Theoretical Uncertainties in Sparticle Mass Predictions

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We contrast the sparticle spectra obtained from three modern publicly available codes along model lines in minimal supersymmetric standard model (MSSM) parameter space. From this we gain an idea of the uncertainties involved with sparticle spectra calculations. The differences in predicted sparticle masses are typically at the several percent-level. In the focus-point scenario, there are differences of 30% in the weak gaugino masses. These uncertainties need to be reduced in order to obtain accurate information about fundamental models of supersymmetry breaking.

MSSM phenomenology is so complicated that studies of the ability of future colliders to search for and measure supersymmetric parameters has focused on isolated ‘bench-mark’ model points Abramowicz et al. [1999], Allanach et al. [2000a], Battaglia et al. [2001]. This approach, while being a start, is not ideal because one is not sure how many of the features used in the analyses will apply to other points of parameter space. In an attempt to cover more of the available parameter space, the Direct Investigations of SUSY Subgroup of SNOWMASS 2001 has proposed eight bench-mark model lines for study.

The lines have been defined to have the spectrum output from the ISASUGRA program (part of the ISAJET7.51 package Baer et al. [1999]) for \( m_t = 175 \) GeV. ISASUGRA solves the MSSM normalization group equations subject to boundary conditions at low energy (measured Standard Model couplings and constraints from consistent electroweak symmetry breaking) and a higher energy scale (the theoretical boundary condition on the soft-mass parameters). Knowledge of the uncertainties will be important when data is confronted with theory, i.e. when information upon a high-energy SUSY breaking sector is sought from low-energy data. Here, we intend to investigate the theoretical uncertainties in sparticle mass determination. To this end, we contrast the sparticle masses predicted by three modern publicly available supported codes: ISASUGRA, SOFTSUSY Allanach [2001] and SUSPECT Djouadi et al. [1998].

Each of the three packages calculates sparticle masses in a similar way, but with different approximations Moretti [2001]. In each of the model line scenarios, we calculate the fractional difference for some sparticle \( s \)

\[
  f_{\text{CODE}} = \frac{m_s^{\text{ISASUGRA}} - m_s^{\text{CODE}}}{m_s^{\text{ISASUGRA}}},
\]

where CODE refers to SOFTSUSY1.2, or SUSPECT2.0. \( f_{\text{CODE}} \) then gives the fractional difference of the mass of sparticle \( s \) between the predictions of CODE and ISASUGRA. A positive value of \( f_{\text{CODE}} \) then implies that \( s \) is heavier in ISASUGRA than in CODE.

We focus upon model lines in scenarios which are currently supported by all three packages, i.e. supergravity mediated supersymmetry breaking (mSUGRA). At a high unification scale \( M_{\text{GUT}} = 1.9 \times 10^{16} \) GeV, the soft-breaking scalar masses are set to be all equal to \( m_0 \), the universal scalar trilinear coupling to \( A_0 \) and each gaugino mass \( M_{1,2,3} \) is set. \( \tan \beta \) is set at \( M_Z \). The three

Table I Model lines in mSUGRA investigated here. \( m_t = 175 \) GeV, \( M_{\text{GUT}} = 1.9 \times 10^{16} \) GeV and \( \alpha_s(M_Z)_{\overline{MS}} = 0.119 \) are used.

<table>
<thead>
<tr>
<th>Model line</th>
<th>( \tan \beta )</th>
<th>( A_0 )</th>
<th>( M_1 )</th>
<th>( M_2 )</th>
<th>( M_3 )</th>
<th>( m_0 )</th>
<th>( \text{sgn} \mu )</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>10</td>
<td>-0.4M_{1/2}</td>
<td>M_{1/2}</td>
<td>M_{1/2}</td>
<td>M_{1/2}</td>
<td>0.4M_{1/2}</td>
<td>+</td>
</tr>
<tr>
<td>B</td>
<td>10</td>
<td>0</td>
<td>1.6M_{2}</td>
<td>M_{2}</td>
<td>M_{2}</td>
<td>M_{2/2}</td>
<td>+</td>
</tr>
<tr>
<td>F</td>
<td>10</td>
<td>0</td>
<td>M_{1/2}</td>
<td>M_{1/2}</td>
<td>M_{1/2}</td>
<td>2M_{1/2} + 800 GeV</td>
<td>+</td>
</tr>
</tbody>
</table>

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choices of model lines are displayed in Table I. Model line A displays gaugino mass dominance, ameliorating the SUSY flavor problem. Model line B has non-universal gaugino masses and model line F corresponds to focus-point supersymmetry Feng et al. [2000], close to the electroweak symmetry breaking boundary.

We pick various sparticle masses that show a large difference in their prediction between the three calculations. For model line A, Fig. 1a shows $f_{\tilde{\tau}_1, \tilde{b}_1, \tilde{q}_1, \tilde{h}_0, \tilde{\chi}^0_1, \tilde{\chi}^+_1, \tilde{g}}$ (the lightest stau, sbottom, squark, neutral Higgs, neutralino, chargino and gluino mass difference fractions respectively). Fig. 1b shows the equivalent results for the output of SUSPECT. Model line B differences are shown in Fig. 2. Jagged curves in the figures are a result of numerical error in the ISASUGRA calculation, and are at the 1% level for squarks, gluinos and the lightest neutralino. The stau, lightest Higgs and lightest chargino do not display any appreciable numerical error. We have checked that SOFTSUSY and SUSPECT do not have any numerical error that is detectable by eye for any of the sparticles.

Figs. 1, 2 share some common features. In general, the largest discrepancies occur for low $M_{1/2}$, where the super-particle spectrum is lightest. The gluino and squark masses are consistently around 5% lower in ISASUGRA than the other two codes, which agree with each other to better than 1%. We note here that this uncertainty is not small, a 5% error on the gluino mass at $M_{1/2} = 700$ GeV in model A corresponds to an error on the predicted gluino mass of 37.5 GeV, for example. The lightest neutralino mass predicted by SUSPECT is in agreement with ISASUGRA to 2%, whereas
SOFTSUSY predicts this neutralino to be lighter by another 2% or so. The Higgs masses also agree to above 2% between each code and ISASUGRA, but SOFTSUSY and SUSPECT have opposite sign differences. This is probably due to the fact that SOFTSUSY uses a FeynHiggsFast calculation of the neutral Higgs masses with important two-loop effects added Heinemeyer et al. [1999], which predicts masses that tend to be higher than the one-loop calculation (as used in ISASUGRA or SUSPECT). The stau mass also looks fairly consistent between SUSPECT and SOFTSUSY (2% lighter than ISASUGRA), but this could conceivably be due to their one-loop running of scalar masses, or their inclusion of threshold corrections to the stau. The lightest neutralino mass shows large deviations between all codes up to 5%, and this is not currently understood.

The focus-point scenario (model line F) is displayed in Fig. 3. The overall view of spectral differences is similar to that in model lines A and B except for the masses of the lightest chargino and neutralino. They display large 10-30% differences. The large spikes come from numerical errors in the ISASUGRA calculation. In focus point supersymmetry, the bilinear Higgs mass parameter \( \mu \) is close to zero and is very sensitive to threshold corrections to \( m_t \) Allanach et al. [2000b]. For small \( \mu < M_Z \), the lightest chargino and neutralino masses become sensitive to its value. The predicted value of \( \mu(M_Z) \) differs by 50%-100% between all of the three code’s output. Only a few of the threshold corrections to \( m_t \) are included in the ISASUGRA calculation, whereas SOFTSUSY, for example, includes all one-loop corrections with sparticles in the loop. SUSPECT also adds many of the sparticle loop corrections to \( m_t \).

In order to discriminate high energy models of supersymmetry breaking, it will necessary to have better than 1% accuracy in both the experimental and theoretical determination of superparticle masses Allanach et al. [work in progress]. An alternative bottom-up approach Blair et al. [2001] is to evolve soft supersymmetry breaking parameters from the weak scale to a high scale once they are ‘measured’. The parameters of the high-scale theory are then inferred, and theoretical errors involved in the calculation will need to be minimised. We note that possible future linear colliders could determine some sparticle masses at the per-mille level Aguilar-Saavedra et al. [2001]. An increase in accuracy of the theoretical predictions of sparticle masses by about a factor 10 will be necessary.

Acknowledgments

I would like to warmly thank Werner Porod for his comments on the work.

References

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