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# Experimental aspects of $B \rightarrow DK$ at $10^{36}$

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# Introduction

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- **Goal: estimate of reach in  $\gamma$  of  $B \rightarrow DK$  analysis at  $10 \text{ ab}^{-1}$** 
  - Look for modes that are experimentally and theoretically clean & easy
  - Systematics will be important, look at modes where we have some understanding of systematic issues
  - Focus on Gronau-London-Wyler ( $B^- \rightarrow D_{\text{CP}}^0 K^-$ ) and Atwood-Dunietz-Soni ( $B^- \rightarrow \bar{D}^0 K^-$ ), [  $D^*$ ,  $K^*$  modes not considered ]
- **Outline**
  - Examine existing GLW analysis, project stat+sys errors on observables at  $10 \text{ ab}^{-1}$
  - Examine ADS analysis effort, project stat+sys errors on observables for  $10 \text{ ab}^{-1}$
  - Combine GLW and ADS projections and look at impact on measurement of  $\gamma$
- **Caveat**
  - There are many unknowns parameters in this prediction that play important role precision extrapolation (strong phases,  $r_B$ , systematic uncertainties)
  - Will consider optimistic and pessimistic assumptions for unknowns



# Gronau-London-Wyler – Introduction

- Method: measure BFs for  $B^- \rightarrow D^0_{(CP)} K^-$
- Observables sensitive to  $\gamma$

$$r_B = \frac{A(b \rightarrow u)}{A(b \rightarrow c)}$$

$$R_{CP\pm} = 2 \frac{\Gamma(B^- \rightarrow D^0_{CP\pm} K^-) + \Gamma(B^+ \rightarrow D^0_{CP\pm} K^+)}{\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^- \rightarrow \bar{D}^0 K^-)} = 1 + r_B^2 \pm 2r_B \cos d_B \cos g$$

$$A_{CP\pm} = \frac{\Gamma(B^- \rightarrow D^0_{CP\pm} K^-) - \Gamma(B^+ \rightarrow D^0_{CP\pm} K^+)}{\Gamma(B^- \rightarrow D^0_{CP} K^-) + \Gamma(B^- \rightarrow \bar{D}^0_{CP} K^-)} = \frac{\pm 2r_B \sin d_B \sin g}{1 + r_B^2 + 2r_B \cos d_B \sin g}$$

- 4 measurements:  $R_{CP+}$ ,  $R_{CP-}$ ,  $A_{CP+}$ ,  $A_{CP-}$ 
  - Actually only 3 independent measurements as  $A_{CP+}$  and  $A_{CP-}$  measure the same combination of unknowns up to a sign
- 3 unknowns:  $\gamma$ ,  $r_B$ ,  $\delta_B$  (strong phase)



# Gronau-London-Wyler – Experimental status

BaBar (89M BB)

Belle (86M BB)

$A_{CP+}$	$0.07 \pm 0.17 \pm 0.06$	$0.06 \pm 0.19 \pm 0.04$
$A_{CP-}$	-	$-0.19 \pm 0.17 \pm 0.05$

$R_{CP+}$	$(8.8 \pm 1.6 \pm 0.5)/(8.31 \pm 0.35 \pm 0.20) =$ $1.06 \pm 0.20 \pm ???$	$1.21 \pm 0.25 \pm 0.14$
$R_{CP-}$	-	$1.41 \pm 0.27 \pm 0.15$

## • Notes

- $R_{CP\pm}$  measured as double ratio

$$R_{CP\pm} = 2 \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D^0 p^-) + \Gamma(B^- \rightarrow \bar{D}^0 p^-)} \bigg/ \frac{\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow \bar{D}^0 K^+)}{\Gamma(B^- \rightarrow D^0 p^-) + \Gamma(B^- \rightarrow \bar{D}^0 p^-)}$$

- BaBar result does not publish double ratio, only its components
  - Systematics on ratio components correlated, cannot trivially combined them.
  - Will assume Belle/BaBar similar here and use Belle systematic



# Gronau-London-Wyler – Extrapolated precision

- Statistical error on  $A_{CP}$  and  $R_{CP}$ 
  - Assume  $\sqrt{N}$  scaling: 100x more data, errors reduce by factor 10
  - $s(A_{CP})_{stat} = 1.6\% \text{ at } 10 \text{ ab}^{-1}$ ,  $s(R_{CP})_{stat} = 2.0\% \text{ at } 10 \text{ ab}^{-1}$ ,

- Systematic uncertainty on  $A_{CP}$

- Magnitude at 100M BB pairs = 0.05-0.06
- Breakdown of systematic uncertainty as advertised:

*Belle: 5% = 2.4-3.4% yield extraction +  
3.2% detector charge asymmetry +  
1% PID charge asymmetry*

*BaBar: 6% = 4% detector charge asymmetry +  
4% yield extraction*

- How will this scale with lumi?
  - Yield extraction component will scale with lumi (signal/bkg shapes fitted from data)
  - Detector charge asymmetry measured from  $B \rightarrow D_{CP}^0 \pi^-$  control sample (BaBar), will improve with increased statistics, but may not scale entirely by  $\sqrt{N}$
- Estimate at 10 ab<sup>-1</sup>:
  - 0.4% yield ext ( $\sqrt{N}$ ) + 1-3% charge asym. (opt-pess).  $\rightarrow$  1.1% - 3%



# Gronau-London-Wyler – Experimental precision

- Systematic uncertainty on  $R_{CP}$ 
  - Magnitude at 100M BB pairs = 0.15 (Belle)
    - No systematic estimate from BaBar on ratio of ratios
  - Breakdown of systematic uncertainty sources
    - BaBar does not have a syst estimate on this ratio
    - Belle PRD not rich with details, indicates sys.err mostly yield extraction
  - Alternative approach: what detector systematic don't cancel in ratio of BF's

$$R_{CP\pm} = 2 \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^- \rightarrow \bar{D}^0 K^-)}$$

- Mainly  $D_{CP}^0$  vs  $D^0$  selection: yield extraction (sqrtN), daughter PID (1-2%?)
  - Estimate at  $10 \text{ ab}^{-1}$ :
    - 1.5% from yield (sqrt N) + 1-4% from PID (opt-pess) = 2.1 - 5%
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- Summary of errors on GLW observables at  $10 \text{ ab}^{-1}$ 
    - $R_{CP} = 0.02 \text{ stat } \dot{\text{A}} (0.02-0.05) \text{ sys}$
    - $A_{CP} = 0.016 \text{ stat } \dot{\text{A}} (0.015-0.04) \text{ sys}$

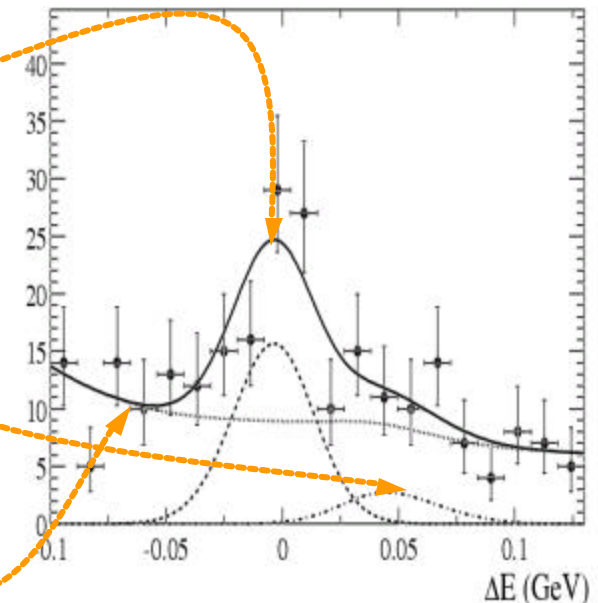


## Gronau-London-Wyler – Adjusting for detector performance

- Sensitivity to detector performance
  - So far have assumed that BaBar and ‘super BaBar’ have similar detector performance.
  - Look at effects of
    - different tracking resolution (mD/DE resolution),
    - PID performance (peaking bkg),
    - increased continuum (or other non-BB) background (flattish background)

- Crude ToyMC study on  $B^- \rightarrow D^0_{CP} K^-$  yield fit

- +/-30% change in  $\Delta E, m(D^0)$  resolution gives ~20% change in stat error on yield
- PID performance change has marginal effect (x4 increase of K/pi misID rate has negligible impact on yield error)
- Factor 2 increase in continuum bkg gives a 23% larger stat error on the signal yield
- Present  $D^0_{CP} K^-$  analysis has still some room for improvement for continuum suppression...





# Atwood-Dunietz-Soni -- Introduction

- Method: Measure  $\text{BF}(B^- \rightarrow [K^+\pi^-]_{D^0} K^-)$ 
  - Interference between (DCB B decay + CF D decay) and (CF B decay + DCS D decay),  $D^0$  to flavor eigenstate
- Observables sensitive to  $\gamma$

$$R_{\pm}^{ADS} = \frac{\Gamma(B^{\mp} \rightarrow [K^{\pm}p^{\mp}]_{D^0} K^{\mp})}{\Gamma(B^{\mp} \rightarrow D^0 K^{\mp})} = r_B^2 + r_D^2 + r_B r_D \cos(\mathbf{d}_B + \mathbf{d}_D \pm \mathbf{g})$$

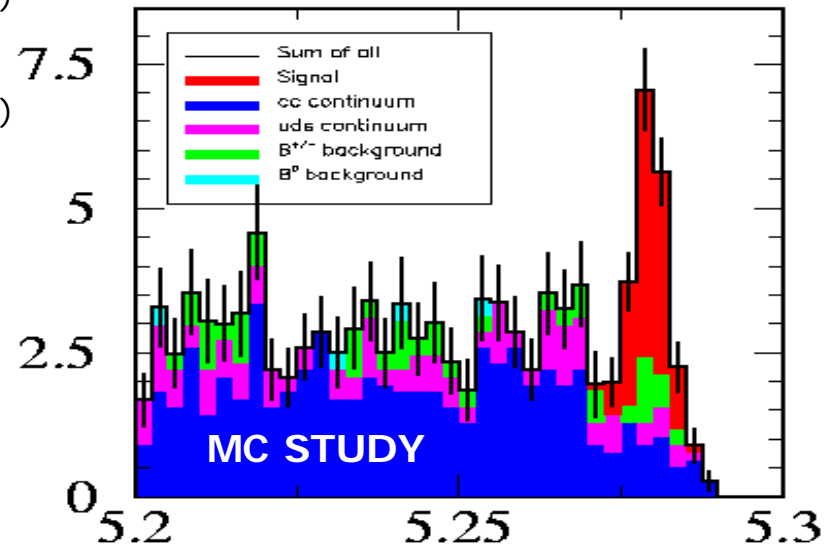
$r_D \equiv \sqrt{\frac{B(D^0 \rightarrow K^+ p^-)}{B(D^0 \rightarrow K^- p^+)}} \approx 0.0624$

- 2 measurements per  $D^0$  mode
- 2 unknowns ( $\gamma, \delta_B$ ) + 1 unknown per  $D^0$  mode ( $\delta_D$ )
- Need at least two  $D^0$  modes for ADS-only constraint on  $\gamma$  (4 measurements with 4 unknowns)
  - But single ADS mode can be combined with GLW results to provide additional constraints
  - $\delta_D$  could also be measured by CLEO-C (one less unknown)



## Atwood-Dunietz-Soni – Experimental status, extrapolation

- BaBar: measurement in progress, Belle unknown
  - No public result yet, but work in progress → have good estimates of stat and sys uncertainties
- Statistical error  $R^{\text{ADS}} (D^0 \rightarrow K\pi)$ 
  - Depends strongly on  $\text{BF}(B^- \rightarrow [K^+\pi^-]_{D^0} K^-)$ , which is not measured up to know. Estimates range from  $[0-10] \times 10^{-7}$ 
    - 0 if  $r_B=0.1$  and fully destructive interf,  $10 \times 10^{-7}$  if  $r_B=0.2$  and constructive interf
  - MC Study: assuming BF of  $5 \times 10^{-7}$  yield is 13 events at  $100 \text{ fb}^{-1}$  (at 21% eff.) → error = 35% at  $100 \text{ fb}^{-1}$ , 3.5% at  $10 \text{ ab}^{-1}$ 
    - If  $\text{BF}=1 \times 10^{-7}$ , stat error 10.8% ( $10 \text{ ab}^{-1}$ )
    - If  $\text{BF}=2 \times 10^{-7}$ , stat error 6.3% ( $10 \text{ ab}^{-1}$ )
    - If  $\text{BF}=10 \times 10^{-7}$ , stat error 2.2% ( $10 \text{ ab}^{-1}$ )
  - Stat error on  $\text{BF}(B^- \rightarrow D^0 K^-)$  (denominator of  $R^{\text{ADS}}$ ) is negligible compared to  $\text{BF}(B^- \rightarrow [K^+\pi^-]_{D^0} K^-)$  contribution





# Atwood-Dunietz-Soni – Extrapolation

- Systematic error on  $R^{\text{ADS}} (D^0 \rightarrow K\pi)$ 
$$R_{\pm}^{\text{ADS}} = \frac{\Gamma(B^- \rightarrow \bar{D}^0 K^-)}{\Gamma(B^- \rightarrow D^0 K^-)}$$
  - *Nearly all systematic uncertainties cancel in ratio*, only left with yield extraction systematics, which scale like  $\sqrt{N}$  and PID asymmetry ( $\sim 1\%$ )
  - Toy MC study shows that yield extraction systematic about half of statistical error
  - Systematic at  $10 \text{ ab}^{-1} = 1\text{-}5\%$ , depending on BF
- Errors on  $R^{\text{ADS}}$  from other  $D^0$  decays
  - $D^0 \rightarrow K^- \pi^+ \pi^0$  and  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$  require investigation of Dalitz plots, systematics of full Dalitz analysis unknown
  - Quasi two-body analysis will probably give sensitivity similar to  $K^- \pi^+$  (higher BF and lower acceptance roughly cancel)
- Summary of errors on ADS observables at  $10 \text{ ab}^{-1}$ 
  - $D^0 \rightarrow K^- \pi^+$ :  $R_{\text{ADS}} = (2\text{-}10)\% \text{ stat} \hat{\wedge} (1\text{-}5)\% \text{ sys (dep. on BF)}$
  - Additional  $D^0$  modes expected to have similar sensitivity, but Dalitz issues complicates analysis and prediction for  $10 \text{ ab}^{-1}$



## Atwood-Dunietz-Soni – Adjusting for detector performance

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- What happens to prediction of tracking resolution, PID performance, backgrounds are different at  $10^{36}$ ?
  - Tracking resolution: 30% change in  $m(D^0)/\Delta E$  resolution will give ~20% change in stat error
  - PID performance: negligible effect, except at very low BF
  - Backgrounds: may go up due to additional non-BB backgrounds. ADS continuum suppression already BaBar state-of-the art.  
Increase in background by factor 2 results 10-60% increase of stat error, depending on BF
    - At  $BF=1 \times 10^{-7}$ : Stat err 11%  $\rightarrow$  18% (60% increase)
    - At  $BF=2 \times 10^{-7}$ : Stat err. 6.3%  $\rightarrow$  7.5%
    - At  $BF=5 \times 10^{-7}$ : Stat err. 3.5%  $\rightarrow$  3.9%
    - At  $BF=10 \times 10^{-7}$ : Stat err. 2.2%  $\rightarrow$  2.4% (10% increase)



# Translating $B \rightarrow DK$ results in measurement of $\gamma$

- Projected uncertainties:
  - **GLW:**  $s(R_{CP}) = 0.02 \text{ stat } \text{\AA} \text{ (0.021-0.05) sys}$  + ~30% uncertainty due to tracking, PID, bkg changes  
 $s(A_{CP}) = 0.016 \text{ stat } \text{\AA} \text{ (0.015-0.04) sys}$
  - **ADS:**  $s(R_{ADS}) = (2-10)\% \text{ stat } \text{\AA} \text{ (1-5)\% sys}$  + ~20-60% uncertainty due to bkg changes
- Resulting experimental **resolution on  $\gamma$**  also **depends** strongly on true values of  **$\gamma$ , strong phases**, and most importantly  **$r_B$** 
  - Sensitivity of both methods proportional to  $r_B^2$  ( $r_B \sim 0.1-0.3$ )
  - Projection on gamma resolution are somewhat speculative...
  - Will run through a few scenarios

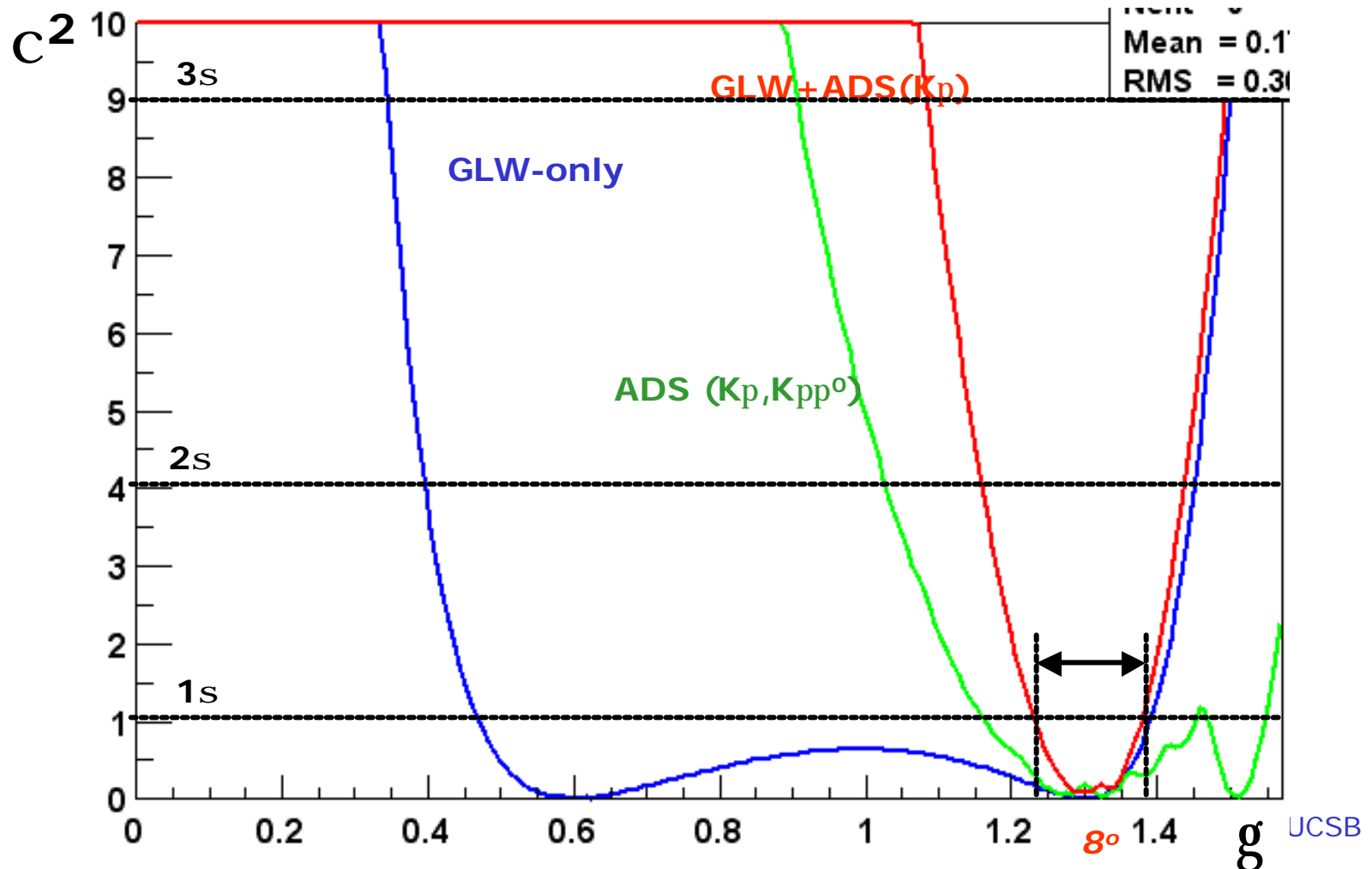


# Translating $B \rightarrow DK$ results in measurement of $\gamma$

- $\gamma_{\text{true}} = 60^\circ$ ,  $r_{B\text{true}} = 0.2$ ,  $\delta B_{\text{true}} = 15^\circ$ ,  $\delta D_{\text{true}} = 30^\circ$ ,  $\sigma(R_{CP}) = 0.03$ ,  $\sigma(A_{CP}) = 0.02$ ,  $\text{BF(ADS)} = 5 \times 10^{-7}$

*$r_{B,S}(\text{GLW}), S(\text{ADS})$  optimistic*

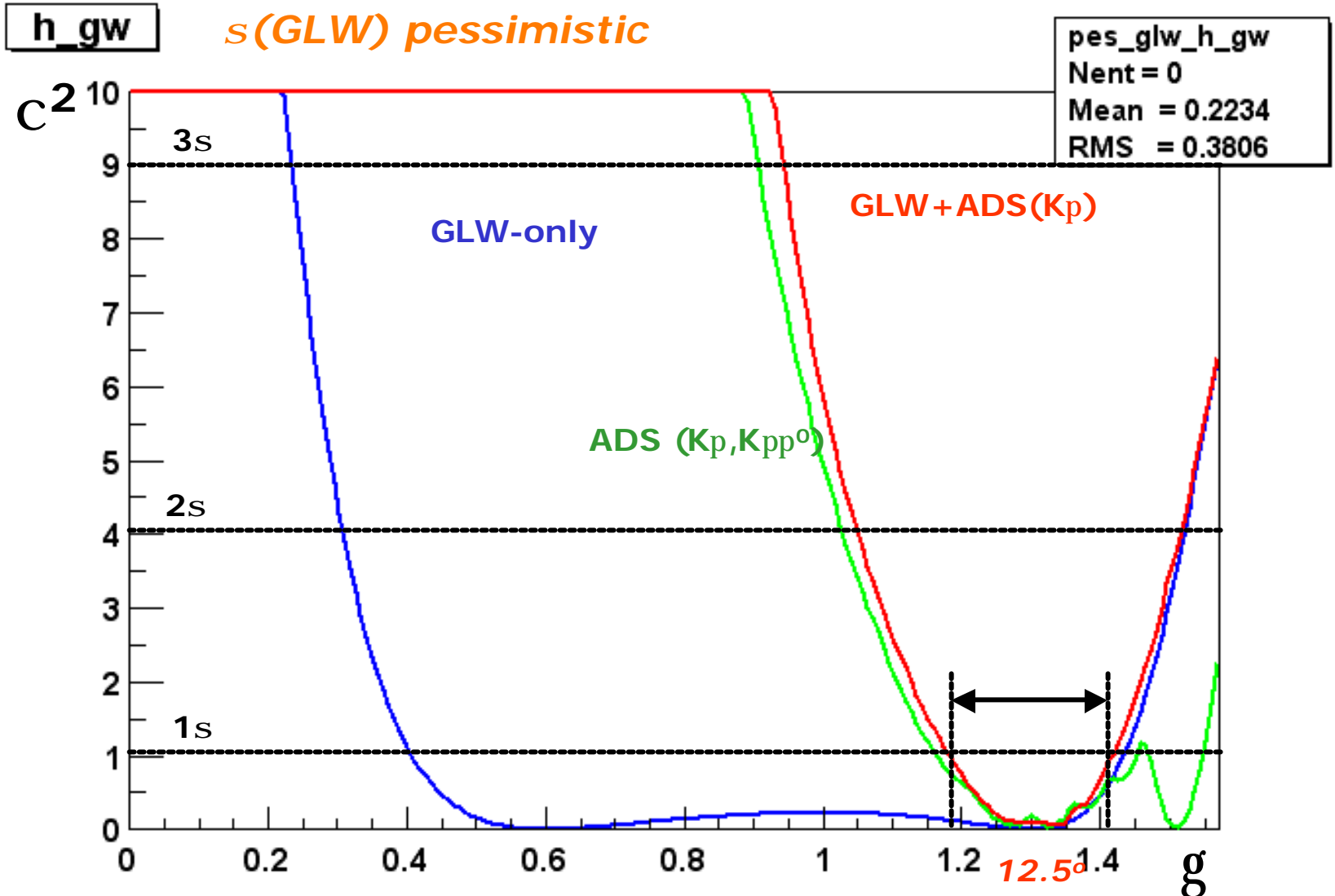
*Combining GLW+ADS  
very effective for  $g$*





# Translating $B \rightarrow DK$ results in measurement of $\gamma$

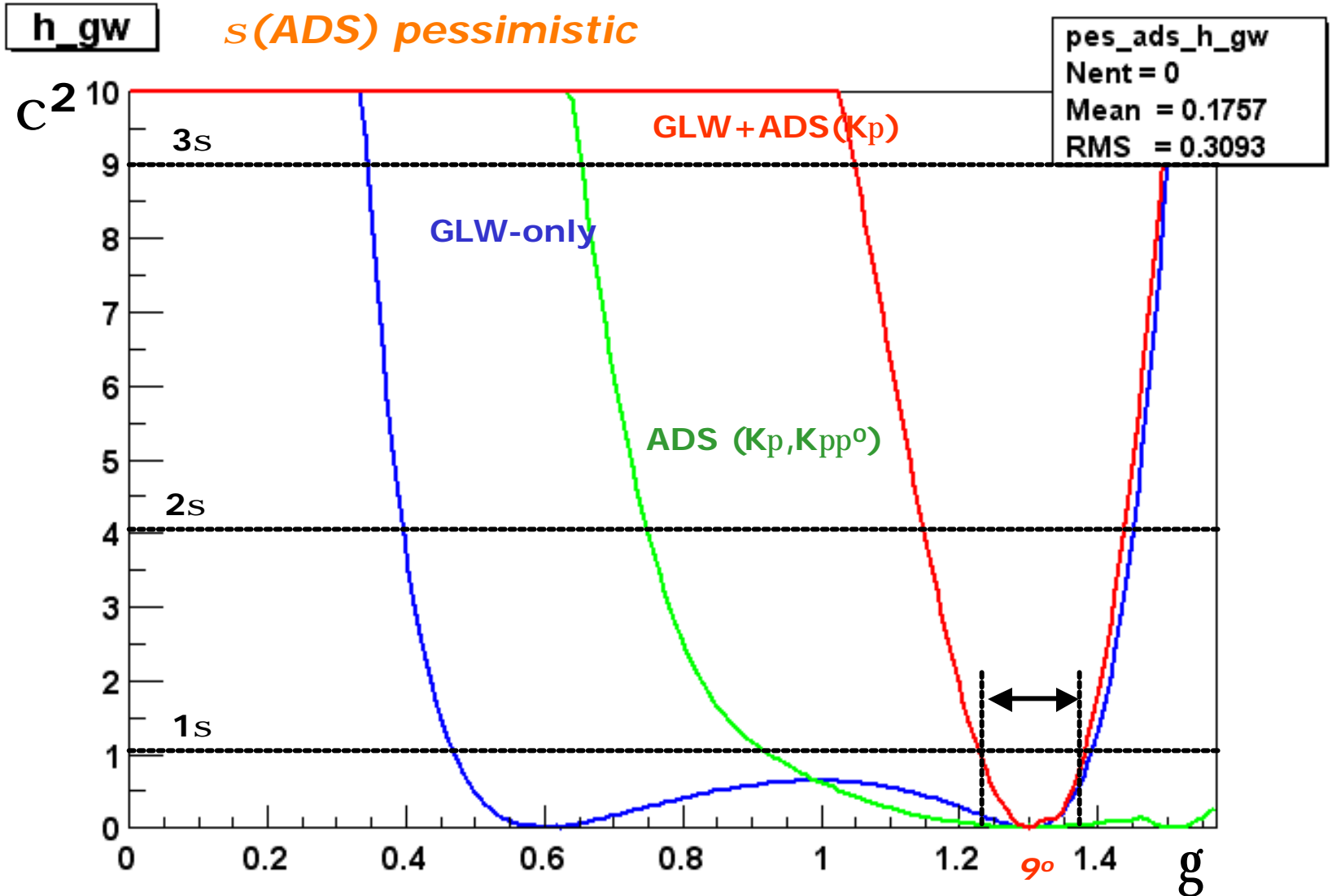
- $\gamma_{\text{true}} = 60^\circ$ ,  $r_{B\text{true}} = 0.2$ ,  $\delta B_{\text{true}} = 15^\circ$ ,  $\delta D_{\text{true}} = 30^\circ$ ,  $s(\mathbf{R}_{CP}) = 0.05$ ,  $s(\mathbf{A}_{CP}) = 0.045$ ,  $\text{BF}(\text{ADS}) = 5 \times 10^{-7}$





# Translating $B \rightarrow DK$ results in measurement of $\gamma$

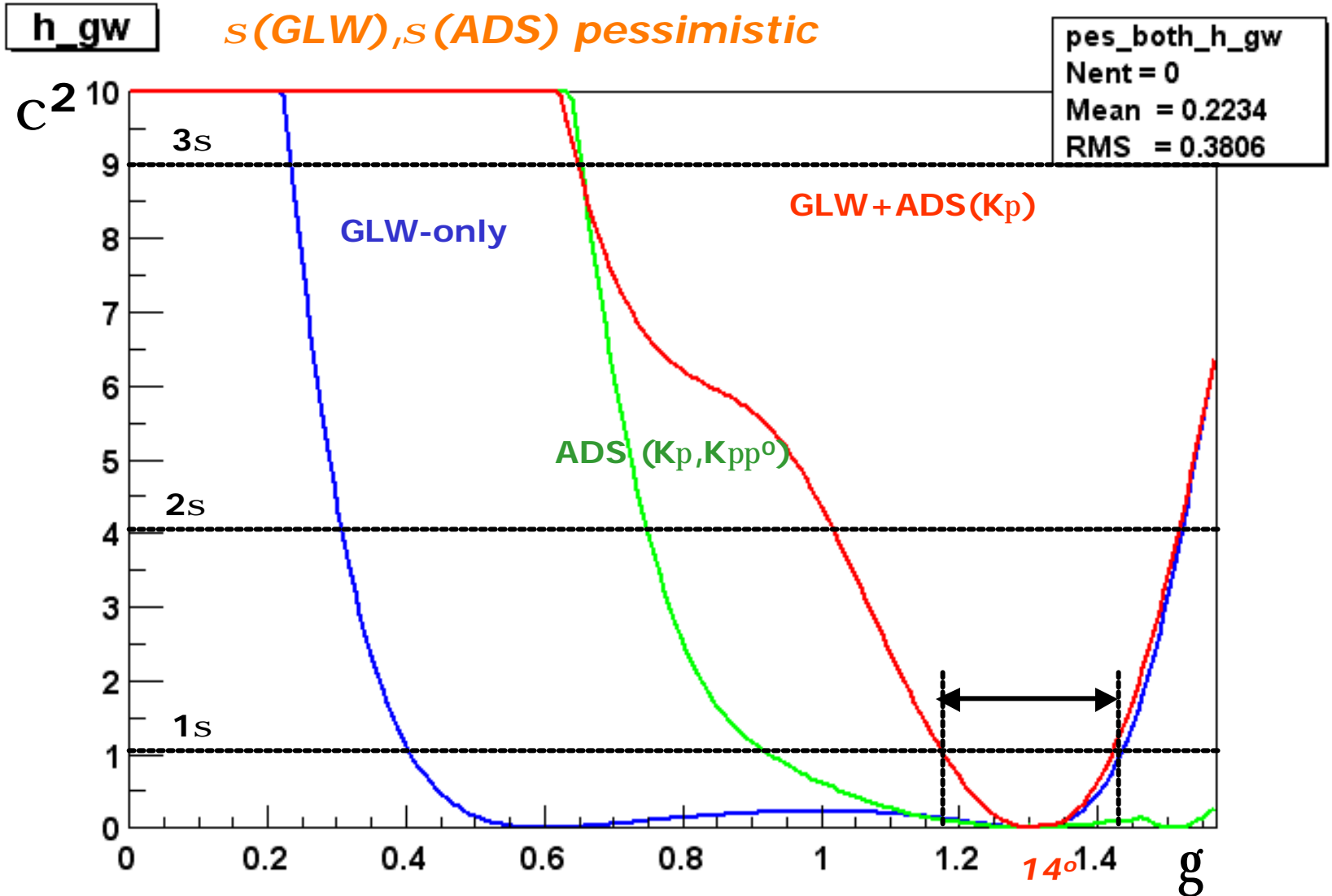
- $\gamma_{\text{true}} = 60^\circ$ ,  $r_{\text{Btrue}} = 0.2$ ,  $\delta B_{\text{true}} = 15^\circ$ ,  $\delta D_{\text{true}} = 30^\circ$ ,  $\sigma(R_{\text{CP}}) = 0.03$ ,  $\sigma(A_{\text{CP}}) = 0.02$ , **BF(ADS) =  $1 \times 10^{-7}$**





# Translating $B \rightarrow DK$ results in measurement of $\gamma$

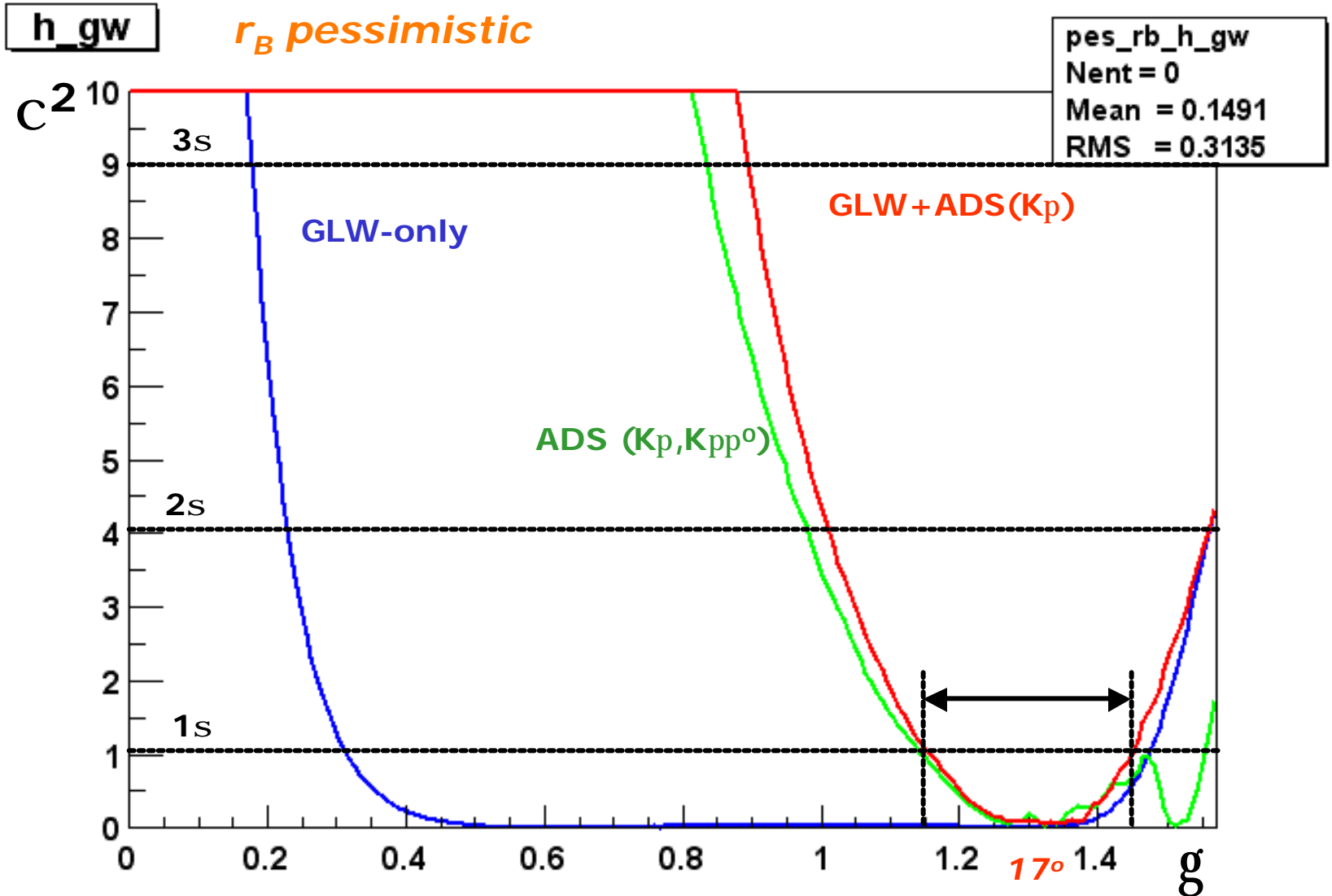
- $\gamma_{\text{true}} = 60^\circ$ ,  $r_{B\text{true}} = 0.2$ ,  $\delta B_{\text{true}} = 15^\circ$ ,  $\delta_{D\text{true}} = 30^\circ$ ,  $s(\mathbf{R}_{CP}) = 0.05$ ,  $s(\mathbf{A}_{CP}) = 0.045$ ,  $\text{BF}(\text{ADS}) = 1 \times 10^{-7}$





# Translating $B \rightarrow DK$ results in measurement of $\gamma$

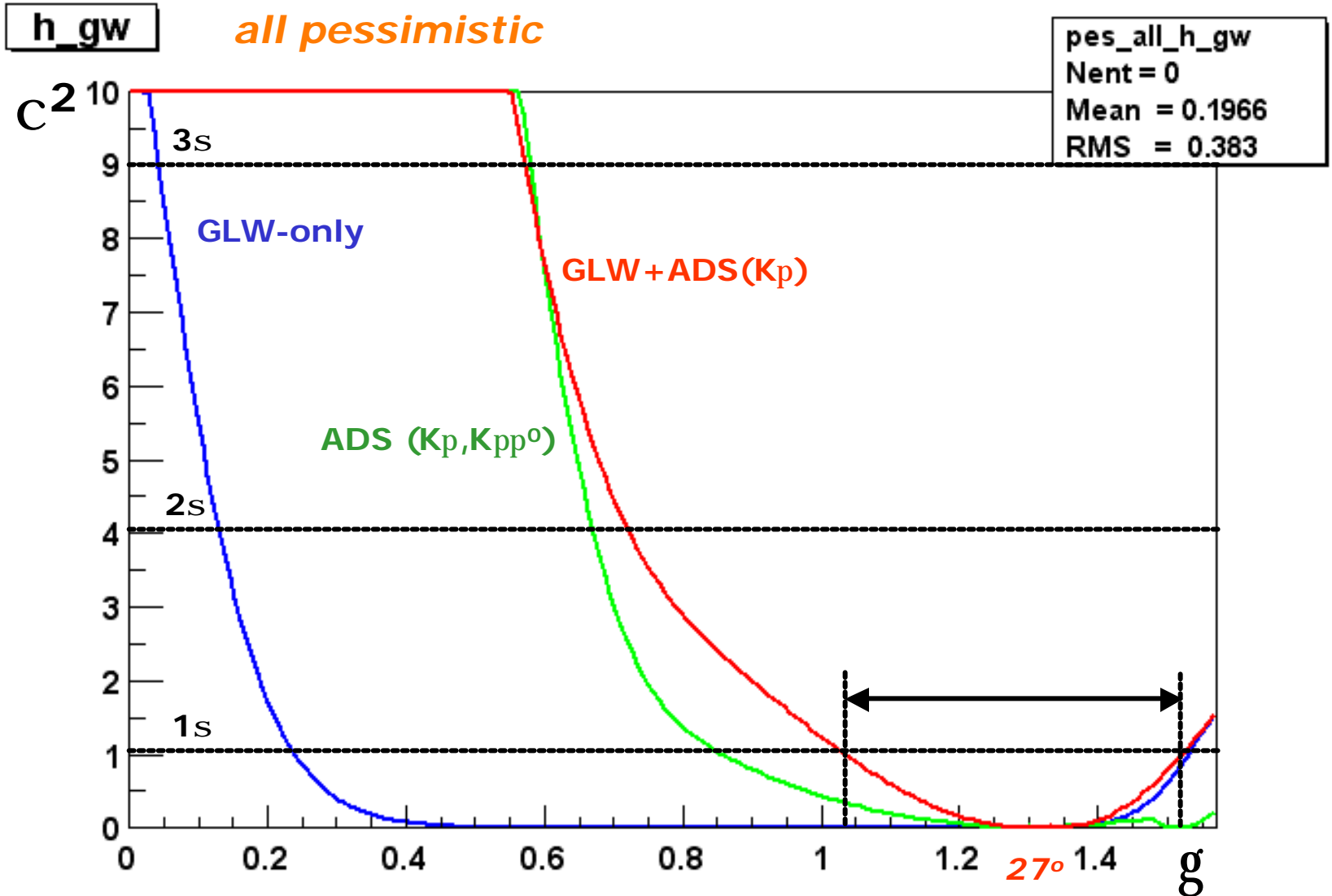
- $\gamma_{\text{true}} = 60^\circ$ ,  $r_{B\text{true}} = 0.1$ ,  $\delta B_{\text{true}} = 15^\circ$ ,  $\delta D_{\text{true}} = 30^\circ$ ,  $\sigma(R_{CP}) = 0.03$ ,  $\sigma(A_{CP}) = 0.02$ ,  $\text{BF(ADS)} = 5 \times 10^{-7}$





# Translating $B \rightarrow DK$ results in measurement of $\gamma$

- $\gamma_{\text{true}} = 60^\circ$ ,  $r_{\text{Btrue}} = 0.1$ ,  $\delta B_{\text{true}} = 15^\circ$ ,  $\delta D_{\text{true}} = 30^\circ$ ,  $s(\mathbf{R}_{\text{CP}}) = 0.05$ ,  $s(\mathbf{A}_{\text{CP}}) = 0.045$ ,  $\text{BF}(\text{ADS}) = 1 \times 10^{-7}$





# Summary

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- Error on GLW and ADS observables may not be strongly systematics dominated (yet) at  $10 \text{ ab}^{-1}$ 
  - **GLW:**  $s(\mathbf{R}_{\text{CP}}) = 0.02 \text{ stat } \text{\AA} (0.021-0.05) \text{ sys}$   
 $s(\mathbf{A}_{\text{CP}}) = 0.016 \text{ stat } \text{\AA} (0.015-0.04) \text{ sys}$  + ~30% uncertainty due to tracking, PID, cont. bkg changes
  - **ADS:**  $s(\mathbf{R}_{\text{ADS}}) = (2-10)\% \text{ stat } \text{\AA} (1-5)\% \text{ sys}$  + ~20-60% uncertainty due to cont. bkg changes
  - Systematic errors relatively well behaved because many 'difficult' systematics (absolute tracking, PID efficiencies) cancel in ratio of BFs used in these methods
  - Level of continuum background may become dominant factor in error on these measurements
- Precision of resulting measurement of  $\gamma$  depends on many additional factors (true values of  $r_B$ ,  $\gamma$ , strong phases)
  - Optimistic scenario gives error around  $8^\circ$ , but pessimistic scenarios can go much lower (15-25 $^\circ$ )
  - Several factors are resolution on  $\gamma$  are 'luck factors' (e.g. true value of  $r_B$ ) that are not in experimenters hands
  - If  $r_B$  is low (0.1) measurement of  $g$  from  $B \rightarrow DK$  by 'regular' B-factories unlikely
- **There exist several other methods to measure  $g$  from other  $B \rightarrow DK$  decays (multi body decays, Dalitz analyses etc) that are not covered in this talk**
  - Combining many modes will help