

$$B \rightarrow K_1(1400)\gamma$$

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2003 October 23

$10^{36}$  *B* Factory Workshop

1. Measurements
2. Modelling
3. Outlook

# Measurements

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- $B \rightarrow K^*(892)\gamma$  and  $B \rightarrow K_2^*(1430)\gamma$  have been measured.
- Belle has measured

$$BR(B^+ \rightarrow K^+ \pi^+ \pi^- \gamma) = (2.5 \pm 0.5_{-0.2}^{+0.4}) \times 10^{-5}$$

without disentangling  $K$  resonances.

- $B \rightarrow K_1(1400)\gamma$  has not been measured.

Theorists suggest  $BR(B \rightarrow K_1\gamma) \sim 0.7 \times 10^{-5}$

*e.g.* Atwood and Soni, 1994

# Polarization

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A more interesting reason to study this mode is to measure the photon polarization:

$$\lambda_\gamma \equiv \frac{|\mathcal{M}(\bar{B} \rightarrow K_{\text{res}}\gamma_L)|^2 - |\mathcal{M}(\bar{B} \rightarrow K_{\text{res}}\gamma_R)|^2}{|\mathcal{M}(\bar{B} \rightarrow K_{\text{res}}\gamma_L)|^2 + |\mathcal{M}(\bar{B} \rightarrow K_{\text{res}}\gamma_R)|^2}$$

It has been shown that for *any*  $K_{\text{res}}$ ,

$$\lambda_\gamma = \frac{|C_{7R}|^2 - |C_{7L}|^2}{|C_{7R}|^2 + |C_{7L}|^2}$$

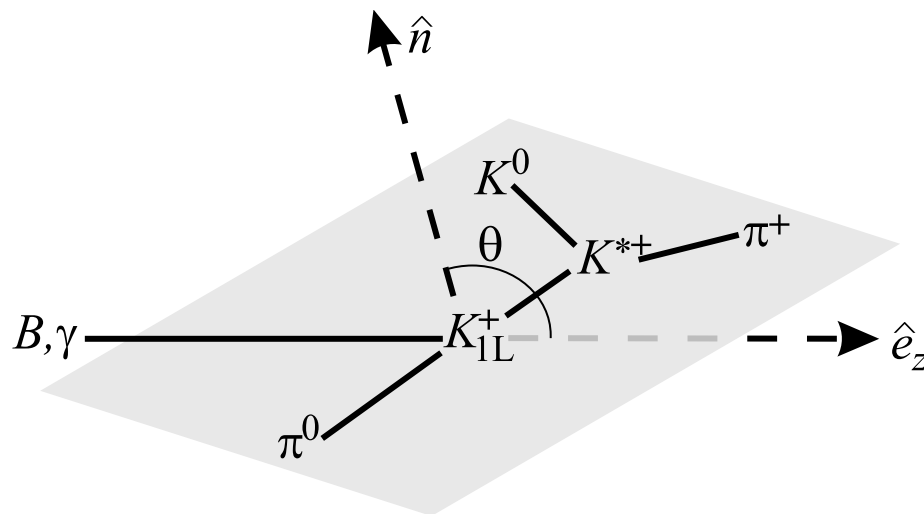
In the SM,  $\lambda_\gamma = +1$  for  $B$  decays and  $\lambda_\gamma = -1$  for  $\bar{B}$  decays, in the limit  $(m_s^2/m_b^2) \ll 1$ .

# Measuring polarization

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How do you measure  $\lambda_\gamma$ ? By measuring the angular distribution of the recoiling hadronic system, you can measure the helicity of  $K_{\text{res}}$ .

- In two-body  $K_{\text{res}}$  decays, such as  $K_2^*(1430) \rightarrow K\pi$ , you cannot construct a parity-odd scalar from the final state momenta.
- You can, however, in three-body decays, e.g.  $\vec{p}_\gamma \cdot (\vec{p}_K \times \vec{p}_\pi)$ .
- Measure angle  $\theta$  between normal  $\hat{n}$  to  $K_1$  decay plane and photon flight axis  $\hat{e}_z$  in  $K_1$  rest frame.



# Measuring polarization

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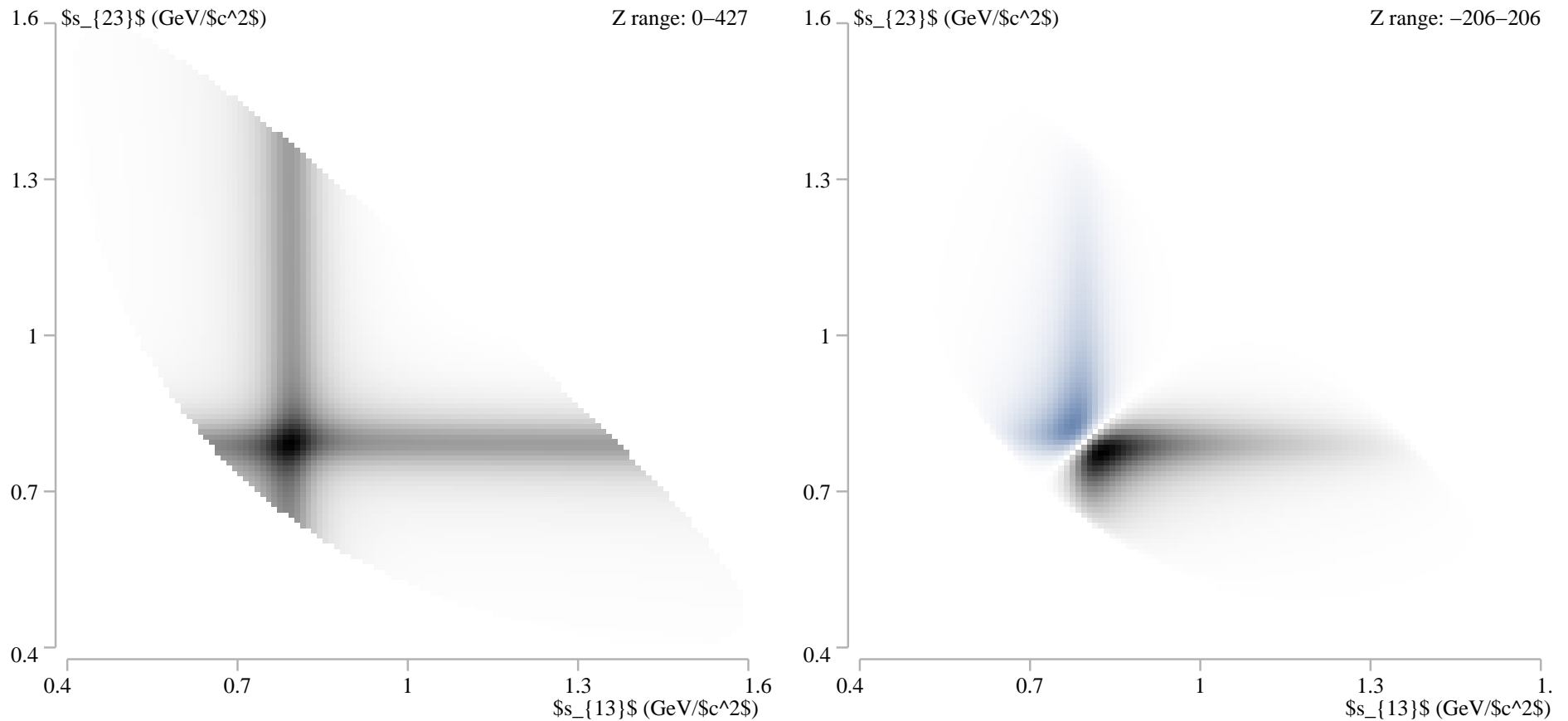
To extract  $\lambda_\gamma$ , use channels in which  $K_1$  decays to the same final state via two  $K^*$  isospin states, *e.g.*

$$\begin{array}{ll} B^+ \rightarrow K_1^+ \gamma & B^+ \rightarrow K_1^+ \gamma \\ K_1^+ \rightarrow K^{*+} \pi^0 & K_1^+ \rightarrow K^{*0} \pi^+ \\ K^{*+} \rightarrow K^0 \pi^+ & K^{*0} \rightarrow K^0 \pi^0 \end{array}$$

# Symmetric and antisymmetric terms

Gronau, Grossman *et al.* (2002) give the Dalitz distribution to be

$$\frac{d\Gamma}{ds_{13}ds_{23}d\cos\theta} \propto |\vec{J}|^2(1 + \cos^2\theta) + 2\lambda_\gamma \text{Im}(\hat{n} \cdot (\vec{J} \times \vec{J}^*)) \cos\theta$$

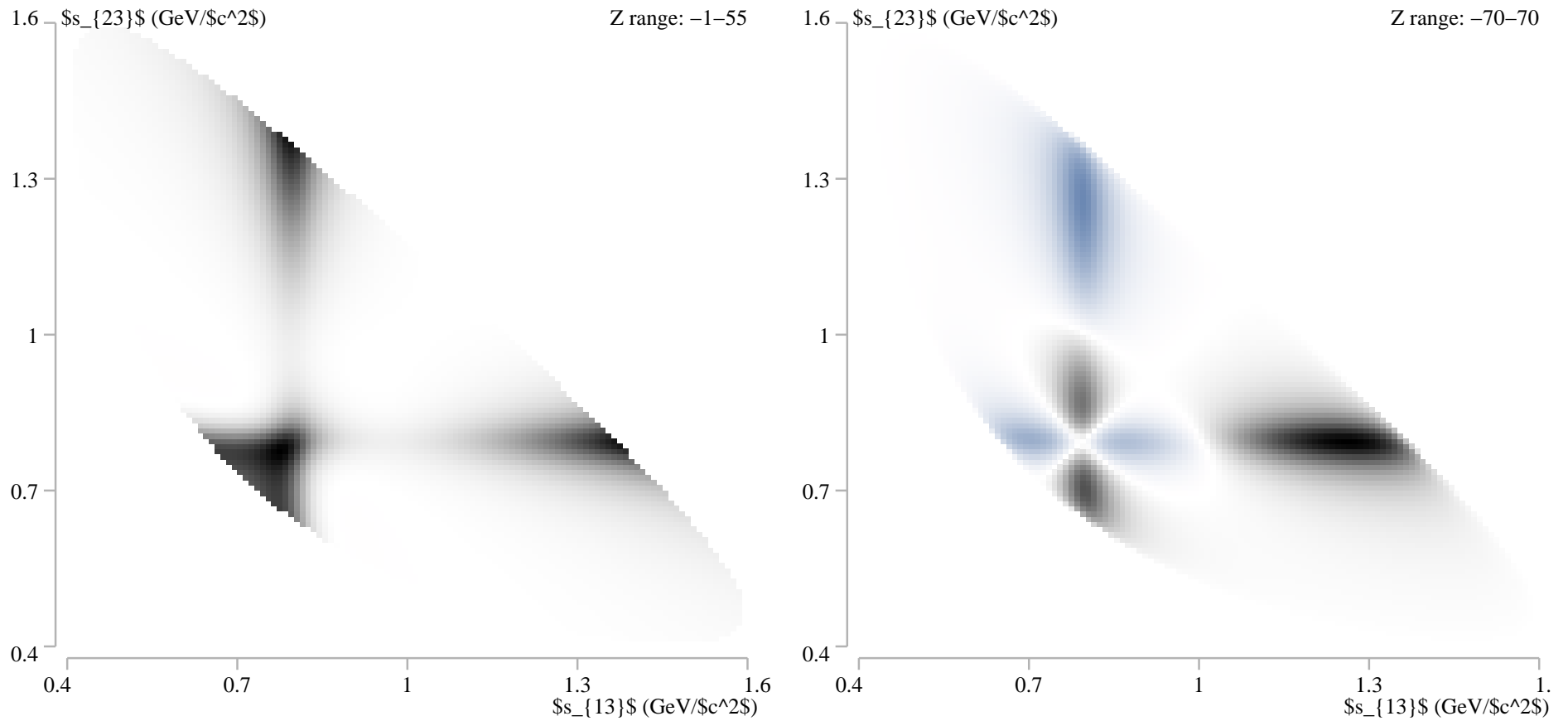


$|\vec{J}|^2$

(S-wave only)

$\text{Im}(\hat{n} \cdot (\vec{J} \times \vec{J}^*))$

# $D$ -wave contribution



$$|\vec{J}|^2$$

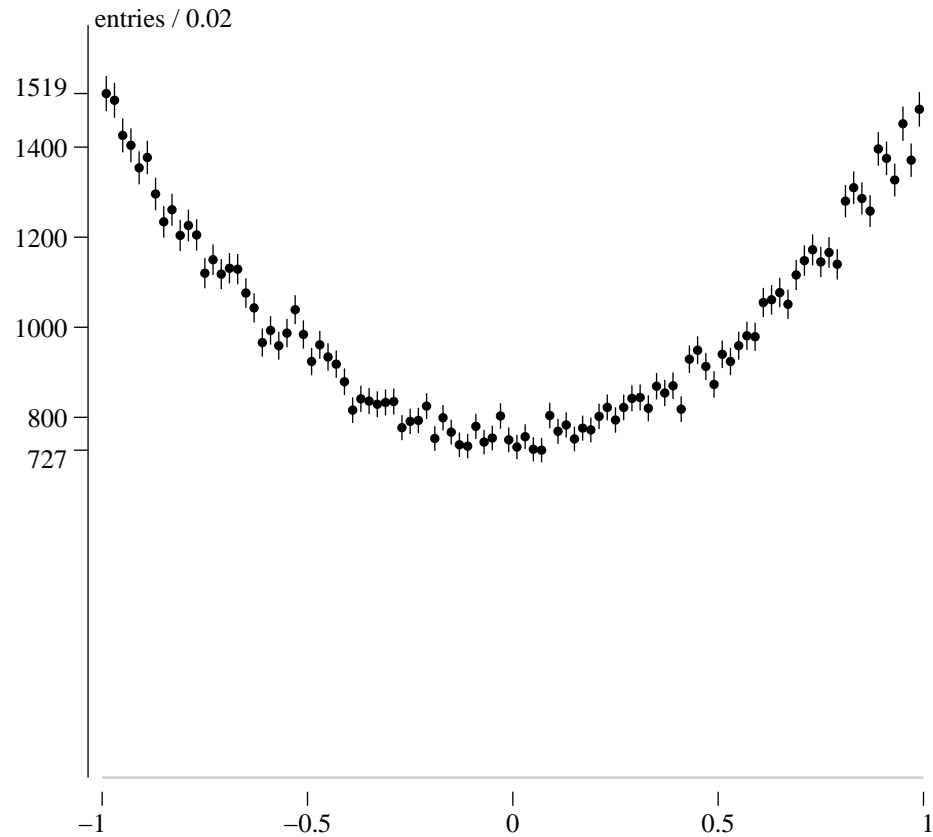
$D$ -wave contributions

$$\text{Im}(\hat{n} \cdot (\vec{J} \times \vec{J}^*))$$

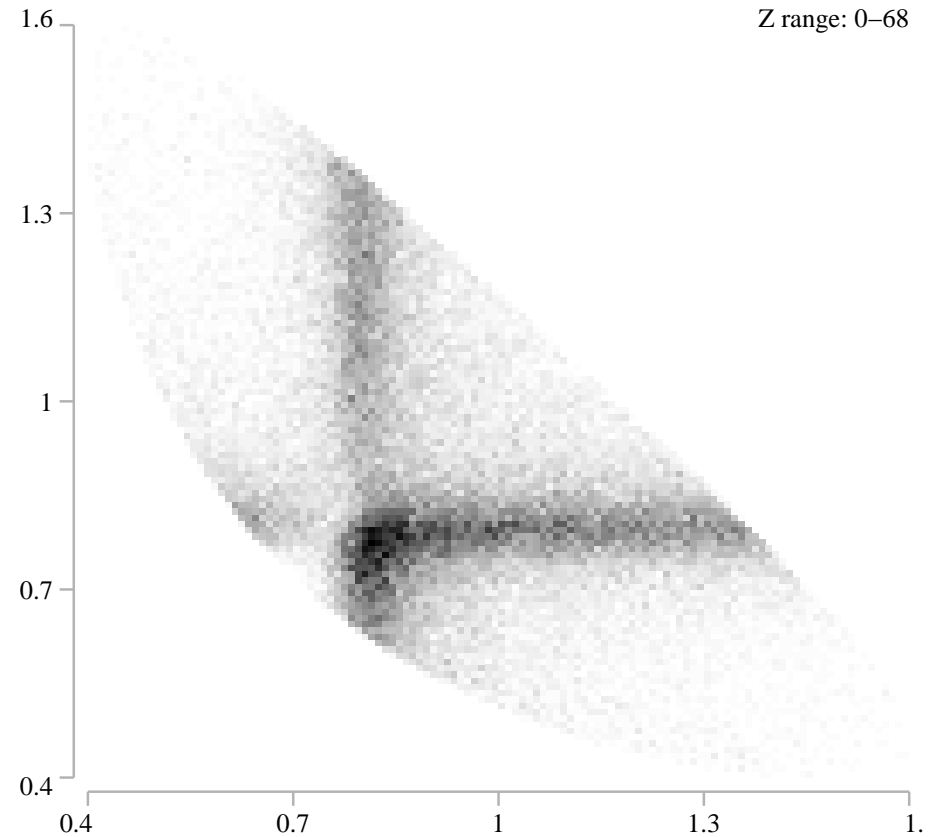
# EvtGen model

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We have developed a Monte Carlo decay model for this process.



$\cos \theta$  distribution



Dalitz plot,  $\cos \theta > 0$

# Complications

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We plan to fit the distribution of  $(s_{13}, s_{23}, \cos \theta)$  to extract  $\lambda_\gamma$ .

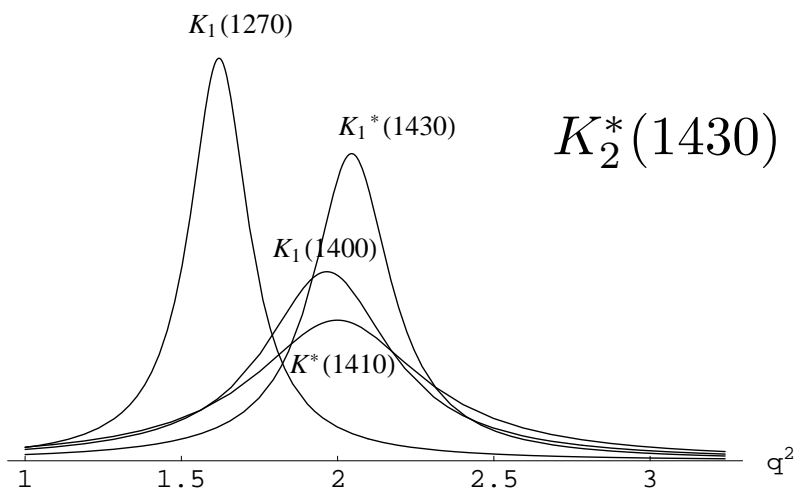
The fit will need to account for

- $S$ - and  $D$ -wave contributions in the  $K_1 \rightarrow K^* \pi$  decay.
- contribution from  $K_1 \rightarrow K \rho$
- contributions from other  $K$  resonances

# Higher $K$ resonances

$K$  resonances with  $J \geq 1$ , which can participate in  $B \rightarrow K_{\text{res}}\gamma$  :

resonance	$J^P$	mass	width	principal decays	
$K_1(1270)$	$1^+$	1.273	0.090	$K\rho$	42%
				$K_0^*(1430)\pi$	28%
				$K^*(892)\pi$	16%
$K_1(1400)$	$1^+$	1.402	0.174	$K^*(892)\pi$	94%
				$K\rho$	3%
$K^*(1410)$	$1^-$	1.414	0.232	$K^*(892)\pi$	> 40%
$K_2^*(1430)$	$2^+$	1.430	0.104	$K\pi$	50%
				$K^*(892)\pi$	25%
				$K^*(892)\pi\pi$	13%



# Estimates

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Assume:

- $1 \text{ at}^{-1} \sim 10^9 B\bar{B}$  pairs
- $\text{Br}(B \rightarrow K_1\gamma) = 0.7 \times 10^{-5}$
- only consider  $K_S \rightarrow \pi^+\pi^-$

# Expectations

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Fraction of total  $B \rightarrow K_1\gamma$ , and expected production:

Mode	Fraction	Produced
$B^0 \rightarrow K_S\pi^0\pi^0\gamma$	1.8%	250
$B^\pm \rightarrow K_S\pi^\pm\pi^0\gamma$	7.1%	1000 ★
$B^0 \rightarrow K_S\pi^\pm\pi^\mp\gamma$	7.1%	1000
$B^\pm \rightarrow K^\pm\pi^0\pi^0\gamma$	5.2%	700
$B^0 \rightarrow K^\pm\pi^\mp\pi^0\gamma$	20.9%	2900 ★
$B^\pm \rightarrow K^\pm\pi^\mp\pi^\pm\gamma$	20.9%	2900

★ can be used for polarization measurement

# Outlook

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- $\text{Br}(B \rightarrow K_1(1400)\gamma)$  can be measured in current  $B$  factories.
- Feasibility of polarization measurement in current  $B$  factories is questionable.
- Polarization should be measurable with a  $\mathcal{L} = 10^{36}$  experiment.