next generation:**

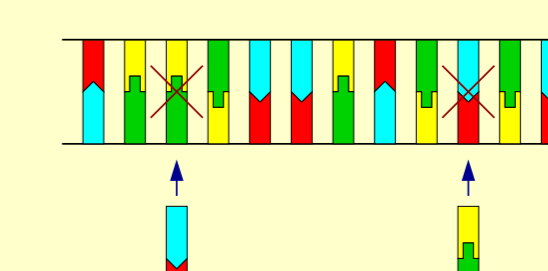
Create individual from each chromosome and calculate its fitness value

**Selection** Select two parent chromosomes by random with a probability proportional to the fitness value

**Crossover** Cross the two parent chromosomes at a random position

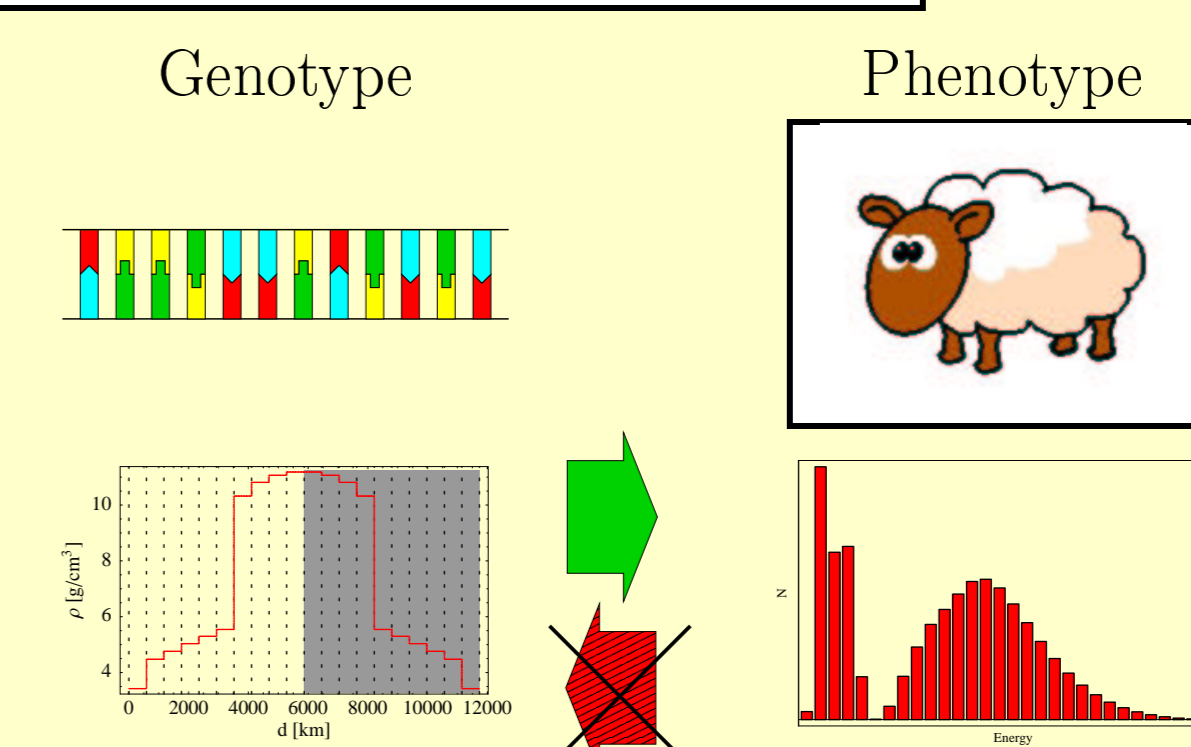


**Mutation** Mutate each position with a certain probability



→ Repeat until new generation is completely populated

Application to the reconstruction problem



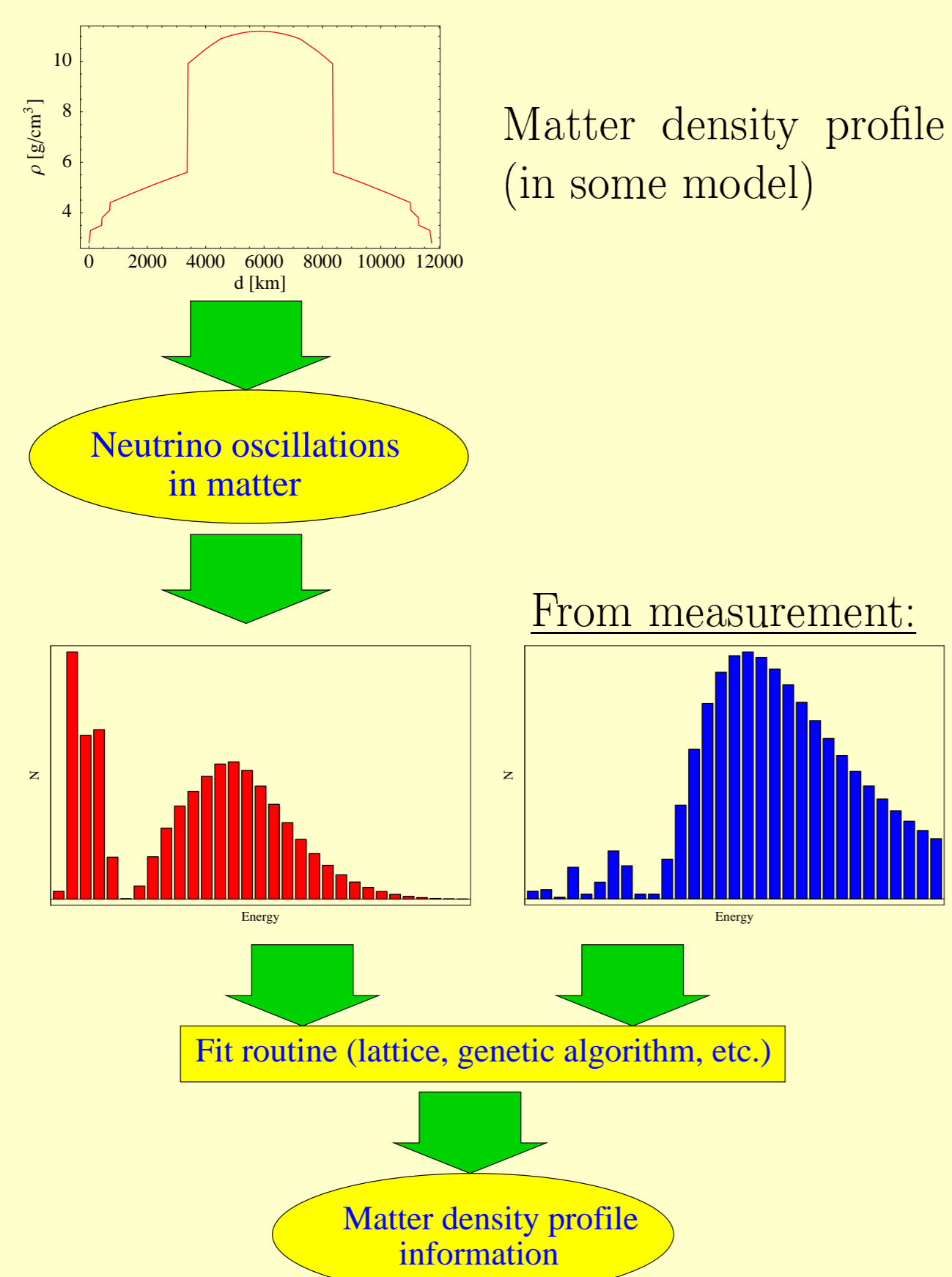
Fit to Measurement:

Genetic algorithms vs. lattice methods

Genetic algorithms	Lattice methods
Polynomial running time $\mathcal{O}(N^k)$	Exponential running time $\mathcal{O}(e^N)$
Finds optima also in between lattice points	May miss minima in between lattice points
May miss regions in parameter space if not enough trial runs	Searches parameter space systematically

## Principles

- Short or long baseline experimental setup
- Oscillation parameters assumed to be measured with high precision:  $\Delta m_{32}^2, \Delta m_{21}^2, \theta_{13}, \theta_{12}, \theta_{23}, \delta_{CP}$



The evolution operator method

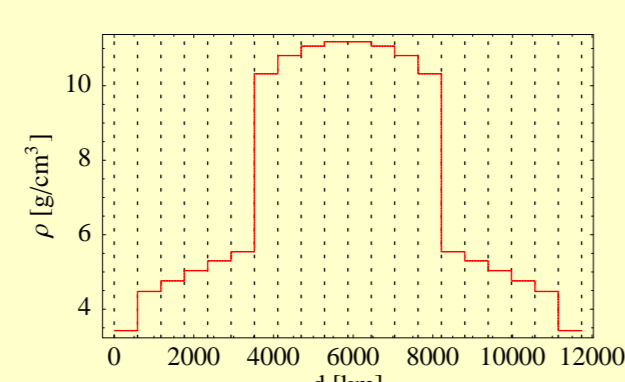
Propagation in a layer of length  $x_j$  and constant density  $\rho_j$  described by evolution operator

$$U(x_j, \rho_j) = e^{-i\mathcal{H}(\rho_j)x_j}$$

where  $\mathcal{H}(\rho_j)$  is the Hamiltonian in constant matter density

$$\mathcal{H}(\rho_j) = U \begin{pmatrix} 0 & 0 \\ 0 & \frac{\Delta m_{31}^2}{2E} \\ 0 & 0 \\ 0 & 0 \\ 0 & \frac{\Delta m_{21}^2}{2E} \\ 0 & 0 \end{pmatrix} U^\dagger + \begin{pmatrix} A(\rho_j) & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

For an arbitrary matter density (step) profile

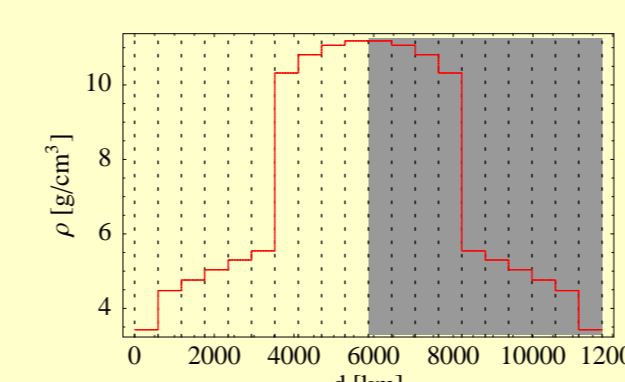


$$P_{\alpha\beta} = |\langle \nu_\beta | U(x_n, \rho_n) \dots U(x_1, \rho_1) | \nu_\alpha \rangle|^2$$

Note that in general  $[U(x_i, \rho_i), U(x_j, \rho_j)] \neq 0$  for  $i \neq j$   
→ Additional information by **interference effects** compared to neutrino absorption tomography

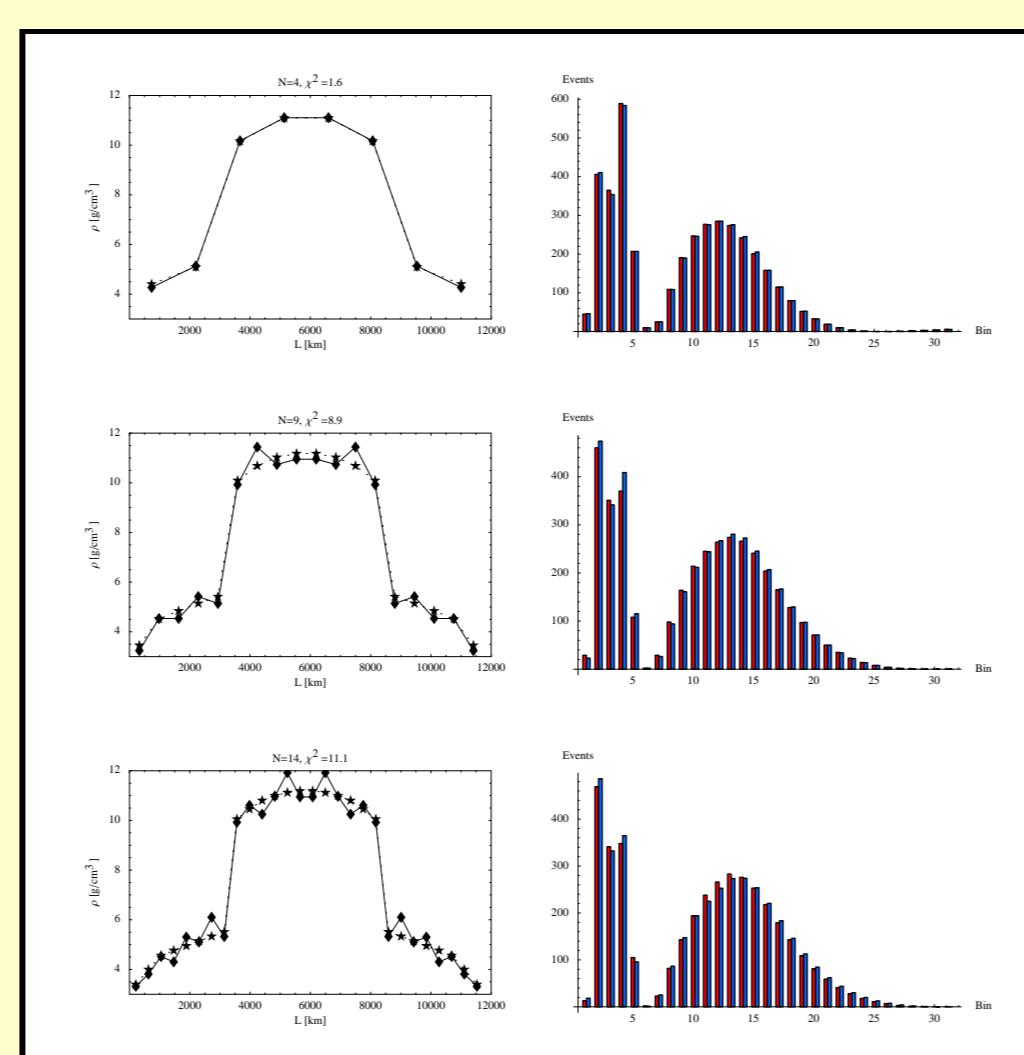
## Reconstruction of the Earth's matter density profile

Experimental setup: 20 GeV neutrino factory, baseline  $L = 11700$  km,  $\nu_\mu \rightarrow \nu_e$   
Symmetric Earth matter density profile with  $2N$  layers assumed, which means that the dimension of the parameter space is  $N$ .



Use **genetic algorithm** with many trial runs to find matter density profiles fitting the measured energy spectrum.

Best results of genetic algorithm fits ( $N = 4, 9, 14$ ):



All results are within the  $1\sigma$  level. Therefore a preciser measurement is not possible and small fluctuations in mantle and core are not resolvable.

Examples for matter density profiles close to the  $1\sigma$  (first row),  $2\sigma$  (second row), and  $3\sigma$  (third row) contours:

